$\rm HP35s$ / $\rm HP12c$ Programs

Daniel J Boulet

June 26, 2021

Revision History

| Revision | Description |
|---------------|---|
| Date | |
| May 25, 2016 | Revised Modular Exponentiation program by using DSE function instead of |
| | direct variable count. |
| June 26, 2021 | Renamed Modular Exponentiation to modexp. |
| | Added blank pages for double sided printing. |
| | Added program to calculate actual VSWR based on measured VSWR and |
| | cable loss. |

Contents

| Ι | HP | 35s | | | | | | | | | | | | | | | | | | | | | 1 |
|---|-----|--------|--|--|--|--|--|--|------|--|--|--|--|--|--|--|--|--|--|--|--|---|---|
| | 0.1 | modexp | | | | | | | | | | | | | | | | | | | | | 2 |
| | | atan2 | | | | | | | | | | | | | | | | | | | | | |
| | 0.3 | avswr | | | | | | | | | | | | | | | | | | | | ! | 5 |

Part I

HP35s

0.1 modexp

Description

This program calculates the modulus of a number raised to a large power. The formula looks like this:

$$modexp = n^p \mod m$$

Usage

| GTO P | λ 001 r | n R/S | p R/S | m R/S |
|-------|-------------------|-------|-------|-------|
|-------|-------------------|-------|-------|-------|

Program Listing

| LBL A | start of program |
|----------|---|
| STO N | store number to the raised to the power P |
| STOP | wait for user R/S |
| STO P | store exponent |
| STOP | wait for user R/S |
| STO M | store modulus |
| 1 | initialize product |
| STO R | and save in memory |
| RCL N | recall base |
| RCL R | recall product |
| × | and multiply the two |
| RCL M | recall the modulus |
| RMDR | and apply it |
| STO R | save the new product |
| DSE P | decrement exponent |
| GTO A009 | and loop back if not finished. |
| RCL R | pull the product from memory |
| RTN | we are done! |
| | STO N STOP STO P STOP STO M 1 STO R RCL N RCL R X RCL M RMDR STO R DSE P GTO A009 RCL R |

Example

In the following example we calculate $5^{101} \mod 31$ using the following steps:

| GTO A001 | 0.00000 | go to start of program |
|----------|-----------|--------------------------|
| 5 R/S | 5.00000 | the "base" |
| 101 R/S | 101.00000 | the "exponent" |
| 31 R/S | 25.00000 | the "modulus" and result |

Comments

The HP35s is not known for it's lightning speed. The above example will take about 12 seconds to run.

0.2 atan2

${\bf Description}$

This program calculates at an2($\frac{y}{x}$). Result is in the range -180° to $+180^{\circ}.$

Usage

```
GTO Z001 x R/S y R/S
```

Program Listing

| Z001 | LBL Z | Start of program. |
|--|---|---|
| Z002 | STO X | Store x in X . |
| Z003 | STOP | Wait for user R/S. |
| Z004 | STO Y | Store y in Y. |
| Z005 | RCL Y | Recall Y. Note: this is also the entry point for subroutine. |
| Z006 | RCL X | Recall X. |
| Z007 | ÷ | Take ratio of rise over run $(\frac{y}{x})$. |
| Z008 | ATAN | Calculate $\arctan(\frac{y}{x})$. |
| Z009 | STO R | Save as an interim result in R. |
| Z010 | RCL X | Test sign of X. |
| Z011 | x > 0? | Is x positive? |
| Z012 | GTO Z027 | If so then go to end of program. |
| Z013 | RCL Y | Recall Y |
| Z014 | SGN | Calculate its sign |
| Z015 | 45 | |
| Z016 | X | then multiply it by 45° . |
| | | |
| Z017 | | Get X value. |
| | RCL X | Get X value. Is it equal to zero? |
| Z017 | RCL X $x = 0$? | |
| Z017 Z018 | $\begin{array}{l} \mathrm{RCL} \ \mathrm{X} \\ x = 0 ? \\ \mathrm{RTN} \end{array}$ | Is it equal to zero? |
| Z017 Z018 Z019 | RCL X $x = 0$? RTN 180 | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ |
| Z017 Z018 Z019 Z020 | RCL X $x=0$? RTN 180 STO -R | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . |
| Z017 Z018 Z019 Z020 Z021 | RCL X $x=0$? RTN 180 STO -R | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. |
| Z017 Z018 Z019 Z020 Z021 Z022 | RCL X $x=0$? RTN 180 STO -R RCL Y $x<0$? | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. Get Y value. |
| Z017 Z018 Z019 Z020 Z021 Z022 Z023 | RCL X $x=0$? RTN 180 STO -R RCL Y $x<0$? GTO 2027 | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. Get Y value. Is it negative? |
| Z017 Z018 Z019 Z020 Z021 Z022 Z023 Z024 | RCL X $x = 0$? RTN 180 STO -R RCL Y $x < 0$? GTO Z027 360 | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. Get Y value. Is it negative? If yes, then we are done since we already subtracted 180° . |
| Z017 Z018 Z019 Z020 Z021 Z022 Z023 Z024 Z025 | RCL X $x = 0$? RTN 180 STO -R RCL Y $x < 0$? GTO Z027 360 STO +R | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. Get Y value. Is it negative? If yes, then we are done since we already subtracted 180° . If y is positive then we have to add 360° |
| Z017 Z018 Z019 Z020 Z021 Z022 Z023 Z024 Z025 Z026 | RCL X $x = 0$? RTN 180 STO -R RCL Y $x < 0$? GTO Z027 360 STO +R | Is it equal to zero? If so then return the value of the stack $(\pm 45^{\circ})$ Setup offset depending on sign of y . Initially subtract 180° — we do this at a minimum. Get Y value. Is it negative? If yes, then we are done since we already subtracted 180° . If y is positive then we have to add 360° for a total addition of 180° . |

Example

In the following example we calculate $atan2(\frac{+1.5}{-1.0})$ using the following steps:

| GTO Z001 | 0.00000 | Go to start of program. |
|----------|-----------|-------------------------|
| 1.5 | 1.5 | Your value for x . |
| R/S | 1.50000 | |
| -1.0 | -1.0 | Your value for y . |
| R/S | -33.69007 | The resulting angle. |

Comments

Users have to be careful about a couple of things:

- 1. Angles are calculated in degrees. Confirm calculator setting before using this function.
- 2. User is responsible for ensuring that x and y are **never** both zero.

0.3 avswr

Description

This program calculates actual VSWR given measured VSWR and cable loss to antenna.

Usage

```
GTO V001 M R/S L R/S
```

Program Listing

| V001 V002 | LBL V STO M | Start of program. Save measured VSWR in M. |
|--------------|----------------|---|
| V003 | STOP | Pause for entry of cable loss (in dB) |
| V004 | +/- | Negate cable loss |
| V005 | 10 | and convert to ratio |
| V006 | • | |
| V007 | 10^{x} | |
| 800V | STO L | Save as cable loss |
| V009 | RCL M | Get measured VSWR and calculate reflected power ratio |
| V010 | 1 | |
| V011 | _ | |
| V012 | RCL M | |
| V013 | 1 | |
| V014 | + | |
| V015 | ÷ | |
| V016 | x^2 | |
| V017 | STO R | Save reflected power ratio |
| V018 | RCL L | Calculate actual VSWR at antenna |
| | \sqrt{x} | |
| | RCL R | |
| V021 | RCL L | |
| V022 | ÷ | |
| V023 | \sqrt{x} | |
| V024 | + | |
| V025 | RCL L | |
| V026 | \sqrt{x} | |
| V027 | RCL R | |
| V028 | RCL L | |
| V029 | ÷ | |
| V030 | \sqrt{x} | |
| V031 | - | |
| V032 | ÷ | Detume to calling function |
| V033 | RTN | Return to calling function. |

Example

Calculate the actual VSWR of an antenna where the measured VSWR is 1:1.13 and cable loss is 4.7dB:

| GTO V001 | 0.00000 | Go to start of program. |
|----------|---------|-------------------------------------|
| 1.13 | | Your value for M (measured VSWR). |
| R/S | 1.13000 | |
| 4.7 | | Your value for cable loss L . |
| R/S | 1.4394 | Actual VSWR at antenna is 1:1.4394 |

How this program works

VSWR is the ratio of the sum and difference of forward and reflected voltages:

$$VSWR = \frac{V_f + V_r}{V_f - V_r} \tag{1}$$

Since power is proportional to the square of the voltage, (1) can be expressed in terms of power

$$VSWR = \frac{\sqrt{P_f} + \sqrt{P_r}}{\sqrt{P_f} - \sqrt{P_r}} \tag{2}$$

By setting P_f equal to 1 and rearranging (2) we can solve for P_r

$$P_r = \left(\frac{VSWR - 1}{VSWR + 1}\right)^2 \tag{3}$$

Cable loss is normally expressed in decibels but for our purposes we can simply express it as a factor of less than 1 where P_a is power at the antenna and P_t is power from the transmitter.

$$L = \frac{P_a}{P_t} \tag{4}$$

Taking into account the cable loss and measured forward and reverse power we can calculate VSWR at the antenna

$$VSWR = \frac{\sqrt{P_f \times L} + \sqrt{P_r \div L}}{\sqrt{P_f \times L} - \sqrt{P_r \div L}}$$
 (5)

Again we set P_f to 1 so a simplied version of (5) becomes the actual VSWR at the antenna

$$VSWR = \frac{\sqrt{L} + \sqrt{P_r \div L}}{\sqrt{L} - \sqrt{P_r \div L}}$$
(6)