Representing Gödel Object Programs in Gödel*

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Abstract

Meta-programs are an important class of programs. When meta-programming is done in logic the object program must be represented in the meta-program. This can be done in two ways: the non-ground and ground representations. The non-ground representation severely limits the meta-program. The ground representation is more powerful, but rarely used because it is thought to be complex, laborious and to have a high computational overhead. Prolog programs therefore use the non-ground representation and supplement it with non-logical features. Gödel is a logic programming language that aims to have similar expressive power to Prolog but with greatly improved declarative semantics. Gödel has types and a module system, and supports declarative meta-programming in the ground representation. It is argued that providing the representation as an abstract data type answers the accusation of inconvenience. The representation of Gödel programs as ground terms is investigated and shown to be practical. The prospect of reducing the computational overhead by partial evaluation exists.

All that I have to say is to tell you that the lanthorn is the moon; I, the Man i' th' Moon; this thorn-bush, my thorn-bush; and this dog, my dog.

-William Shakespeare, "A Midsummer Night's Dream" Act 5 Scene I.

1 Introduction

Computer programming is difficult. Anyone who reads the computing press will know that an alarming number of software development projects fail, simply because the programs cannot be made to work with the available resources. The precise reasons for these failures may be various, but one is surely chief among them: unmastered complexity.

By programming in logic we can go a long way towards mastering complexity. A programmer using a logic programming language is likely to be able to handle a more intricate problem before being overwhelmed than a programmer using a procedural language. This is because the logic language is compact, high-level and expressive. Since first-order logic developed out of attempts to mechanise certain aspects of human reasoning, it is close to the way we naturally express ideas about the world. It has a simple, clean semantics that is easy to understand. Add types and modules to the logic, and the advantage is greater still.

Another way to handle complexity is to seek help from automation. Programs written in a language with simple declarative semantics can more easily be synthesised, transformed, analysed and debugged by other programs, and the soundness of these processes can be verified. For these reasons, we have a chance of contributing to the future of computing by taking seriously the central thesis of logic programming: that a program is a theory, and computation is deduction.

Meta-programs are an important class of programs. A meta-program is any program that treats one or more other programs, called object programs, as data. Interpreters, compilers, program transformers and debuggers are all examples of meta-programs. If our idea that programs are first-order theories is a natural and useful one, clearly we should be able to express meta-programs in this form. The natural way to view meta-programs is as first-order theories over domains that are representations of their object theories. There are two distinct ways in which this representation of object programs can be accomplished: the non-ground and ground representations [5].

In the non-ground representation, object-level variables are represented by variables at the meta-level. This imposes severe restrictions on the power of the meta-program; for example, it cannot inspect the variables of the object program, and it cannot add statements to the object program. The latter restriction arises because it is impossible to distinguish between representations of statements containing free object-level variables and incomplete statement representations containing meta-level variables.

In the ground representation, object-level variables are represented by ground terms at the meta-level. This gives a much more powerful formalism for meta-programming in which object-level variables can be manipulated in exactly the same way as any other syntactic element of the object program. If the entire object program is represented as a single term in the meta-program, it is easy to add, remove or change statements in the object program, and object-level goals can be proved by means of a meta-interpreter [7].

2 1 INTRODUCTION

If meta-programming is to be done in logic, there is no obvious alternative to making the ground representation effective. There is surely little prospect of discovering a logic in which meta-programs using a non-ground representation can inspect object-level variables and yet retain semantics as simple, intuitive and tractable as classical first-order logic.

Despite its power, elegance and logical purity, the ground representation is rarely used in current logic programming practice. This is because it appears to have the following drawbacks:

- the representation of object programs as terms is too complex;
- meta-programming in the ground representation is laborious, because large procedures are required to do simple things such as unifying object-level terms;
- object-level variables and their bindings must be handled explicitly, an overhead that makes the meta-program unacceptably slow.

As a consequence of these perceived difficulties, unsatisfactory solutions to the problem of meta-programming are commonly adopted. The majority of meta-programs written in Prolog use the non-ground representation, and circumvent the inadequacy of that representation by resorting to non-logical facilities that have been added to the language for that purpose. Programs that use the meta-logical predicates of Prolog such as var, nonvar, assert and retract cannot be understood directly as theories, and therefore lose the advantages of a simple declarative semantics. They are much harder to debug and transform, for example, and also harder to execute in parallel because the non-logical features have a procedural component that implies sequential execution.

Several attempts have been made to address this deficiency of Prolog. The MetaProlog language [1] provides more declarative forms of assert and retract by keeping track of named theories, and has a mechanism for distinguishing between object-variables and meta-variables when theories are updated. However MetaProlog is still mainly based on the non-ground representation. The language 'LOG (pronounced quotelog) [3] directly supports the ground representation of a Prolog-like language, and has built-in predicates for creating such representations. The representations are based on lists, and a large part of the labour of manipulating them is left to the programmer.

Gödel is a logic programming language intended as a successor to Prolog. It aims to have power and expressiveness similar to that of Prolog, but with greatly improved declarative semantics. Gödel also has a type system and a module system; the value of these is well-known in software engineering. Indeed, these features greatly benefit Gödel's meta-programming facilities.

Although it is possible to write programs using the non-ground representation in Gödel, the ground representation is far more important. Using the ground representation, Gödel gives completely declarative counterparts to Prolog's var, nonvar, assert, retract, =.. etc. By providing the ground representation as an abstract data type, Gödel frees the programmer from concern with the details of the representation, and allows access to it at a relatively high level by means of an extensive library of predicates, each with a precise semantic definition. This renders meta-programming in Gödel almost as straightforward as it is in Prolog, with the advantage of declarative semantics, and answers the objec-

tions based on complexity and labour that have previously discouraged use of the ground representation.

The thought of representing entire object programs, even Prolog object programs, as single terms can seem rather daunting. In representing a Gödel program, we have the extra burden of object programs written in a much richer language. The representation has to include the module structure of the object program, its type declarations, statements and control annotations. It is, of course, these very features that enable effective use of the ground representation in Gödel.

In the remainder of this paper a specific representation for Gödel programs in Gödel is described, a representation that is sufficient to meet the specifications of the metapredicates in Gödel's system modules. This representation is in a pure polymorphic many-sorted logic, and does not use any features outside the Gödel language. Apart from being declarative, this logical representation theoretically allows construction of a tower of metalevels for free; that is, since the representation is a Gödel term, it can itself be represented. In practice the size of the representation increases dramatically with each meta-level and becomes unmanageable for even small programs after the third or fourth level. The paper demonstrates that as long as careful attention is paid to certain design considerations, the representation in typed logic of a structure as complex as a Gödel program can be accomplished in a fairly straightforward way, and still allow standard access and update operations to be performed simply and reasonably efficiently. The Gödel programmer is of course unaware of the details of the representation, as it is presented as an abstract data type. This leaves the language implementors free to alter the structure at will.

The paper is organised as follows. In the next section a brief overview of the Gödel language is presented. The reader is given the flavour of meta-programming in Gödel and then a representation for Gödel object programs is described in detail. Finally, we draw some conclusions and suggest directions for future research.

2 The Gödel Language

Space does not permit more than a cursory overview of Gödel here. For a complete technical description and specification the reader is referred to [6].

Symbols in Gödel either begin with an upper case-letter, or are composed entirely of non-alphanumeric characters. Variables begin with a lower-case letter. Gödel statements and goals can have arbitrary first-order formulas in the body, and may also contain a *commit* pruning operator, and the *IF-THEN-ELSE* conditionals of [8].

Gödel program are written in a language defined by a set of language declarations. Every symbol in the language has a declaration that places it in one of the six categories: BASE, CONSTRUCTOR, CONSTANT, FUNCTION, PROPOSITION and PREDICATE. The types (or sorts) of this language are built from the symbols declared as bases and constructors, together with *parameters*, in the same way that terms are built from constants, functions and variables. Every constructor symbol is assigned an arity by its declaration. Parameters provide polymorphism; they are type variables and range over all the type symbols in the language. Thus given the declarations

BASE Hat.
CONSTRUCTOR List/1.

we have a type Hat, a polymorphic type List(a), and instances of this type List(Hat), List(List(a)) and so on.

When a constant, function or predicate symbol is declared, it is assigned a domain and/or range type as appropriate from this set of types. Functions and predicates may also be specified as prefix, infix or postfix operators by including an *indicator* in their declaration. A typical operator declaration might be

FUNCTION + : yFx(510) :
 Integer
 * Integer
-> Integer.

The indicator yFx(510) specifies the precedence and associativity of the operator.

Gödel predicates may have control declarations, called DELAY declarations. These are syntactic variants of the when declarations of NU-Prolog [10]. DELAY declarations have the form

DELAY Atom UNTIL Condition

where Atom is an atom (the head) and Condition is constructed from NONVAR(var), GROUND(var), TRUE, and connectives & and $\$. Variable var must occur in Atom. Delay declarations influence the computation rule as follows: if a call unifies with Atom, it is delayed until it becomes an instance of Atom and then until Condition is satisfied. There may be several delay declarations for the same predicate, provided no pair of heads have a common instance.

Most Gödel modules consist of two parts, a local part and an export part. The *local* part of a module is indicated by a LOCAL or MODULE module declaration. The *export* part is indicated by an EXPORT or CLOSED module declaration. These keywords are followed by the name of the module. Modules are linked by IMPORT declarations that name imported modules.

The export part of a module can contain IMPORT declarations, language declarations and control declarations. The local part can contain IMPORT declarations, language declarations, control declarations and statements. If a module consists only of a local part, it has a MODULE declaration rather than a LOCAL declaration. The keyword CLOSED appearing in the export part of a module implies that it is a system module and specially protected. Modules that are not closed are said to be *open*.

A Gödel module exports all the symbols declared in its export part, and all the symbols it imports into its export part. The declaration

IMPORT Hats.

appearing in a part of a module imports all the symbols exported by module Hats into that part of the module. Thus a module can import module Hats either *directly* (by naming Hats in an import declaration) or *indirectly* (by importing another module that imports Hats into its export part). The set of symbols declared in and imported into both parts of

a module forms the *module language*, and is the language in which the statements of the module are written.

We say that a module M refers to a module N if either part of M contains the declaration IMPORT N. We define the relation depends upon to be the transitive closure of the relation refers to. A Gödel program is then a set of modules, consisting of one main module that is not imported by any other module, together with all the modules upon which this main module depends.

The definition of a type in a Gödel program is the set of constants and functions that have that type as their range type. The definition of a predicate (or proposition) in a Gödel program is the set of statements in the program that have that predicate (or proposition) in the head. The definition of a predicate or proposition must reside entirely within the module that declares it. Similarly, the definition of a type must reside within the module that declares its top-level constructor, or that declares the type itself if it is a base type.

Gödel is flexible in allowing overloading. The only condition on the naming of symbols is that distinct symbols cannot be declared in the same module with the same category, name and arity. The data structures described in this paper make liberal use of overloading: there are several instances where a function and its type have the same declared name.

The name that appears in the declaration for a symbol is called the *declared name* of the symbol. The possibility of overloading means that this name is not necessarily unique. In order to form the ground representation, we need the *flat name* of the symbol, which is the quadruple consisting of the name of the module in which the symbol is declared, its declared name, its category and its arity. The condition imposed on naming ensures that this quadruple uniquely identifies the symbol. The *flat form* of a program is obtained by replacing each occurrence of the declared name of a symbol in the program by its flat name. The *flat language* of a program is the language defined by the set of language declarations in the flat form of the program.

Gödel provides a rich set of system modules, such as Integers, Lists, Rationals, Floats, Strings, Sets and IO to support the commonly used data types and common operations on those types. Importing the Lists module makes the conventional notation for lists available. Similarly importing Strings allows the familiar notation "abcd" to be used for sequences of characters.

We conclude this overview with a tiny example program. The module Inclusion defines a predicate IncludedIn which can be used to check that all the elements of a list also appear in another list. This module forms a program together with the module Lists and the module Integers (which is imported into the export part of Lists and so indirectly into Inclusion).

```
MODULE Inclusion.

IMPORT Lists.

PREDICATE IncludedIn : List(a) * List(a).

IncludedIn(x,y) <-
ALL [z] (Member(z,y) <- Member(z,x)).
```

3 Meta-programming in Gödel

Three system modules are provided by Gödel for meta-programming in the ground representation: Syntax, Programs and Theories. The Theories module, which is concerned with representing full first-order theories (rather than logic programs) is outside the scope of this paper.

The Syntax module is concerned with representing object expressions in Gödel syntax, and is imported into the export parts of both Programs and Theories. The export part of Syntax declares the abstract data types

```
BASE Name, Type, Term, Formula, TypeSubst, TermSubst, VarTyping.
```

Terms of type Name represent the names of symbols; terms of type Type, Term, and Formula represent types, terms, and formulas, respectively; terms of type TypeSubst and TermSubst represent type and term substitutions; and terms of type VarTyping represent variable typings (a variable typing is set of assignments of variables to types).

Syntax exports many predicates for manipulating these types. For example

```
PREDICATE And : Formula * Formula * Formula.
```

And(u,v,w) is intended to be true when w represents the conjunction of the formulas represented by u and v.

The module Programs supports the representation of Gödel programs as terms, and exports the abstract data type Program. The export part of Programs also declares a type ModulePart and constants

```
CONSTANT Export, Local, Closed, Module : ModulePart.
```

to represent the part keywords of module declarations.

A typical predicate exported by Programs is the predicate FormulaInModule that is used to check whether a term of type Formula represents a formula that is valid in the language of a specific module. The declaration of FormulaInModule is

PREDICATE FormulaInModule :

```
% Representation of a program.
 Program
* String
                  % Name of a module in this program.
* ModulePart
                  % Representation of a part keyword of this module.
* VarTyping
                  % Representation of a variable typing in the
                  % flat language of this module.
* Formula
                  % Representation of a formula in the
                  % flat language of this module.
                  % Representation of the variable typing obtained by
* VarTyping.
                  % combining the variable typing in the fourth argument
                  % with the types of all free variables occurring in
                  % the formula.
```

Among many others, the Programs module also exports a pair of predicates called StringToProgramFormula and ProgramFormulaToString. The former invokes the Gödel parser in order to convert the intuitive representation of an object formula as a String into its ground representation. The latter works in the opposite direction, generating a string from the Formula abstract data type. These predicates are similar to the built-in primitive <=> of 'LOG [3].

The predicate Succeed invokes a full-scale interpreter for Gödel object programs. Its declaration is

PREDICATE Succeed:

```
Program % Representation of a program.
```

* Formula % Representation of the body of a goal in the

% flat language of this program.

* TermSubst. % Representation of a computed answer for this goal

% and the flat form of this program.

There are several other similar predicates in **Programs** that provide different flavours of interpreter.

To facilitate the creation of representations of object programs, Gödel provides a utility called the *program compiler*. This takes the source of the object program and generates its ground representation in a file. The system module ProgramsIO exports a predicate

```
PREDICATE GetProgram : InputStream * Program.
```

that reads the representation from the file. This IO operation is not declarative, but as long as Gödel programmers keep all IO in the top-level module the logical purity of the majority of the program is preserved.

4 Representing Gödel Syntax in Gödel

In this section we discuss the representation of syntactic expressions in polymorphic many-sorted logic: symbol names, types, terms and formulas. These objects are represented independently of the context of any particular object program, by structures declared in the Syntax module.

The abstract data type Name is provided to represent symbol names. The Name type is the basic unit from which syntax is constructed; the Syntax module can fulfil its specification without ever examining the internal structure of an Name term, except in one case only: since Name is an abstract data type, Syntax must provide a means for the programmer to create instances of the type.

Clearly we would like Gödel meta-programs to be independent of any particular object program, so we must avoid having to declare explicitly the meta-level constants that represent object-level names. We need a data type that has enough instances already available, and the possibility of an easily defined mapping between these instances and the object-level names. This clearly suggests using the String type.

We will see later that for representing Gödel programs it is convenient to have the four components of Gödel flat names explicit in the Name term so that they can be easily

extracted and separated. Gödel flat names are therefore represented by the following function, declared in the local part of Syntax:

```
FUNCTION Name :
```

```
String % Name of module where symbol is declared.

* String % Declared name of symbol.

* Category % Symbol's category.

* Integer % Symbol's arity.

-> Name.
```

The base type Category gives the category of the symbol and is defined by six constants:

CONSTANT

```
Base, Constructor,
Constant, Function, Proposition, Predicate: Category.
```

Since the Syntax module is not dedicated to the representation of Gödel programs, Name must also support the representation of names other than flat names. For this the function

```
FUNCTION SimpleName :
```

String

-> Name.

is used; the argument can be any string.

Object types are represented by ground terms built from the following two functions:

```
FUNCTION BType :
```

```
Name % Name of base type symbol. -> Type.
```

FUNCTION Type :

```
Name % Name of constructor symbol.

* List(Type) % List of argument types.

-> Type.
```

The Type function represents a compound type with its arguments in a list, and the BType function represents a base type. This strategy follows a principle of good logic programming style (see [9]) that the top-level function symbol of a term should express maximum information about the term.

Type parameters are represented by ground terms using the function Par:

```
FUNCTION Par :
```

```
String % String representing the parameter name.

* Integer % Parameter index.

-> Type.
```

The index argument is provided so that type parameters can be renamed by simply incrementing the index. This needs to be done, for example, when finding the type of a term (see the algorithm in [6]).

In a similar way to types, object terms are represented by functions of type Term:

FUNCTION CTerm :

Name % Name of constant symbol.

-> Term.

FUNCTION Term :

Name % Name of function symbol. * List(Term) % List of argument terms.

-> Term.

and object atoms by functions of type Formula:

FUNCTION PAtom :

Name % Name of proposition symbol.

-> Formula.

FUNCTION Atom :

Name % Name of predicate symbol.

* List(Term) % List argument terms.

-> Formula.

Of course, since this is a *ground* representation, object-level variables are represented by ground terms at the meta-level. Like those used to represent parameters, these terms also have an index argument, in this case to facilitate standardisation apart.

FUNCTION Var :

String % String representing the variable name.

* Integer % Variable index.

-> Term.

Representations of formulas, which are all terms of type Formula, are built from terms representing atoms, the constant Empty (representing the empty formula), and functions representing connectives. Among these are the unary function ~', binary functions &', \\', ->', <-' and <->'. Quantifiers are represented by

FUNCTION All, Some :

List(Term) % List of quantified variables.

* Formula % Quantified formula.

-> Formula.

and commits by

FUNCTION Commit: % Full Goedel commit.

* Formula in the scope of this commit.

-> Formula.

Lastly, there are four functions to represent four different flavours of conditional, of which the most sophisticated is

```
FUNCTION ISTE: % Quantified IF-THEN-ELSE.
List(Term) % List of quantified variables.

* Formula % Condition.

* Formula % Then part.

* Formula % Else part.

-> Formula.
```

5 Representing a Gödel Program in Gödel

We now come to the main topic of this paper, which is the structure of terms of type Program. Each Program term represents an entire Gödel object program, including its module structure, language declarations, control declarations and statements. It is actually the flat form of the object program that is represented; in this form every symbol has a unique name and there is no overloading.

Clearly, a dictionary structure of some kind is required to keep all these components together and readily accessible in one term. Unfortunately, there is no convenient logical data structure that will allow us to access the data in constant time. It is well-known among compiler constructors that users (or in our case, perhaps automatic program synthesisers) sometimes declare large numbers of symbols in a lexical order, causing catastrophic degradation in the performance of simple binary tree dictionaries because the ordered insertion creates linear structures; a balanced tree dictionary is therefore appropriate. We also observe that lookup operations are performed very much more frequently than update operations on the Program structure, so the additional cost of rebalancing after insertions and deletions is not significant. We have chosen (arbitrarily) to use AVL-tree dictionaries, although other schemes (such as 2-3 trees) are available which, like AVL-trees, guarantee logarithmic time for lookup, insertion and deletion. Algorithms for insertion and deletion can be found in [12]; they are straightforward to code as Horn-clauses, see for example [2, 11].

In accordance with the principle of encapsulation, the predicates that manipulate dictionaries are provided by a subsidiary module AVLTrees that is imported into the local part of the Programs module (and is therefore invisible to the users of Programs). Each dictionary associates a key and a value. AVLTrees exports the constructor AVLTree/1 so that the dictionary has the parametric type AVLTree(a), where parameter a is instantiated to the type of the value the AVL-tree associates with the key. The key is always of type String.

At the top level, every term of type Program has the 4-place function Program, whose declaration is

```
FUNCTION Program:

String % Name of the main module.

* AVLTree(ModuleDefinition) % Module structure.

* Language % Flat language of the program.

* AVLTree(ModuleCode) % Statements and delays.

-> Program.
```

The four arguments represent the three main components of a Gödel program: the module structure (represented by the first two arguments), the flat language, and the program statements and delay declarations expressed in this flat language. We consider each of these in turn.

5.1 Representing the Module Structure

The module structure of a Gödel program is a tree rooted at the main module. The set of modules making up the program form the nodes of the tree, and the edges are formed by import declarations. The edges can be divided into two classes, depending on whether the import declaration is in the local part or the export part of the importing module.

It would, of course, be possible to use this tree structure directly to represent itself. However, it is more convenient to use a dictionary that simply associates the name of each module with the names of the modules that it imports. This structure has less duplication, is easier to update, is more appropriate to the questions usually asked of it, and has the useful property that the representation of each node is independent of its child nodes.

The module structure is represented by a dictionary of type

AVLTree(ModuleDefinition)

where the keys are module names. There is one function of type ModuleDefinition:

```
FUNCTION ModDef :
```

```
OModuleKind % What kind of module this is.

* List(String) % Import declarations in export part.

* List(String) % Import declarations in local part.

-> ModuleDefinition.
```

and the type OModuleKind is defined by

```
CONSTANT NormalKind, ClosedKind, ModuleKind: OModuleKind.
```

These constants indicate whether the named module has an ordinary export and local part, is closed, or has a MODULE keyword in its local part and no export part, respectively.

For example, if on looking up the name "Hats" in the module structure we obtain the term

```
ModDef(NormalKind, [], ["Lists"])
```

then Hats is an ordinary module that has the declaration IMPORT Lists in its local part.

5.2 Representing the Program Language

The structure of the term used to represent the flat language of the object program has an important effect on the efficiency of the system, and it must meet several different requirements.

1. It must contain a representation of the declaration of every symbol in the program.

- 2. It should be able to act as the symbol table for the parser, and handle overloading. When the Gödel parser meets a declared name in the program source, it needs to look up that name in the symbol table and recover a list of all the symbols that have that declared name.
- 3. It should allow access to the declaration of any symbol given its flat name. Speed is important since the declaration of every symbol in an expression must be examined during the process of validating the expression with respect to a language, and such validations are performed frequently in routine meta-programming.
- 4. It is often necessary to validate an expression with respect to one of the various views of the program language, such as the export language of a specific module. It should therefore be possible to retrieve any of these views from the program language, and do so at reasonable cost.

We also consider it important that the representation is as compact as it can be while meeting the above requirements.

A naive approach to representing the language structure might be as a simple dictionary linking flat names with their declarations. For example, the string

"Hats.Topper.Constant"

might represent the flat name of the constant Topper in the module Hats, and could be used as a key to index the declaration of this constant. However, this scheme does not meet requirements 2 and 4 very well.

To solve this problem we make use of the internal structure imposed on the Name type in Syntax. We can then make use of all the components of the name to minimise the number of comparisons that are made for each access. The idea is to use nested dictionaries: the outer containing an entry for each module, which entry is in turn a dictionary linking each declared name in the module with all the symbols declared in the module with that declared name, and their declarations.

As far as the representation of syntactic expressions is concerned, any name can appear anywhere. The Syntax module is unaware of the concepts of module, category and arity, even though they appear in the Name structure. However, when a declaration for a name is inserted into the representation of a program, the Programs module ensures that the components of the name are consistent with its declaration. We can therefore safely assume that any name that has the string "Hats" as its module component is declared in module "Hats" or has no declaration at all.

The flat language of the object program and the other flat languages it defines are represented by terms of type Language, formed from the function¹

FUNCTION Language:

AVLTree (ModuleDescriptor)

-> Language.

¹This function is a remnant of a previous design incarnation; it is not essential for the representation, but gives the term representing the program language a simple (base) type.

The key for the dictionary AVLTree(ModuleDescriptor) is the name of a module, and the base type ModuleDescriptor is defined by

```
FUNCTION Module :
```

Accessibility % Which symbols are accessible.

- * CategoryTable % Dictionary of symbols.
- -> ModuleDescriptor.

The Accessibility argument is present to satisfy requirement 4. It is a flag that can take two values:

BASE Accessibility.

CONSTANT Exported, Hidden: Accessibility.

The accessibility flag determines the role that this module plays in the language as a whole by indicating which of the symbols declared in the module are actually present in the language. If the accessibility of the module is Hidden, all the symbols it declares are present; if its accessibility is Exported only those symbols declared in the export part of the module are present in the language.

In the representation of flat language of the program, all the module descriptors have an accessibility of Hidden. In, for example, the representation of the flat language of some component module (the language in which the statements of the module are written) the module descriptor for the module itself has accessibility Hidden; the only other module descriptors present are those for the modules it imports, and they all have their accessibilities set to Exported.

Different views of the program language are easily constructed in this representation. For example, to find the flat language of a module M, first use the representation of the module structure to find all the modules M imports, directly or indirectly. Extract the ModuleDescriptor terms for these modules from the program language, set their accessibility to Exported and place them in a new dictionary. Finally, add to this dictionary the ModuleDescriptor for M with accessibility Hidden.

Since there are typically only a dozen or so modules in a medium-sized Gödel program, this is not a large computation. In an implementation using something like the structure-sharing techniques of the WAM, this procedure is also quite space efficient, because the representations of different views of the same language share the bulk of their structure.

In an early version of the ground representation² the module languages were precalculated, so the entry for each module in the language representation included the declarations of all symbols accessible in that module instead of just those symbols declared in the module. Although computationally efficient, this made the language representation very large because each declaration had to appear many times. This is a valid approach, but the space saving seems to be more important than the small additional computation. The size of the representation is however a critical factor at higher meta-levels, where the representation is itself represented; unless special techniques are used these terms quickly become very large indeed.

²Due to Alistair Burt

The other argument of the ModuleDefinition structure is a term describing all the symbols declared in this module. This term has type CategoryTable.

-> CategoryTable.

As a slight optimisation, this dictionary is split into two parts. Since it is part of the flat name, we can use the category of a symbol as an index to reduce the overhead of locating its entry in the language representation. However, we have also to meet requirement 2 and it is crucial to the usability of the system that the parser is as fast as possible. When the parser meets a symbol in its input, it can't tell the category of the symbol in advance, but it can tell from the context whether the symbol is part of a type or part of a formula. We can therefore divide the symbols into two classes without compromising the efficiency of the parser, whereas if we separated all six categories, the parser would have to search four dictionaries for every symbol it encountered while parsing a statement or goal.

The two AVL-trees associate the declared name of a symbol with the list of declarations with this declared name in this module and class. Linear search is completely adequate here; overloading is uncommon so there is usually only one entry in the list. The representation used for declarations encodes the category, and where appropriate the arity, of the symbol so that the correct declaration is uniquely identified by the flat name.

Every symbol is described by a structure of type SymbolDescriptor with the following function:

FUNCTION Symbol:

Accessibility

- * Declaration
- -> SymbolDescriptor.

The Accessibility component is the same as the flag that guards the entire module descriptor, but here it indicates where the symbol is declared. An accessibility of Exported indicates a symbol declared in the export part of the module; such symbols are always visible regardless of the accessibility of the module. Hidden indicates a symbol declared in the local part, which is only visible if the accessibility of the module is also Hidden.

Finally, there are constants of type Declaration to represent the declarations of base and proposition symbols, and functions with range type Declaration to represent the declarations of constructor, constant, function and predicate symbols together with the attributes, such as type, that these declarations provide.

```
FUNCTION ConstructorDecl :
                                 % The arity of the constructor.
   Integer
-> Declaration.
FUNCTION ConstantDecl :
                                 % The type of the constant.
   Type
-> Declaration.
FUNCTION FunctionDecl :
                                 % The arity of the function.
   Integer
                                 % Its indicator.
 * FunctionInd
 * List(Type)
                                 % Its domain type.
 * Type
                                 % Its range type.
-> Declaration.
FUNCTION PredicateDecl:
                                 % The arity of the predicate.
   Integer
 * PredicateInd
                                 % Its indicator.
 * List(Type)
                                 % Its domain type.
-> Declaration.
```

The types FunctionInd and PredicateInd and the constants and functions that define them are declared in the export part of Programs and so are public. These represent the indicator component of functions and predicates declared in the object program in a straightforward way.

5.3 Representing the Program Code

The final element of the representation is the fourth argument of the Program function, the dictionary containing representations of the object program's statements and control declarations. By looking up the flat name of a predicate symbol in this dictionary all the statements in the definition of the predicate, and all the delay declarations for the predicate can be found. Note that there is no predicate exported by the Programs module that is capable of returning the statements (or delay declarations made in the local part) of a closed module; these are completely protected from user access. In practice we do not need to represent them, and only the delay declarations that appear in the export parts of the closed modules are actually present in the entries for these modules in the code dictionary.

It is convenient to organise the code dictionary analogously to the language dictionary, with two nested AVL-trees exploiting the flat name structure. The outer structure, keyed on the module name, has type AVLTree(ModuleCode); the ModuleCode type is defined by

```
FUNCTION Code :
```

Integer

- * AVLTree(List(PredicateDefinition))
- -> ModuleCode.

The Integer argument here is not part of the representation in logic, but is used in the implementation of Succeed and the predicates similar to it that simulate Gödel computations for representations of object goals with respect to representations of object programs. Rather than interpreting the representation directly, it is more efficient to reflect the representation of program and goal down to the object level, perform the computation directly to obtain a computed answer, and reflect this answer back up to its meta-level representation. The programmer is of course completely unaware of this implementation technique. To facilitate this technique, and reduce the overhead of reflection, the system retains the code compiled by the reflection process and only recompiles a module of an object program when necessary. Recompilation is required when the module represented in the object program to be executed is different from a module with the same name that was previously reflected to produce the compiled code. This integer argument acts as a version number and allows the system to keep track of such changes.

Dividing the representation of the object program code into separate modules allows the reflection operation to recompile module by module only those modules that have changed since the last time they were reflected, rather than having to recompile the whole object program. A better scheme would be to actively reflect only predicates whose definition has changed, or even to operate statement by statement. This leads naturally towards a representation for dynamic object theories like that used in MetaProlog [1].

The code portion of each module is represented by a term of type

AVLTree(List(PredicateDefinition))

which is keyed by the declared names of predicates declared in the module. Overloading of course means that there can be more than one such predicate per declared name, but these can be distinguished by their arities. Hence there is a list of PredicateDefinition terms for each declared name, each with the function

FUNCTION PredDef :

It does not make sense for a predicate to have delay declarations in both the export part and the local part of the module that declares it, so one of the lists of representations of delay declarations is always empty.

The base type Delay is not exported by Programs. Instead delay declarations appear to the programmer in two parts: the head atom, represented by a term of type Formula, and the condition, represented by a term of type Condition. The Delay function joins these components in an Delay term.

FUNCTION Delay :

Formula

- * Condition
- -> Delay.

Delay conditions are represented by terms built from functions of type Condition in an obvious way.

```
CONSTANT TrueCond : Condition.

FUNCTION Nonvar, Ground :
    Term
-> Condition.

FUNCTION And, Or :
    Condition
    * Condition
-> Condition.
```

6 Conclusion

We have described a scheme for repesenting Gödel object programs in Gödel. This is not the fearsome task it might appear to be at first sight. By presenting the representation to the programmer as an abstract data type, providing an exhaustive library of predicates to perform standard operations on the data type, and also providing a program compiler to generate the representation from the object program source, the labour and complexity of writing meta-programs in the ground representation is considerably reduced. When writing a meta-program in Gödel one can start on the problem straight away, without having to set up the representation first.

A prototype implementation of the Gödel modules Syntax and Programs has been produced, based on the above representation. It has been and is being used successfully by students and researchers at Bristol and elsewhere to build programs such as interpreters, theorem provers, partial evaluators, declarative debuggers, and knowledge assimilators.

The reader's attention is especially drawn to [4], in which some experiments in partial evaluation of Gödel meta-programs are reported. These suggest that, if the meta-program is carefully written, a large part of the computational overhead of using the ground representation can be compiled away. Partial evaluation is also effective in reducing the overhead that results from using an abstract data type when the underlying engine is highly optimised for pattern matching. In addition, we have the prospect of increased parallelism obtained by eliminating the sequential properties of Prolog's extra-logical features. Finally, a small computational overhead seems a more than reasonable price to pay for delarative semantics.

More research needs to be done on the topic of compilation techniques for metaprograms, in order to reduce the overhead further. It will also be interesting to consider how the underlying system can provide support for the ground representation, for example by using implicit reflection to implement meta operations such as unification of object terms.

This research described here is, of course, only the first step on the road to effective use of the ground representation, but we contend that we *can* have the full power of the ground representation with at least the convenience and (given sophisticated compilation

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techniques and parallelism) efficiency of the non-logical route; and we can have all this without straying from first-order logic.

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