Różniczkowanie numeryczne

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Forward difference:

$$\frac{df}{dx} = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

Backward difference:

$$\frac{df}{dx} = \lim_{h \to 0} \frac{f(x) - f(x - h)}{h}$$

Taylor expansion of f(x+h) about x

$$f(x+h) = f(x) + (x+h-x)f'(x) + \frac{1}{2}(x+h-x)^2 f''(x) + \dots$$
$$f(x+h) = f(x) + hf'(x) + \frac{1}{2}h^2 f''(x) + \dots$$
$$f'(x) = \left[\frac{f(x+h) - f(x)}{h}\right] + \frac{h}{2}f''(x)$$

what is the ideal h? small, but can't be 0 -rounding error is bad if h is too small

Central difference

$$\frac{df}{dx} = \lim_{h \to 0} \frac{f(x+h/2) - f(x-h/2)}{h}$$