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Be sure to use correct units and significant figures throughout all your answers.

Showing full work for answers will unlock possible partial credit. Save as .pdf and upload to Canvas assignment.

1. The average human hair grows 1.5cm longer per month. After a 2 hour 45 minute physics lab how much longer will your hair be in μm from the time lab started? FYI: average human hair width is 17-180 μm .

$$0.15 \frac{\text{m}}{\text{mo}} \cdot \frac{1\text{mo}}{30.416 \text{days}} \cdot \frac{1\text{day}}{24 \text{hrs}} \cdot \frac{1\text{hr}}{60 \text{min}} \cdot 165 \text{min} = 5.661 \times 10^{-5} \text{ m} = 56 \mu\text{m}$$

$$2 \text{h } 45 \text{ min} = 165 \text{ min}$$

2. (a) How many regulation sized ping pong balls would fill the entire volume of a standard size faculty member's office in the College of Arts & Sciences (125sqft with 9ft ceilings)? Assume you can obtain the optimal sphere packing fraction of 74% volume. radius of PPTB: $\frac{1.57}{2} = .0625 \text{ ft}$

$$V_{\text{facility}} = 125 \text{ ft}^2 \cdot 9 \text{ ft} = 1125 \text{ ft}^3$$

$$\text{Packing fraction: } N \cdot .74 = 832.5 \text{ ft}^3$$

$$V_{\text{PPTB}} = \frac{4}{3} \pi (0.0625 \text{ ft})^3 = .00102 \text{ ft}^3$$

$$\frac{V_{\text{facility}}}{V_{\text{PPTB}}} = \frac{832.5 \text{ ft}^3}{.00102 \text{ ft}^3} = 814058 \text{ ping pong balls}$$

- (b) Same question, but for regulation tennis balls.

$$r \text{ of tennis ball} = \frac{2.635 \text{ in}}{2} = 1.3175 \text{ in} = .10979 \text{ ft}$$

$$V_{\text{TB}} = \frac{4}{3} \pi (.10979 \text{ ft})^3 = .0055 \text{ ft}^3$$

$$\frac{V_{\text{facility}}}{V_{\text{TB}}} = \frac{832.5 \text{ ft}^3}{.0055 \text{ ft}^3} = 150171 \text{ tennis balls}$$

3. How long is the Legacy walk (including an uncertainty) in meters from where it starts opposite the roadway from Henderson Building to where it ends at the landscaping below the Eagle/Plane sculpture? You must devise a physical means of measuring the distance, NOT using a map or app. Explain your measurement method including an estimate of your uncertainty. Error propagation will probably be necessary, if so show it.

$$1192.5 \pm 10 \text{ David Feet} \cdot \frac{32 \text{ cm}}{1 \text{ David ft}} \cdot \frac{1 \text{ m}}{100 \text{ cm}} = 381.6 \pm 3.2 \text{ m}$$

Our method of measuring the Legacy walk was to measure the number of shoe lengths it was.
My shoe is about 32cm.

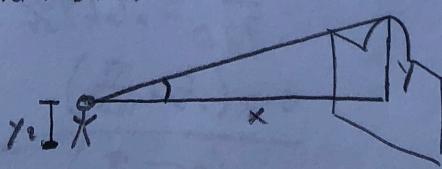
The uncertainty is based off of accidentally missed counting & walking perfectly with feet exactly in line.

4. Devise a measurement method to determine the vertical height from ground level to the top of the telescope dome of the COAS Building, without the ability to be on the building's roof. Describe your method and give an estimation for this height. Hint: Think how you would estimate the height of a tree without climbing it.

$$x = 133 \text{ David Feet} \cdot \frac{32 \text{ cm}}{1 \text{ David ft}} = 4256 \text{ cm}$$

$$\theta = 55^\circ \text{ from Rohit's forehead}$$

$$y_1 = 170 \text{ cm}$$



$$144.5^\circ$$

$$\tan \theta = \frac{y}{x}$$

$$y = x \tan \theta$$

$$y = 4256 \tan(55^\circ)$$

$$y = 6079.2 \text{ cm}$$

$$y + y_1 = 6079.2 \text{ cm} = 62 \pm 5 \text{ m}$$

5. The equation that describes the motion of an object is $s = \frac{1}{2}at^2 + v_0t + s_0$, where s is position, a is acceleration, t is time, and v is velocity. Using standard SI units, show that the dimensional units in the equation are consistent. $a = \frac{\text{m}}{\text{s}^2}$ $v = \frac{\text{m}}{\text{s}}$ $s = \text{m}$ $t = \text{s}$

$$m = \frac{1}{2} \left(\frac{\text{m}}{\text{s}^2} \right) (\text{s})^2 + \left(\frac{\text{m}}{\text{s}} \right) (\text{s}) + \text{m}$$

$$m = \frac{\text{m}}{\text{s}^2} \cdot \text{s}^2 + \frac{\text{m}}{\text{s}} \cdot \text{s} + \text{m} \rightarrow m = m + m + m \rightarrow m = m$$

6. Give the number of significant figures in each of the following numbers:

a. 112.4 ± 0.2 4

b. 10.0 3

c. 3.14159 6

d. 1700 2

e. 1250 ± 50 3

f. 5.0030 5

g. 9.33×10^3 3

h. 0.02240 4

7. Discuss the merits and drawback of using a person's foot as a length standard in terms of accessibility, invariability, indestructibility, reproducibility, and uncertainty. Consider both (a) a particular person's foot, and

Accessibility- a) Can be hard if you need the foot of Queen Elizabeth II
b) Everyone (usually) has a foot, very easy access

Indestructibility - a) + b) Most peoples' feet are fairly indestructible, excluding rare bone disorders

Invariability a) As long as the person is an adult the magnitude won't change
b) Very high variability because everyone's foot size will be slightly different

Reproducibility a) It is easy to reproduce results when you use only 1 foot from a specific person
b) Every person's foot is a slightly different size so no reproducibility when using just "a foot" instead of "her foot"

8. You measure the radius of a wheel to be 4.16cm. If you multiply by 2 to get the diameter, should you record the result as 8cm or 8.32cm? Justify your answer.

8.32cm; 2 is an exact constant and effectively has an infinite amount of significant figures. When multiplying you stick with the lowest amount of significant figures and 3 < 0

9. What is the percent uncertainty for each of the following measurements?

a. $3.75 \pm 0.25\text{m}$

$$\frac{.25}{3.75} \cdot 100 = 6.67\%$$

b. $116.3 \pm 0.1\text{g}$

$$\frac{.1}{116.3} \cdot 100 = .08598\%$$

10. Find the percent uncertainty in θ and in $\sin\theta$ for the two following measurements. Note: for error propagation of $\sin\theta$ the uncertainty in θ must be in radians where $180^\circ = \pi$ radians.

a. $\theta = 15.0^\circ \pm 0.5^\circ$

$$\frac{.5}{15.0} = 3.33\%$$

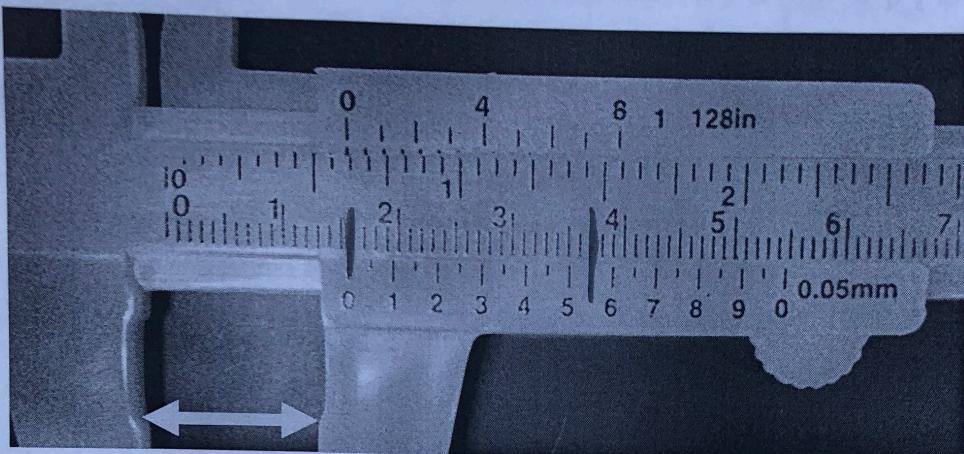
$$\frac{\sin(.5 \cdot \frac{\pi}{180})}{\sin(15 \cdot \frac{\pi}{180})} = 3.33\%$$

b. $\theta = 75.0^\circ \pm 0.5^\circ$

$$\frac{.5}{75.0} = .667\%$$

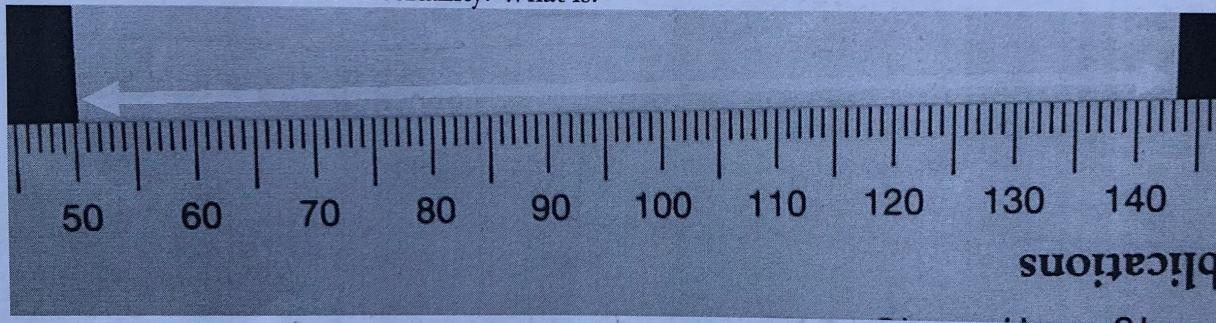
$$\frac{\sin(.5 \cdot \frac{\pi}{180})}{\sin(75 \cdot \frac{\pi}{180})} = .667\%$$

11. Given the image, what is:



- (a) The resolution of the Vernier caliper [mm]? 0.05 mm
- (b) The width reading on the Vernier caliper in [mm]? 15.55 mm
- (c) The uncertainty of the above width reading in [mm]? $\pm 0.05\text{ mm}$

12. The ruler in the image is marked to the nearest mm. Note: Each edge measurement is technically a position measurement with its own uncertainty. What is:



- (a) The resolution of the ruler in [mm]? 1 mm
- (b) The position measurement uncertainty you feel possible with the ruler in [mm]? $\pm 0.5\text{ mm}$
- (c) The width of the piece of paper in [mm]? 93 mm
- (d) The propagated uncertainty on the paper width in [mm]?

$$\begin{aligned} \delta &= \sqrt{(1.5)^2 + (1.5)^2} \\ &= \sqrt{.25 + .25} \\ &= \sqrt{.5} \approx .71\text{ mm} \end{aligned}$$