$\begin{array}{c} MA~448-Lab~\#3\\ Solving~Systems~of~ODEs~in~Matlab/Python \end{array}$

Due: 10/01/2019

1. Write a code in Matlab/Python to implement the RKF45 method to solve the following system of ODEs.

(1)
$$\begin{cases} x'(t) = x(t) - y(t) + 2t - t^2 - t^3 \\ y'(t) = x(t) + y(t) - 4t^2 + t^3 \end{cases} \quad 0 \le t \le 1$$

with the initial conditions x(0) = 1 and y(0) = 0. Note that exact solution for this system is

$$x(t) = e^t \cos t + t^2$$

$$y(t) = e^t \sin t - t^3$$

- 2. Use the Matlab's ODE solver ode45 or SciPy ODE solver solve_ivp to solve the initial value problem of (1).
- 3. Compare the results from your RKF45 code and ode45 (or solve_ivp with method="RK45") by plotting the numerical solutions and the exact solution together with appropriate labels and title.
- 4. Submit your code and the graphical output (lab3.zip) the following thru your course Canvas.