

plumeAnalyserSyntheticVertical

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```
[1]: from fumarolePlumeModel import (derivs, wind, objectiveFn, objectiveFn2,
                                     objectiveFn3, loadICsParameters, loadExptData,
                                     pathname, integrator2 as integrator)

from scipy.io.matlab import loadmat
from scipy.integrate import ode, solve_ivp
from itertools import product
import pandas
import numpy as np
import matplotlib.pyplot as plt
import matplotlib as mpl
import os, sys
import json

# Set numpy options, notably for the printing of floating point numbers
np.set_printoptions(precision=6)

# Set matplotlib options
mpl.rcParams['figure.dpi'] = 300

%reload_ext autoreload
%autoreload 2
```

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[2]: run = 3

# Import table of experimental conditions
GCTA = pandas.read_excel('./data/ExpPlumes_for_Dai/TableA1.xlsx',
                        sheet_name='CGSdata', skiprows=2,
                        names=('exptNo', 'rhoa0', 'sig_rhoa0',
                              'N', 'sig_N', 'rho0', 'sig_rho0',
                              'U0', 'sig_U0', 'W', 'sig_W',
                              'gp', 'sig_gp', 'Q0', 'sig_Q0',
                              'M0', 'sig_M0', 'F0', 'sig_F0',
                              'Ri_0', 'sig_Ri_0', 'W*', 'sig_W*'))

# Extract densities of ambient and plume, and calculate g' at the source
expt = GCTA[GCTA['exptNo'] == run]
rhoa0 = expt['rhoa0']
rho0 = expt['rho0']
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g = 981 #cm/s2
gp0 = (rhoa0 - rho0) / rhoa0 * g

parameters = pandas.read_excel('./data/ExpPlumes_for_Dai/TableA1.xlsx',
                                sheet_name='CGSparameters')
b0theoretical = parameters[parameters['property'] == 'nozzleSize']['value'].
    ↪values[0]
u0theoretical = expt['U0'].values[0]

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0.0.1 Create synthetic dataset for vertical plume and add noise

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[3]: exptNo      = 3
      plotResults = True

      V0, p = loadICsParameters(pathname, exptNo, alpha=0.09, beta=0, m=1)

      # Order of "p": alpha, beta, N, m, w
      p = list(p)
      p[1], p[4] = 0., 0. # Set "wind" entrainment coefficient (beta),
                          # and wind speed (w) to zero
      p = tuple(p)

      t1 = 30.
      dt = .1
      sexp = np.arange(0., t1 + dt, dt)
      dsexp = np.diff(sexp)

      Q0, M0, F0, theta0 = V0
      s, V = integrator(V0, p)

      sexp = np.copy(sexp)

      fig, ax = plt.subplots(1, 1, sharey=True, figsize=(4, 6))
      # ax[0].plot(V, s, '-')

      Q, M, F, theta = [V[:,i] for i in range(4)]
      b, u, gp = Q / np.sqrt(M), M / Q, F / Q

      V2 = np.array([b, u, gp]).T
      # ax[1].plot(V2, s, '-')
      # ax[1].set_xlim((-5, 30))
      # ax[1].grid()

      sexp = np.copy(s)
      dsexp = np.diff(sexp)

      ax.plot(V2, s, '-')

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ax.legend([r'radius, $b$', 'velocity, $u$', 'red. gravity, $g\backslash'$'])
V3 = V2.copy()
for i in range(3):
    noise = np.random.normal(0, .2, len(sexp))
    V3[:,i] = V2[:,i] + noise
    ax.plot(V3[:,i], s, '.', c='C%d' % i, ms=1.5)
ax.set_xlim((-5, 30))
ax.set_xlabel('Plume parameter')
ax.set_ylabel('Distance along plume axis')
ax.grid()

bexp, uexp, gpexp = [V3[:,i] for i in range(3)]

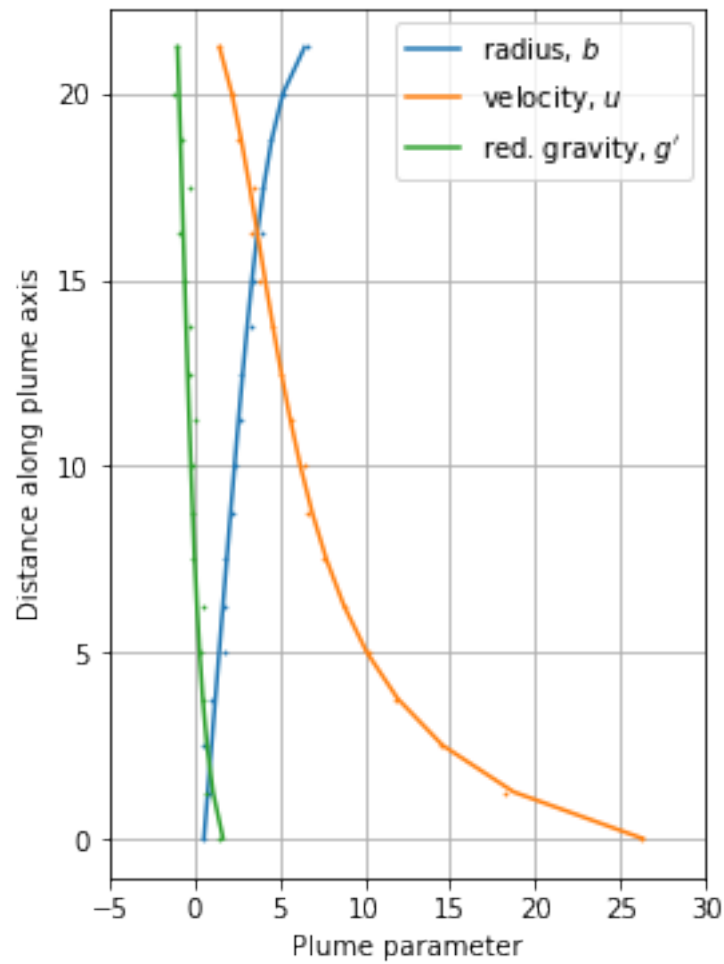
gp0 = V0[2] / V0[0]

```

/home/david/Modelling/fumarolePlumeModel/fumarolePlumeModel.py:154:

RuntimeWarning: invalid value encountered in sqrt

b, u, gp = Q / np.sqrt(M), M / Q, F / Q



0.0.2 Run jobs in parallel to search parameter space for maxima

```
[4]: from joblib import Parallel, delayed

import time
import warnings

njobs = 16
nGrid = 201                                # Number of grid points
b0Vec = np.linspace(.01, 2, nGrid) #cm
u0Vec = np.linspace(1, 30, nGrid) #cm/s
Q0Vec = u0Vec * b0Vec**2              #cm3/s
M0Vec = Q0Vec * u0Vec                 #cm4/s2
theta0 = np.pi / 2

sequence = [Q0Vec, M0Vec]

dexp = np.array([bexp, gpexp]).T

def parallel_job(Q0, M0):
    warnings.filterwarnings('ignore')

    F0 = gp0 * Q0
    v0 = [Q0, M0, F0, theta0]

    return objectiveFn3(v0, derivs, p, sexp, dexp, mode='lsq'), v0

t = time.time()
results = Parallel(n_jobs=njobs)(delayed(parallel_job)(Q0, M0)
                                for (Q0, M0) in list(product(*sequence)))
print("Job ran in %.3f s" % (time.time() - t))

## Deal out the results so as to
objFn, initialConds = [], []

for result in results:
    objFn.append(result[0])
    initialConds.append(result[1])

initialConds = np.array(initialConds)
objFn = np.array(objFn).reshape((nGrid, nGrid))
```

Job ran in 31.232 s

0.0.3 Minimization using Nelder-Mead (or other) algorithm

```
[5]: from scipy.optimize import minimize

def residual(pars, x, data=None, eps=None):
    return

# Start at random location within parameter space
v0 = initialConds[np.random.randint(0, len(initialConds))]
print("Initial vector: ", v0)
minimum = minimize(objectiveFn3, v0,
                    args=(derivs, p, sexp, dexp), method='Nelder-Mead',
                    bounds=((Q0Vec[0], Q0Vec[-1]),
                             (M0Vec[0], M0Vec[-1]),
                             (gp0*Q0Vec[0], gp0*Q0Vec[-1]),
                             (np.pi/2, np.pi/2)))
print(minimum)
Qopt, Mopt, Fopt, thetaopt = minimum.x
bopt, uopt, gpopt = Qopt / np.sqrt(Mopt), Mopt / Qopt, Fopt / Qopt

Initial vector: [ 86.467869 1108.836454 144.419094  1.570796]
final_simplex: (array([[ 7.991505, 212.085833, 12.467962,  1.570796],
 [ 7.991501, 212.085743, 12.467958,  1.570796],
 [ 7.991507, 212.085855, 12.46796 ,  1.570796],
 [ 7.991509, 212.085834, 12.467971,  1.570796],
 [ 7.991506, 212.0858 , 12.467961,  1.570796]]), array([-0.51013,
-0.51013, -0.51013, -0.51013]))
    fun: -0.510129822553647
    message: 'Optimization terminated successfully.'
     nfev: 362
      nit: 208
    status: 0
   success: True
         x: array([ 7.991505, 212.085833, 12.467962,  1.570796])

[9]: %matplotlib inline
from matplotlib.colors import LogNorm

objFn  = np.abs(objFn)
ui, bi = np.where(objFn == np.nanmax(objFn))
# objFn[objFn == 0.] = np.nan
norm   = LogNorm(vmin=1e-3, vmax=np.nanmax(objFn))
MS = 10

print("\n", "_" * 42, sep='')
```

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print("%42s" % "b,      u,      g\'")
print("-" * 42, sep='')
print("Theoretical values: %6.3f, %6.3f, %6.3f" %
      (b0theoretical, u0theoretical, gp0))
print("Optimised values:   %6.3f, %6.3f, %6.3f" %
      (bopt, uopt, gpopt))
print(r"Max of $\Theta(m,d)$: %6.3f, %6.3f, %6s" %
      (b0Vec[bi], u0Vec[ui], '-'))
print("-" * 42, sep='')

fig, ax = plt.subplots(figsize=(6, 4))

pco = ax.pcolor(b0Vec, u0Vec, objFn, norm=norm)

p_ = ax.plot(b0theoretical, u0theoretical, '.w', label=r'theoretical max.',
             markersize=MS, markeredgewidth=.3, markeredgecolor='k')

q_ = ax.plot(b0Vec[bi], u0Vec[ui], '.r', label=r'max. of $\Theta(m, d)$',
             markersize=MS, markeredgewidth=.3, markeredgecolor='k')

r_ = ax.plot(bopt, uopt, '.m', label=r'N.-M. optimum',
             markersize=MS, markeredgewidth=.3, markeredgecolor='k')

ax.set_xlabel(r'Vent radius, $b_0$/[cm]')
ax.set_ylabel(r'Vent velocity, $u_0$/[cm/s]')
leg = plt.legend()
cba = plt.colorbar(pco)
cba.set_label('Relative probability')

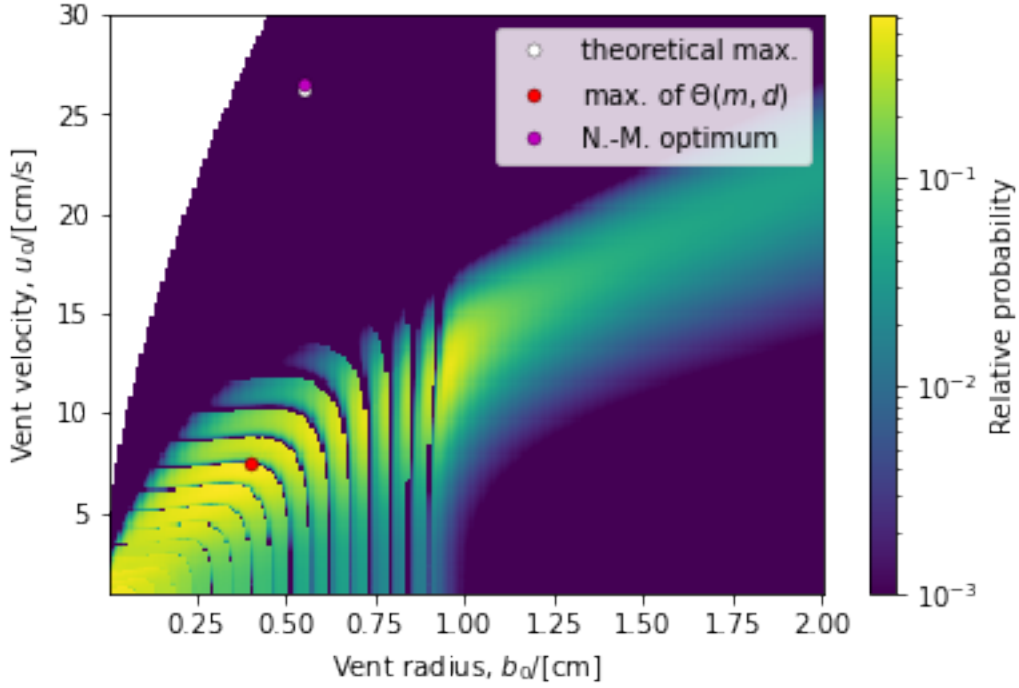
fig.savefig('images/ProbDensityFn_CA_run%d.png' % exptNo, dpi=300)

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                        b,      u,      g'
-----
Theoretical values:  0.550, 26.307,  1.670
Optimised values:   0.549, 26.539,  1.560
Max of $\Theta(m,d)$: 0.398,  7.525,  -
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```



	b	u	g'
Theoretical values:	0.550	26.307	1.670
Optimised values:	0.549	26.539	1.560
Max of $\Theta(m, d)$:	0.398	7.525	-

0.0.4 Comparison of final plot with synthetic data

```
[10]: s, V = integrator(minimum.x, p)

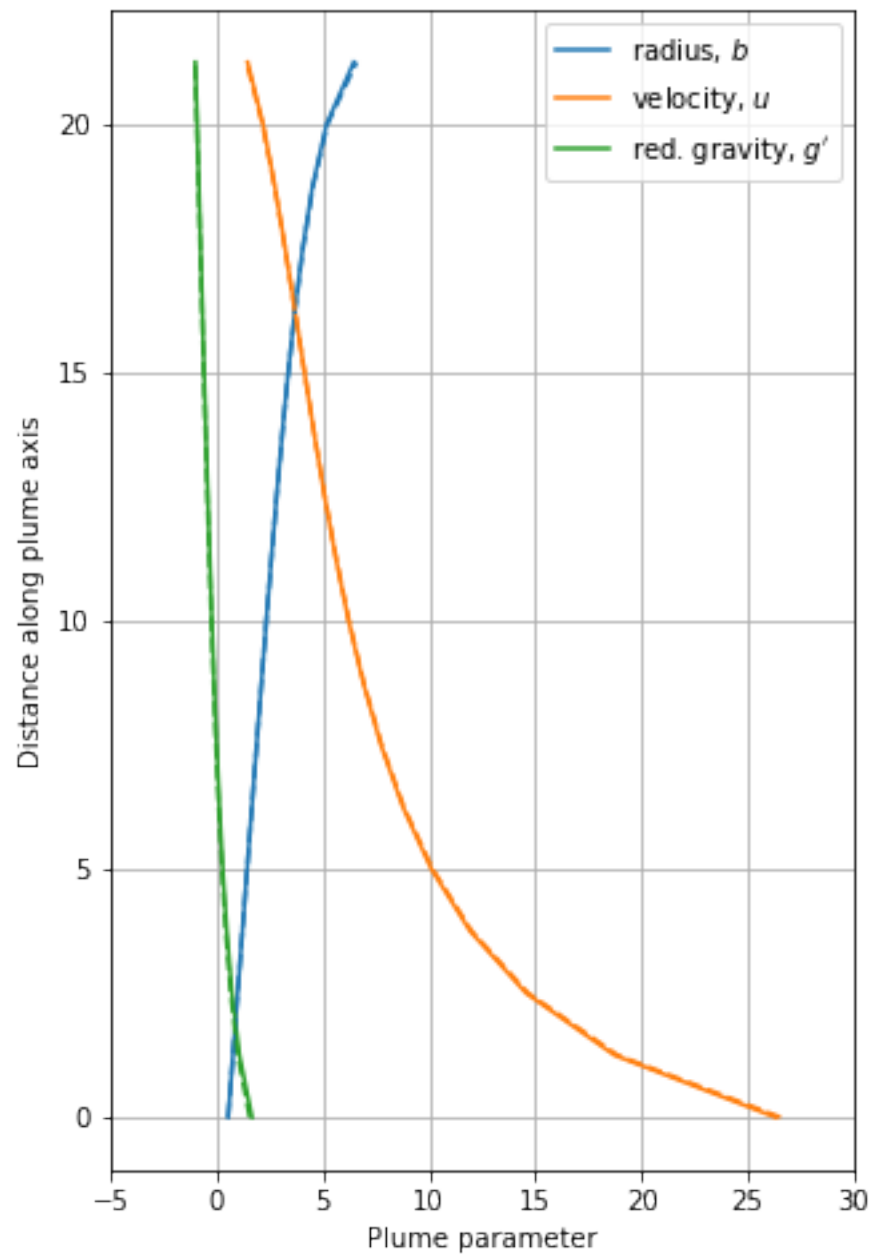
Q, M, F, theta = V.T
b, u, gp = Q / np.sqrt(M), M / Q, F / Q
Vfinal = np.array([b, u, gp])

fig, ax = plt.subplots(figsize=(5, 8))

ax.plot(V2, s, '-')
ax.legend([r'radius, $b$', 'velocity, $u$', 'red. gravity, $g\backslash'$'])
for i in range(3):
    ax.plot(Vfinal[i], s, '--', c='C%d' % i)

ax.set_xlim((-5, 30))
ax.set_xlabel('Plume parameter')
ax.set_ylabel('Distance along plume axis')
```

```
ax.grid()
```



```
[ ]: # from lmfit import minimize, Parameters, Model  
  
# params = Parameters()  
# # minimum = minimize(objectiveFn3, params, args=(derivus, p, sevp, dexp))
```

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[ ]:
```