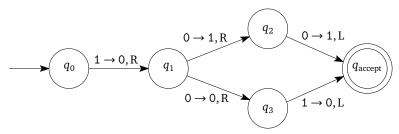
Prework 7.3a: Languages in NP

Write your preliminary solutions to each problem and submit a PDF on Canvas. The names in brackets indicate the subset responsible for presenting the problem.

1. [Ky, Todd, Levi] A formula in Boolean (i.e., propositional) logic is *satisfiable* if there are 1/0 values (i.e., T/F values) that can be assigned to the variables to make the statement true. See pp. 14–15 if you need to refresh your memory. Determine whether the following formula is satisfiable.

$$(x \lor y) \land (x \lor \bar{y}) \land (\bar{x} \lor y) \land (\bar{x} \lor \bar{y})$$

- 2. [Grace, Meghan, Ben] Let $SAT = \{ \langle \phi \rangle \mid \phi \text{ is a satisfiable Boolean formula} \}$. Show that $SAT \in NP$. Specifically, explain what a certificate is in this example, and estimate the running time of a verifier when the input formula $\langle \phi \rangle$ has n variables.
- 3. [Allie, Micah] A *coloring* of a graph is an assignment of colors to its vertices so that no two adjacent vertices have the same color. Let $3COLOR = \{\langle G \rangle \mid G \text{ is colorable with 3 colors}\}$. Estimate the running time of a verifier when the input is a graph with n vertices. Is $3COLOR \in NP$?
- 4. [Curtis, Connor, Andrew] The following nondeterministic TM has two nondeterministic branches when executed on input *w* = 101. For each of these branches, draw the tableau whose rows are the configurations of the NTM, as in Figure 7.38 on page 305 (page 277 in the 2nd edition).



5. [Joshua, David] A *window* in a tableau is a 2 × 3 rectangle of table cells. There are examples of "legal" windows on page 308 (p. 280 in 2/e). For the tableau in question 3 that represents the accepting branch, find legal windows that correspond to (a) a rightward tape move, (b) a leftward tape move, and (c) something else.

BEGIN YOUR SOLUTIONS BELOW THIS LINE