



# Deep Learning Seminar Day-3

Master of Science in Signal Theory and Communications
TRACK: Signal Processing and Machine Learning for Big Data

Departamento de Señales, Sistemas y Radiocomunicaciones E.T.S. Ingenieros de Telecomunicación Universidad Politécnica de Madrid

### Recurrent Neural Networks (RNN) concepts

#### What's new with Recurrent Nets?

- They allow us to operate over sequences of vectors
- Applications areas are broad:
  - Signals: video, speech, sensors,....
  - Time series: financial series, log messages,...
  - Sequence of characters: Natural Language Processing,...

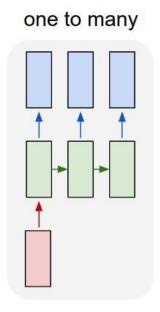
RNN can use sequences in the input, the output, or both.

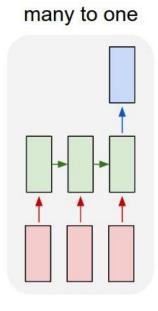
Tenemos entradas salidas y estados

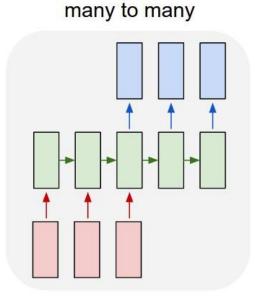


### Recurrent Neural Networks (RNN) concepts

one to one







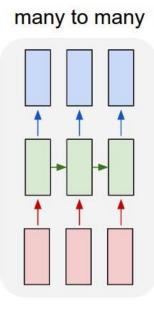


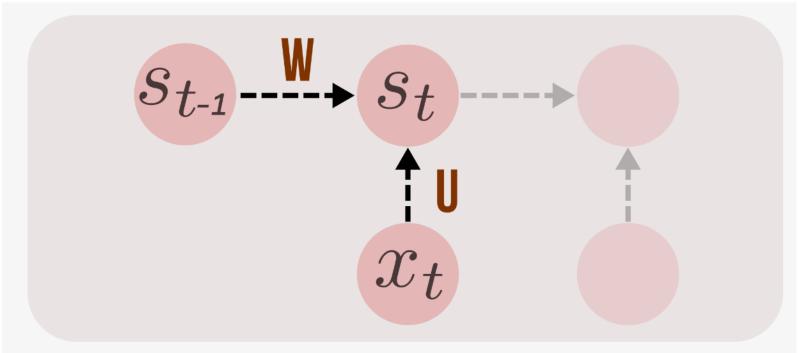
Image description using text Emotion Recognition

Language Model Machine Translation Video frame labelling

Phoneme Recognition



 RNNs combine the input vector with their state vector with a fixed (but learned) function to produce a new state vector.

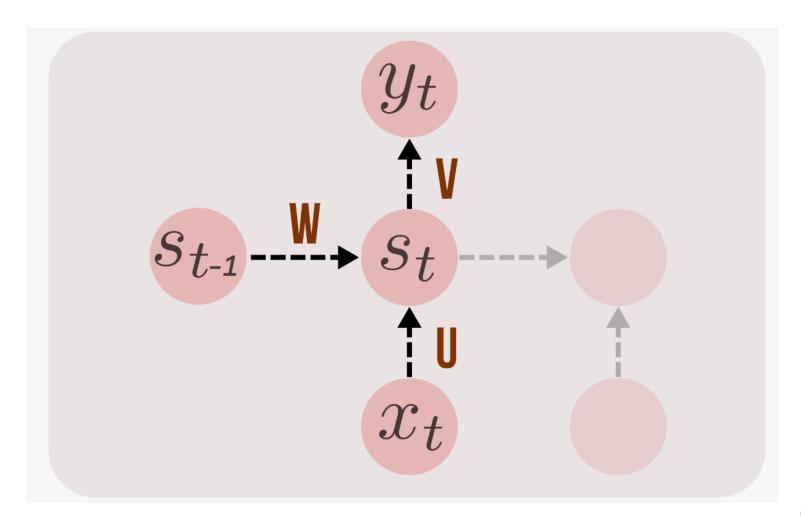


Moving from one state to a new one using conections (W) and activation functions

$$s_t = tanh(Ux_t + Ws_{t-1}),$$



OUTPUT  $y_t$ logits = tf.matmul(state, V) + b
predictions = tf.nn.softmax(logits)





## RNN essentially describe programs:

inputs + some internal variables.

 In fact, it is known that <u>RNNs are Turing-Complete</u> in the sense that they can to simulate arbitrary programs (with proper weights).

...path to AI??

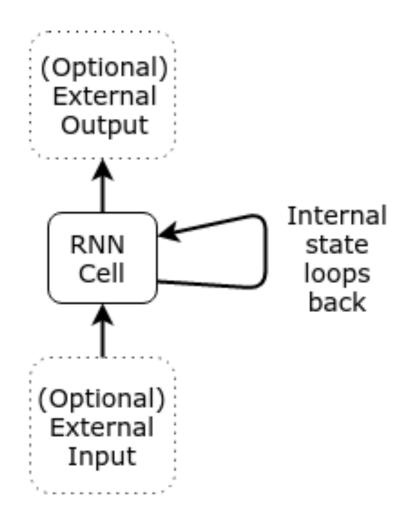
.... But "forget I said anything."

Andrej Karpathy http://karpathy.github.io/2015/05/21/rnn-effectiveness

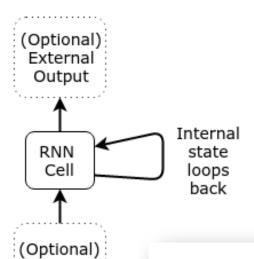


# Written Memories: Understanding, Deriving and Extending the LSTM

http://r2rt.com/written-memories-understanding-deriving-and-extending-the-lstm.html







External

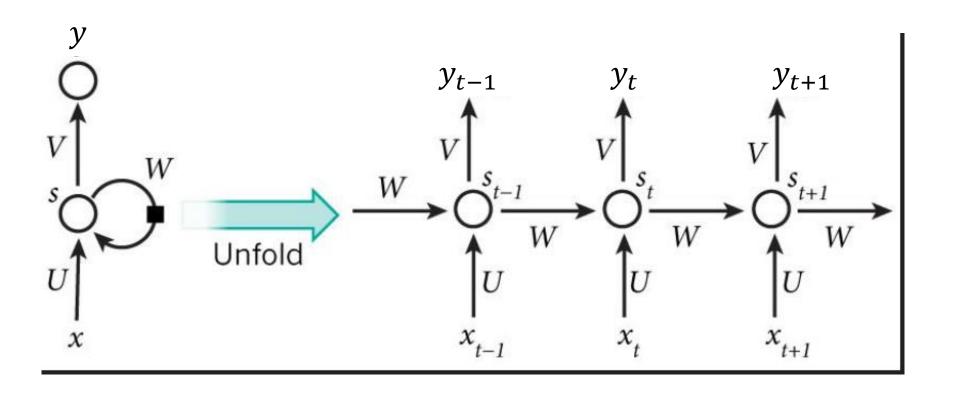
Input

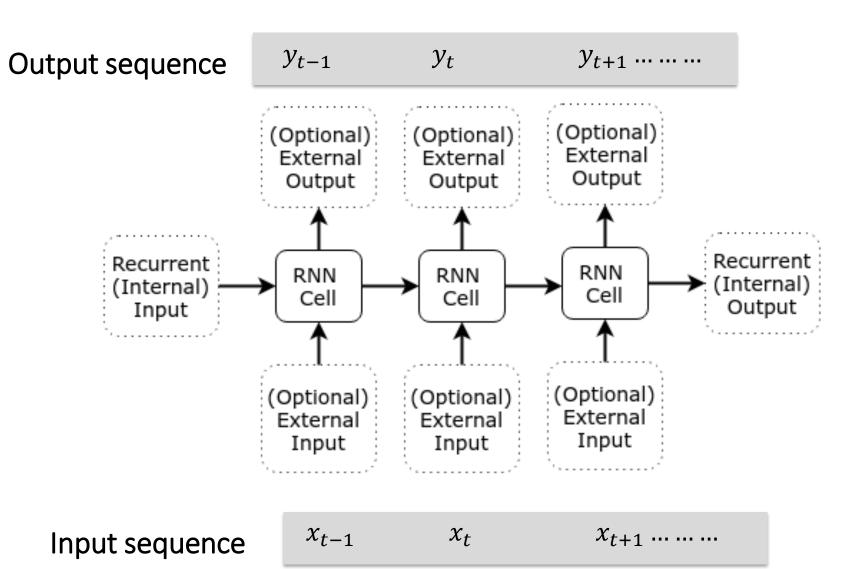
Here is the algebraic description of the RNN cell:

$$\left(egin{array}{c} s_t \ o_t \end{array}
ight) = f \left(egin{array}{c} s_{t-1} \ x_t \end{array}
ight)$$

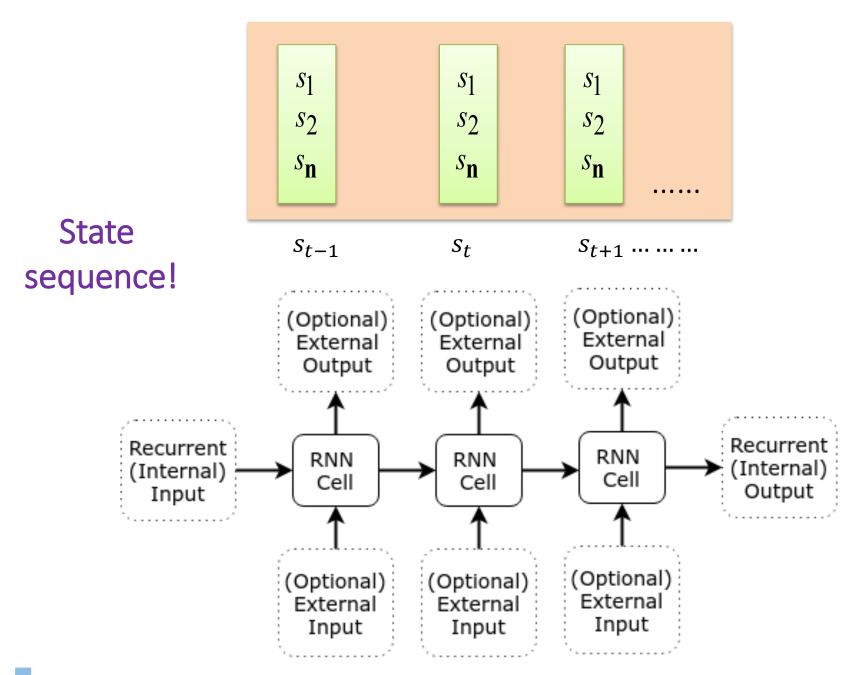
#### where:

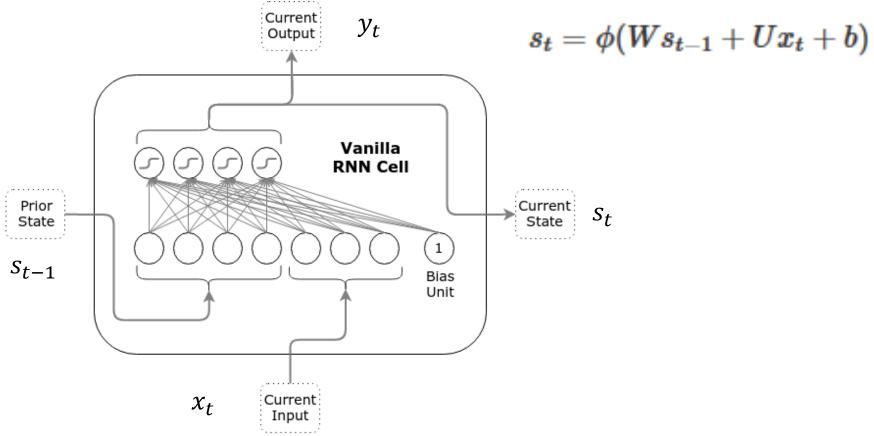
- $s_t$  and  $s_{t-1}$  are our current and prior states,
- o<sub>t</sub> is our (possibly empty) current output,
- $x_t$  is our (possibly empty) current input, and
- f is our recurrent function.











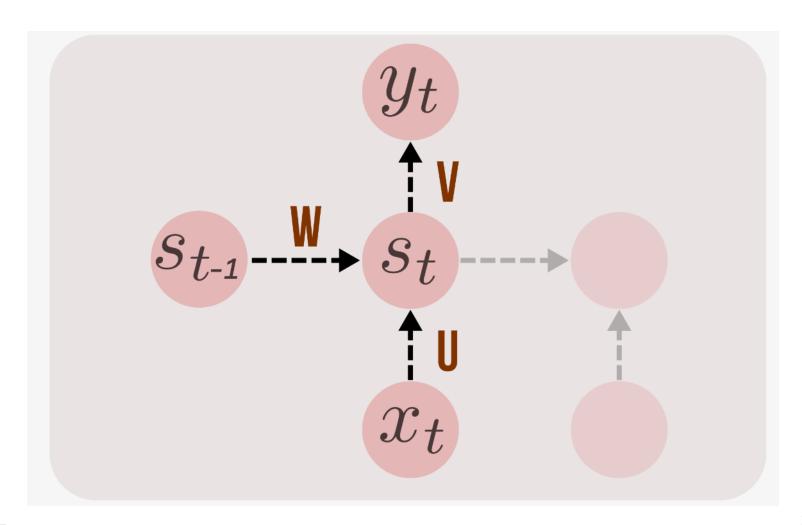
where:

- $\phi$  is the activation function (e.g., sigmoid, tanh, ReLU),
- $s_t \in \mathbb{R}^n$  is the current state (and current output),
- $s_{t-1} \in \mathbb{R}^n$  is the prior state,
- $x_t \in \mathbb{R}^m$  is the current input,
- $W \in \mathbb{R}^{n \times n}$ ,  $U \in \mathbb{R}^{m \times n}$ , and  $b \in \mathbb{R}^n$  are the weights and biases, and
- n and m are the state and input sizes.



#### TRAINING RNN: W, U, V?

- BPTT: Backpropagation Through Time
- Truncated





## Backpropagation Through Time (BPTT)

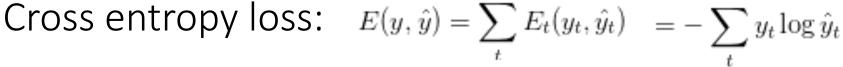
- Because the parameters are shared by all time steps in the network
- The gradient at each output depends not only on the calculations of the current time step, but also the previous time steps.

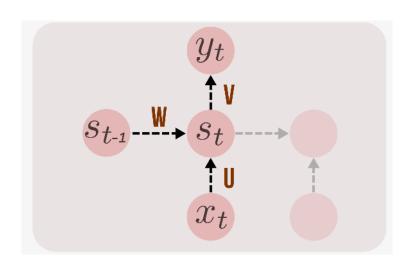
http://www.wildml.com/2015/09/recurrent-neural-networks-tutorial-part-2-implementing-a-language-model-rnn-with-python-numpy-and-theano/



## Backpropagation Through Time (BPTT)

$$s_t = \tanh(Ux_t + Ws_{t-1})$$
  
 $\hat{y}_t = \operatorname{softmax}(Vs_t)$ 





- The output value does depend on the state of the hidden layer,
- which depends on all previous states of the hidden layer
- and thus, all previous inputs



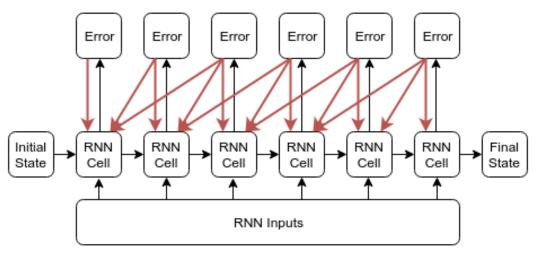
## Backpropagation Through Time (BPTT)

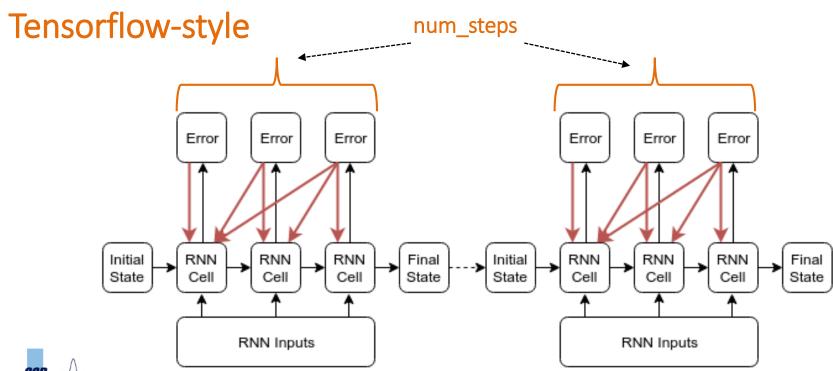
- But the recurrent net can be seen as a (very deep) feedforward net with shared weights
  - The forward pass builds up a stack of the activities of all the units at each time step.
  - The backward pass peels activities off the stack to compute the error derivatives at each time step.
  - After the backward pass we add together the derivatives at all the different times for each weight

$$\frac{\partial E_t}{\partial W} = \sum_{k=0}^{t} \frac{\partial E_t}{\partial y_y} \frac{\partial y_t}{\partial s_t} \frac{\partial s_t}{\partial s_k} \frac{\partial s_k}{\partial W} \xrightarrow{E_0} \underbrace{E_1}_{E_1} \underbrace{E_2}_{E_2} \underbrace{E_3}_{E_3} \underbrace{E_4}_{E_3} \xrightarrow{E_4} \underbrace{E_5}_{E_2} \xrightarrow{E_5}_{E_3} \xrightarrow{E_4} \underbrace{E_5}_{E_3} \xrightarrow{E_4} \underbrace{E_5}_{E_5} \xrightarrow{E_5}_{E_5} \xrightarrow{E_5}_{E_5} \xrightarrow{E_5}_{E_5} \xrightarrow{E_5}_{E_5} \xrightarrow{E_5}_{E_5}$$



## Styles of Truncated Backpropagation





## Vanishing gradient problem

In an RNN trained on long sequences (e.g. 100 time steps) the gradients can easily explode or vanish.

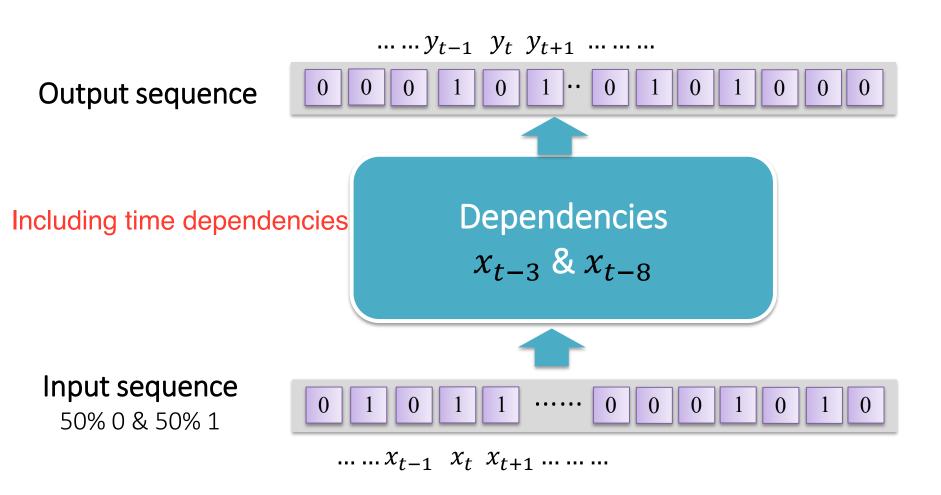
Led to the development of **LSTM**s and **GRU**s, two of the currently most popular and powerful models

http://www.wildml.com/2015/09/recurrent-neural-networks-tutorial-part-2-implementing-a-language-model-rnn-with-python-numpy-and-theano/

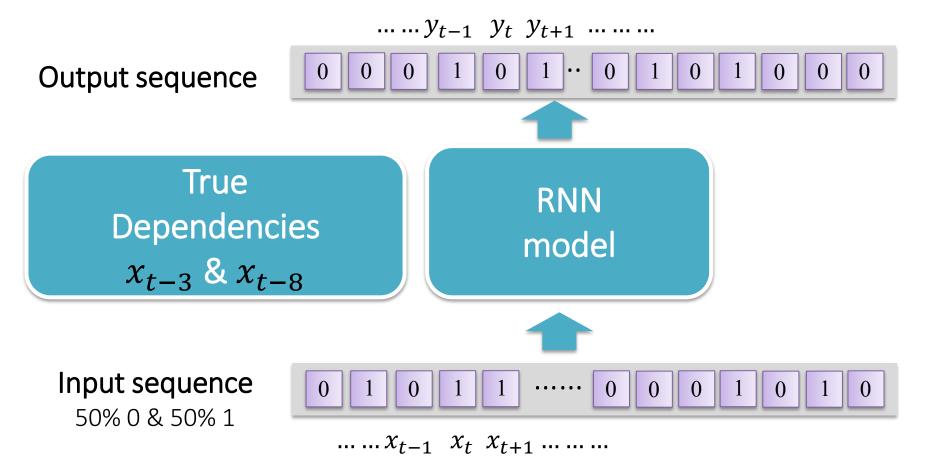


### Simple Example: RNN for a Binary Sequence

http://r2rt.com/recurrent-neural-networks-in-tensorflow-i.html







#### Expected cross entropy loss if the model:

- learns neither dependency: 0.661563238158
- learns first dependency: 0.519166699707
- learns both dependencies: 0.454454367449



### We will start with a BasicRNNCell

MSTC\_RNN\_1.ipynb



### First: dealing with data

- Generate our binary sequences
- Prepare for feeding data into the graph: from raw data to batches





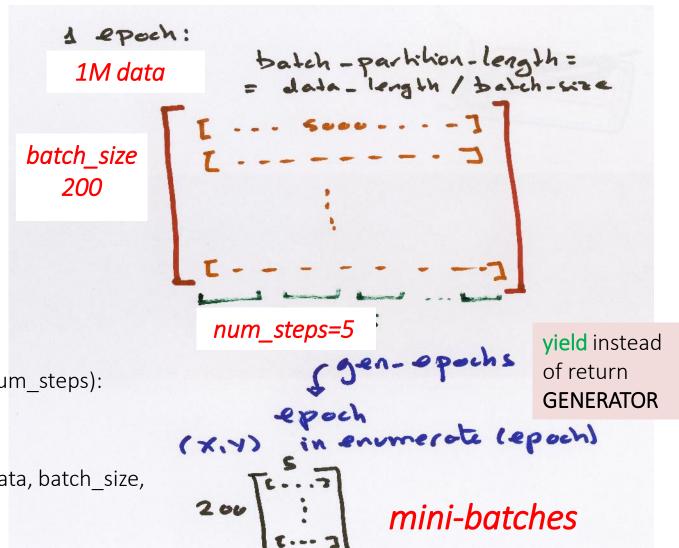
# Prepare for feeding data into the graph: *from* raw data to batches

 Remember: Neural networks are trained by approximating the gradient of loss function using only a small subset of the data, also known as a mini-batch.





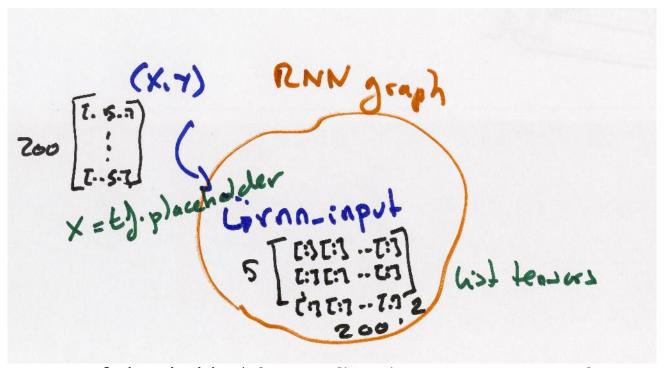
## Prepare for feeding data into the graph: *from raw data to batches*



def gen\_epochs(n, num\_steps):

def gen\_batch(raw\_data, batch\_size,
num\_steps):



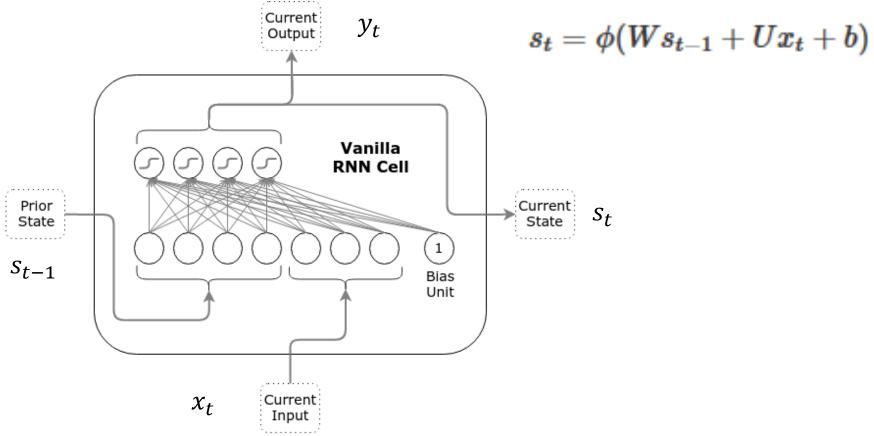


x = tf.placeholder(tf.int32, [batch\_size, num\_steps],
name='input\_placeholder')



```
x_one_hot =
                                  tf.one_hot(tf.cast(tf.transpose(x, perm=[1,
                                  0]), tf.int64), num_classes, 1,0)
             x-one-hot 0 -> [1]

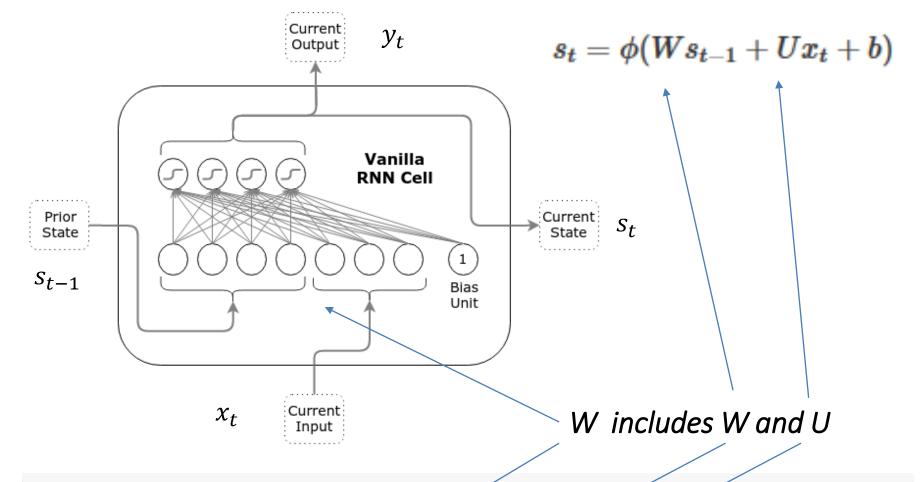
z categ.
Luu-indot
                                          rnn_inputs =
                                          tf.unpack(tf.cast(x_one_hot,
                                          tf.float32))
```



where:

- $\phi$  is the activation function (e.g., sigmoid, tanh, ReLU),
- $s_t \in \mathbb{R}^n$  is the current state (and current output),
- $s_{t-1} \in \mathbb{R}^n$  is the prior state,
- $x_t \in \mathbb{R}^m$  is the current input,
- $W \in \mathbb{R}^{n \times n}$ ,  $U \in \mathbb{R}^{m \times n}$ , and  $b \in \mathbb{R}^n$  are the weights and biases, and
- n and m are the state and input sizes.





```
Definition of rnn_cell
def rnn_cell(rnn_input, state):
    with tf.variable_scope('rnn_cell', reuse=True):
        W = tf.get_variable('W', [num_classes + state_size, state_size])
        b = tf.get_variable('b', [state_size], initializer=tf.constant_initializer(0.0))
    return tf.tanh(tf.matmul(tf.concat(1, [rnn_input, state]), W) + b)
```

```
Adding rnn_cells to graph

state = init_state
rnn_outputs = []
for rnn_input in rnn_inputs:
    state = rnn_cell(rnn_input, state)
    rnn_outputs.append(state)
final_state = rnn_outputs[-1]
```

```
Processed as:

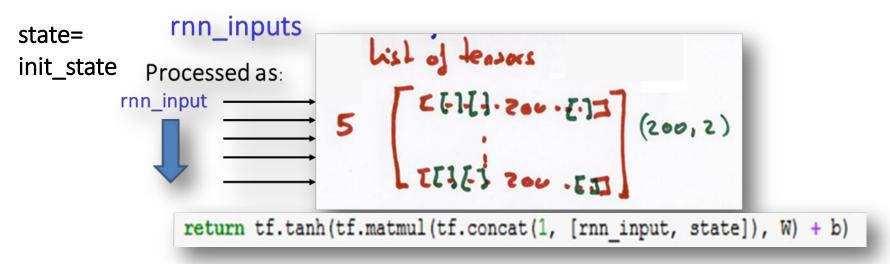
The processed as:

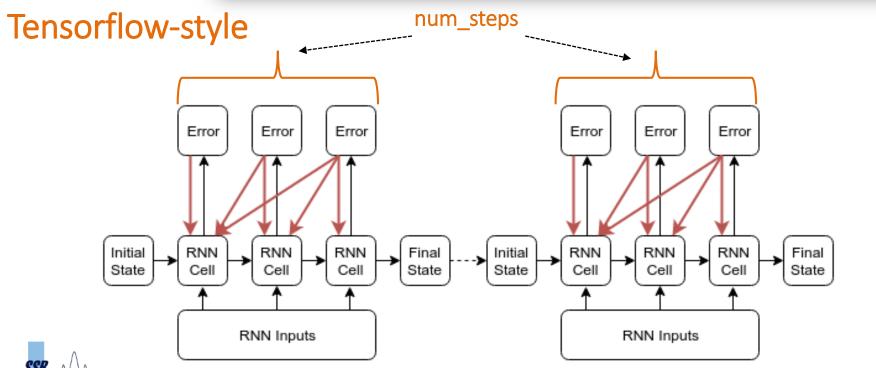
The processed as:

The process of the process o
```

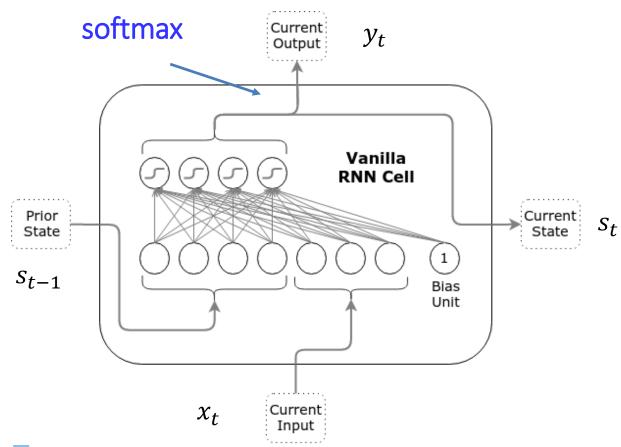
return tf.tanh(tf.matmul(tf.concat(1, [rnn input, state]), W) + b)

## Styles of Truncated Backpropagation





```
#logits and predictions
with tf.variable_scope('softmax'):
    W = tf.get_variable('W', [state_size, num_classes])
    b = tf.get_variable('b', [num_classes], initializer=tf.constant_initializer(0.0))
logits = [tf.matmul(rnn_output, W) + b for rnn_output in rnn_outputs]
predictions = [tf.nn.softmax(logit) for logit in logits]
```



#### Loss function and training step



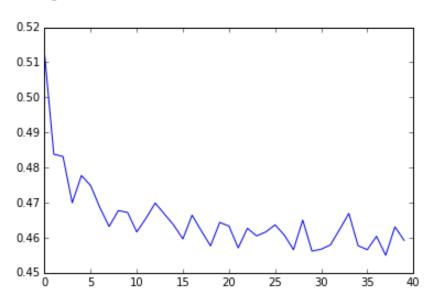


## Understand your results

#### Plotting training losses

```
plt.plot(training_losses)
```

[<matplotlib.lines.Line2D at 0x7f30b0df9790>]



#### Set GLOBAL Configuration Variables

```
# Global config variables
num_epochs=10
num_steps = 10 # number of truncated backprop steps
batch_size = 200
num_classes = 2
state_size = 16
learning_rate = 0.1
```



#### Now:

Translating our model to Tensorflow

Using a dynamic RNN

MSTC\_RNN\_2\_dynamic.ipynb





#### Tensorflow RNN static vs. dynamic

- Tensorflow contains two different functions for RNNs: tf.nn.rnn and tf.nn.dynamic\_rnn.
- Internally, tf.nn.rnn creates an unrolled static-graph for a fixed RNN length.
  - First, graph creation is slow.
  - Second, you're unable to pass in longer sequences than you've originally specified.
- **tf.nn.dynamic\_rnn** solves this. It uses a tf.While loop to dynamically construct the graph when it is executed.
  - Graph creation is faster;
  - and you can feed batches of variable size.

What about performance? dynamic is faster?

In short, just use tf.nn.dynamic\_rnn. There is no benefit to tf.nn.rnn and I wouldn't be surprised if it was deprecated in the future.



http://www.wildml.com/2016/08/rnns-in-tensorflow-a-practical-guide-and-undocumented-features/



#### Tensorflow RNN static vs. dynamic

rnn\_inputs are different

rnn\_inputs to tf.nn.rnn is a list of tensors

rnn\_inputs to tf.nn.dynamic\_rnn is:

A Tensor with dimension [batch\_size, n\_step, n\_input]



rnn\_inputs to tf.nn.dynamic\_rnn is:

A Tensor with dimension [batch size, n step, n input] rnn-inpul Tensor: Non-steps

X-one-hot \ 1 - [0]

2 categ.

Talch-size

200

[:][:] ... [:]

Tight

Tigh Datch-size x num-steps x n- Jeal. rnn\_inputs = tf.one\_hot(x, num\_classes)





#### Translating our model to a BasicRNNCel in Tensorflow's API is easy:

- We simply replace two sections by two lines!!!
- We use: tf.nn.dynamic\_rnn

```
Definition of rnn_cell in TENSORFLOW's API
"""

cell = tf.nn.rnn_cell.BasicRNNCell(state_size)
rnn_outputs, final_state = tf.nn.dynamic_rnn(cell, rnn_inputs, initial_state=init_state)
```



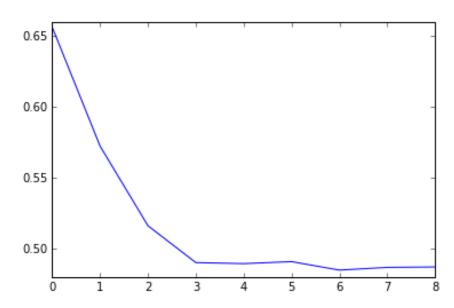


## Understand your results

#### Plotting training losses

```
plt.plot(training_losses)
```

[<matplotlib.lines.Line2D at 0x7fa6b940ef90>]



#### Set GLOBAL Configuration Variables

```
# Global config variables
num_epochs=1
num_steps = 5 # number of truncated backprop steps
batch_size = 200
num_classes = 2
state_size = 8
learning_rate = 0.1
```



## Finally:

We will use LSTM and GRU

- For a Simple NLP Task:
  - character-level language model to generate character sequences

MSTC\_RNN\_3.ipynb

#### Simplified from:

http://r2rt.com/recurrent-neural-networks-in-tensorflow-ii.html

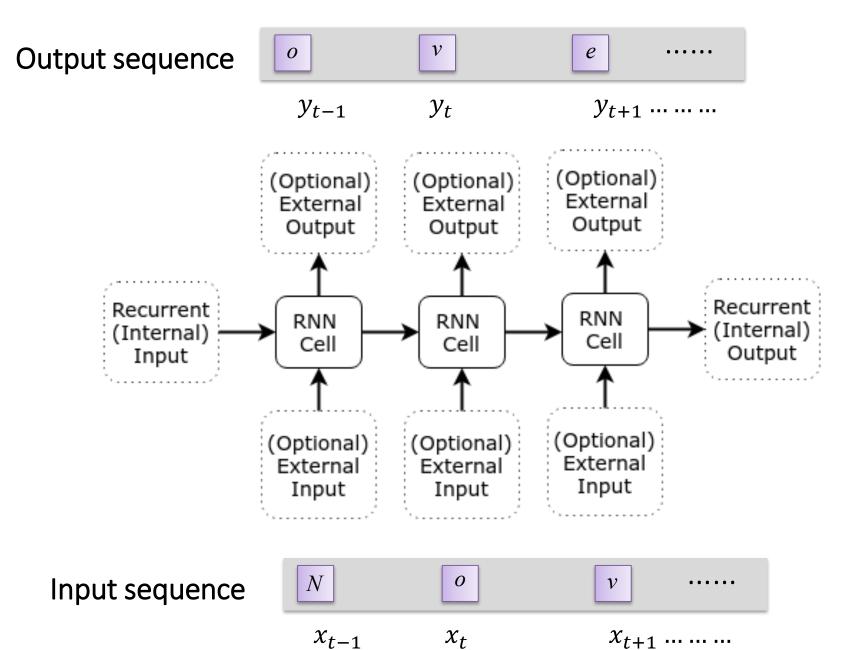


# The NLP Task: language modeling to capture the statistical relationship among words / chars

The objective of the network is to observe the input *x*, one character at a time and produce the output sentence *y*, one character at a time

X (string)	Y (string)
November 2016If you'	ovember 2016If you'r
re a California vote	e a California voter
r, there is an impor	, there is an import
tant proposition on	ant proposition on y
your ballot this yea	our ballot this year







#### For this NLP Task:

- We read a txt file: tinyshakespeare.txt, cervantes.txt
- Read all characters = vocab and generating a mapping from chars to numbers vocab\_to\_idx and viceversa idx\_to\_vocab

```
print vocab

set(['\n', '!', ' ', '$', "'", '&', '-', ',', '.', '3', ';', ':', '?', 'A', 'C', 'B', 'E',
'Q', 'P', 'S', 'R', 'U', 'T', 'W', 'V', 'Y', 'X', 'Z', 'a', 'c', 'b', 'e', 'd', 'g', 'f',
'r', 'u', 't', 'w', 'v', 'y', 'x', 'z'])

vocab_size

tocab_size
```



raw\_data[0:10]

'First Citi'



vocab\_to\_idx

data[0:10]

[19, 46, 57, 56, 59, 2, 14, 46, 59, 46]



idx\_to\_vocab

recover\_data = [idx\_to\_vocab[c] for c in data]

recover\_data[0:10]

['F', 'i', 'r', 's', 't', ' ', 'C', 'i', 't', 'i']



# Epochs and Batches are generated in a similar way as in MSTC\_RNN\_1:

PTB\_iterator from Penn Tree Bank (PTB) dataset is used

Example for: num\_steps=200 batch\_size=32

X (string)	Y (string)
November 2016If you'	ovember 2016If you'r
re a California vote	e a California voter
r, there is an impor	, there is an import
tant proposition on	ant proposition on y
your ballot this yea	our ballot this year

```
X information....
                            Y information....
(32, 200)
                             (32, 200)
<type 'numpy.ndarray'>
                            <type 'numpy.ndarray'>
[[19 46 57 ..., 62 52 58]
                            [[46 57 56 ..., 52 58 2]
 [45 52 57 ..., 50 39 62]
                             [52 57 2 ..., 39 62 2]
 [ 2 14 52 ..., 19 46 57]
                             [14 52 57 ..., 46 57 56]
 [52 58 2 ..., 58 56 55] [58 2 60 ..., 56 55 46]
 [ 2 47 52 ..., 45 2 60] [47 52 60 ..., 2 60 52]
                             [45 52 52 ..., 56 42 2]]
 [ 2 45 52 ..., 52 56 42]]
```



## **Embedings**

```
X information....
(32, 200)
<type 'numpy.ndarray'>
[[19 46 57 ..., 62 52 58]
[45 52 57 ..., 50 39 62]
[ 2 14 52 ..., 19 46 57]
...,
[52 58 2 ..., 58 56 55]
[ 2 47 52 ..., 45 2 60]
[ 2 45 52 ..., 52 56 42]]
```

- Indices by themselves, carry no semantic meaning
- This is where embedding comes in; more commonly known as word vector or word embedding.



## **Embedings**

```
X information...

(32, 200)

<type 'numpy.ndarray'>

[[19 46 57 ..., 62 52 58]

[45 52 57 ..., 50 39 62]

[ 2 14 52 ..., 50 39 62]

...,

[52 58 2 ..., 58 56 55]

[ 2 47 52 ..., 58 56 55]

[ 2 45 52 ..., 52 56 42]]
```

In this case, we will map the characters to low dimensional vectors of size state\_size.

low-dimensional vector
(state\_size = n\_inputs)



```
X information...

(32, 200)

<type 'numpy.ndarray'>

[[19 46 57 ..., 62 52 58]

[45 52 57 ..., 50 39 62]

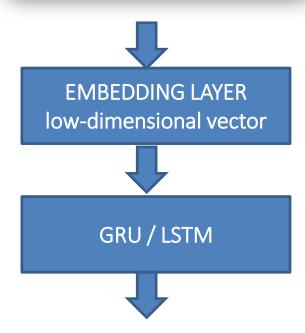
[ 2 14 52 ..., 19 46 57]

...,

[52 58 2 ..., 58 56 55]

[ 2 47 52 ..., 45 2 60]

[ 2 45 52 ..., 52 56 42]]
```



http://stackoverflow.com/questions/40184537/what-does-embedding-do-in-tensorflow



## In this example embedings are done by:

- creating an embedding matrix of shape
   [vocab\_size=num\_classes, state\_size]
- and selecting a row of the matrix by index of character

```
embeddings = tf.get_variable('embedding_matrix',
[num_classes, state_size])
```

# Note that our inputs are no longer a list, but a tensor of dims batch\_size x num\_steps x state\_size we will use DYNAMIC RNN

rnn\_inputs = tf.nn.embedding\_lookup(embeddings, x)



- The embedding\_matrix is a "layer" so Tensorflow does backprop of the error INTO this lookup table,
- and hopefully what starts off as a randomly initialized dictionary will gradually become "significant"

```
X information...

(32, 200)

<type 'numpy.ndarray'>

[[19 46 57 ..., 62 52 58]

[45 52 57 ..., 50 39 62]

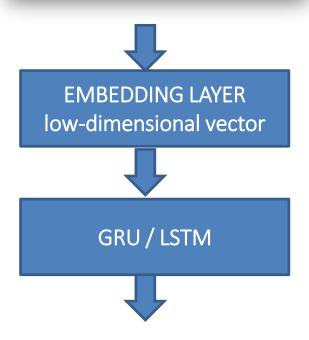
[ 2 14 52 ..., 19 46 57]

...,

[52 58 2 ..., 58 56 55]

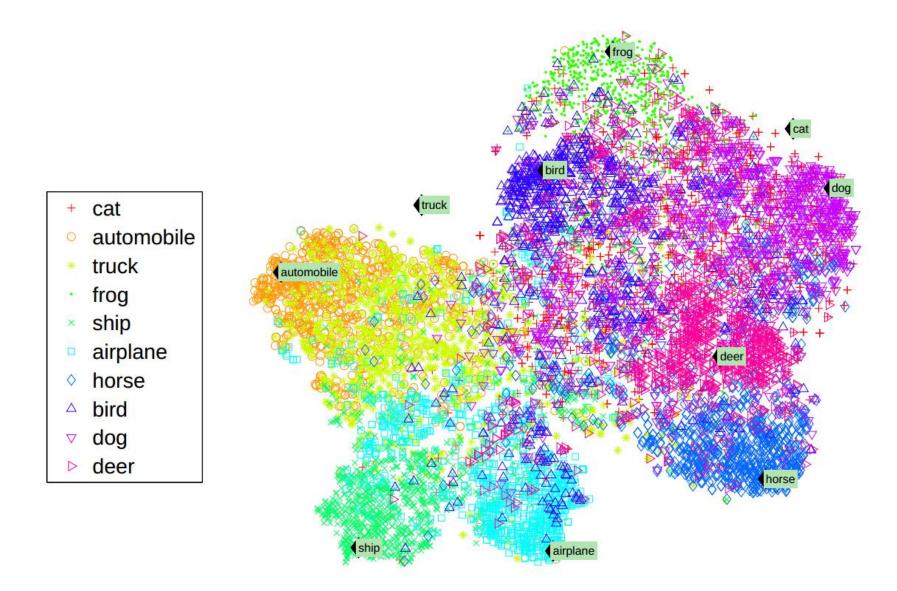
[ 2 47 52 ..., 45 2 60]

[ 2 45 52 ..., 52 56 42]]
```



http://stackoverflow.com/questions/40184537/what-does-embedding-do-in-tensorflow





http://colah.github.io/posts/2014-07-NLP-RNNs-Representations/





#### See also:

Word2vec https://www.tensorflow.org/tutorials/word2vec

<u>Vector space models</u> (VSMs) represent (embed) words in a continuous vector space where **semantically similar words** are mapped to nearby points ('are embedded nearby each other')





## Now we can test using LSTM:

```
#LSTM
cell = tf.nn.rnn_cell.LSTMCell(state_size,
    state_is_tuple=True)
cell = tf.nn.rnn_cell.MultiRNNCell([cell] * num_layers,
    state_is_tuple=True)
```

#### or GRU

```
# GRU
cell = tf.nn.rnn_cell.GRUCell(state_size)
```





## Now we can test using LSTM or GRU

+ much more to consider...

#Dropout

# Regularization

# Batch normalization

# Adding noise...





## Models LSTM or GRU can be saved:

```
saver = tf.train.Saver()
saver.save(sess, 'RNN_GRU_model_shakespeare')
```



# Models LSTM or GRU can be used to generate TEXT

 NOTE that for this we need to rebuild the graph so as to accept a single character at a time





A se dije a su la caral mar entus de la mucho al disto escundas el maloras de sus entre de su como lo haballe que de sin cuanto en llaba en el muestra me camiminor las, coralas des como ello, que estroras de esprento, y asigo, podros compastra de aquellao es a todo de lo que a sercido al vene de la contuento entaron esa camo, separ en esta estusando a lo hallar de su amo, y con la alvando.

Y le caballero, que lleguado al por el mano, a su por mas quiero a toda el pocina dejor la porte en serventar a la cual de algún estar en alguna dejuna me de ella embro que se le cabrese las ma



## Basic concepts: LSTM & GRU

http://colah.github.io/posts/2015-08-Understanding-LSTMs/

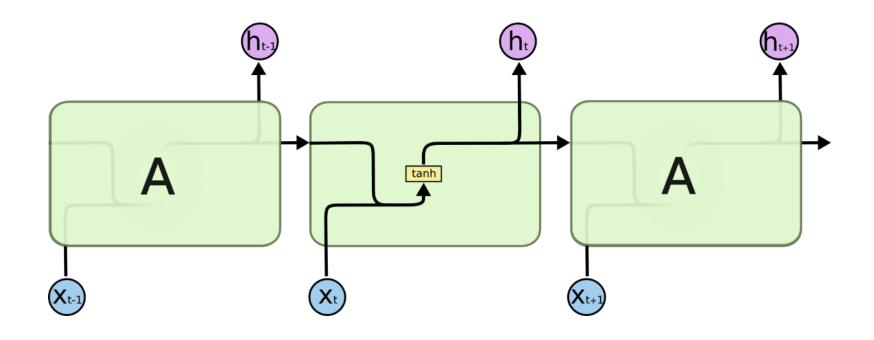
Vanishing gradients: a problem?

it may be that for some tasks we want gradients to vanish completely, and for others, it may be that we want them to grow

 Are RNNs capable of handling "long-term dependencies?"

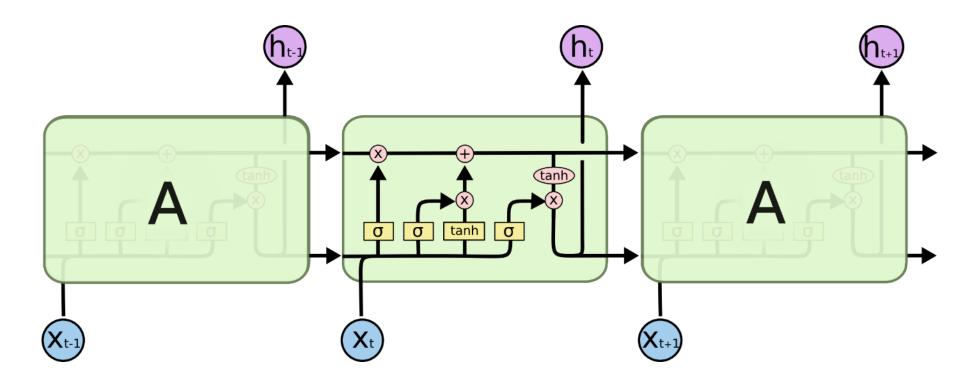
> Long Short Term Memory networks – LSTMs Hocreiter and Schmidhuber (1997)





The repeating module in a standard RNN contains a single layer

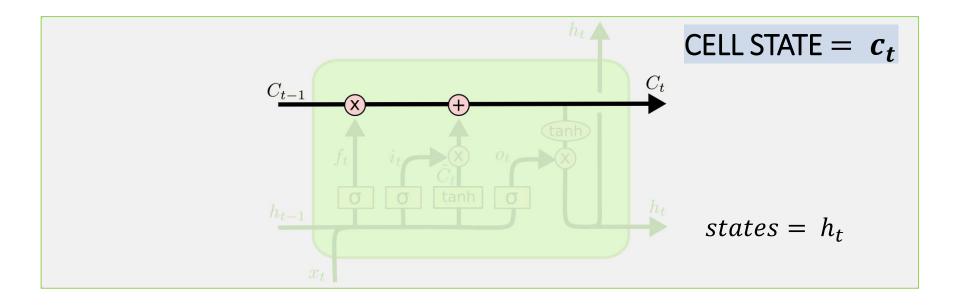


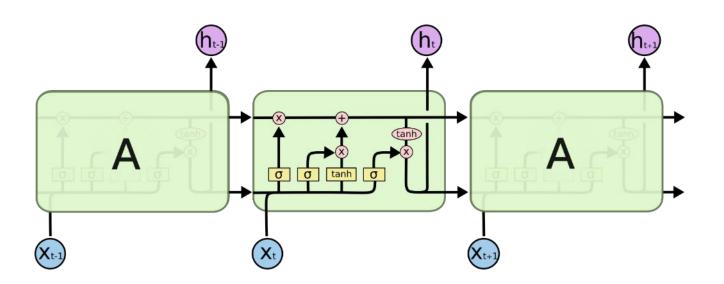


The repeating module in LSTM contains four interacting layers



#### Core Idea Behind LSTM







#### Tensorflow NOTE:



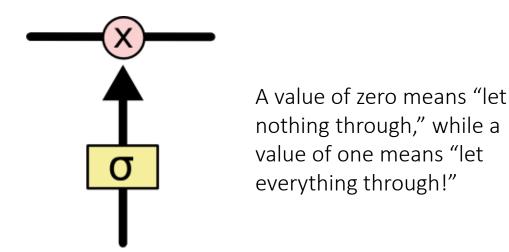
cell = tf.nn.rnn\_cell.LSTMCell(state\_size, state\_is\_tuple=True)

• "Hidden State"  $h_t$  and "Cell State" , $\mathcal{C}_t$ 



#### Core Idea Behind LSTM

- The LSTM does have the ability to remove or add information to the cell state, carefully regulated by structures called gates.
- Gates are a way to optionally let information through.
- They are composed out of a sigmoid neural net layer and a pointwise multiplication operation.



An LSTM has three of these gates, to protect and control the cell state



## Basic concepts: LSTM & GRU

#### Hocreiter and Schmidhuber (1997)

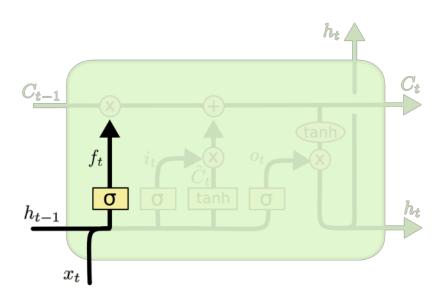
- The fundamental principle of LSTMs: to ensure the integrity of our messages in the real world, we write them down
- The fundamental challenge of LSTMs and **keeping our state** under control is to be selective in three things:
  - 1. what we write (write selectivity),
  - what we read (because we need to read something to know what to write) (read selectivity)
  - 3. and what we forget (because obsolete information is a distraction and should be forgotten) (forget selectivity)

Gates as a mechanism for selectivity



**Forget gate**: The first step in our LSTM is to decide what information we're going to throw away from the cell state.

When we "see" something new relevant we decide forget....

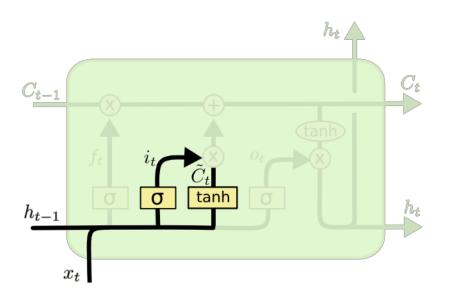


$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$



The next step is to decide what new information we're going to store in the cell state. This has two parts.

- First, a sigmoid layer called the "input gate layer" decides which values we'll
  update.
- Next, a **tanh layer** creates a vector of new candidate values,  $\widetilde{C}_t$ , that could be added to the state.

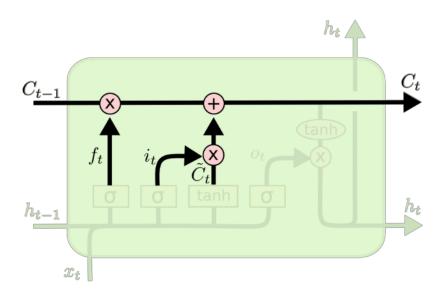


$$i_t = \sigma \left( W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
  
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$



It's now time to update the old cell state,  $C_{t-1}$ , into the new cell state  $C_t$ 

- The previous steps already decided what to do, we just need to actually do it.
- We multiply the old state by  $f_t$ (forget gate) then we add  $i_t* ilde{\mathcal{C}}_t$

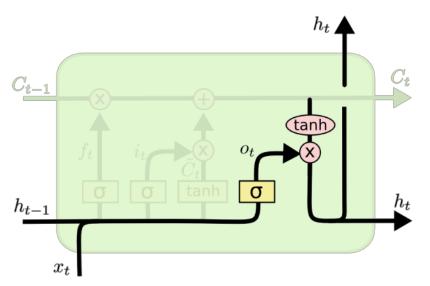


$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$



Finally, we need to decide what we're going to output  $h_t$ . This output will be based on our cell state, but will be a filtered version.

- First, we run a sigmoid layer which decides what parts of the cell state we're going to output.
- Then, we put the cell state through tanh (to push the values to be between −1 and 1) and multiply it by the output of the sigmoid gate, so that we only output the parts we decided to.

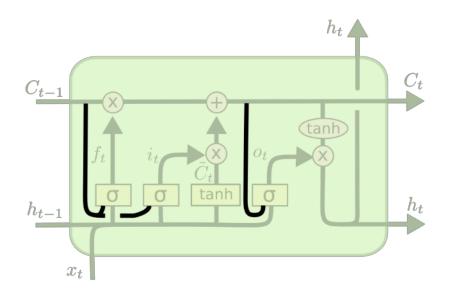


$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh(C_t)$$



One popular LSTM variant, introduced by Gers & Schmidhuber (2000), is adding "peephole connections."

This means that we let the gate layers look at the cell state.



$$f_t = \sigma \left( W_f \cdot [\boldsymbol{C_{t-1}}, h_{t-1}, x_t] + b_f \right)$$

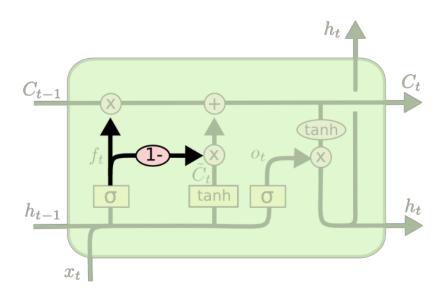
$$i_t = \sigma \left( W_i \cdot [\boldsymbol{C_{t-1}}, h_{t-1}, x_t] + b_i \right)$$

$$o_t = \sigma \left( W_o \cdot [\boldsymbol{C_t}, h_{t-1}, x_t] + b_o \right)$$

The above diagram adds peepholes to all the gates, but many papers will give some peepholes and not others.

Another variation is to use coupled forget and input gates.

• We only input new values to the state when we forget something older



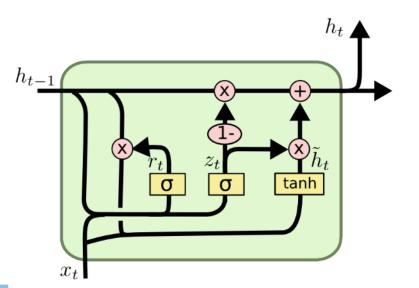
$$C_t = f_t * C_{t-1} + (1 - f_t) * \tilde{C}_t$$



Gated Recurrent Unit, or GRU, introduced by Cho, et al. (2014).

- It combines the forget and input gates into a single "update gate."
- It also merges the cell state and hidden state, and makes some other changes.

The resulting model is simpler than standard LSTM models, and has been growing increasingly popular.



$$z_{t} = \sigma (W_{z} \cdot [h_{t-1}, x_{t}])$$

$$r_{t} = \sigma (W_{r} \cdot [h_{t-1}, x_{t}])$$

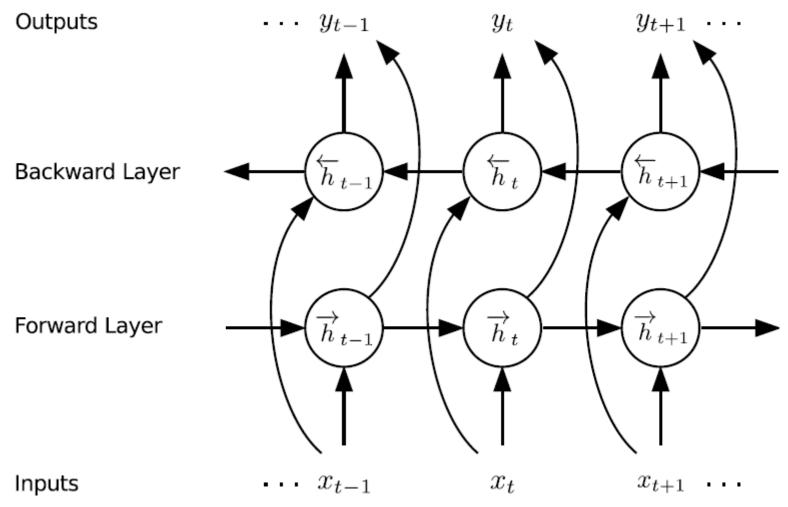
$$\tilde{h}_{t} = \tanh (W \cdot [r_{t} * h_{t-1}, x_{t}])$$

$$h_{t} = (1 - z_{t}) * h_{t-1} + z_{t} * \tilde{h}_{t}$$



These are only a few of the most notable LSTM variants.

See for example: **BLSTM** Bi-directional LSTM

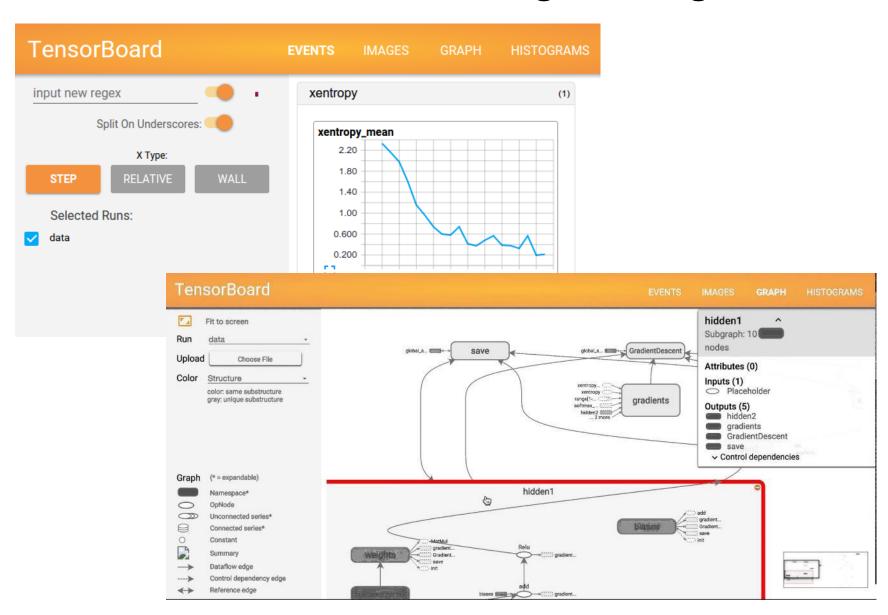


Which of these variants is best? Do the differences matter?

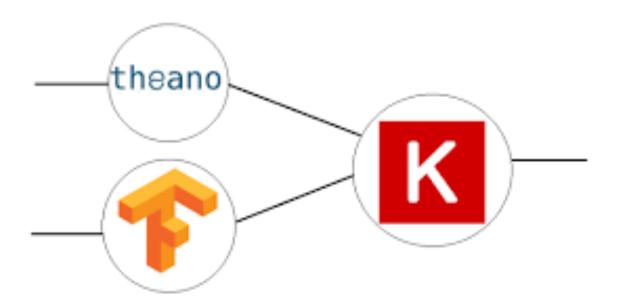
- Greff, et al. (2015) do a nice comparison of popular variants, finding that they're all about the same.
- Jozefowicz, et al. (2015) tested more than ten thousand RNN architectures, finding some that worked better than LSTMs on certain tasks.



## TensorBoard: Visualizing Learning







https://keras.io/

### **Scikit Flow**

http://terrytangyuan.github.io/2016/03/14/scikit-flow-intro/



## References (I)

https://theneuralperspective.com/2016/10/04/05-recurrent-neural-networks-rnn-part-1-basic-rnn-char-rnn/

http://colah.github.io/posts/2015-08-Understanding-LSTMs/

http://www.wildml.com/2015/09/recurrent-neural-networks-tutorial-part-2-implementing-a-language-model-rnn-with-python-numpy-and-theano/

https://github.com/suriyadeepan/rnn-from-scratch

http://stats.stackexchange.com/questions/241985/understanding-lstm-units-vs-cells

http://monik.in/a-noobs-guide-to-implementing-rnn-lstm-using-tensorflow/

https://medium.com/@erikhallstrm/hello-world-rnn-83cd7105b767

http://suriyadeepan.github.io/2017-01-07-unfolding-rnn/

http://archive.eetindia.co.in/www.eetindia.co.in/VIDEO\_DETAILS\_700001601.HTM



#### References (I)

http://r2rt.com/styles-of-truncated-backpropagation.html

http://akkikiki.github.io/assets/LSTM+and+GRU.html

http://campuspress.yale.edu/yw355/deep\_learning/

http://datascience.stackexchange.com/questions/12964/what-is-the-meaning-of-the-number-of-units-in-the-lstm-cell

http://stackoverflow.com/questions/37901047/what-is-num-units-in-tensorflow-basicIstmcell

