

# DS 621 Fall2020: Homework 1 (Group3)

## Moneyball Linear Regression

Zach Alexander, Sam Bellows, Donny Lofland, Joshua Registe, Neil Shah, Aaron Zalki

Source code: [https://github.com/djlofland/DS621\\_F2020\\_Group3/tree/master/Homework\\_1](https://github.com/djlofland/DS621_F2020_Group3/tree/master/Homework_1)

### Overview

In professional sports, there is a huge interest in attempting to leverage historic statistics to both predict future outcomes (wins/losses) and explore opportunities for tuning or improving a team or individual's performance. This data-driven approach to sports has gained a large following over the last decade and entered mass media in the form of fantasy leagues, movies (e.g. Moneyball), and websites/podcasts (e.g. FiveThirtyEight). In this analysis, we will be using a classic baseball data set with the goal to build several different models capable of predicting team wins over a season given on other team stats during that season (i.e. home-runs, strikeouts, base hits, etc).

We will first explore the data looking for issues or challenges (i.e. missing data, outliers, possible coding errors, multicollinearity, etc). Once we have a handle on the data, we will apply any necessary cleaning steps. Once we have a reasonable dataset to work with, we will build and evaluate three different linear models that predict seasonal wins. Our dataset includes both training data and evaluation data - we will training using the main training data, then evaluate models based on how well they perform against the holdout evaluation data. Finally we will select a final model that offers the best compromise for accuracy and simplicity.

### 1. Data Exploration

*Describe the size and the variables in the moneyball training data set. Consider that too much detail will cause a manager to lose interest while too little detail will make the manager consider that you aren't doing your job. Some suggestions are given below. Please do NOT treat this as a check list of things to do to complete the assignment. You should have your own thoughts on what to tell the boss. These are just ideas.*

#### Dataset

The moneyball training set contains 17 columns—with one column our target variable “TARGET\_WINS” and 2276 rows, covering baseball team performance statistics from the years 1871 to 2006 inclusive. The data has been adjusted to match the performance of a typical 162 game season. The data-set was entirely numerical and contained no categorical variables.

Below, we created a chart that describes each variable in the dataset and the theoretical effect it will have on the number of wins projected for a team.

Given that the Index column had no impact on the target variable, number of wins, it was dropped.

VARIABLE NAME	DEFINITION	THEORETICAL EFFECT
INDEX	Identification Variable (do not use)	None
TARGET_WINS	Number of wins	
TEAM_BATTING_H	Base Hits by batters (1B,2B,3B,HR)	Positive Impact on Wins
TEAM_BATTING_2B	Doubles by batters (2B)	Positive Impact on Wins
TEAM_BATTING_3B	Triples by batters (3B)	Positive Impact on Wins
TEAM_BATTING_HR	Homeruns by batters (4B)	Positive Impact on Wins
TEAM_BATTING_BB	Walks by batters	Positive Impact on Wins
TEAM_BATTING_HBP	Batters hit by pitch (get a free base)	Positive Impact on Wins
TEAM_BATTING_SO	Strikeouts by batters	Negative Impact on Wins
TEAM_BASERUN_SB	Stolen bases	Positive Impact on Wins
TEAM_BASERUN_CS	Caught stealing	Negative Impact on Wins
TEAM_FIELDING_E	Errors	Negative Impact on Wins
TEAM_FIELDING_DP	Double Plays	Positive Impact on Wins
TEAM_PITCHING_BB	Walks allowed	Negative Impact on Wins
TEAM_PITCHING_H	Hits allowed	Negative Impact on Wins
TEAM_PITCHING_HR	Homeruns allowed	Negative Impact on Wins
TEAM_PITCHING_SO	Strikeouts by pitchers	Positive Impact on Wins

Figure 1: Variables of Interest

## Summary Stats

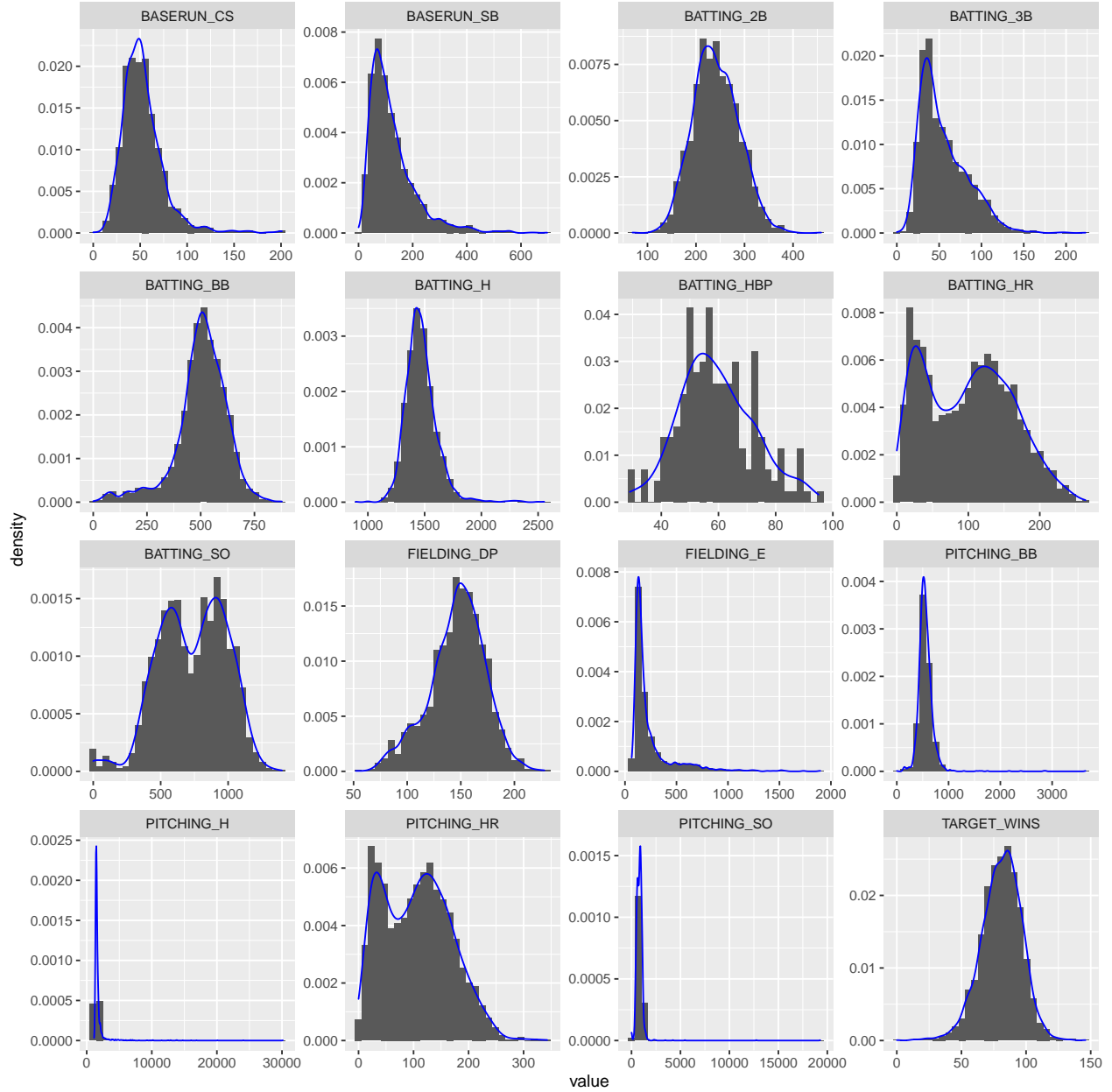
We compiled summary statistics on our data set to better understand the data before modeling.

```
## TARGET_WINS      BATTING_H      BATTING_2B      BATTING_3B
## Min.   : 0.00    Min.   : 891    Min.   : 69.0    Min.   : 0.00
## 1st Qu.: 71.00    1st Qu.:1383    1st Qu.:208.0    1st Qu.: 34.00
## Median : 82.00    Median :1454    Median :238.0    Median : 47.00
## Mean   : 80.79    Mean   :1469    Mean   :241.2    Mean   : 55.25
## 3rd Qu.: 92.00    3rd Qu.:1537    3rd Qu.:273.0    3rd Qu.: 72.00
## Max.   :146.00    Max.   :2554    Max.   :458.0    Max.   :223.00
##
## BATTING_HR      BATTING_BB      BATTING_SO      BASERUN_SB
## Min.   : 0.00    Min.   : 0.0    Min.   : 0.0    Min.   : 0.0
## 1st Qu.: 42.00    1st Qu.:451.0    1st Qu.: 548.0    1st Qu.: 66.0
## Median :102.00    Median :512.0    Median : 750.0    Median :101.0
## Mean   : 99.61    Mean   :501.6    Mean   : 735.6    Mean   :124.8
## 3rd Qu.:147.00    3rd Qu.:580.0    3rd Qu.: 930.0    3rd Qu.:156.0
## Max.   :264.00    Max.   :878.0    Max.   :1399.0    Max.   :697.0
##
##                NA's :102      NA's :131
## BASERUN_CS      BATTING_HBP      PITCHING_H      PITCHING_HR
## Min.   : 0.0    Min.   :29.00    Min.   : 1137    Min.   : 0.0
## 1st Qu.: 38.0    1st Qu.:50.50    1st Qu.: 1419    1st Qu.: 50.0
## Median : 49.0    Median :58.00    Median : 1518    Median :107.0
## Mean   : 52.8    Mean   :59.36    Mean   : 1779    Mean   :105.7
## 3rd Qu.: 62.0    3rd Qu.:67.00    3rd Qu.: 1682    3rd Qu.:150.0
## Max.   :201.0    Max.   :95.00    Max.   :30132    Max.   :343.0
##
## NA's :772      NA's :2085
## PITCHING_BB      PITCHING_SO      FIELDING_E      FIELDING_DP
## Min.   : 0.0    Min.   : 0.0    Min.   : 65.0    Min.   : 52.0
## 1st Qu.: 476.0    1st Qu.: 615.0    1st Qu.: 127.0    1st Qu.:131.0
## Median : 536.5    Median : 813.5    Median : 159.0    Median :149.0
## Mean   : 553.0    Mean   : 817.7    Mean   : 246.5    Mean   :146.4
## 3rd Qu.: 611.0    3rd Qu.: 968.0    3rd Qu.: 249.2    3rd Qu.:164.0
## Max.   :3645.0    Max.   :19278.0    Max.   :1898.0    Max.   :228.0
##
##                NA's :102      NA's :286
```

The first observation is the prevalence of NA's throughout the dataset. On a cursory view, we can quickly see that the average wins per season for a team is about 81, which is exactly half of the total games played in a typical MLB season. Additionally, batters hit, on average, about 9 base hits per game, pitchers throw about 4 base-on-balls (walks) per game, and pitchers record about 5 strikeouts per game, when calculated out over a 162-game season.

## Distributions

Next, we wanted to get an idea of the distribution profiles for each of the variables.



The distribution profiles sure the prevalence of kurtosis, specifically right skew in variables BASERUN\_CS, BASERUN\_CB, FIELDING\_E, PITCHING\_RB, PITCHING\_H and PITCHING\_SO. These deviations from a traditional normal distribution can be problematic for linear regression assumptions, and thus we might need to transform the data. Furthermore BATTING\_HBP, BATTING\_HR, PITCHING\_HR and BATTING\_SO appear bimodal. Bimodal features in a dataset are both problematic and interesting and potentially an area of opportunity and exploration. Bimodal data suggests that there are possibly two different groups or classes of baseball season data. During those seasons, teams tended to score higher or lower for the bimodal feature.

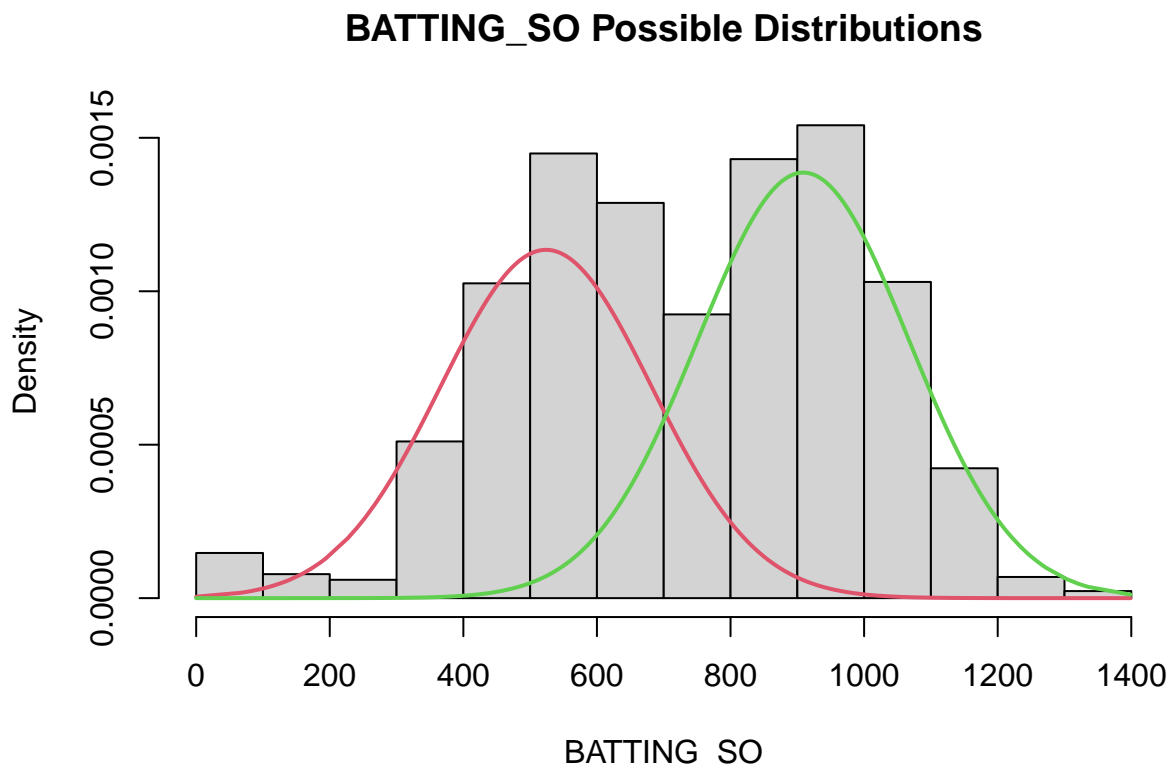
Two possibilities immediately come to mind. The bimodal nature could be caused by a rule change such that games before a specific time point had lower values and games after that point had higher values. Unfortunately, we do not have any features on which year the data is associated. The second is that teams either do well or not for the given KPI. Let's consider BATTING\_SO (Batters striking out) - if some teams have better players, they might have a reasonable normal distribution lower than those teams with worse players. We do know that certain teams are able to attract and pay for better players (let's call them Tier

1) and some teams with lower budgets and less visibility (let's call them Tier 2). Even with a given team, they might have “good years” and “off years”. It's possible the distribution of BATTING\_SO represents the overlap or superposition of this two distinct curves representing different classes of team.

While we don't tackle feature engineering in this analysis, if we were performing a more in-depth analysis, these are some possible options.

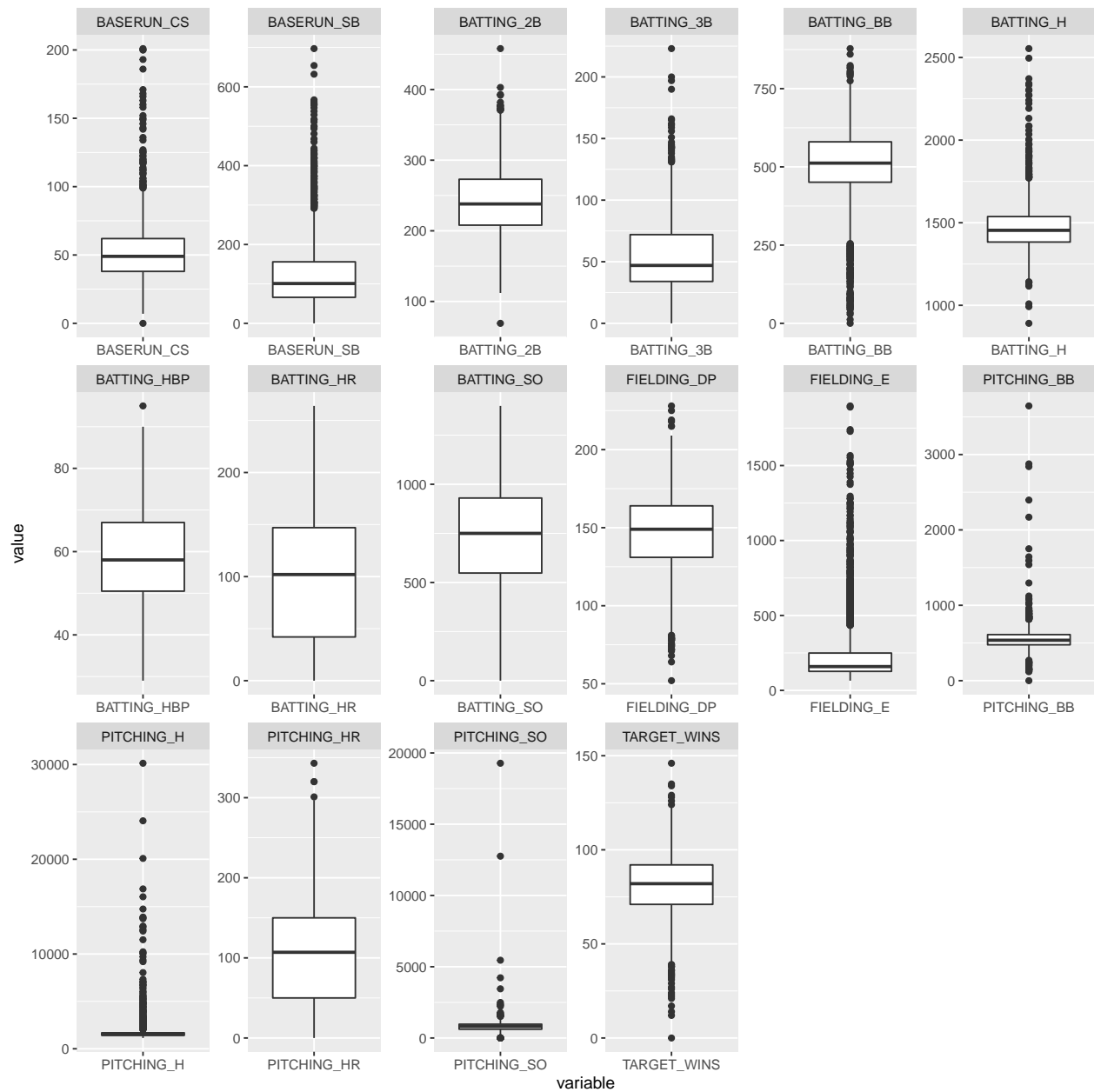
- We have no data linking rows with specific years. We might attempt to locate additional data sets that link performance to year and leverage change point detection to see if bimodal relationships are linked with all teams at specific points in time. If change points are present, that suggests something changed affecting all teams (e.g. new rules that improved or lowered the bimodal feature). We would then create a new categorical feature indicating which class the row data came from, before or after the change point.
- We have no data lining rows with specific teams so cannot directly tell if there are more than one Tier of team. Instead, we could explore whether there are correlation between the bimodal nature across different bimodal features (i.e. do rows with lower BATTING\_HR line up with rows with lower/higher BATTING\_SO) within rows. If there are strong correlations between bimodal features, that suggests there might be two classes of teams (or yearly team performance) and we could create a new categorical variable(s) indicating the probable Tier per row. Alternatively, we could assign a new numerical feature indicating the probability a row fell into which class.
- R provides a package, `mixtools` (see R Vignette) which helps regress *mixed models* where data can be subdivided into subgroups. Here is a quick example showing a possible mix within BATTING\_SO:

```
## number of iterations= 48
```



### Boxplots

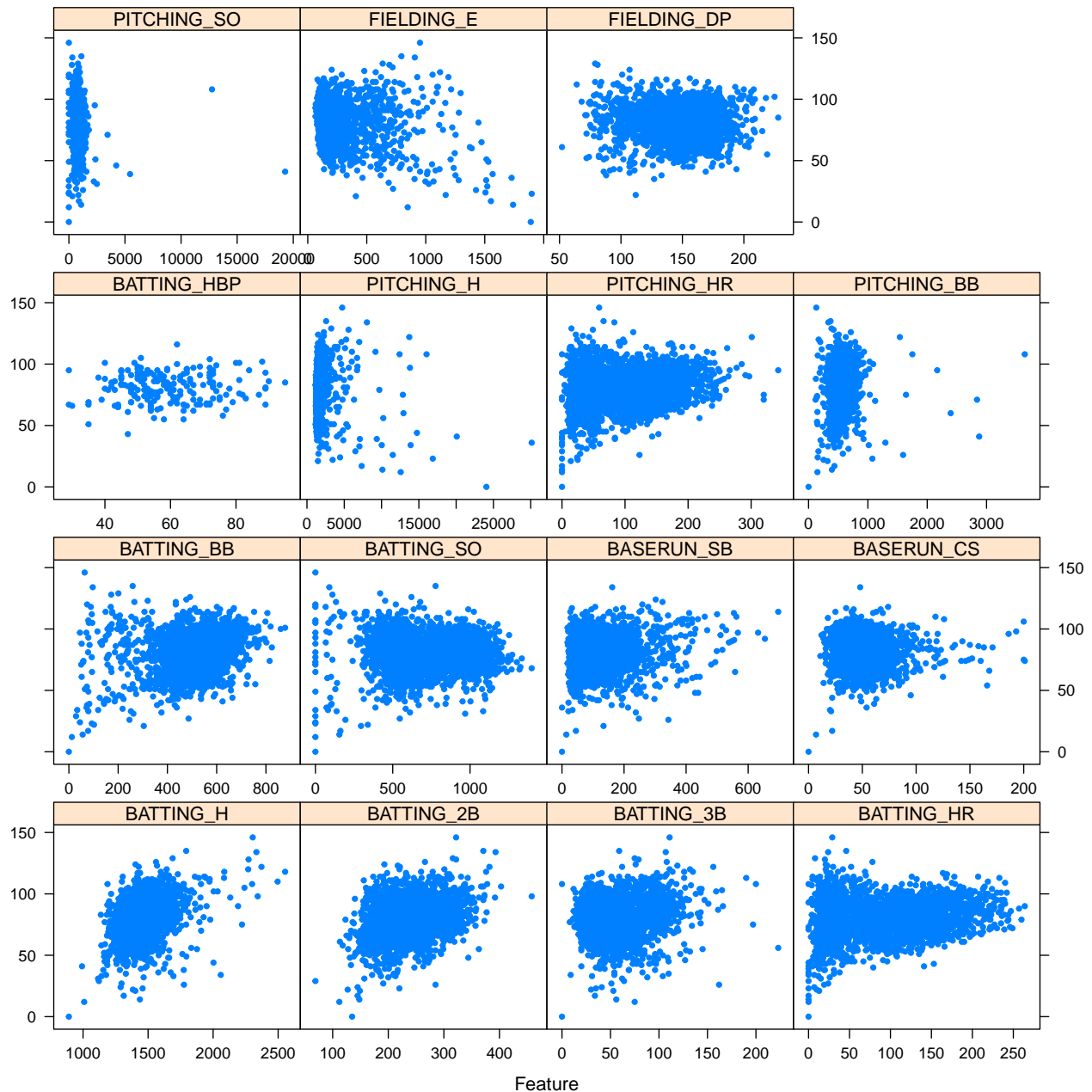
In addition to creating histogram distributions, we also elected to use box-plots to get an idea of the spread of each variable.



The box-plots reveal significant outliers and uniform (zero-only) values for many of our predictor variables. Outliers will need to be imputed if necessary, and sparse data-sets might need to be dropped.

## Variable Plots

Finally, we wanted to plot scatter plots of each variable versus the target variable, TARGET\_WINS, to get an idea of the relationship between them.



The plots indicate some clear relationships, such as hitting more doubles or more home runs clearly improves the number of wins.

Overall, although our plots indicate some interesting relationships between our variables, they also reveal some significant issues with the data.

For instance, most of the predictor variables are skewed or non-normally distributed, and will need to be transformed. Additionally, there are many data points that contain missing data that will need to be either imputed or discarded. It also appears we have some missing data encoded as 0 and some nonsensical outliers.

There is a team with 0 wins in the dataset. This seems unlikely. Many of the hitting categories include teams at 0; it is unlikely that a team hit 0 home runs over the course of a season.

The pitching variables also include many 0's, for instance there are multiple teams with 0 strikeouts by their pitchers over the season which is extremely unlikely. The pitching data also includes strange outliers such as a team logging 20,000 strikeouts, that would be an average of 160 strikeouts per game which is impossible.

Also team pitching walks and team pitching hits have strange outliers.

Lastly, the error variable makes little sense. From my experience watching baseball, teams usually score 2 or less errors per game, which would lead to an overall team error of approximately 320 over the course of a season, which does not match the scale of the error variable.

## Missing Data

When we initially viewed the first few rows of the raw data, we already noticed missing data. Let's assess which fields have missing data.

```
##      values      ind
## 1    91.61 BATTING_HBP
## 2    33.92 BASERUN_CS
## 3    12.57 FIELDING_DP
## 4     5.76 BASERUN_SB
## 5     4.48 BATTING_SO
## 6     4.48 PITCHING_SO
## 7     0.00 TARGET_WINS
## 8     0.00  BATTING_H
## 9     0.00 BATTING_2B
## 10    0.00 BATTING_3B
## 11    0.00 BATTING_HR
## 12    0.00 BATTING_BB
## 13    0.00 PITCHING_H
## 14    0.00 PITCHING_HR
## 15    0.00 PITCHING_BB
## 16    0.00 FIELDING_E
```

Notice that ~91.6% of the rows are missing the BATTING\_HBP field - we will just drop this column from consideration. The columns BASERUN\_CS (base run caught stealing) and BASERUN\_SB (stolen bases) both have missing values. According to baseball history, stolen bases weren't tracked officially until 1887, so some of the missing data could be from 1871-1886. We will impute those value. There are a high percentage of missing BATTING\_SO (batter strike outs) and PITCHING\_SO (pitching strike outs) which seem highly unlikely - we will also impute those missing values.

## Feature-Target Correlations

With our missing data imputed correctly, we can now build off the scatter plots from above to quantify the correlations between our target variable and predictor variable. We will want to choose those with stronger positive or negative correlations. Features with correlations closer to zero will probably not provide any meaningful information on explaining wins by a team.

```
##      values      ind
## 1    0.383313355  BATTING_H
## 2    0.285964582  BATTING_2B
## 3    0.225471523  BATTING_BB
## 4    0.186326615 PITCHING_HR
## 5    0.173551988  BATTING_HR
## 6    0.164738136 PITCHING_BB
## 7    0.139073830  BATTING_3B
## 8    0.121110012  BASERUN_SB
```



```

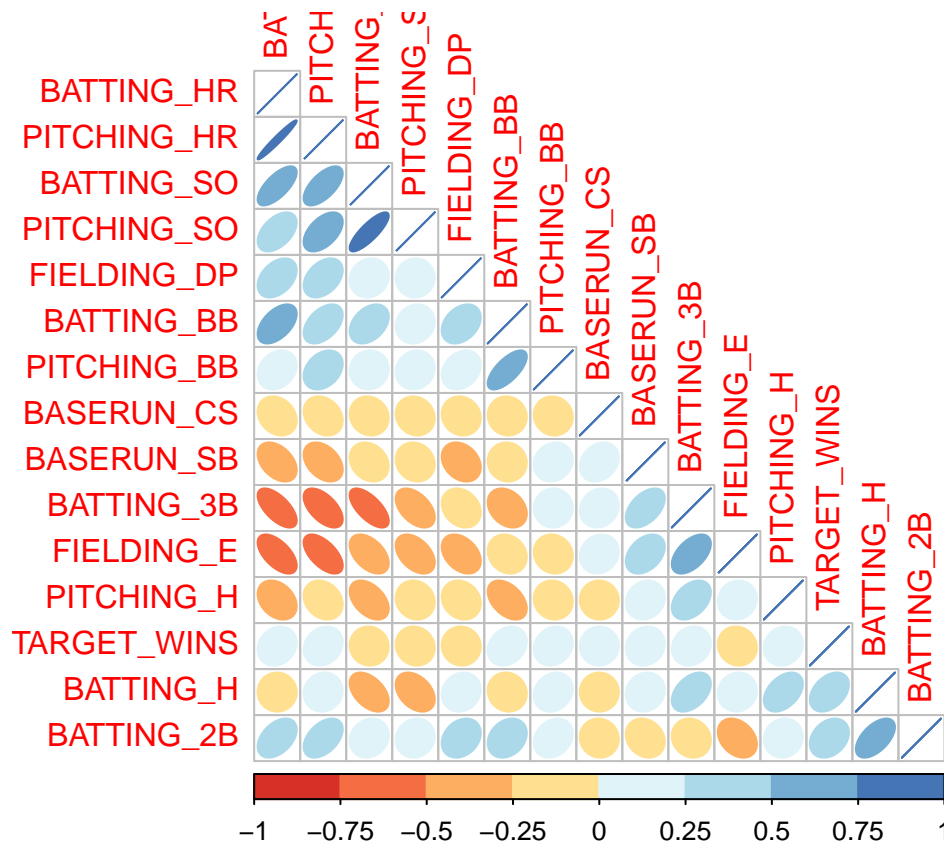
## 9    0.105034615  PITCHING_H
## 10   0.009835166  BASERUN_CS
## 11  -0.030050754  FIELDING_DP
## 12  -0.037712096  BATTING_SO
## 13  -0.083637577  FIELDING_E
## 14  -0.089519609  PITCHING_SO

```

BATTING\_H and BATTING\_2B have the highest correlation (positive) with TOTAL\_WINS; this makes sense given that more hits means more points/runs, and thus likelihood to win the game. The other variables have weak or slightly negative correlation, which can imply they might have little predictive power.

## Multicollinearity

One problem that can occur with multi-variable regression is correlation between variables, or multicollinearity. A quick check is to run correlations between variables.



We can see that some variables are highly correlated with one another, such as PITCHING\_BB and BATTING\_BB. When we start considering features for our models, we'll need to account for the correlations between features and avoid including pairs with strong correlations.

As a note, this dataset is challenging as many of the predictive features go hand-in-hand with other feature and multicollinearity will be a problem. Better teams will see all positive features go up and negative features go down and vice versa. Many features are also inherently associated, for example, as batter strike outs increase, we would expect a decrease in hit metrics. As Base Hits increase, we would expect to see increases in the 2B, 3B and 4B columns, etc.

## 2. Data Preparation

To summarize our data preparation and exploration, we can distinguish our findings into a few categories below:

### Removed Fields

We removed the `BATTING_HBP` field as it was missing >90% of the data and the `INDEX` field as it offers no information for a model.

### Missing Values

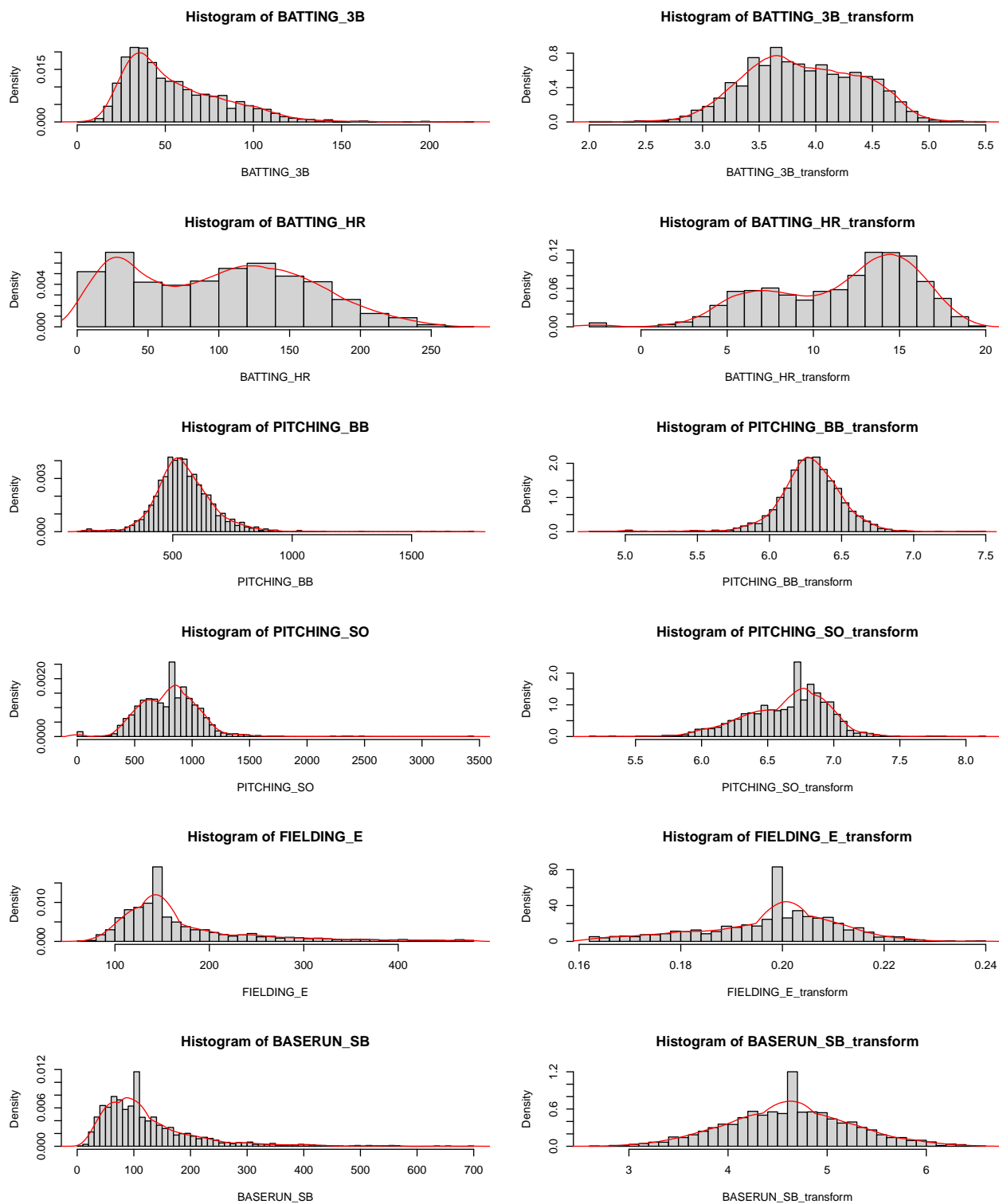
There were missing values found in `BASERUN_CS` (Caught Stolen Bases), `FIELDING_DP` (Double plays), `BASERUN_SB` (Stolen Bases), `BATTING_SO` (Batter Strike outs), `PITCHING_SO` (Pitcher Strike outs) so we decided to replace these missing values with their corresponding median values. It is highly unlikely that teams had none of these during an entire season.

### Outliers

There are unreasonable outliers found in `PITCHING_SO` (pitching strikeouts), `PITCHING_H` (allowed hits per game), `PITCHING_BB` (walks), and `FIELDING_E` (fielding errors) that exceed what is reasonable or possible given standard game length. While specific games might have outliers (e.g. in a game with extra innings), we wouldn't expect the totals per season to allow for outliers in every game. Given this, we will replace any outliers with the median for the data set. Limits we set included: > 4000 `PITCHING_SO` (25 strikeouts per game), > 5000 `PITCHING_H` (30 hits allowed per game), > 2000 `PITCHING_BB` (13 walks per game) and > 480 `FIELDING_E` (3 errors per game).

### Transform non-normal variables

Finally, as mentioned earlier in our data exploration, and our findings from our histogram plots, we can see that some of our variables are highly skewed. To address this, we decided to perform some transformations to make them more normally distributed. Here are some plots to demonstrate the changes in distributions before and after the transformations:



## Finalizing the dataset for model building

With our transformations complete, we can now add these into our `clean_df` dataframe and continue on to build our models.

### 3. Build Models

*Using the training data set, build at least three different multiple linear regression models, using different variables (or the same variables with different transformations). Since we have not yet covered automated variable selection methods, you should select the variables manually (unless you previously learned Forward or Stepwise selection, etc.). Since you manually selected a variable for inclusion into the model or exclusion into the model, indicate why this was done. Discuss the coefficients in the models, do they make sense? For example, if a team hits a lot of Home Runs, it would be reasonably expected that such a team would win more games. However, if the coefficient is negative (suggesting that the team would lose more games), then that needs to be discussed. Are you keeping the model even though it is counter intuitive? Why? The boss needs to know.*

#### Model-building methodology

With a solid understanding of our dataset at this point, and with our data cleaned, we can now start to build out some of our multiple linear regression models.

First, we decided to split our cleaned dataset into a training and testing set (80% training, 20% testing). Then, using our training dataset, we decided to run a multiple linear regression model (Model #1) that included all non-transformed features that we hadn't removed following our data cleaning process mentioned above. Next, in Model #2, to help us select the optimal set of features, we ran the `stepAIC` function in R to perform stepwise selection on our initial model to help reduce the number of features and address some of our multicollinearity issues from Model #1 (explained more below). Finally, our last model (Model #3) included all data from our cleaned dataset, but also contained some of our transformed features in replacement of their non-transformed counterparts. Additionally, we ran this model through stepwise selection as well to determine the optimal set of features and to reduce multicollinearity as much as possible.

#### Examining our model coefficients

Throughout our model-building process, we noticed that many of our model outputs yielded a few coefficient values that seemed to contradict our initial estimates. For instance, in Model #1:

##### Negative values for coefficients that we'd expect to be positive

- `BATTING_2B` - logically more doubles hit by batters would increase the likelihood of winning more games
- `BATTING_HR` - logically more homeruns hit by batters would increase the likelihood of winning more games
- `PITCHING_SO` - logically more strikeouts thrown by pitchers would increase the likelihood of winning more games
- `FIELDING_DP` - logically more double plays turned by a team would increase the likelihood of winning more games

##### Positive values for coefficients that we'd expect to be negative

- `BATTING_SO` - logically more strikeouts by batters would lead to less of a likelihood of winning more games
- `PITCHING_H` - logically more hits given up by pitchers would lead to less of a likelihood of winning more games

- PITCHING\_HR - logically more homeruns given up by pitchers would lead to less of a likelihood of winning more games

This is a trend we saw throughout the three models that we built, although Model #3 was able to adjust for this better than our first two models – we can likely attribute this phenomenon to multicollinearity. Since we noticed in our initial data exploration that many variables in the dataset were highly correlated with one another (i.e. BATTING\_2B and BATTING\_HR), this phenomenon likely is increasing the variance of the coefficient estimates, making them difficult to interpret (and in some cases such as the features listed above, they are switching the signs). This was also supported by our Variance Inflation Factor (VIF) tests, which showed high values for features such as BATTING\_HR, BATTING\_SO, PITCHING\_HR, and PITCHING\_SO. In our final model (Model #3), we made sure to keep this in mind in order to get a better handle on our coefficients and reduce multicollinearity – mainly, we removed certain variables that had high VIF scores through our stepwise selection process. Later in our discussion, we'll discuss whether or not we'd keep our final model based on this issue.

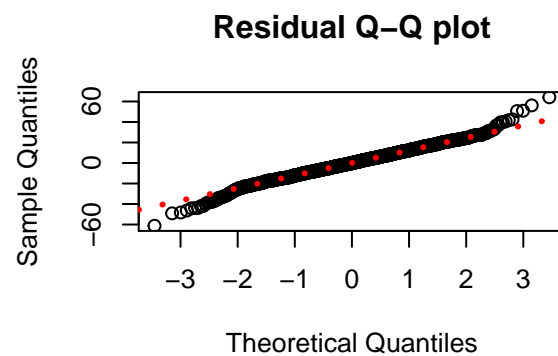
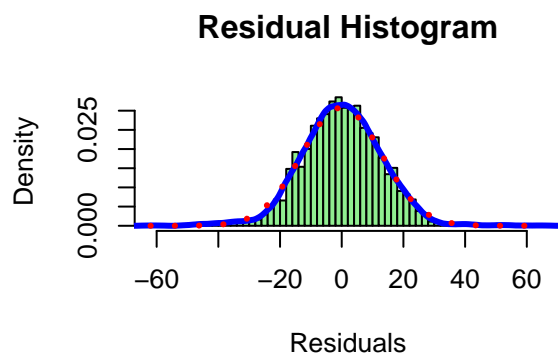
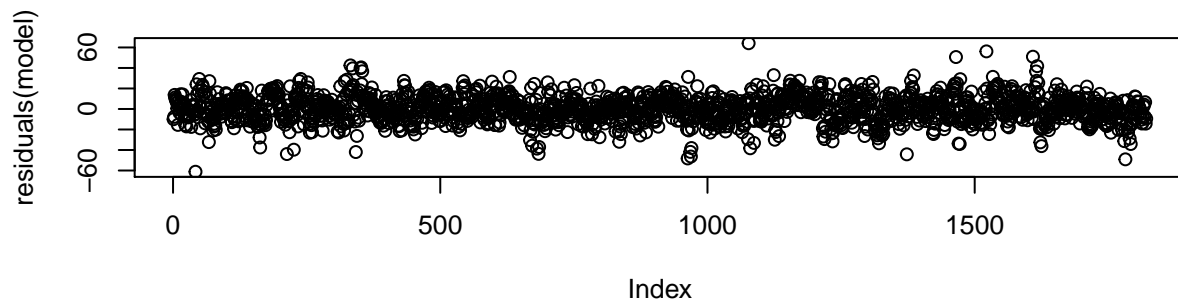
## Model 1

As mentioned above, below is our initial multiple linear regression model that includes all features from our cleaned dataset.

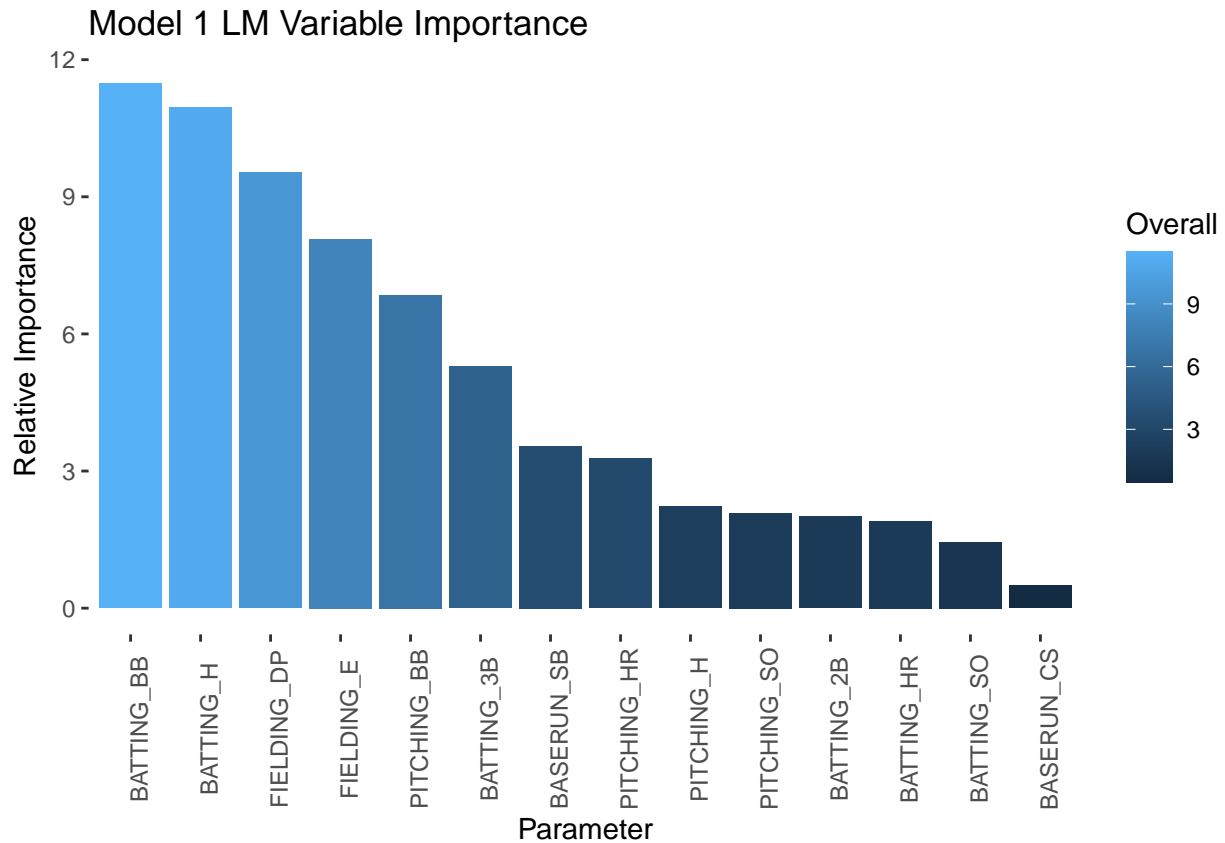
```
##
## Call:
## lm(formula = TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B +
##     BATTING_HR + BATTING_BB + BATTING_SO + BASERUN_SB + BASERUN_CS +
##     PITCHING_H + PITCHING_HR + PITCHING_BB + PITCHING_SO + FIELDING_E +
##     FIELDING_DP, data = df_train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -61.219  -8.227  -0.078   8.275  64.097
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  19.159307   6.307639   3.037 0.002420 **
## BATTING_H     0.045729   0.004176  10.950 < 2e-16 ***
## BATTING_2B   -0.020206   0.010083  -2.004 0.045228 *
## BATTING_3B    0.098643   0.018671   5.283 1.42e-07 ***
## BATTING_HR   -0.064392   0.033802  -1.905 0.056944 .
## BATTING_BB    0.062187   0.005419  11.476 < 2e-16 ***
## BATTING_SO    0.006454   0.004455   1.449 0.147609
## BASERUN_SB    0.016532   0.004656   3.550 0.000394 ***
## BASERUN_CS   -0.008546   0.017416  -0.491 0.623716
## PITCHING_H    0.002280   0.001022   2.231 0.025803 *
## PITCHING_HR   0.098044   0.029903   3.279 0.001063 **
## PITCHING_BB  -0.031403   0.004585  -6.848 1.02e-11 ***
## PITCHING_SO  -0.006677   0.003202  -2.085 0.037196 *
## FIELDING_E   -0.046709   0.005781  -8.080 1.17e-15 ***
## FIELDING_DP  -0.141952   0.014887  -9.535 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.99 on 1806 degrees of freedom
## Multiple R-squared:  0.3143, Adjusted R-squared:  0.309
```

```
## F-statistic: 59.14 on 14 and 1806 DF, p-value: < 2.2e-16
```

```
##           2.5 %           97.5 %  
## (Intercept) 6.7882721761 31.5303425736  
## BATTING_H   0.0375385910 0.0539198420  
## BATTING_2B -0.0399821239 -0.0004299296  
## BATTING_3B  0.0620239169 0.1352624539  
## BATTING_HR -0.1306881198 0.0019035737  
## BATTING_BB  0.0515586246 0.0728152929  
## BATTING_SO -0.0022838297 0.0151917050  
## BASERUN_SB  0.0073994809 0.0256640050  
## BASERUN_CS -0.0427037715 0.0256123654  
## PITCHING_H  0.0002756037 0.0042835297  
## PITCHING_HR 0.0393959474 0.1566927835  
## PITCHING_BB -0.0403967131 -0.0224100318  
## PITCHING_SO -0.0129569170 -0.0003966439  
## FIELDING_E  -0.0580462638 -0.0353716216  
## FIELDING_DP -0.1711508024 -0.1127541087
```



We can explicitly call out our variable importance using the Caret package which will determine our feature importance for each of the multiple linear regression models individually.



```
## [1] "VIF scores of predictors"
```

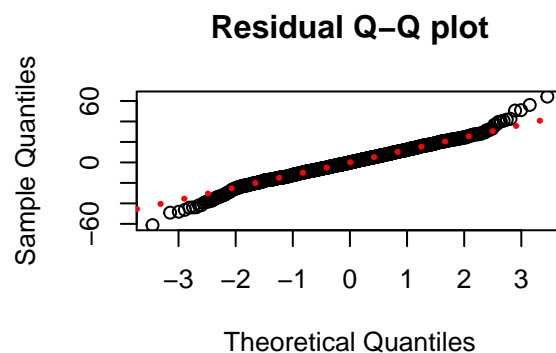
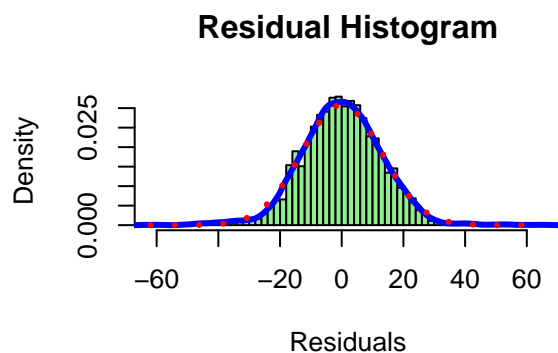
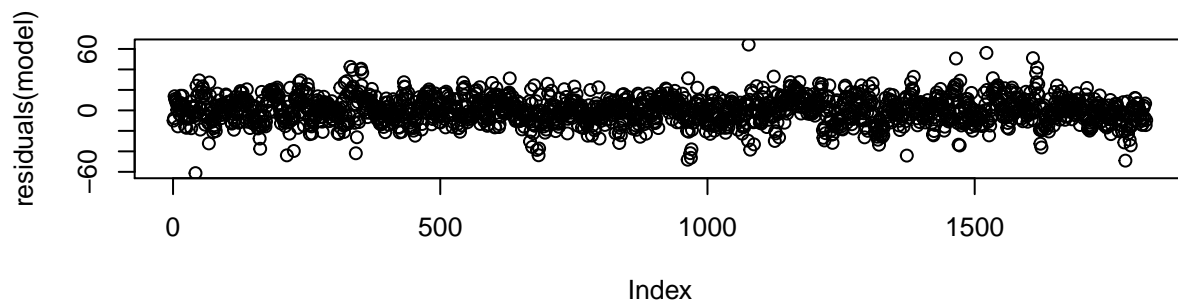
```
##      BATTING_H  BATTING_2B  BATTING_3B  BATTING_HR  BATTING_BB  BATTING_SO
##      3.982149   2.392001   2.908248   44.695422    4.722647   12.426490
##      BASERUN_SB  BASERUN_CS  PITCHING_H  PITCHING_HR  PITCHING_BB  PITCHING_SO
##      1.700422    1.122540    2.059995   35.894247    3.740457    7.148733
##      FIELDING_E  FIELDING_DP
##      1.993090    1.438791
```

## Model 2

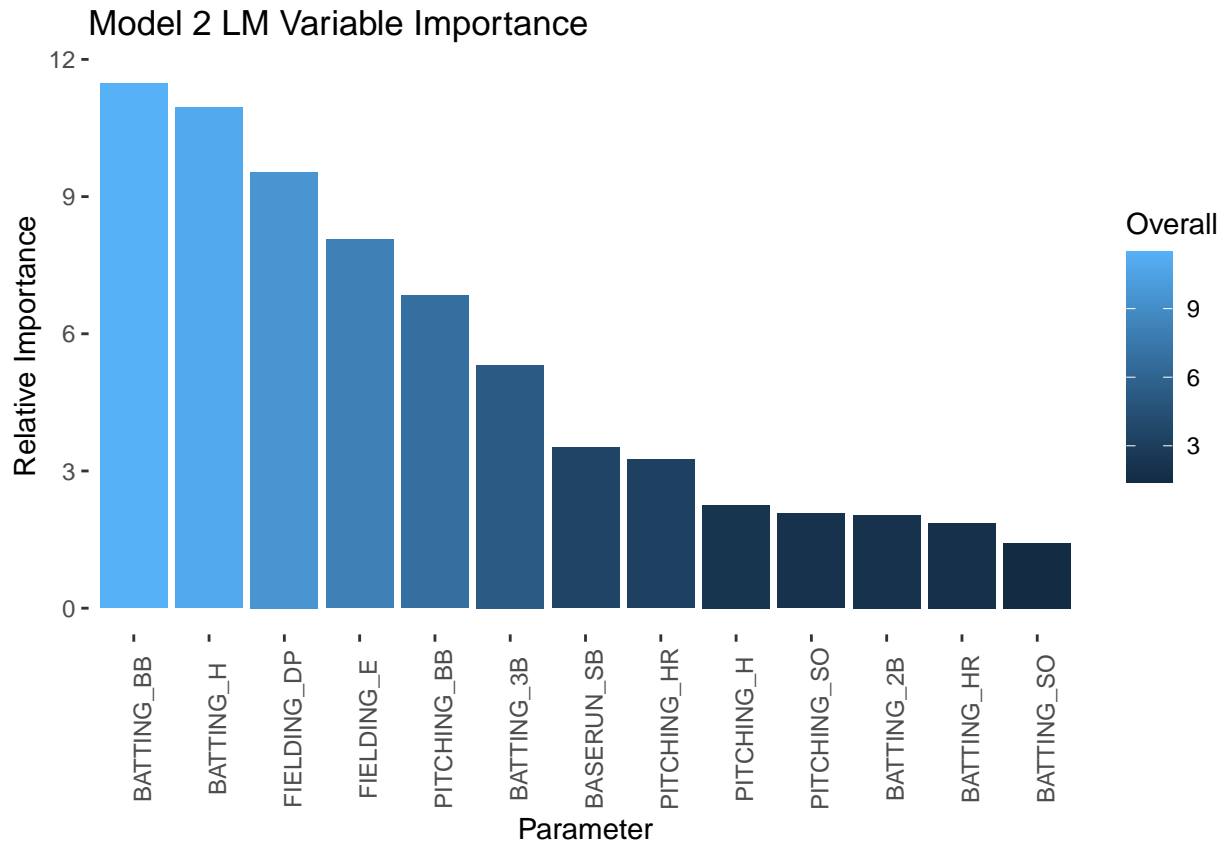
In our second model, below, we decided to use stepwise selection in order to help us determine the optimal set of features from our original, cleaned dataset.

```
##
## Call:
## lm(formula = TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B +
##      BATTING_HR + BATTING_BB + BATTING_SO + BASERUN_SB + PITCHING_H +
##      PITCHING_HR + PITCHING_BB + PITCHING_SO + FIELDING_E + FIELDING_DP,
##      data = df_train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -61.233  -8.200  -0.015   8.302  64.234
##
```

```
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 18.720588   6.242634   2.999 0.002747 **
## BATTING_H    0.045677   0.004174  10.943 < 2e-16 ***
## BATTING_2B   -0.020475   0.010066  -2.034 0.042098 *
## BATTING_3B    0.099109   0.018643   5.316 1.19e-07 ***
## BATTING_HR   -0.062516   0.033578  -1.862 0.062794 .
## BATTING_BB    0.062017   0.005407  11.470 < 2e-16 ***
## BATTING_SO    0.006336   0.004448   1.425 0.154462
## BASERUN_SB   0.016165   0.004595   3.518 0.000446 ***
## PITCHING_H    0.002305   0.001020   2.260 0.023947 *
## PITCHING_HR   0.097186   0.029846   3.256 0.001150 **
## PITCHING_BB  -0.031213   0.004568  -6.833 1.13e-11 ***
## PITCHING_SO  -0.006602   0.003198  -2.064 0.039115 *
## FIELDING_E   -0.046569   0.005772  -8.068 1.29e-15 ***
## FIELDING_DP  -0.141912   0.014884  -9.534 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 12.99 on 1807 degrees of freedom
## Multiple R-squared:  0.3143, Adjusted R-squared:  0.3093
## F-statistic: 63.7 on 13 and 1807 DF, p-value: < 2.2e-16
```







```
## [1] "VIF scores of predictors"
```

```
##      BATTING_H  BATTING_2B  BATTING_3B  BATTING_HR  BATTING_BB  BATTING_SO
##      3.979587   2.384946   2.900725   44.123572    4.703397   12.390288
##      BASERUN_SB  PITCHING_H  PITCHING_HR  PITCHING_BB  PITCHING_SO  FIELDING_E
##      1.656576   2.054487   35.771529    3.713621    7.132372    1.988251
##      FIELDING_DP
##      1.438747
```

### Model 3

In our third model, we decided to utilize some of our transformed variables to compare against our initial model. Additionally, similar to model 2, we used stepwise selection to determine feature importance and select the simplest model possible.

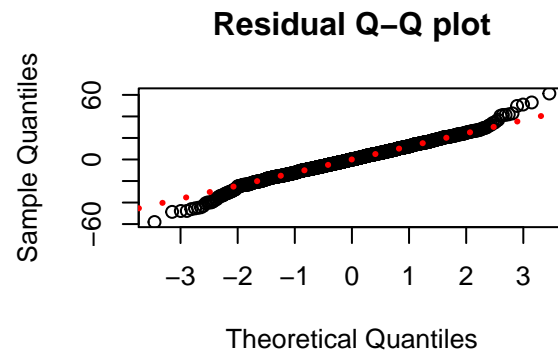
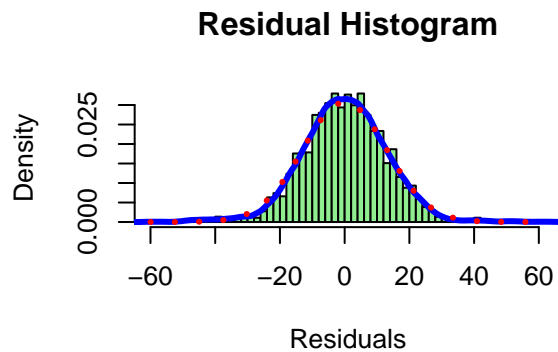
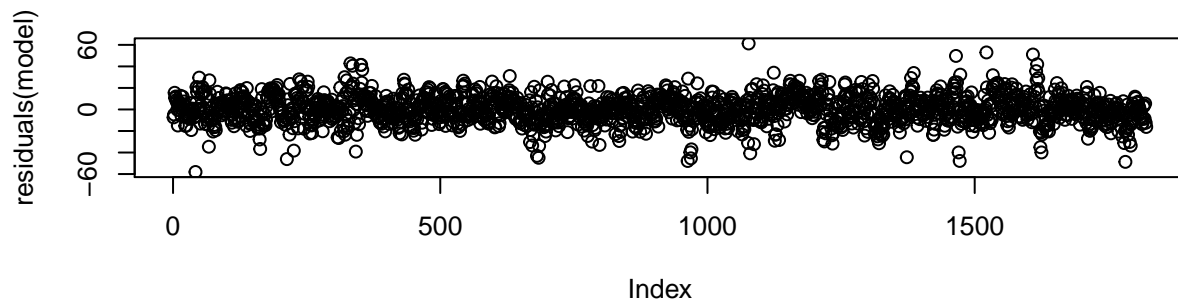
```
##
## Call:
## lm(formula = TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B_transform +
##      BATTING_HR_transform + BATTING_BB + BATTING_SO + BASERUN_SB_transform +
##      BASERUN_CS + PITCHING_H + PITCHING_HR + PITCHING_BB_transform +
##      PITCHING_SO_transform + FIELDING_E_transform + FIELDING_DP,
##      data = df_train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```

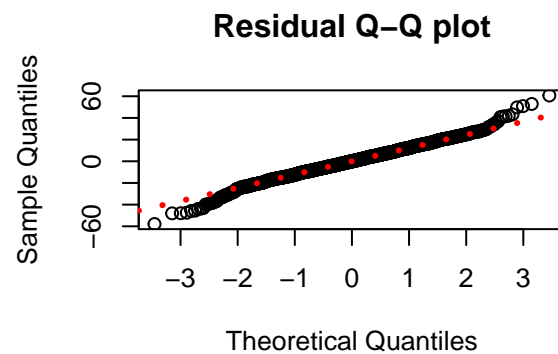
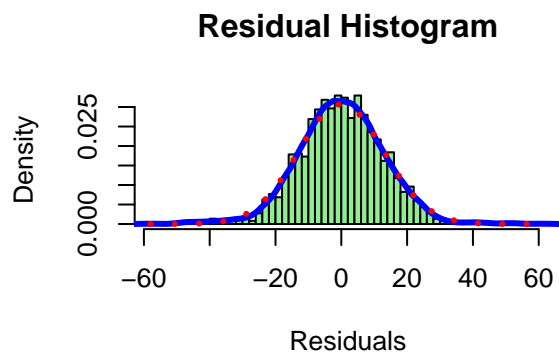
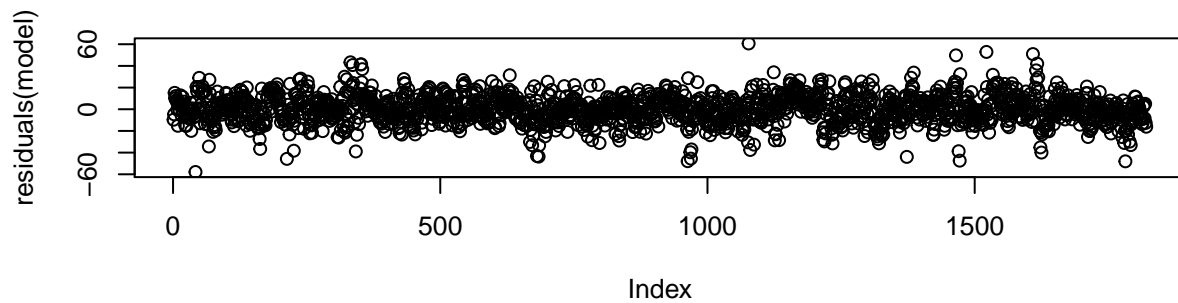
## -58.076  -8.145   0.051   8.272  61.294
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      8.476e+00  2.086e+01   0.406  0.68449
## BATTING_H         4.645e-02  4.162e-03  11.162 < 2e-16 ***
## BATTING_2B        -2.051e-02  1.004e-02  -2.044  0.04113 *
## BATTING_3B_transform  6.305e+00  1.013e+00   6.226 5.92e-10 ***
## BATTING_HR_transform -5.733e-02  3.423e-01  -0.168  0.86699
## BATTING_BB         6.444e-02  6.292e-03  10.241 < 2e-16 ***
## BATTING_SO        -3.839e-03  4.378e-03  -0.877  0.38064
## BASERUN_SB_transform  2.106e+00  6.474e-01   3.252  0.00117 **
## BASERUN_CS        -7.216e-03  1.811e-02  -0.398  0.69038
## PITCHING_H         1.226e-04  1.077e-03   0.114  0.90934
## PITCHING_HR         4.067e-02  2.032e-02   2.002  0.04547 *
## PITCHING_BB_transform -1.649e+01  2.685e+00  -6.140 1.01e-09 ***
## PITCHING_SO_transform  1.557e+00  2.857e+00   0.545  0.58575
## FIELDING_E_transform  2.789e+02  3.613e+01   7.720 1.92e-14 ***
## FIELDING_DP        -1.384e-01  1.530e-02  -9.049 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.04 on 1806 degrees of freedom
## Multiple R-squared:  0.309, Adjusted R-squared:  0.3037
## F-statistic: 57.69 on 14 and 1806 DF, p-value: < 2.2e-16

##              2.5 %      97.5 %
## (Intercept)    -32.428934106  4.938152e+01
## BATTING_H        0.038288318  5.461267e-02
## BATTING_2B       -0.040197396 -8.267731e-04
## BATTING_3B_transform  4.319302256  8.291619e+00
## BATTING_HR_transform -0.728612807  6.139452e-01
## BATTING_BB        0.052098342  7.678028e-02
## BATTING_SO       -0.012425392  4.747207e-03
## BASERUN_SB_transform  0.835919512  3.375463e+00
## BASERUN_CS       -0.042738724  2.830686e-02
## PITCHING_H       -0.001988975  2.234216e-03
## PITCHING_HR        0.000821262  8.052069e-02
## PITCHING_BB_transform -21.754732546 -1.122123e+01
## PITCHING_SO_transform -4.045693300  7.160179e+00
## FIELDING_E_transform 208.032462919  3.497396e+02
## FIELDING_DP      -0.168440098 -1.084293e-01

```

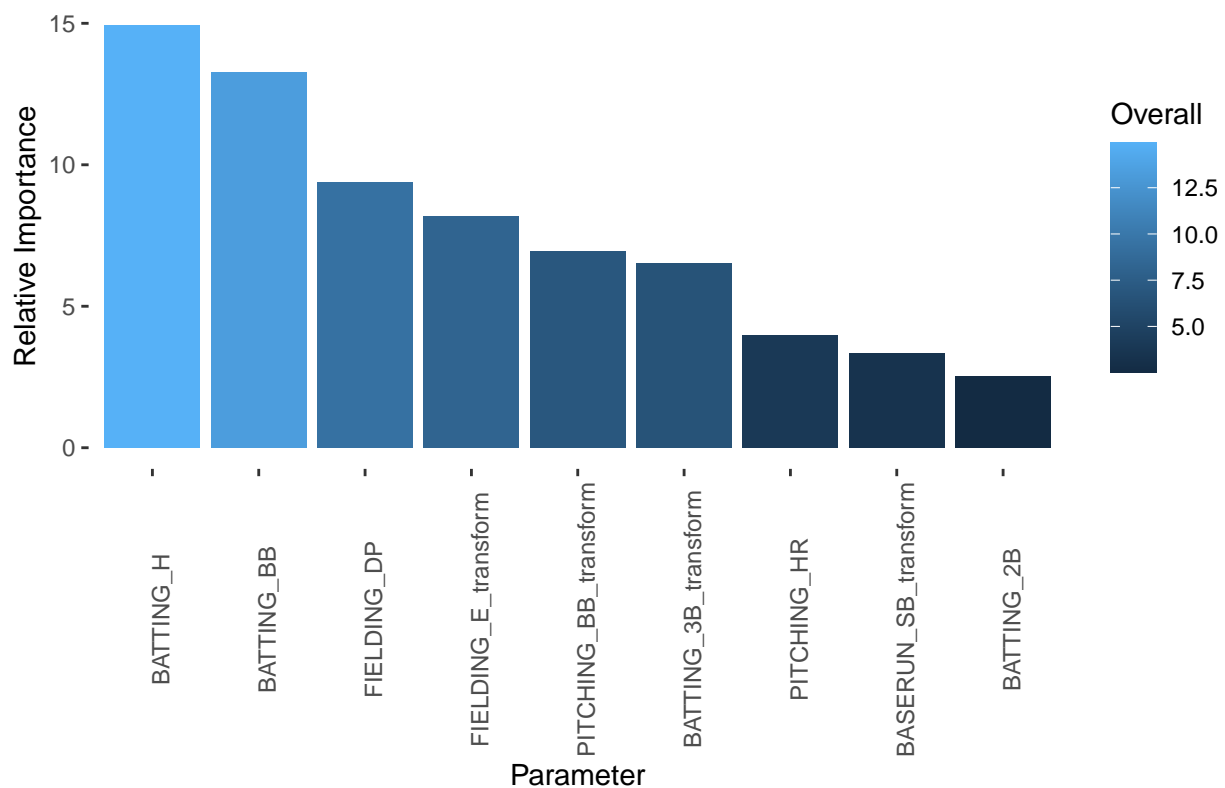


```
##
## Call:
## lm(formula = TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B_transform +
##   BATTING_BB + BASERUN_SB_transform + PITCHING_HR + PITCHING_BB_transform +
##   FIELDING_E_transform + FIELDING_DP, data = df_train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -57.878  -8.218  -0.006   8.246  60.682
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    6.879163   13.255656   0.519  0.603852
## BATTING_H        0.048322    0.003235  14.938 < 2e-16 ***
## BATTING_2B     -0.024057    0.009552  -2.518  0.011871 *
## BATTING_3B_transform  6.489195    0.995661   6.517  9.24e-11 ***
## BATTING_BB       0.060577    0.004561  13.283 < 2e-16 ***
## BASERUN_SB_transform  1.892989    0.565988   3.345  0.000841 ***
## PITCHING_HR      0.034267    0.008648   3.962  7.71e-05 ***
## PITCHING_BB_transform -15.064064    2.166169  -6.954  4.93e-12 ***
## FIELDING_E_transform 280.475431   34.237604   8.192  4.80e-16 ***
## FIELDING_DP     -0.138331    0.014738  -9.386 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.03 on 1811 degrees of freedom
## Multiple R-squared:  0.3083, Adjusted R-squared:  0.3049
## F-statistic: 89.7 on 9 and 1811 DF, p-value: < 2.2e-16
```



We can assess variable importance of our model with our original dataset (model 2) to our transformed dataset (model 3) as shown below. We notice that “Batting\_BB” and “Batting\_H” are much closer together in terms of weight in predicting target\_wins than in model 1 (pre-transformed)

### Model 3 LM Variable Importance



```
## [1] "VIF scores of predictors"
```

```
##          BATTING_H          BATTING_2B  BATTING_3B_transform
##          2.374987          2.133918          2.575616
##          BATTING_BB  BASERUN_SB_transform          PITCHING_HR
##          3.324985          1.333406          2.984269
## PITCHING_BB_transform  FIELDING_E_transform          FIELDING_DP
##          2.784566          2.238671          1.401629
```

## 4. Model Selection & Analysis

*For the multiple linear regression model, will you use a metric such as Adjusted R<sup>2</sup>, RMSE, etc.? Be sure to explain how you can make inferences from the model, discuss multi-collinearity issues (if any), and discuss other relevant model output. Using the training data set, evaluate the multiple linear regression model based on (a) mean squared error, (b) R<sup>2</sup>, (c) F-statistic, and (d) residual plots. Make predictions using the evaluation data set.*

The following table discusses each of the model performance metrics on the training dataset. These values indicate there is a minor improvement in model performance after applying transformations and selecting for significant parameters.

All models achieved a positive adjusted R<sup>2</sup> pointing to a weakly-positive relationship between the target variable TOTAL\_WINS and the model predictor variables.

From the previous section and residual diagnostics (both the residual histogram and QQ plot)—all three models have normally distributed residuals with mean 0. There appears to be no heteroskedasticity (non-constant variance) or serial-correlation within the residuals—thus strictly from a linear regression perspective, none of the assumptions are violated and thus we can make inferential predictions based on our model.

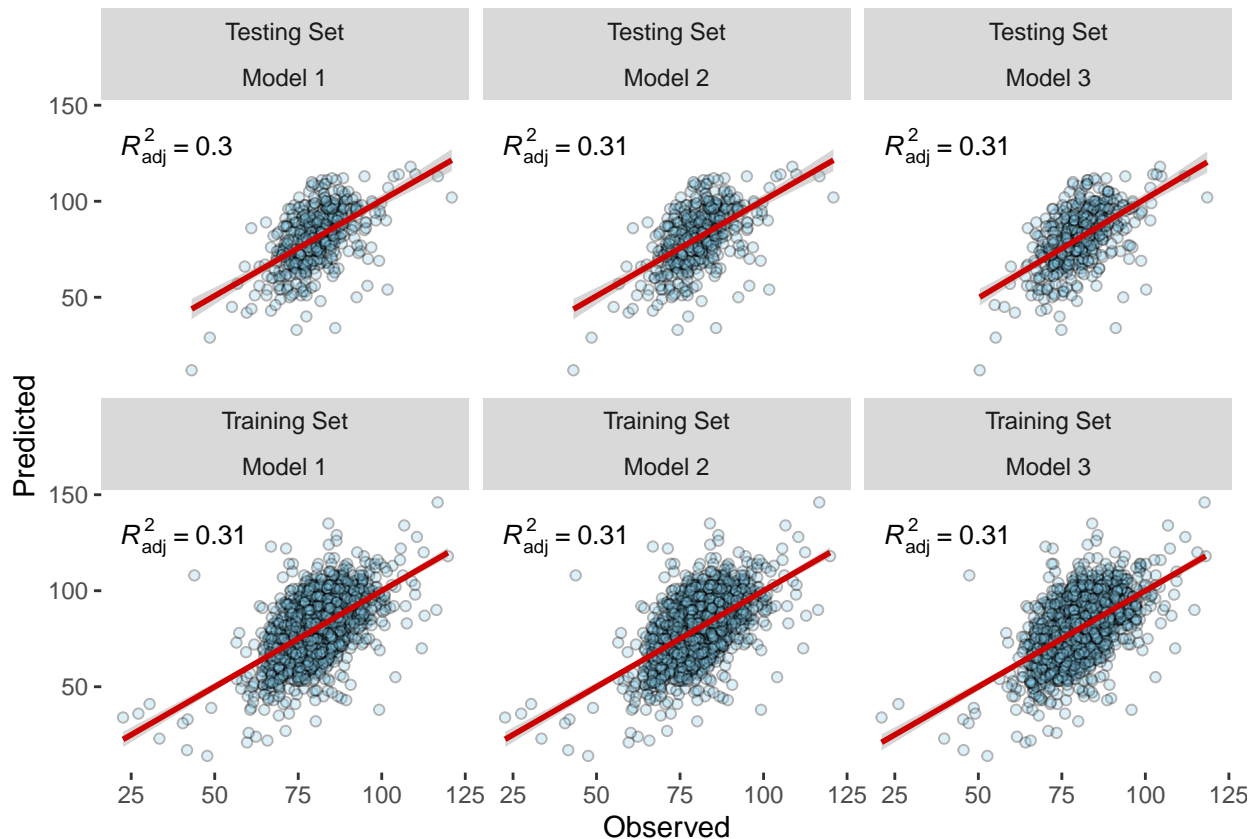
Next looking at the F-statistic for all models were large and achieved a statistically significant p-value than than a default alpha of .05; thus for all three models the Null hypothesis that is rejected that 0s for our regression coefficients would fit the data better.

From the exploratory data analysis we saw that many of the predictor variables were correlated with each other—this makes sense given that baseball is a team sport, and thus different position scoring/runs helps contribute to wins. However this could be an issue from a multicollinearity, that can lead to unstable regression fits. From the previous section we used VIF (Variable Inflation Factor) to gauge better models by preferring VIF values less than 5.

	RSE	Adj.R2	F.Statistic
Model 1	12.99105	0.3090296	59.14120
Model 2	12.98832	0.3093199	63.69877
Model 3	13.02985	0.3048964	89.70165

The following figure represents the performance of 3 of the models on both the testing and on the training dataset. for this multiple linear regression problem, the adjusted R<sup>2</sup> value was used as the metric for performance on predicting the target wins.

```
## `geom_smooth()` using formula 'y ~ x'
```



The analysis shows the following results:

Model 1 - This model is based on the all predictors on an un-transformed dataset. Results for this model provided an  $R^2$  of about of 0.31 on the training set and 0.3 on the testing dataset.

Model 2 - This model is based on a subset of significant predictors on an un-transformed dataset. Results for this model provided an  $R^2$  of about of 0.31 on the training set and 0.31 on the testing dataset.

Model 3 - This model is based on a subset of significant predictors on an transformed dataset. Results for this model provided an  $R^2$  of about of 0.31 on the training set and 0.31 on the testing dataset.

### Model of choice

Based on these analyses, Model 2 and Model 3 both performed marginally better than Model 1 and could be selected as the linear model of choice when looking at adjusted  $R^2$ . However, there is greater statistical significance under the third model relative to the others and uses less unnecessary variables to compute our prediction without sacrificing much in terms of adjusted  $R^2$  value. Additionally, Model 3 seems to have lower VIF scores than Models 1 and 2. Because of these factors, as well as its better adjustment for multicollinearity (we noticeably saw less sign-flipping in coefficients) and thus model 3 would be the model of choice.

### References

- A Modern Approach to Regression with R: Simon Sheather
- Linear Models with R: Julian Faraway.
- R package vignette, mixtools: An R Package for Analyzing Finite Mixture Models
- 7 Classic OLS assumptions
- Detecting Multicollinearity with VIF

## Appendix

### A. Moneyball Dataset Columns

- INDEX: Identification Variable(Do not use)
- TARGET\_WINS: Number of wins
- TEAM\_BATTING\_H : Base Hits by batters (1B,2B,3B,HR)
- TEAM\_BATTING\_2B: Doubles by batters (2B)
- TEAM\_BATTING\_3B: Triples by batters (3B)
- TEAM\_BATTING\_HR: Home runs by batters (4B)
- TEAM\_BATTING\_BB: Walks by batters
- TEAM\_BATTING\_HBP: Batters hit by pitch (get a free base)
- TEAM\_BATTING\_SO: Strikeouts by batters
- TEAM\_BASERUN\_SB: Stolen bases
- TEAM\_BASERUN\_CS: Caught stealing
- TEAM\_FIELDING\_E: Errors
- TEAM\_FIELDING\_DP: Double Plays
- TEAM\_PITCHING\_BB: Walks allowed
- TEAM\_PITCHING\_H: Hits allowed
- TEAM\_PITCHING\_HR: Homeruns allowed
- TEAM\_PITCHING\_SO: Strikeouts by pitchers

### R Code

```
# =====  
# Load Libraries and Define Helper functions  
# =====  
  
library(MASS)  
library(rpart.plot)  
library(ggplot2)  
library(ggfortify)  
library(gridExtra)  
library(forecast)  
library(fpp2)  
library(fma)  
library(kableExtra)  
library(e1071)  
library(mlbench)  
library(ggcorrplot)  
library(DataExplorer)  
library(timeDate)  
library(caret)  
library(GGally)  
library(corrplot)  
library(RColorBrewer)  
library(tibble)  
library(tidyr)  
library(tidyverse)  
library(dplyr)  
library(reshape2)  
library(mixtools)  
library(tidymodels)
```

```

library(ggpmisc)
library(regclass)

#' Print a side-by-side Histogram and QQPlot of Residuals
#'
#' @param model A model
#' @examples
#' residPlot(myModel)
#' @return null
#' @export
residPlot <- function(model) {
  # Make sure a model was passed
  if (is.null(model)) {
    return
  }

  layout(matrix(c(1,1,2,3), 2, 2, byrow = TRUE))
  plot(residuals(model))
  hist(model[["residuals"]], freq = FALSE, breaks = "fd", main = "Residual Histogram",
        xlab = "Residuals",col="lightgreen")
  lines(density(model[["residuals"]], kernel = "ep"),col="blue", lwd=3)
  curve(dnorm(x,mean=mean(model[["residuals"]]), sd=sd(model[["residuals"]])), col="red", lwd=3, lty="dotted",
        main = "Residual Q-Q plot")
  qqnorm(model[["residuals"]], main = "Residual Q-Q plot")
  qqline(model[["residuals"]],col="red", lwd=3, lty="dotted")
  par(mfrow = c(1, 1))
}

#' Print a Variable Importance Plot for the provided model
#'
#' @param model The model
#' @param chart_title The Title to show on the plot
#' @examples
#' variableImportancePlot(myLinearModel, 'My Title')
#' @return null
#' @export
variableImportancePlot <- function(model=NULL, chart_title='Variable Importance Plot') {
  # Make sure a model was passed
  if (is.null(model)) {
    return
  }

  # use caret and ggplot to print a variable importance plot
  varImp(model) %>% as.data.frame() %>%
    ggplot(aes(x = reorder(rownames(.), desc(Overall)), y = Overall)) +
    geom_col(aes(fill = Overall)) +
    theme(panel.background = element_blank(),
          panel.grid = element_blank(),
          axis.text.x = element_text(angle = 90)) +
    scale_fill_gradient() +
    labs(title = chart_title,
         x = "Parameter",
         y = "Relative Importance")
}

```



```

#' Print a Facet Chart of histograms
#'
#' @param df Dataset
#' @param box Facet size (rows)
#' @examples
#' histbox(my_df, 3)
#' @return null
#' @export
histbox <- function(df, box) {
  par(mfrow = box)
  ndf <- dimnames(df)[[2]]

  for (i in seq_along(ndf)) {
    data <- na.omit(unlist(df[, i]))
    hist(data, breaks = "fd", main = paste("Histogram of", ndf[i]),
         xlab = ndf[i], freq = FALSE)
    lines(density(data, kernel = "ep"), col = 'red')
  }

  par(mfrow = c(1, 1))
}

#' Extract key performance results from a model
#'
#' @param model A linear model of interest
#' @examples
#' model_performance_extraction(my_model)
#' @return data.frame
#' @export
model_performance_extraction <- function(model=NULL) {
  # Make sure a model was passed
  if (is.null(model)) {
    return
  }

  data.frame("RSE" = model$sigma,
            "Adj R2" = model$adj.r.squared,
            "F-Statistic" = model$fstatistic[1])
}

# =====
# Load Data set
# =====

# Load Moneyball baseball dataset
df <- read.csv('datasets/moneyball-training-data.csv')
df_eval <- read.csv('datasets/moneyball-evaluation-data.csv')

# Remove superfluous TEAM_ from column names
names(df) <- names(df) %>%
  str_replace_all('TEAM_', '')

# Drop the INDEX column - this won't be useful

```

```

df <- df %>%
  dplyr::select(-INDEX)

# =====
# Summary Stats
# =====

# Display summary statistics
summary(df)

# =====
# Distributions
# =====

# Prepare data for ggplot
gather_df <- df %>%
  gather(key = 'variable', value = 'value')

# Histogram plots of each variable
ggplot(gather_df) +
  geom_histogram(aes(x=value, y = ..density..), bins=30) +
  geom_density(aes(x=value), color='blue') +
  facet_wrap(. ~variable, scales='free', ncol=4)

# Select BATTING_SO column and remove any missing data
df_mix <- df %>%
  dplyr::select(BATTING_SO) %>%
  drop_na()

# Calculate mixed distributions for BATTING_SO
batting_so_mix <- normalmixEM(df_mix$BATTING_SO,
                             lambda = .5,
                             mu = c(400, 1200),
                             sigma = 5,
                             maxit=60)

# Simple plot to illustrate possible bimodal mix of groups
plot(batting_so_mix,
     whichplots = 2,
     density = TRUE,
     main2 = "BATTING_SO Possible Distributions",
     xlab2 = "BATTING_SO")

# =====
# Boxplots
# =====

# Prepare data for ggplot
gather_df <- df %>%
  gather(key = 'variable', value = 'value')

# Boxplots for each variable
ggplot(gather_df, aes(variable, value)) +
  geom_boxplot() +

```

```

    facet_wrap(. ~variable, scales='free', ncol=6)

# =====
# Variable Plots
# =====

# Plot scatter plots of each variable versus the target variable
featurePlot(df[,2:ncol(df)], df[,1], pch = 20)

# =====
# Missing Data
# =====

# Identify missing data by Feature and display percent breakout
missing <- colSums(df %>% sapply(is.na))
missing_pct <- round(missing / nrow(df) * 100, 2)
stack(sort(missing_pct, decreasing = TRUE))

# Drop the BATTING_HBP field
df <- df %>%
  select(-BATTING_HBP)

# We have chosen to impute the median as there are strong outliers that may skew the mean. Could revisit
no_outlier_df <- df

# 4000 strikeouts is an average of 25 strikeouts per game, which is ridiculous.
no_outlier_df$PITCHING_SO <- ifelse(no_outlier_df$PITCHING_SO > 4000, NA, no_outlier_df$PITCHING_SO)

# 5000 hits is an average of 30 hits allowed per game, which is also ridiculous.
no_outlier_df$PITCHING_H <- ifelse(no_outlier_df$PITCHING_H > 5000, NA, no_outlier_df$PITCHING_H)

# 2000 walks is an average of 13 walks per game which is unlikely.
no_outlier_df$PITCHING_BB <- ifelse(no_outlier_df$PITCHING_BB > 2000, NA, no_outlier_df$PITCHING_BB)

# more than 480 errors is an average of 3 per game which is unlikely.
no_outlier_df$FIELDING_E <- ifelse(no_outlier_df$FIELDING_E > 480, NA, no_outlier_df$FIELDING_E)

clean_df <- no_outlier_df %>%
  impute(what = 'median') %>% as.data.frame()

# From the plots, the team with 0 wins has 0 in multiple other categories. I believe this is missing data
clean_df <- clean_df %>%
  filter(TARGET_WINS != 0)

gather_clean_df <- clean_df %>%
  gather(key = 'variable', value = 'value', -TARGET_WINS)

# =====
# Feature-Target Correlations
# =====

# Show feature correlations/target by decreasing correlation
stack(sort(cor(clean_df[,1], clean_df[,2:ncol(clean_df)]), decreasing=TRUE))

```

```

# =====
# Multicollinearity
# =====

correlation = cor(clean_df, use = 'pairwise.complete.obs')

corrplot(correlation, 'ellipse', type = 'lower', order = 'hclust',
          col=brewer.pal(n=8, name="RdYlBu"))

# =====
# Transform non-normal variables
# =====

# created empty data frame to store transformed variables
df_temp <- data.frame(matrix(ncol = 1, nrow = length(clean_df$TARGET_WINS)))

# performed boxcox transformation after identifying proper lambda
df_temp$BATTING_3B <- clean_df$BATTING_3B
batting3b_lambda <- BoxCox.lambda(clean_df$BATTING_3B)
df_temp$BATTING_3B_transform <- log(clean_df$BATTING_3B)

# performed boxcox transformation after identifying proper lambda
df_temp$BATTING_HR <- clean_df$BATTING_HR
battingHR_lambda <- BoxCox.lambda(clean_df$BATTING_HR)
df_temp$BATTING_HR_transform <- BoxCox(clean_df$BATTING_HR, battingHR_lambda)

# performed a log transformation
df_temp$PITCHING_BB <- clean_df$PITCHING_BB
df_temp$PITCHING_BB_transform <- log(clean_df$PITCHING_BB)

# performed a log transformation
df_temp$PITCHING_SO <- clean_df$PITCHING_SO
df_temp$PITCHING_SO_transform <- log(clean_df$PITCHING_SO)

# performed an inverse log transformation
df_temp$FIELDING_E <- clean_df$FIELDING_E
df_temp$FIELDING_E_transform <- 1/log(clean_df$FIELDING_E)

# performed a log transformation
df_temp$BASERUN_SB <- clean_df$BASERUN_SB
df_temp$BASERUN_SB_transform <- log(clean_df$BASERUN_SB)

df_temp <- df_temp[, 2:13]

histbox(df_temp, c(6, 2))

# =====
# Final Cleaned Dataframe with transformations
# =====

# Build clean dataframe with transformation
clean_df <- data.frame(cbind(clean_df,
                             BATTING_3B_transform = df_temp$BATTING_3B_transform,

```

```

        BATTING_HR_transform = df_temp$BATTING_HR_transform,
        BASERUN_SB_transform = df_temp$BASERUN_SB_transform,
        PITCHING_BB_transform = df_temp$PITCHING_BB_transform,
        PITCHING_SO_transform = df_temp$PITCHING_SO_transform,
        FIELDING_E_transform = df_temp$FIELDING_E_transform))

is.na(clean_df) <- sapply(clean_df, is.infinite)

# Impute missing value with the mean
mean = mean(clean_df$BATTING_3B_transform, na.rm = TRUE)
mean2 = mean(clean_df$BASERUN_SB_transform, na.rm = TRUE)
mean3 = mean(clean_df$PITCHING_SO_transform, na.rm = TRUE)

clean_df$BATTING_3B_transform[is.na(clean_df$BATTING_3B_transform)] <- mean
clean_df$BASERUN_SB_transform[is.na(clean_df$BASERUN_SB_transform)] <- mean2
clean_df$PITCHING_SO_transform[is.na(clean_df$PITCHING_SO_transform)] <- mean3

# =====
# Model 1 (without stepAIC)
# =====

# Splitting the dataset into train/testing set with 80/20 split
set.seed(3)
df_split <- initial_split(clean_df, prop = 0.8)
df_train <- training(df_split)
df_test <- testing(df_split)

# Model 1 - Include all features and leverage stepAIC to help identify ideal features

multi_lm <- lm(TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B + BATTING_HR + BATTING_BB + BATTING_SO
(lm_s <- summary(multi_lm))
confint(multi_lm)
residPlot(lm_s)

# Model 1 - Display Variable feature importance plot
variableImportancePlot(multi_lm, "Model 1 LM Variable Importance")

# model 1 - print variable inflation factor score
print('VIF scores of predictors')

VIF(multi_lm)

# =====
# Model 2 (with stepAIC)
# =====

# Build model 2 - this is Model 1 with only significant features (using stepAIC)
mult_lm_final <- stepAIC(multi_lm, direction = "both",
                        scope = list(upper = multi_lm, lower = ~ 1),
                        scale = 0, trace = FALSE)

# Display Model 2 Summary
(lmf_s <- summary(mult_lm_final))

# Display Model 2 RResidual plots

```

```

residPlot(lmf_s)

# model 2 - Display Variable feature importance plot
variableImportancePlot(mult_lm_final, "Model 2 LM Variable Importance")

# model 2 - print variable inflation factor score
print('VIF scores of predictors')

VIF(mult_lm_final)

# =====
# Model 3 (with stepAIC and transformed features)
# =====

# Model 3 - Build linear model
multi_lm_2 <- lm(TARGET_WINS ~ BATTING_H + BATTING_2B + BATTING_3B_transform + BATTING_HR_transform + B

# Model 3 - Show model summary info
(lm_s_2 <- summary(multi_lm_2))

# Model 3 - Show Confidence and Residual Plots
confint(multi_lm_2)
residPlot(lm_s_2)

# Model 3 - use stepAIC to select significant features
multi_lm_final_2 <- stepAIC(multi_lm_2, direction = "both",
                           scope = list(upper = multi_lm_2, lower = ~ 1),
                           scale = 0, trace = FALSE)

# Model 3 - Show feature importance in final model after stepAIC
variableImportancePlot(mult_lm_final_2, "Model 3 LM Variable Importance")

# Model 3 - show Variance Inflation Factor score
print('VIF scores of predictors')

VIF(mult_lm_final_2)

# =====
# Select Models
# =====

# Build summary table with each model performance metrics
SummaryTable <- bind_rows(
  model_performance_extraction(lm_s),
  model_performance_extraction(lmf_s),
  model_performance_extraction(lmf_s_2)
)

# Add row names
rownames(SummaryTable) <- c("Model 1", "Model 2", "Model 3")

# Display nice format table
SummaryTable %>%
  kable() %>%

```

```

kable_styling(
  bootstrap_options = c("hover", "condensed", "responsive"),
  full_width = F)

# Build prediction results dataset for plotting (each model with training and test data)
results <- multi_lm %>%
  predict(df_train) %>%
  as.data.frame() %>%
  mutate(Predicted = df_train$TARGET_WINS, model = "Model 1") %>%
  bind_rows(mult_lm_final %>%
    predict(df_train) %>%
    as.data.frame() %>%
    mutate(Predicted = df_train$TARGET_WINS, model = "Model 2"),
    mult_lm_final_2 %>%
    predict(df_train) %>%
    as.data.frame() %>%
    mutate(Predicted = df_train$TARGET_WINS, model = "Model 3")) %>%
  rename("Observed" = ".") %>%
  mutate(dataset = "Training Set") %>%
  bind_rows(
    results_test <- multi_lm %>%
      predict(df_test) %>%
      as.data.frame() %>%
      mutate(Predicted = df_test$TARGET_WINS, model = "Model 1") %>%
      bind_rows(mult_lm_final %>%
        predict(df_test) %>%
        as.data.frame() %>%
        mutate(Predicted = df_test$TARGET_WINS, model = "Model 2"),
        mult_lm_final_2 %>%
        predict(df_test) %>% as.data.frame() %>%
        mutate(Predicted = df_test$TARGET_WINS, model = "Model 3")) %>%
      rename("Observed" = ".") %>%
      mutate(dataset = "Testing Set")
  )

# Plot each model with datapoints, model prediction line and R^2
results %>%
  ggplot(mapping = aes(x = Observed, y = Predicted)) +
  geom_point(pch = 21, alpha = 0.3, fill = "skyblue") +
  geom_smooth(method = "lm", color = "red3") +
  facet_wrap(dataset~model) +
  stat_poly_eq(aes(label = paste(..adj.rr.label.., sep = "~~~")),
    label.x.npc = "left", label.y.npc = .9,
    formula = y~x, parse = TRUE, size = 3.5)+
  theme(panel.background = element_blank(),
    panel.grid = element_blank())

```