

## Applied Statistic Modeling Assignment 2

Jiaming Deng 22302794

1)

1.  $\beta_0$  is the expected value of  $y_i$  when  $x_{i1}$  is equal to 0, that is, when the user is in group A.
2.  $\beta_1$  is the difference in the expected value of time  $y$  which is the time that users use the product between groups B and A when all other variables are held constant.
3.  $\epsilon_i$  is the random error term.

2)

1.  $\beta_0$  is the expected value of  $y_i$  when all other variables are 0.
  2.  $\beta_1$  is the influence of  $x_{i1}$  on  $y_i$  when  $x_{i2}$  is 1.
  3.  $\beta_2$  is the effect of  $x_{i2}$  equal to 2 on  $y_i$  when  $x_{i1}$  is 0.
  4.  $\beta_3$  is the effect of  $x_{i2}$  equal to 3 on  $y_i$  when  $x_{i1}$  is 0.
  5.  $\beta_4$  is the effect of the interaction between  $x_{i1}$  and  $x_{i2}=2$  on  $y_i$ .
  6.  $\beta_5$  is the effect of the interaction between  $x_{i1}$  and  $x_{i2}=3$  on  $y_i$ .
- Both  $\beta_2$  and  $\beta_3$  are used to obtain the influence of  $x_{i2}$  on  $y_i$ , because  $x_{i2}$  has three categories, namely 1, 2, and 3; according to the formula, it can be seen that  $x_{i2}=1$  is the control category, and  $\beta_2$  means that the category of  $x_{i2}=2$  and the control category are in the  $Y_i$  gap. In the same way,  $\beta_3$  represents the difference in  $y_i$  between the category with  $x_{i2}=3$  and the control category.
- $\beta_4$  and  $\beta_5$  are interaction terms that represent the effect of the combination of  $x_{i1}$  and  $x_{i2}$  on  $y_i$ . Specifically, as above,  $x_{i2}=1$  is the control category.  $\beta_4$  represents the difference in the effect of  $x_1$  on  $y$  between the class with  $x_2=2$  and the control class, while  $\beta_5$  represents the difference in the effect of  $x_1$  on  $y$  between the class with  $x_2=3$  and the control class.

The interpretation of the coefficients in Model 2 differs from that in Model 1 in that Model 2 includes an interaction term that allows the effect of  $x_{i1}$  on  $y_i$  to vary depending on the value of  $x_{i2}$  whereas Model 1 includes only a single coefficient for the effect of  $x_{i1}$  on  $y_i$ , assuming all Values are all affected the same.

3)

1. The coefficient of group B is estimated to be 0.004632, but  $\Pr(>|t|) = 0.993$  means that it is not statistically significant, indicating that users do not spend significantly more time using the new interface than the old interface.
2. Adjusted R-squared is -0.00505, indicating that the model has almost no change in the data, and F-statistic is 6.662e-05, indicating that the model has no significant statistical significance. All in all, according to Model 1, there is no significant evidence that users' usage time has changed significantly after switching to the new interface.

#### 4)

1. The coefficient of groupB:user\_levelmedium is -1.2829, which means that under the premise of keeping all other variables constant, the product use time  $y$  of users with medium level in groupB is 1.2829 lower than that of users with the same level in groupA.  $\Pr(>|t|) = 0.07303$  shows that the statistics are interesting.

2. The coefficient of groupB:user\_levelhigh is -3.2593, which means that under the premise of keeping all other variables constant, the product usage time  $y$  of the high-level users in groupB is 3.2593 lower than that of the same-level users in groupA.  $\Pr(>|t|) = 8.41e-06$  shows statistical significance.

Overall, the model is statistically significant. Negative and different coefficients for both interaction terms indicate that the new interface is less effective for users with intermediate or advanced experience, and the statistical significance is different for different levels of users.

#### 5)

Model 1 concludes that there is no significant difference in streaming time between users in Group A and Group B. The conclusion drawn from model 2 is that according to different user levels, after updating to the new interface, the usage time of medium-level users does not change significantly, but for your high-level users, the usage time has a slight negative impact. These two conclusions are not contradictory, because model 1 does not consider user levels, while model 2 considers user levels, so the conclusions drawn are more detailed.

We recommend that the streaming service continue to use the new user interface, and focus on the experience of high-level and mid-level users, and collect feedback from these users to improve the interface.