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Homework 1

9/13/2023

-----1.

- a) Answer for 5: 5
Answer for 10: 55
Answer for 20: 6765
- b) No it does not finish in a reasonable time, it has a $O(2^n)$
- c) The program is written well as it is concise and easy to follow the code. It clearly displays the equation for the fibonacci sequence.
- d) As for negative parts of the code, considering the $O(2^n)$ it is exponential and for large numbers in n it will take a long time to execute the code. Which can also lead to stack overflow when it comes to large n values and the recursive calls

-----2. Yes, the runtime stack might run out of space, due to a exponential growth of the function.

-----3. Slowest --> Fastest Growing

$2/N$, 37, \sqrt{N} , N , $N\log(\log(N))$, $N\log(N)$, $N\log(N^2)$, $N\log^2(N)$, $N^{1.5}$, N^2 , $N^{2\log(N)}$, N^3 , $N/2$, $2N$

--Similar Rates--

$N \log(N^2)$ and $N \log N$

$N^2 \log N$ and N^3

$N \log \log N$ and $N \log_2 N$

-----4.

```
//Cost //Time
(1) sum = 0; //c1 1
for( i = 0; //c2 1
    i < n; //c3 n+1
    ++i ) //c4 n
++sum; //c5 n
```

$T(N) = c1 * 1 + c2 * 1 + c3 * n+1 + c4 * n + c5 * n$

$T(N) = O(n)$

```
//Cost //Time
(2) sum = 0; //c1 1
for( i = 0; //c2 1
    i < n; //c3 n+1
    ++i ) //c4 n
for( j = 0; //c5 n
    j < n; //c6 n^2
    ++j ) //c7 n^2
++sum; //c8 n^2
```

$T(N) = c1 * 1 + c2 * 1 + c3 * n+1 + c4 * n + c5 * n + c6 * (n^2)+1 + c7 * n^2 + c8 * n^2$

$T(N) = O(n^2)$

```
//Cost //Time
(3) sum = 0; //c1 1
for( i = 0; //c2 1
    i < n; //c3 n+1
    ++i ) //c4 n
for( j = 0; //c5 n
    j < n * n; //c6 n(n^2 + 1)
    ++j ) //c7 n^3
++sum; //c8 n^3
```

$T(N) = c1 * 1 + c2 * 1 + c3 * n+1 + c4 * n + c5 * n + c6 * n(n^2 + 1) + c7 * n^3 + c8 * n^3$

$T(N) = O(?)$

```
//Cost //Time
(4) sum = 0; //c1 1
for( i = 0; //c2 1
    i < n; //c3 n+1
    ++i ) //c4 n
for( j = 0; //c5 n
    j < i; //c6 n!
    ++j ) //c7 (n-1)!
++sum; //c8 (n-1)!
```

$T(N) = c1 * 1 + c2 * 1 + c3 * n+1 + c4 * n + c5 * n + c6 * n! + c7 * (n-1)! + c8 * (n-1)!$

$T(N) = O(n!)$