

**Operating Systems**  
**Course Code: 71203002004**  
**Page Replacement Strategies**

*by -*  
*Asst. Prof. Minal Rajwar*



# Page Replacement Algorithms

Page replacement algorithms are techniques used in OS to manage memory efficiently when the physical memory is full.

## **Common Page Replacement Techniques:**

- First In First Out (FIFO)
- Optimal Page Replacement
- Least Recently Used (LRU)
- Most Recently Used (MRU)

# FIFO - First In First Out

- a. The oldest page in memory is replaced when a new page is needed.
- b. Uses a queue structure - new pages are added to the tail, and the page at the head is replaced when needed.
- c. Is simple to implement.
- d. Doesn't consider page usage frequency - might replace frequently used pages.

**Example:** Consider page reference string 1,3,0,3,5,6,3 with 3-page frames. Find the number of page faults using FIFO Page replacement Algorithm,

Page  
reference

1, 3, 0, 3, 5, 6, 3

1	3	0	3	5	6	3
		0	0	0	0	3
	3	3	3	3	6	6
1	1	1	1	5	5	5
Miss	Miss	Miss	Hit	Miss	Miss	Miss

Total Page Fault = 6

# Optimal Page Replacement

- a. Pages are replaced which would not be used for the longest duration of time in the future.
- b. Acts as the theoretical benchmark for other algorithms.
- c. Unrealistic in practice since it requires future knowledge.
- d. How it works:
  - i. When a page fault occurs, check future page references.
  - ii. replace the page that either:
    - 1. will never be used again, OR
    - 2. Has the longest wait until its next use.

**Example:** Consider page reference string 7,0,1,2,0,3,0,4,2,3,0,3,2,3 with 4 -page frames. Find the number of page faults using Optimal Page replacement Algorithm,

Page reference	7,0,1,2,0,3,0,4,2,3,0,3,2,3													No. of Page frame - 4	
7	0	1	2	0	3	0	4	2	3	0	3	2	3		
			2	2	2	2	2	2	2	2	2	2	2		
		1	1	1	1	1	4	4	4	4	4	4	4		
	0	0	0	0	0	0	0	0	0	0	0	0	0		
7	7	7	7	7	3	3	3	3	3	3	3	3	3		
Miss	Miss	Miss	Miss	Hit	Miss	Hit	Miss	Hit	Hit	Hit	Hit	Hit	Hit		

Total Page Fault = 6

# LRU - Least Recently Used

- a. The page that hasn't been used for the longest time is replaced.
- b. Tracks when each page was last accessed and replaces the one with the oldest access time.
- c. Better performance than FIFO as it considers page usage patterns.
- d. More complex implementation as it requires tracking access times.

**Example:** Consider page reference string 7,0,1,2,0,3,0,4,2,3,0,3,2,3 with 4 page frames. Find the number of page faults using LRU Page replacement Algorithm,

Page reference	7,0,1,2,0,3,0,4,2,3,0,3,2,3														No. of Page frame - 4													
	7	0	1	2	0	3	0	4	2	3	0	3	2	3														
				2	2	2	2	2	2	2	2	2	2	2														
			1	1	1	1	1	4	4	4	4	4	4	4														
		0	0	0	0	0	0	0	0	0	0	0	0	0														
	7	7	7	7	7	3	3	3	3	3	3	3	3	3														
	Miss	Miss	Miss	Miss	Hit	Miss	Hit	Miss	Hit	Hit	Hit	Hit	Hit	Hit														

Total Page Fault = 6

Here LRU has same number of page fault as optimal but it may differ according to question.



# MRU - Most Recently Used

- a. Replaces most recently used page when a new page is needed.
- b. Fast for certain access patterns (e.g., when recent pages won't be needed soon).
- c. Can suffer Belady's Anomaly
  - i. Increasing available memory can sometime increase page faults instead of reducing them.

**Example:** Consider page reference string 7,0,1,2,0,3,0,4,2,3,0,3,2,3 with 4 page frames. Find the number of page faults using MRU Page replacement Algorithm,

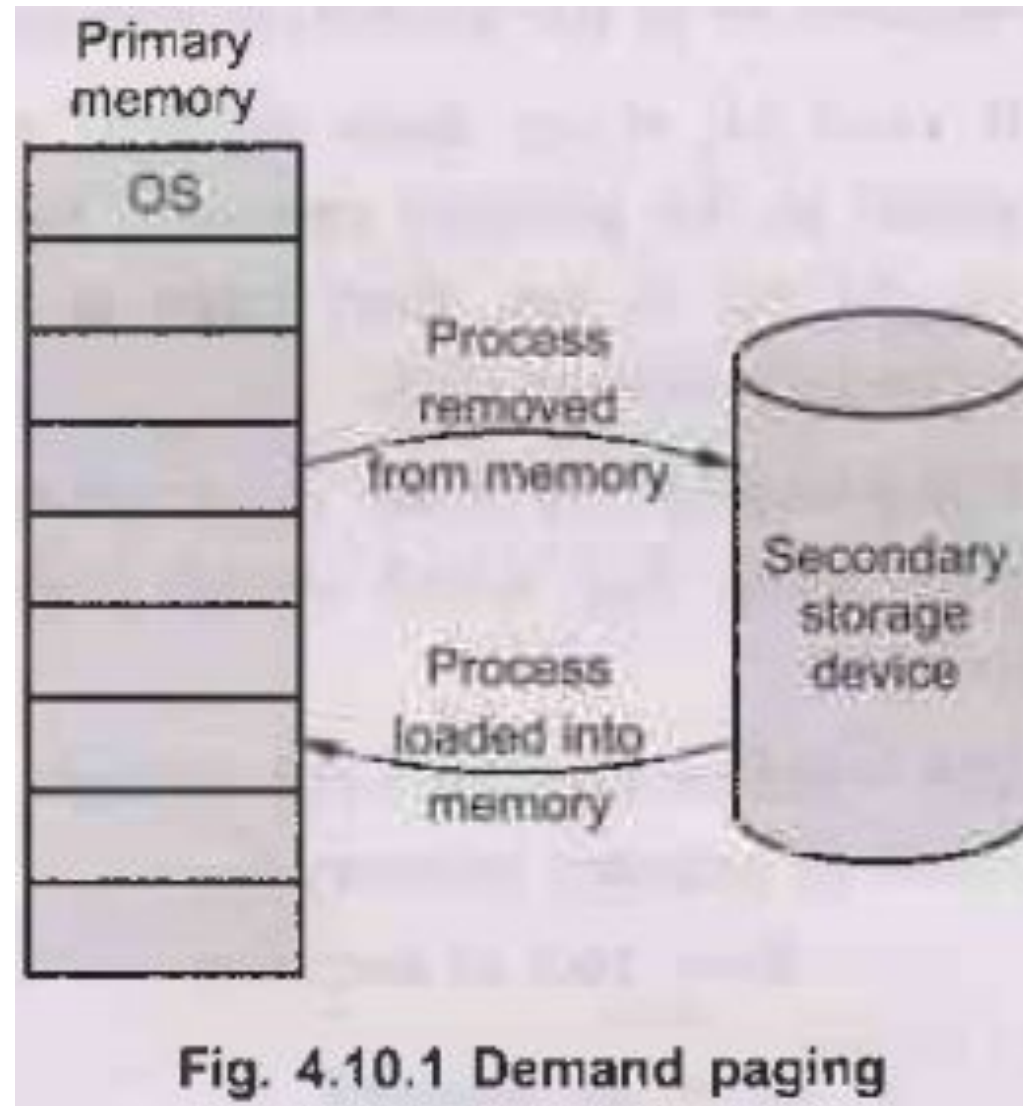
Page reference	7,0,1,2,0,3,0,4,2,3,0,3,2,3							No. of Page frame - 4						
7	0	1	2	0	3	0	4	2	3	0	3	2	3	
			2	2	2	2	2	2	3	0	3	2	3	
		1	1	1	1	1	1	1	1	1	1	1	1	
	0	0	0	0	3	0	4	4	4	4	4	4	4	
7	7	7	7	7	7	7	7	7	7	7	7	7	7	
Miss	Miss	Miss	Miss	Hit	Miss	Miss	Miss	Hit	Miss	Miss	Miss	Miss	Miss	
Total Page Fault = 12														

# Demand Paging

It is a memory management technique where the OS loads only the required parts (pages) of a program into RAM when needed , rather than loading the entire program at startup.

How It Works:

- ★ Program runs > Only essential pages are loaded initially.
- ★ Page Fault > If the CPU requests a page not in RAM, the OS:
  - Pauses the program.
  - Fetches the missing page from disk.
  - Loads it into memory (replacing another page if needed).
  - Resumes execution.



## Pros

- ★ Saves Memory (only active pages are loaded).
- ★ Faster startup (no need to load entire programs).
- ★ Supports large programs (even bigger than RAM).

## Cons

- ★ Page faults slow execution (disk access is slower than RAM).
- ★ Thrashing (if too many page faults occur, system performance drops).

# Performance of Demand Paging

Demand paging improves memory efficiency but has performance trade-offs. Key factors affecting performance:

- **Page Fault Rate (PFR)**
  - frequency at which a requested page is not in RAM (triggering a disk fetch).
  - LOW PFR > Smooth performance.
  - High PFR > Thrashing (system wastes time swapping pages).

- **Effective Access Time (EAT)**

- $EAT = (1 - p) \times \text{Memory Access Time} + p \times \text{Page Fault Time}$

- $p$  = Page fault probability
    - Memory Access Time = time to access RAM (in nanoseconds).
    - Page Fault time = Time to handle page faults (including disk I/O, swapping, etc.)

- Example
  - If  $p = 10\%$ , RAM access = 100ns , Disk access = 10ms:  
10,000,000 ns

Apply the Formula:

$$EAT = (1-0.1) \times 100 + 0.1 \times 10,000,000$$

$$EAT = 0.9 \times 100 + 0.1 \times 10,000,000$$

$$EAT = 90 + 1,000,000 = 1,000,090 \text{ ns}$$



- **Optimizations to Improve Performance**
  - Working Set Model : Keep actively used pages in RAM.
  - Prepaging ; Load anticipated pages in advance.
  - Good Page Replacement Algorithm (e.g., LRU over FIFO).
  - Fast Storage : SSDs reduce page fault penalty vs. HDDs.
  
- **Thrashing**
  - Too many processes > high page faults > system spends more time swapping then executing.
  - Solution:
    - Limit multiprogramming (fewer concurrent processes).
    - Increase RAM or optimize memory usage.

## Discussion & Revision

- What does demand paging load into memory only when needed?
- Which algorithm replaces the page not used recently?
- What occurs when a needed page is not in RAM?
- What is the slowdown caused by excessive page faults called?
- Which storage device reduces page fault delays compared to HDDs?