

# <sup>1</sup> Interfere: Studying Intervention Response Prediction in Complex Dynamic Models

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## Software

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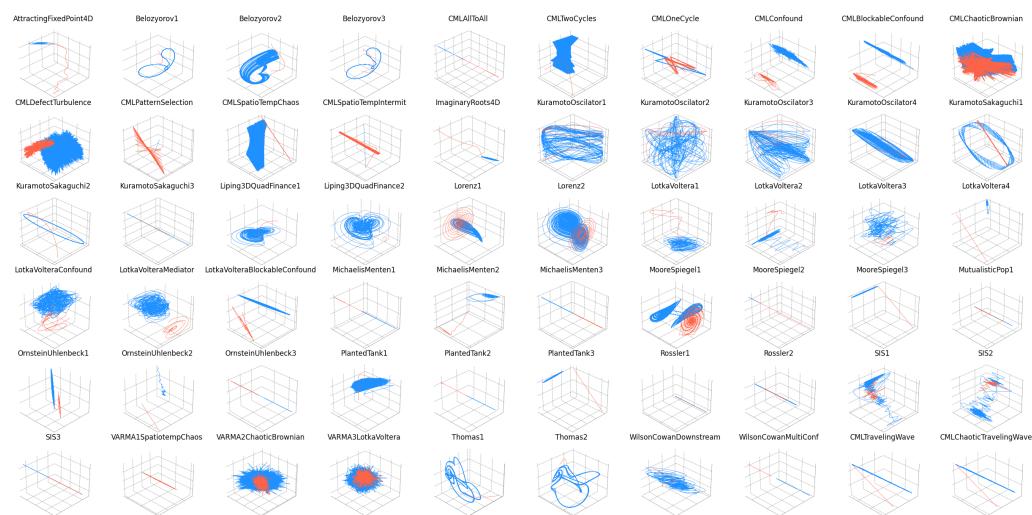
## <sup>11</sup> Summary

<sup>8</sup> The *Interfere* package focuses on *intervention response prediction*—forecasting how complex, <sup>9</sup> dynamic systems respond to novel interventions. When developing predictive methods capable of <sup>10</sup> solving this problem, ideal benchmarking data comes from controlled, longitudinal experiments. <sup>11</sup> Such experiments are often infeasible due to confounding, cost, and ethical constraints.

<sup>12</sup> Synthetic benchmarks, which are often used in response to this problem [cite], typically rely on <sup>13</sup> models with static linear relationships and/or overly independent noise profiles that lack the <sup>14</sup> complex interdependent feedback we find in the real world.

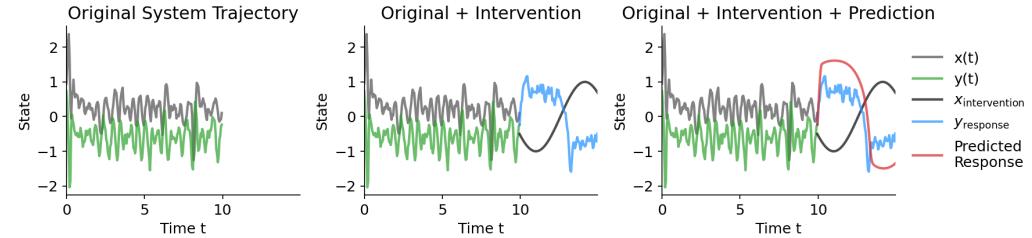
<sup>15</sup> As a solution, we propose a middle ground: Scientists in many disciplines, such as economics, <sup>16</sup> ecology, systems biology and others, employ mechanistic dynamic models as a part of their <sup>17</sup> research and application toolkit (Baker et al., 2018; Banks et al., 2017; Brayton et al., 2014; <sup>18</sup> Izhikevich & Edelman, 2008). Many of these models are accompanied by a body of evidence <sup>19</sup> demonstrating that they do indeed capture important characteristics of the real world problems <sup>20</sup> they emulate. We propose using datasets generated by such models of complex systems to <sup>21</sup> benchmark methods that predict intervention response. If a scientific model captures important <sup>22</sup> characteristics of the world and a method can accurately predict intervention response *for that* <sup>23</sup> *model* then the method might also predict intervention response for similar real-world systems.

<sup>24</sup> *Interfere* offers the first steps towards this vision by combining (1) a general interface for <sup>25</sup> simulating the effect of interventions on dynamic models, (2) a suite of predictive methods <sup>26</sup> and cross validated hyper parameter optimization tools, and (3) the first known [extensible](#) <sup>27</sup> [benchmark data set](#) of dynamic intervention response scenarios see Figure 1.



**Figure 1:** Three-dimensional trajectories of sixty scenarios simulated with the `Interfere` package. Simulated models are either differential equations or discrete time difference equations. Trajectories in blue represent the natural behavior of the system, while red depicts response to a specified intervention. For models with more than three dimensions, only the three dimensions with highest variance are shown. These sixty scenarios, make up the downloadable [Interfere Benchmark 1.1.1](#).

## 28 Statement of Need



**Figure 2: Original System Trajectory (Left):** The natural, uninterrupted evolution of the quadratic Belozyorov system ([Belozyorov, 2015](#)) simulated using the `Interfere` package with a small amount of stochastic noise. **System Trajectory After Intervention (Center):** The effect that taking exogenous control of  $x(t)$  by via  $\text{do}(x(t) = \sin(t))$  beginning at time  $t = 10$  has on  $y$ . The intervention (black) and response (blue), depict a clear departure from the natural behavior of the system (green and gray). **Intervention Response Prediction (Right):** Example of forecasting the response of the Belozyorov system to the sinusoidal intervention. The ground truth response,  $y(t)$  for  $t > 10$  is plotted in blue. Here, an equation discovery algorithm, SINDy, ([Brunton et al., 2016](#)) is fit to the data that occurs prior to the intervention and makes an attempt to predict the intervention response (red curve).

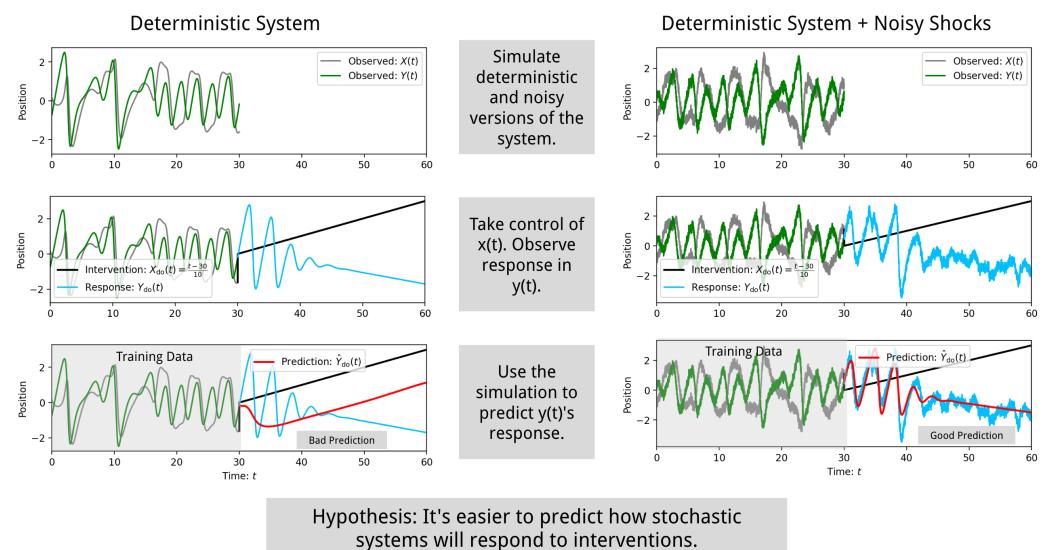
29 Over the past twenty years, multiple frameworks have emerged for identifying causal relationships  
30 in observational data ([Imbens & Rubin, 2015](#); [Pearl, 2009](#); [Wieczorek & Roth, 2019](#)). The most  
31 influential frameworks are probabilistic and, while it is not a necessary condition for identifying  
32 causality, a static, linear relationship has often been assumed. However, when attempting to  
33 anticipate the response of complex dynamic systems in the medium and long term, a linear  
34 approximation of the dynamics can be insufficient. Therefore, non-linear, dynamic techniques  
35 have been employed for causal discovery and forecasting (e.g. [Runge, 2022](#)). Nevertheless,  
36 there are relatively few intervention oriented techniques that are able to fit dynamic nonlinear  
37 models to data.

38 `Interfere`'s use of scientific models for systematic method evaluation bridges the gap between

39 idealized synthetic data and real-world problems. This benchmarking approach is enabled  
 40 by Interfere's a unified toolkit for intervention response simulation, standardized method  
 41 evaluation, and systematic cross-validation across diverse dynamic systems. By lowering  
 42 barriers to rigorous method evaluation, Interfere facilitates the development of prediction  
 43 methods that translate from theory to real-world application in complex systems science.

## 44 Primary Contributions

45 Interfere provides three primary contributions: (1) dynamically diverse counterfactuals, (2)  
 46 cross-disciplinary forecast methods, and (3) comprehensive and extensible benchmarking.



**Figure 3:** Example experimental setup possible with Interfere: Can stochasticity help reveal associations between variables? Interfere can be used to compare intervention response prediction for deterministic and stochastic versions of the same system.

## 47 1. Dynamically Diverse Counterfactuals at Scale

48 Whereas most predictive methods for complex dynamics are typically benchmarked on fewer  
 49 than ten systems (Brunton et al., 2016; Challu et al., 2023; Pathak et al., 2018; Prasse &  
 50 Van Mieghem, 2022; Vlachas et al., 2020), Interfere's "dynamics" submodule contains over  
 51 fifty dynamic models, with a mix of linear, nonlinear, chaotic, continuous-time, discrete-time,  
 52 stochastic, and deterministic models, from a variety of disciplines including finance, ecology,  
 53 biology, neuroscience and public health. Most importantly, Interfere is built for studying  
 54 interventions: each model inherits the Interfere BaseDynamics type, with possible exogenous  
 55 control of any observed state, added measurement noise, and, for most models, stochasticity  
 56 controlled by a scalar parameter or fine tuned with a covariance matrix. Interfere thus offers  
 57 a user-friendly framework to produce complex dynamic intervention response and standard  
 58 forecasting scenarios at scale.

## 59 2. Cross Disciplinary Forecast Methods

60 Interfere integrates dynamic *forecasting* methodologies from deep learning (LSTM, NHITS),  
 61 applied mathematics (SINDy, Reservoir Computers) and social science (VAR). The Interfere  
 62 "ForecastingMethod" class is expressive enough to describe, fit and predict with multivariate  
 63 dynamic models and apply interventions to the states of the models during prediction.

### 64     3. Comprehensive and Extensible Benchmarking

65     Interfere organizes a variety of dynamic scenarios into the [Interfere Benchmark](#), a comprehensive  
66     and extensible set containing 60 intervention response scenarios for testing, each simulated  
67     with different levels of stochastic noise. Each scenario is housed in a JSON file, with metadata  
68     annotation, documentation, versioning and commit hashes marking the commit of Interfere  
69     that was used to generate the data. The scenarios were reviewed by hand with some systems  
70     exposed to exogenous input to ensure that none of the key variables settle into a steady state.  
71     Additionally, all interventions were chosen so that the target variable response significantly  
72     departs from its prior behavior. We aim for this benchmark to facilitate future progress towards  
73     correctly anticipating how complex systems will respond to never before seen scenarios.

## 74     Related Software and Mathematical Foundations

### 75     Predictive Methods

76     Interfere draws from the Nixtla open source ecosystem for time series forecasting. We  
77     implemented intervention support for LSTM and NHITS from the NeuralForecast package,  
78     and for ARIMA from the StatsForecast package ([Azul Garza, 2022](#); [Olivares et al., 2022](#)). We  
79     followed Nixtla's example for cross validation and hyperparameter optimization approaches. We  
80     integrated predictive methods from the PySINDy ([Kaptanoglu et al., 2022](#)) and StatsModels  
81     ([Seabold & Perktold, 2010](#)) packages. We also include ResComp, a reservoir computing  
82     method for global forecasts from ([Harding et al., 2024](#)). Hyperparameter optimization is  
83     designed around the Optuna framework ([Akiba et al., 2019](#)).

84     While other forecasting methods exist, integrating a method with Interfere requires that  
85     the method is capable of (1) multivariate endogenous dynamic forecasting, (2) support for  
86     exogenous variables, and (3) support for flexible length forecast windows or recursive predictions.  
87     Few forecasting methods meet these criteria, and it is our hope that this package will encourage  
88     development of additional methods.

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