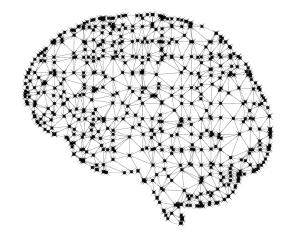
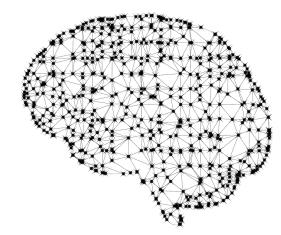
Reinforcement Learning with Pytorch









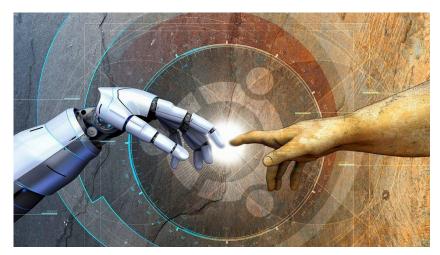
Before we start

What is this course about?

Is this course for me?

What are requirements?

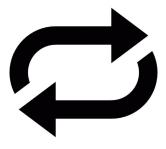
Contact: marcin@atamai.biz



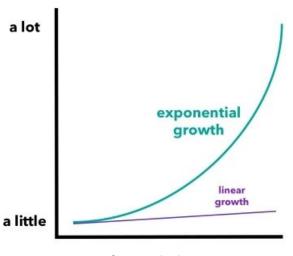
Source: freedomandsafety.com

Artificial Intelligence. Why getting so popular?

- Moore law
- Reinforcement learning + Deep Learning
- Brain power
- More learning resources
- More people involved
- More projects
- Better results



Source: freepik.com



Source: charlesngo.com

Example of Deepmind

2013 paper

https://arxiv.org/pdf/1312.5602.pdf

Google + Deepmind

https://techcrunch.com/2014/01/26/google-deepmind/

2015 paper

https://storage.googleapis.com/deepmind-media/dqn/DQNNaturePaper.pdf

AlphaGo, AlphaGo Zero













https://deepmind.com/blog/alphago-zero-learning-scratch/

What will we do ...



Source: python.org



Source: pytorch.org



Source: openai.com

Recommended resources:

http://www0.cs.ucl ac.uk/staff/d.silver/web/Teaching.html

http://incompleteideas.net/book/the-book-2nd.html

What is Reinforcement learning?

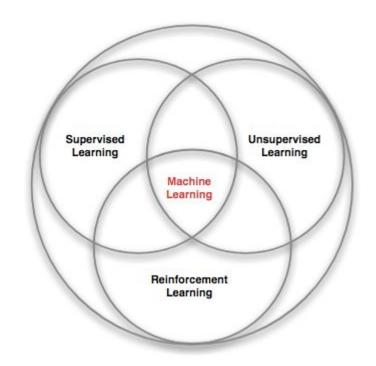
Supervised vs unsupervised learning

No supervisor

Rewards

Feedback

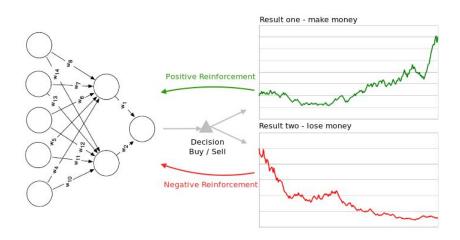
Time



Source: David Silver

What is Reinforcement learning?

Examples





Source: stanford.edu

Source: turingfinance.com

What is Reinforcement learning?



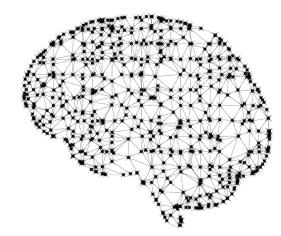


Deepmind Atari

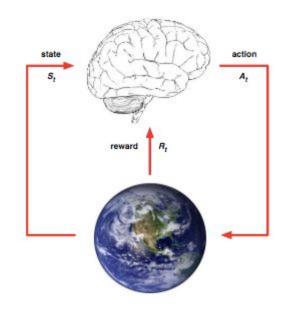
Source: google

Tabular methods





Some theory



Source: David Silver

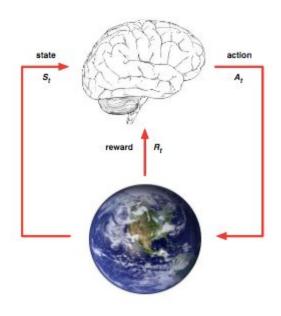
History:

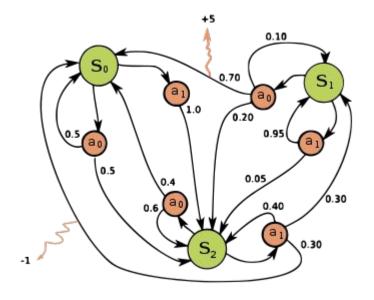
$$H = O1, A1, R1, O2, A2, R2, ..., On, An, Rn$$

State:

$$state = f(H)$$

Markov Decision Process





Source: David Silver Source: wikipedia

Openai gym

https://gym.openai.com/docs/

https://gym.openai.com/envs/

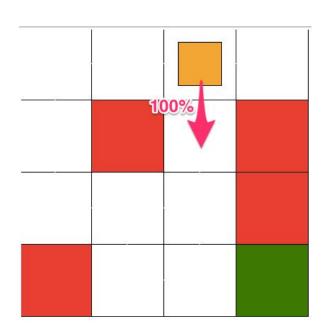
https://github.com/openai/gym

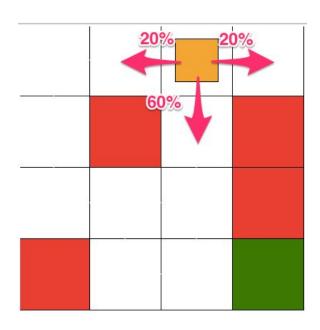
https://github.com/openai/gym/wiki



Source: openai.com

Deterministic vs Stochastic





Rewards

Rewards

$$R_t = r_t + r_{t+1} + r_{t+2} + \dots + r_n$$



Discount:

$$\gamma \in \{0..1\}$$

Source: pixabay.com

$$R_t = r_t + \gamma * r_{t+1} + \gamma^2 * r_{t+2} + \dots + \gamma^{n-t} * r_n$$

Solution

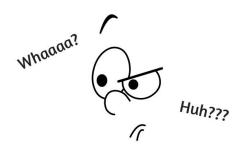
https://en.wikipedia.org/wiki/Markov decision process

$$V(s) := \sum_{s'} P_{\pi(s)}(s,s') \left(R_{\pi(s)}(s,s') + \gamma V(s')
ight)$$

$$\pi(s) := rg \max_a \left\{ \sum_{s'} P_a(s,s') \left(R_a(s,s') + \gamma V(s')
ight)
ight\}$$

$$V_{i+1}(s) := \max_a \left\{ \sum_{s'} P_a(s,s') \left(R_a(s,s') + \gamma V_i(s')
ight)
ight\},$$

$$Q(s,a) = \sum_{s'} P_a(s,s') (R_a(s,s') + \gamma V(s')).$$



Source: kmazing.net

Solution

Source for equations: http://cs231n.stanford.edu

$$Q^\pi(s,a) = \mathbb{E}\left[\sum_{t\geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$

Q-value function at state s - taking action a How good is a state-action pair

$$Q^*(s,a) = \max_{\pi} \mathbb{E}\left[\sum_{t \geq 0} \gamma^t r_t | s_0 = s, a_0 = a, \pi
ight]$$
 Optimal Q value

$$Q^*(s, a) = \mathbb{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q^*(s', a') | s, a \right]$$

Solution for deterministic environment

Bellman equation:

$$Q(s, a) = r + \gamma * max_{a'}Q(s', a')$$



Source: wikipedia

Algorithm for deterministic environment

initialize Q[num_states, num_actions]

observe initial state s

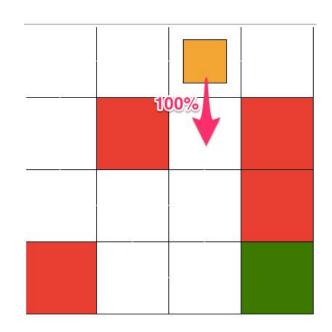
repeat until terminated:

select and perform action a

observe reward r and new state s'

$$Q(s,a) = r + \gamma * max Q(s',a')$$

$$s = s'$$



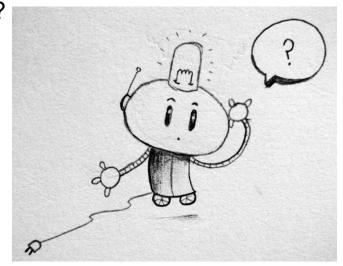
Stochastic environment

What if we don't know everything about environment?

What if we only know set of states and actions?

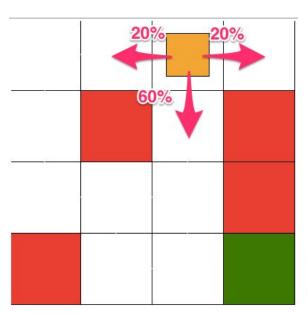
It's about learning!

Q learning as an answer



Source: flickr.com

Temporal difference



observations before

VS

observation now

$$[r + \gamma * max_{a'}Q(s', a')] - [Q(s, a)]$$

Q learning

$$Q_t(s, a) = Q_{t-1}(s, a) + \alpha * TD$$



Source: Max Pixel

$$Q(s,a) = Q(s,a) + \alpha[r + \gamma * max_{a'}Q(s',a') - Q(s,a)]$$

$$Q(s,a) = (1-\alpha)Q(s,a) + \alpha[r + \gamma * max_{a'}Q(s',a')]$$

Algorithm for stochastic environment

initialize Q[num_states, num_actions]

observe initial state s

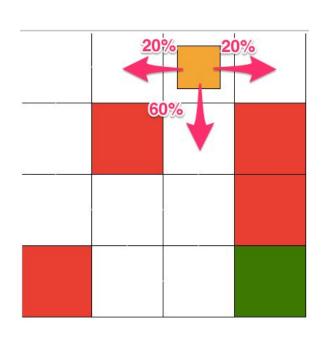
Repeat until terminated:

select and perform action a

observe reward r and new state s'

$$Q(s,a) = (1-\alpha) Q(s,a) + \alpha [r + \gamma * max Q(s',a')]$$

$$S = S'$$

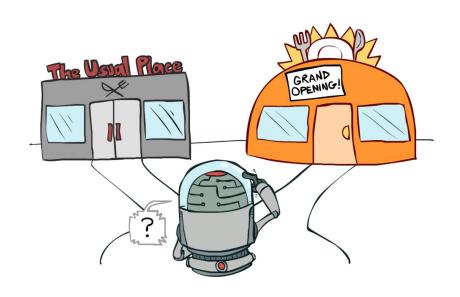


Exploitation vs Exploration

best decision vs more information

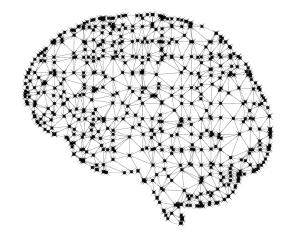
e - greedy:

$$a = \begin{cases} optimal \ a^* & 1 - \varepsilon \\ random & \varepsilon \end{cases}$$



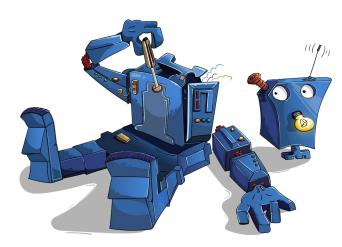
Source: berkeley.edu





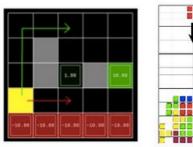
Problems with current approach?

- → Set of states
- → Resources needs
- → Performance

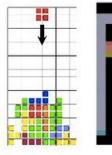


Source: pixabay

Discrete environments



Gridworld 10^1

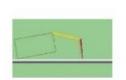


Tetris 10^60



Atari 10^308 (ram) 10^16992 (pixels)

Continuous environments (by crude discretization)



Crawler 10^2



Hopper 10^10



Humanoid 10^100

Source: Berkeley Al Research Lab

Solution:

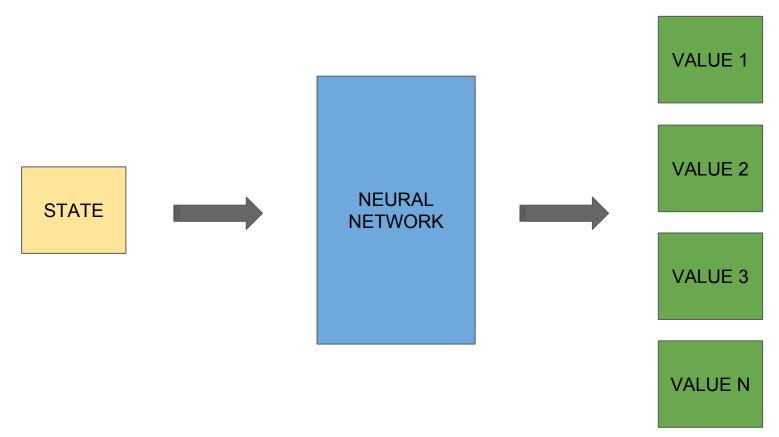
Generalize

Function approximation

Understand the rules and apply it to future, similar situations

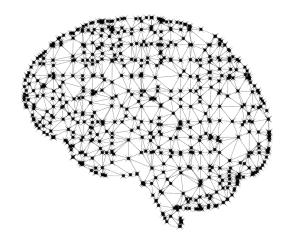


Source: pixabay

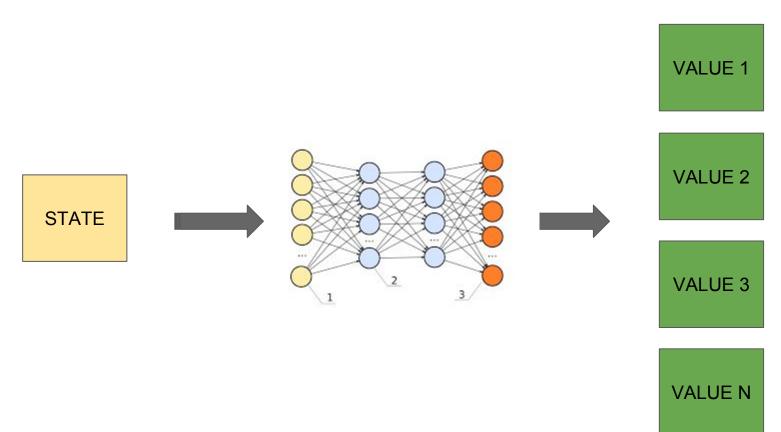


Neural Networks revisited



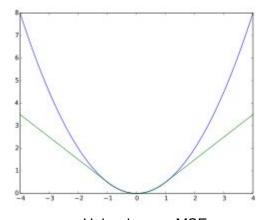


Neural Networks



Neural Networks

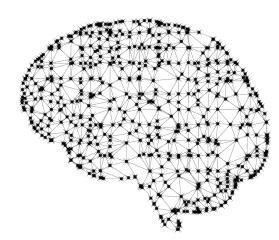
- Activation functions
 - o ReLU
 - Tanh
- Loss functions
 - MSE
 - Huber loss
- Optimizers
 - Adam
 - RMSProp



Huber loss vs MSE Source: wikipedia

DQN





Deep Q learning

Paper "Playing Atari with Deep Reinforcement Learning"

https://arxiv.org/pdf/1312.5602v1.pdf



Source: Deepmind

Deep Q learning

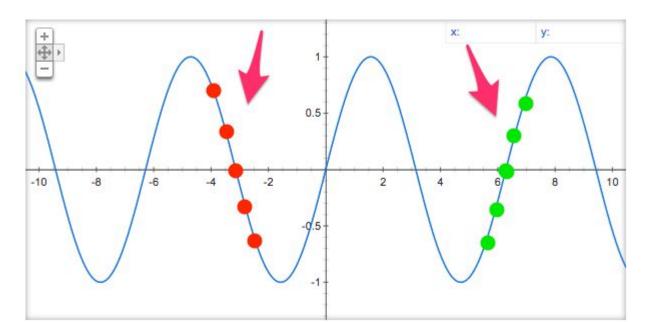
Problems listed in Deepmind's paper:

→ highly correlated data

→ non-stationary distributions

Problems listed in Deepmind's paper:

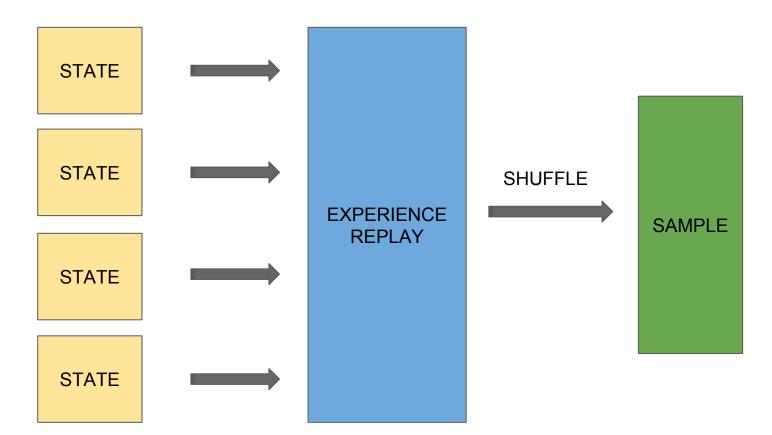
→ Highly correlated data

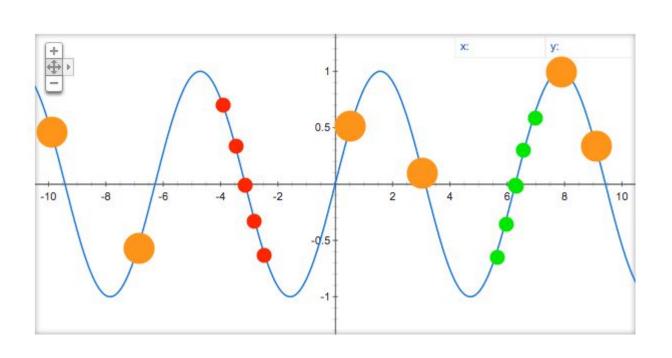


Problems listed in Deepmind's paper:

→ Non stationary distributions

$$Q(s, a) = r + \gamma * max_{a'}Q(s', a')$$





```
Algorithm 1 Deep Q-learning with Experience Replay
   Initialize replay memory \mathcal{D} to capacity N
   Initialize action-value function Q with random weights
  for episode = 1, M do
       Initialise sequence s_1 = \{x_1\} and preprocessed sequenced \phi_1 = \phi(s_1)
       for t = 1. T do
            With probability \epsilon select a random action a_t
            otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
            Execute action a_t in emulator and observe reward r_t and image x_{t+1}
            Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
            Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
            Sample random minibatch of transitions (\phi_j, a_j, r_j, \phi_{j+1}) from \mathcal{D}
           Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
            Perform a gradient descent step on (y_j - Q(\phi_j, a_j; \theta))^2 according to equation 3
       end for
  end for
```

Source: DeepMind's "Playing Atari with Deep Reinforcement Learning"

Paper "Human-level control through deep reinforcement learning"

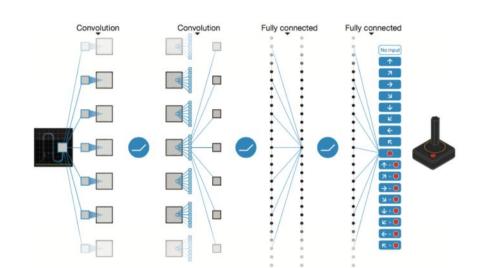
https://storage.googleapis.com/deepmind-media/dgn/DQNNaturePaper.pdf

Code:

https://github.com/deepmind/dqn

Patent:

https://patents.google.com/patent/US20150100530A1/en

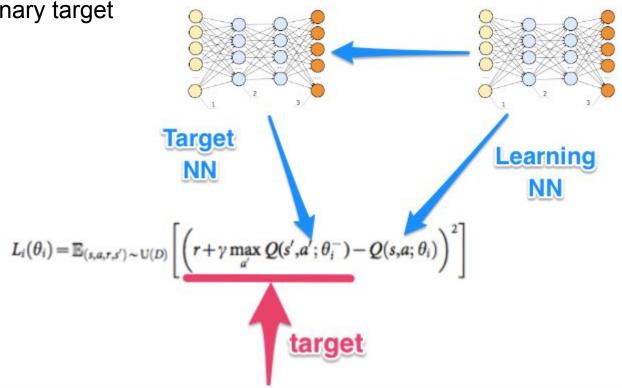


Problems listed in Deepmind's paper:

→ Non stationary target

$$L_i(\theta_i) = \mathbb{E}_{(s,a,r,s') \sim U(D)} \left[\underbrace{\left(r + \gamma \max_{a'} Q(s',a';\theta_i^-) - Q(s,a;\theta_i)\right)^2}_{\text{target}} \right]$$

→ Non stationary target



Additional "trick":

→ Error clipping

Pytorch implementation:

```
loss.backward()

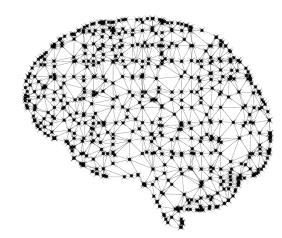
for param in self.agent.parameters():
    param.grad.data.clamp_(-1, 1)

self.optimizer.step()
```

```
Initialize replay memory D to capacity N
Initialize action-value function Q with random weights \theta
Initialize target action-value function Q with weights \theta^- = \theta
For episode = 1, M do
   Initialize sequence s_1 = \{x_1\} and preprocessed sequence \phi_1 = \phi(s_1)
   For t = 1, T do
        With probability \varepsilon select a random action a_t
        otherwise select a_t = \operatorname{argmax}_{a} Q(\phi(s_t), a; \theta)
        Execute action a_t in emulator and observe reward r_t and image x_{t+1}
        Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
        Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in D
        Sample random minibatch of transitions (\phi_j, a_j, r_j, \phi_{j+1}) from D
       Set y_j = \begin{cases} r_j & \text{if episode terminates at step } j+1 \\ r_j + \gamma \max_{a'} \hat{Q}(\phi_{j+1}, a'; \theta^-) & \text{otherwise} \end{cases}
        Perform a gradient descent step on (y_j - Q(\phi_j, a_j; \theta))^2 with respect to the
        network parameters \theta
        Every C steps reset \hat{Q} = Q
   End For
End For
```

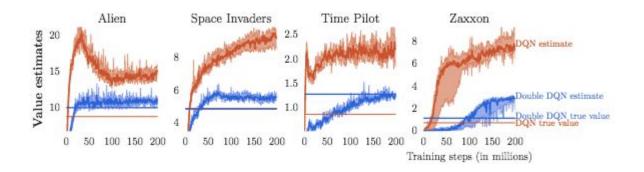
Source: DeepMind's "Human-level control through deep reinforcement learning"



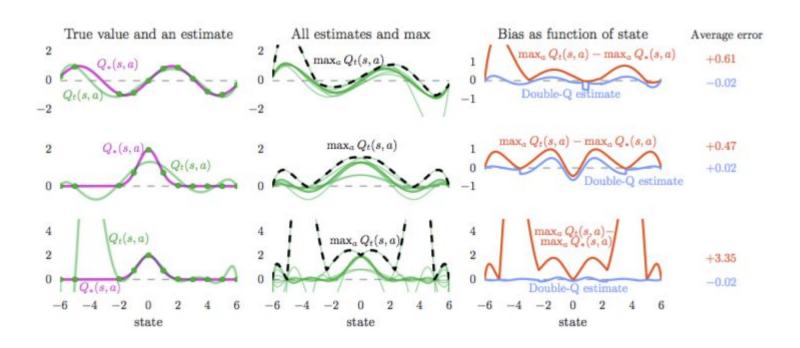


Paper "Deep Reinforcement Learning with Double Q-learning"

https://arxiv.org/pdf/1509.06461.pdf



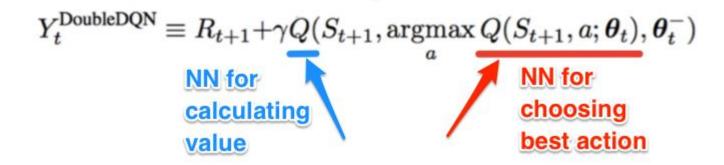
Double Q Learning



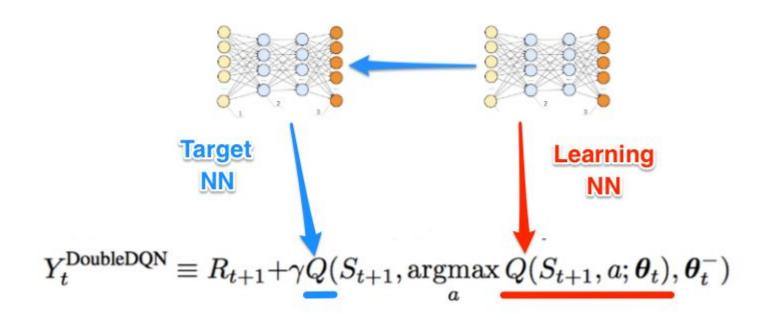
Double Q Learning

$$Y_t^{\text{DoubleDQN}} \equiv R_{t+1} + \gamma Q(S_{t+1}, \underset{a}{\operatorname{argmax}} Q(S_{t+1}, a; \boldsymbol{\theta}_t), \boldsymbol{\theta}_t^-)$$

Explanation:

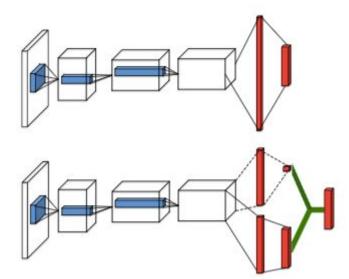


Double Q Learning



Paper "Dueling Network Architectures for Deep Reinforcement Learning"

https://arxiv.org/pdf/1511.06581.pdf



Dueling DQN

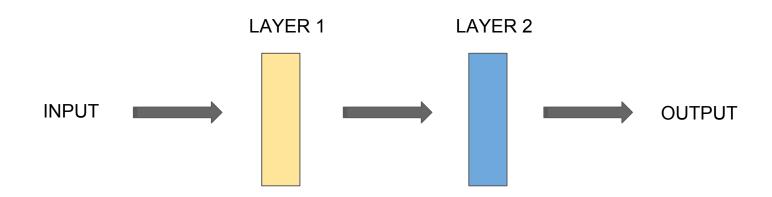
Advantage function:

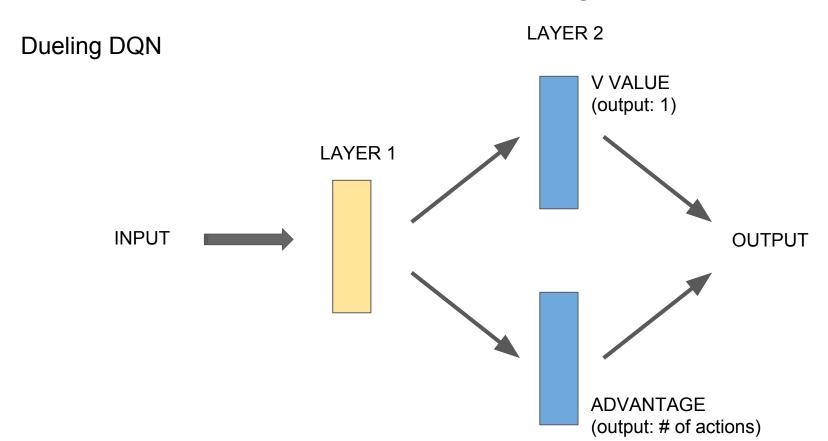
$$A^\pi(s,a) = Q^\pi(s,a) - V^\pi(s)$$

Q function:

$$Q(s, a; \theta, \alpha, \beta) = V(s; \theta, \beta) + \left(A(s, a; \theta, \alpha) - \frac{1}{|\mathcal{A}|} \sum_{a'} A(s, a'; \theta, \alpha)\right)$$

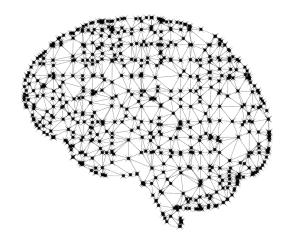
Dueling DQN





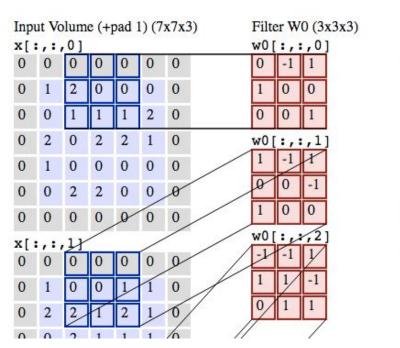
DQN + CNN

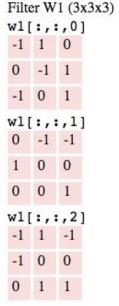


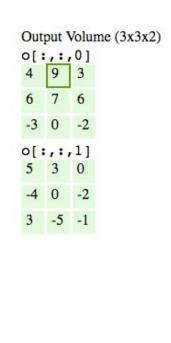


Deep Reinforcement learning

CNN







Source: cs231n.github.io

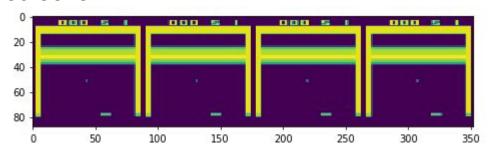
Deep Reinforcement learning

Deepmind's CNN

		Filter				
Layer	Input	size	Stride	# of filters	Activation	Output
conv1	84x84x4	8	4	32	ReLU	20x20x32
conv2	20x20x32	4	2	64	ReLU	9x9x64
conv3	9x9x64	3	1	64	ReLU	7x7x64
fc1	7x7x64			512	ReLU	512
fc2	512				Linear	# of actions

DQN potential improvements

→ Stack 4 screens



- → Play around with number of layers / settings of Neural Networks
- → Play around with number of neurons in hidden layer(s)
- → Play around with hyperparameters, optimizer and loss function
- → Get more / different kind of experience (egreedy)
- → More DQN improvements (for example PER, Rainbow)
- Different methods

Example - Pong

learning_rate = 0.0001

replay_mem_size = 100000

update_target_frequency = 5000

qamma = 0.99

batch size = 32

egreedy = 0.9

double_dqn = True

Possible results

(GeForce GTX 1080)
considering solved as of average > 18 points over last 100 episodes

```
egreedy_final = 0.01
                                                                                              egreedy_decay = 10000
*** Episode 290 ***
                                                                                               clip error = True
Av.reward: [last 10]: 19.50, [last 100]: 17.67, [all]: -0.09
                                                                                              normalize image = True
epsilon: 0.01, frames_total: 633567
                                                                                  Rewards
Elapsed time: 01:14:30
SOLVED! After 300 episodes
*** Episode 300 ***
Av.reward: [last 10]: 19.20, [last 100]: 18.03, [all]: 0.55
epsilon: 0.01, frames_total: 652434
Elapsed time: 01:16:44
                                        -10 -
                                        -20 -
                                                              100
                                                                              200
                                                                                             300
                                                                                                             400
                                                                                                                             500
```

What's next?



