Warning: The hard deadline has passed. You can attempt it, but you will not get credit for it. You are welcome to try it as a learning exercise.

These interview questions are for your own enrichment and are not assessed. If you click the *Submit Answers* button, you will get a hint.

☐ In accordance with the Coursera Honor Code, I (David Resnick) certify that the answers here are my own work.

## **Question 1**

**Dynamic median.** Design a data type that supports insert in logarithmic time, find-the-median in constant time, and remove-the-median in logarithmic time.

## **Question 2**

Randomized priority queue. Describe how to add the methods sample() and delRandom() to our binary heap implementation. The two methods return a key that is chosen uniformly at random among the remaining keys, with the latter method also removing that key. The sample() method should take constant time; the delRandom() method should take logarithmic time. Do not worry about resizing the underlying array.

## **Question 3**

**Taxicab numbers.** A *taxicab* number is an integer that can be expressed as the sum of two cubes of integers in two different ways:  $a^3 + b^3 = c^3 + d^3$ . For example,  $1729 = 9^3 + 10^3 = 1^3 + 12^3$ . Design an algorithm to find all taxicab numbers with a, b, c, and d less than N.

- *Version 1:* Use time proportional to  $N^2 \log N$  and space proportional to  $N^2$ .
- *Version 2:* Use time proportional to  $N^2 \log N$  and space proportional to N.
- ☐ In accordance with the Coursera Honor Code, I (David Resnick) certify that the answers here are my own work.

Submit Answers

Save Answers

You cannot submit your work until you agree to the Honor Code. Thanks!