Arrays Problem Statement 1: Linear Search Given an array, and an element num the task is to find if num is present in the given array or not. If present print the index of the element or print -1. Example 1: Input: arr[] = 1 2 3 4 5, num = 3Output: 2 Explanation: 3 is present in the 2nd index Example 2: Input: arr[] = 5 4 3 2 1, num = 5Output: 0 Explanation: 5 is present in the 0th index In [1]: """ Time Complexity : O(n) Space Complexity : 0(1) def linear_search(arr, num): n = len(arr)for i in range(0, n): if arr[i] == num: return i return -1 test cases = [{'arr': [1,2,3,4,5], 'num': 3}, {'arr': [5,4,3,2,1], 'num': 5}, {'arr': [5,4,3,2,1], 'num': 7}] for tc in test cases: arr = tc['arr'] num = tc['num'] print('arr:', arr, 'num:', num, 'Index:', linear search(arr, num)) arr: [1, 2, 3, 4, 5] num: 3 Index: 2 arr: [5, 4, 3, 2, 1] num: 5 Index: 0 arr: [5, 4, 3, 2, 1] num: 7 Index: -1 Problem Statement 2: Check if an Array is Sorted Given an array of size n, write a program to check if the given array is sorted in (ascending / Increasing / Non-decreasing) order or not. If the array is sorted then return True, Else return False. **Note:** Two consecutive equal values are considered to be sorted. Example 1: Input: N = 5, array[] = $\{1,2,3,4,5\}$ Output: True. Explanation: The given array is sorted. Example 2: Input: N = 5, array[] = $\{5,4,6,7,8\}$ Output: False. Explanation: The given array is not sorted. Element 5 is not smaller than or equal to its next elements. In [3]: """ Time Complexity : O(n) Space Complexity : 0(1) def is_sorted(arr): n = len(arr)for i in range(1, n): if arr[i-1] > arr[i]: return False return True In [4]: test cases = $[{'arr': [1,2,3,4,5]},$ {'arr': [4,6,5,7,8]}] for tc in test cases: arr = tc['arr'] print('arr:', arr, 'is sorted:', is sorted(arr)) arr: [1, 2, 3, 4, 5] is sorted: True arr: [4, 6, 5, 7, 8] is sorted: False Problem Statement 3: Find the largest & smallest elements in an array Given an array, find the largest and the smallest elements in the array. Example 1: Input: $arr[] = \{2,5,1,3,0\};$ Output: (0, 5) Example2: Input: $arr[] = \{8,10,5,7,9\};$ Output: (5, 10) In [5]: """ Time Complexity : O(n) Space Complexity : O(1) def find_min_max(arr): mini = maxi = arr[0]n = len(arr)for i in range(1, n): mini = min(arr[i], mini) maxi = max(arr[i], maxi) return mini, maxi In [6]: test cases = $[{'arr': [2,5,1,3,0]},$ {'arr': [8,10,5,7,9]}] for tc in test cases: arr = tc['arr'] print('arr:', arr, '(min, max):', find min max(arr)) arr: [2, 5, 1, 3, 0] (min, max): (0, 5)arr: [8, 10, 5, 7, 9] (min, max): (5, 10) Problem Statement 4: Find the second largest & smallest elements in an array Given an array, find the second smallest and second largest element in the array. Print '-1' in the event that either of them doesn't exist. Example 1: Input: [1,2,4,7,7,5] Output: (2, 5) Example 2: Input: [1] Output: (-1, -1)In [7]: """ Brute force solution Time Complexity : O(n log n) [For sorting the array] Space Complexity : 0(1) def find 2nd mini maxi BFS(arr): arr.sort() #If it is guaranteed that the array has no duplicates #return arr[1], arr[-2] mini = float('inf') maxi = float('-inf') n = len(arr)for i in range(0, n): if arr[i] != arr[0]: mini = min(arr[i], mini) **if** arr[i] != arr[-1]: maxi = max(arr[i], maxi)mini = -1 if mini == float('inf') else mini maxi = -1 if maxi == float('-inf') else maxi return mini, maxi In [8]: test_cases = [{'arr': [1]}, {'arr': [1,1,1,1,1,1]}, {'arr': [1,1,3]}, {'arr': [1,2,4,7,7,5]}, {'arr': [8,10,5,7,9]}] print('arr:', test_cases[0]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BFS(arr = test_cases[0]['arr'])) print('arr:', test_cases[1]['arr'], '\t(min, max):', find_2nd_mini_maxi_BFS(arr = test_cases[1]['arr'])) print('arr:', test_cases[2]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BFS(arr = test_cases[2]['arr'])) print('arr:', test_cases[3]['arr'], '\t(min, max):', find_2nd_mini_maxi_BFS(arr = test_cases[3]['arr']))
print('arr:', test_cases[4]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BFS(arr = test_cases[4]['arr'])) $(\min, \max): (-1, -1)$ arr: [1] arr: [1, 1, 1, 1, 1, 1] $(\min, \max): (-1, -1)$ arr: [1, 1, 3] $(\min, \max): (3, 1)$ arr: [1, 2, 4, 5, 7, 7] $(\min, \max): (2, 5)$ arr: [5, 7, 8, 9, 10] $(\min, \max): (7, 9)$ In [9]: """ Better solution Time Complexity : O(2n) Space Complexity : 0(1) def find 2nd mini maxi BS(arr): n = len(arr)mini = maxi = arr[0] for i in range(1, n): mini = min(arr[i], mini) maxi = max(arr[i], maxi)second_mini = float('inf') second maxi = float('-inf') for i in range(0, n): if arr[i] != mini: second mini = min(arr[i], second mini) if arr[i] != maxi: second maxi = max(arr[i], second maxi) second mini = -1 if second mini == float('inf') else second mini second_maxi = -1 if second_maxi == float('-inf') else second_maxi return second_mini, second_maxi In [10]: test cases = [{'arr': [1]}, {'arr': [1,1,1,1,1,1]}, {'arr': [1,1,3]}, {'arr': [1,2,4,7,7,5]}, {'arr': [8,10,5,7,9]}] print('arr:', test_cases[0]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BS(arr = test_cases[0]['arr'])) print('arr:', test_cases[1]['arr'], '\t(min, max):', find_2nd_mini_maxi_BS(arr = test_cases[1]['arr'])) print('arr:', test_cases[2]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BS(arr = test_cases[2]['arr'])) print('arr:', test_cases[3]['arr'], '\t(min, max):', find_2nd_mini_maxi_BS(arr = test_cases[3]['arr']))
print('arr:', test_cases[4]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_BS(arr = test_cases[4]['arr'])) $(\min, \max) : (-1, -1)$ arr: [1] $(\min, \max): (-1, -1)$ arr: [1, 1, 1, 1, 1, 1] arr: [1, 1, 3] (min, max): (3, 1)arr: [1, 2, 4, 7, 7, 5] (min, max): (2, 5)arr: [8, 10, 5, 7, 9] (min, max): (7, 9)In [11]: """ Optimal solution Time Complexity : O(n) Space Complexity : O(1) def find_2nd_mini_maxi_OS(arr): n = len(arr)mini, second_mini = arr[0], float('inf') second_maxi, maxi = float('-inf'), arr[0] for i in range(1, n): #Finds the second smallest element if arr[i] < mini:</pre> second mini = mini mini = arr[i] elif arr[i] > mini and arr[i] < second mini:</pre> second mini = arr[i] #Finds the second largest element if arr[i] > maxi: second maxi = maxi maxi = arr[i] elif arr[i] < maxi and arr[i] > second_maxi: second maxi = arr[i] second mini = -1 if second mini == float('inf') else second mini second maxi = -1 if second maxi == float('-inf') else second maxi return second_mini, second_maxi In [12]: test_cases = [{'arr': [1]}, {'arr': [1,1,1,1,1,1]}, {'arr': [1,1,3]}, {'arr': [1,2,4,7,7,5]}, {'arr': [8,10,5,7,9]}] print('arr:', test_cases[0]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_OS(arr = test_cases[0]['arr'])) print('arr:', test_cases[1]['arr'], '\t(min, max):', find_2nd_mini_maxi_OS(arr = test_cases[1]['arr'])) print('arr:', test_cases[2]['arr'], '\t\t(min, max):', find_2nd_mini_maxi_OS(arr = test_cases[2]['arr'])) print('arr:', test_cases[3]['arr'], '\t(min, max):', find_2nd_mini_maxi_OS(arr = test_cases[3]['arr'])) print('arr:', test cases[4]['arr'], '\t\t(min, max):', find 2nd mini maxi OS(arr = test cases[4]['arr'])) arr: [1] $(\min, \max) : (-1, -1)$ arr: [1, 1, 1, 1, 1, 1] $(\min, \max): (-1, -1)$ $(\min, \max): (3, 1)$ arr: [1, 1, 3] arr: [1, 2, 4, 7, 7, 5] $(\min, \max): (2, 5)$ arr: [8, 10, 5, 7, 9] $(\min, \max): (7, 9)$ Problem Statement 5: Reverse an array in-place Given an array, reverse it in-place (i.e. without using extra space). Example 1: Input: [1,2,4,7,7,5] Output: [5,7,7,4,2,1] Example 2: Input: [1] Output: [1] In [13]: Time Complexity : O(n) Space Complexity: 0(1) def inplace reverse(arr): i = 0 j = len(arr) - 1while i < j: arr[i], arr[j] = arr[j], arr[i]i += 1 j **-=** 1 In [14]: test_cases = [{'arr': [1,2,4,7,7,5]}, {'arr': [1]}] for tc in test_cases: arr = tc['arr'] inplace_reverse(arr) print('Reversed arr:', arr) Reversed arr: [5, 7, 7, 4, 2, 1] Reversed arr: [1] Problem Statement 6: Move all Zeros to the end of the array You are given an array of integers, your task is to move all the zeros in the array to the end of the array and move non-negative integers to the front by maintaining their order. Example 1: Input: 1 ,0 ,2 ,3 ,0 ,4 ,0 ,1 Output: 1 ,2 ,3 ,4 ,1 ,0 ,0 ,0 Explanation: All the zeros are moved to the end and non-negative integers are moved to front by maintaining order Example 2: Input: 1,2,0,1,0,4,0 Output: 1,2,1,4,0,0,0 Explanation: All the zeros are moved to the end and non-negative integers are moved to front by maintaining order In [15]: """ Time Complexity : O(n) Space Complexity : 0(1) def move zeroes(arr): n = len(arr)for i in range(0, n): **if** arr[i] == 0: j = i break for i in range(j+1, n): if arr[i] != 0: arr[i], arr[j] = arr[j], arr[i]In [16]: test cases = $[{'arr': [1,0,2,3,0,4,0,1]},$ { 'arr': [1,2,0,1,0,4,0,0] }] for tc in test cases: arr = tc['arr'] move zeroes(arr) print('New arr:', arr) New arr: [1, 2, 3, 4, 1, 0, 0, 0] New arr: [1, 2, 1, 4, 0, 0, 0, 0] Problem Statement 7: Remove duplicates in-place from Sorted Array Given an integer array sorted in ascending order, remove the duplicates in place such that each unique element appears only once. The relative order of the elements should be kept the same. If there are k elements after removing the duplicates, then the first k elements of the array should hold the final result. It does not matter what you leave beyond the first k elements. **Note:** Return k after placing the final result in the first k slots of the array. Example 1: Input: arr[1,1,2,2,2,3,3] Output: arr[1,2,3,_,_,_] Explanation: Total number of unique elements are 3, i.e [1,2,3] and Therefore return 3 after assigning [1,2,3] in the beginning of the array. Example 2: Input: arr[1,1,1,2,2,3,3,3,3,4,4] Output: arr[1,2,3,4,_,_,_,_,_] Explanation: Total number of unique elements are 4, i.e[1,2,3,4] and Therefore return 4 after assigning [1,2,3,4] in the beginning of the array. In [17]: def remove duplicates(arr): n = len(arr)j = 0 for i in range(0, n): **if** arr[i] != arr[j]: j **+=** 1 arr[i], arr[j] = arr[j], arr[i]return j+1 In [18]: test cases = $[{'arr': [1,1,2,2,2,3,3]},$ {'arr': [1,1,1,2,2,3,3,3,3,4,4]}] arr = test cases[0]['arr'] print(f"arr: {arr}\t\tUnique Elements: {remove duplicates(arr)}\tNew arr: {arr}") arr = test cases[1]['arr'] print(f"arr: {arr}\tUnique Elements: {remove duplicates(arr)}\tNew arr: {arr}") arr: [1, 1, 2, 2, 2, 3, 3] Unique Elements: 3 New arr: [1, 2, 3, 2, 2, 1, 3] arr: [1, 1, 1, 2, 2, 3, 3, 3, 3, 4, 4] Unique Elements: 4 New arr: [1, 2, 3, 4, 2, 1, 3, 3, 3, 1, 4] Problem Statement 8: Rotate array by K elements Given an array of integers, rotating array of elements by k elements either left or right. Example 1: Input: arr = [1,2,3,4,5,6,7], k = 2, rightOutput: arr = [6,7,1,2,3,4,5]Explanation: array is rotated to right by 2 position. Example 2: Input: arr = [3,7,8,9,10,11], k = 3, leftOutput: arr = [9,10,11,3,7,8]Explanation: Array is rotated to right by 3 position. In [19]: """ Better solution Time Complexity : O(n) Space Complexity : O(k) def rotate BS(arr, k, direction): n = len(arr)k = k % nif direction == 'LEFT': tmp arr = arr[:k] for i in range(k, n): arr[i - k] = arr[i]for i in range(n-k, n): $arr[i] = tmp_arr[i - k]$ tmp arr = arr[n-k:] **for** i **in** range(n-k-1, -1, -1): arr[i + k] = arr[i]for i in range(0, k): arr[i] = tmp_arr[i] In [20]: test_cases = [{'arr': [1,2,3,4,5,6,7], 'k': 2, 'direction': 'RIGHT'}, {'arr': [3,7,8,9,10,11], 'k': 3, 'direction': 'LEFT'}] for tc in test cases: print(f"arr: {tc['arr']}\tk: {tc['k']}\tdirection: {tc['direction']}\t", end='') rotate BS(arr=tc['arr'], k=tc['k'], direction=tc['direction']) print(f"New arr: {tc['arr']}") arr: [1, 2, 3, 4, 5, 6, 7] k: 2 direction: RIGHT New arr: [6, 7, 1, 2, 3, 4, 5] k: 3 direction: LEFT New arr: [9, 10, 11, 3, 7, 8] arr: [3, 7, 8, 9, 10, 11] In [21]: """ Optimal solution Time Complexity : O(2n) Space Complexity : 0(1) def reverse inplace(arr, i, j): while i < j: arr[i], arr[j] = arr[j], arr[i]i += 1 j **-=** 1 def rotate OS(arr, k, direction): n = len(arr)k = k % n if direction == 'LEFT': reverse inplace(arr, 0, k-1) reverse inplace(arr, k, n-1) reverse_inplace(arr, 0, n-1) else: reverse inplace(arr, 0, n-k-1) reverse inplace(arr, n-k, n-1) reverse inplace(arr, 0, n-1) In [22]: test cases = [{'arr': [1,2,3,4,5,6,7], 'k': 2, 'direction': 'RIGHT'}, {'arr': [3,7,8,9,10,11], 'k': 3, 'direction': 'LEFT'}] for tc in test cases: print(f"arr: {tc['arr']}\tk: {tc['k']}\tdirection: {tc['direction']}\t", end='') rotate OS(arr=tc['arr'], k=tc['k'], direction=tc['direction']) print(f"New arr: {tc['arr']}") arr: [1, 2, 3, 4, 5, 6, 7] k: 2 direction: RIGHT New arr: [6, 7, 1, 2, 3, 4, 5] arr: [3, 7, 8, 9, 10, 11] k: 3 direction: LEFT New arr: [9, 10, 11, 3, 7, 8] Problem Statement 9: Count max consecutive 1's in an array Given an array that contains only 1's and 0's, return the count of maximum consecutive 1's in the array. Example 1: Input: arr = [1, 1, 0, 1, 1, 1]Explanation: There are 2 consecutive 1's and 3 consecutive 1's in the array out of which maximum is 3. Example 2: Input: arr = [1, 0, 1, 1, 0, 1]Output: Explanation: There are 2 consecutive 1's in the array. In [23]: """ Time Complexity : O(n) Space Complexity : 0(1) def find max consecutive ones(arr): n = len(arr)one count = 0max one count = 0 for i in range(0, n): **if** arr[i] == 1: one count += 1 else: one count = 0 max one count = max(one count, max one count) return max one count In [24]: test cases = $[{'arr': [1,1,0,1,1,1]},$ {'arr': [1,0,1,1,0,1]}] for tc in test cases: print('arr:', tc['arr'], "Max consecutive 1's:", find max consecutive ones(arr = tc['arr'])) arr: [1, 1, 0, 1, 1, 1] Max consecutive 1's: 3 arr: [1, 0, 1, 1, 0, 1] Max consecutive 1's: 2 Problem Statement 10: Find the number that appears once, while others appear twice Given a non-empty array of integers arr, every element appears twice except for one. Find that single one. Example 1: Input Format: arr = [2,2,1]Result: 1 Explanation: In this array, only the element 1 appear once and so it is the answer. Example 2: Input Format: arr = [4,1,2,1,2]Explanation: In this array, only element 4 appear once and the other elements appear twice. In [25]: """ Better solution Time Complexity : $O(n + n/2 + 1) \sim O(n)$ Space Complexity: O(n/2 + 1) ~ O(n)def get single element BS(arr): n = len(arr)freq map = dict() for i in range(0, n): freq map[arr[i]] = freq map.get(arr[i], 0) + 1 for num, freq in freq map.items(): **if** freq == 1: return num return -1 In [26]: test cases = $[{'arr'}: [2,2,1]},$ {'arr': [4,1,2,1,2]}] print('arr:', test cases[0]['arr'], "\t\tNum that appears once:", get single element BS(arr = test cases[0]['ar print('arr:', test_cases[1]['arr'], "\tNum that appears once:", get_single_element_BS(arr = test_cases[1]['arr' Num that appears once: 1 arr: [2, 2, 1] Num that appears once: 4 arr: [4, 1, 2, 1, 2] In [27]: """ Optimal solution Note: XOR Property 1: $a ^ a = 0$ XOR Property 2: $0 ^a = a$ Time Complexity : O(n) Space Complexity : 0(1) def get single element OS(arr): n = len(arr)result = 0 for i in range(0, n): result = result ^ arr[i] return result In [28]; test cases = $[{'arr': [2,2,1]},$ {'arr': [4,1,2,1,2]}] print('arr:', test cases[0]['arr'], "\t\tNum that appears once:", get single element OS(arr = test cases[0]['ar print('arr:', test_cases[1]['arr'], "\tNum that appears once:", get_single_element_OS(arr = test_cases[1]['arr' arr: [2, 2, 1] Num that appears once: 1 arr: [4, 1, 2, 1, 2] Num that appears once: 4 Problem Statement 11: Find the missing number in an array Given an integer N and an array of size N-1 containing N-1 numbers between 1 to N. Find the number (between 1 to N), that is not present in the given array. Example 1: Input Format: N = 5, arr = [1,2,4,5] Explanation: In the given array, number 3 is missing. So, 3 is the answer. Example 2: Input Format: N = 3, arr = [1,3]Explanation: In the given array, number 2 is missing. So, 2 is the answer. In [29]: """ Time Complexity : O(n) [For summing the array] Space Complexity : 0(1) def missing number(arr, n): **return** (n*(n+1))//2 - sum(arr) In [30]: test cases = $[{'arr': [1,2,4,5], 'n': 5},$ {'arr': [1,3], 'n': 3}] arr = test cases[0]['arr'] n = test cases[0]['n'] print('arr:', arr, "\tn:", n, "\tMissing num:", missing number(arr, n)) arr = test cases[1]['arr'] n = test cases[1]['n'] print('arr:', arr, "\t\tn:", n, "\tMissing num:", missing number(arr, n)) Missing num: 3 arr: [1, 2, 4, 5] n: 5 n: 3 arr: [1, 3] Missing num: 2 In [31]: """ Note: XOR Property 1: $a ^ a = 0$ XOR Property 2: $0 ^ a = a$ Time Complexity : O(n) Space Complexity: 0(1) def missing_number(arr, n): xor1 = 0xor2 = 0for i in range(0, n-1): xor1 ^= arr[i] xor2 **^=** i+1 xor2 **^=** n return xor1 ^ xor2 In [32]: test cases = $[{'arr': [1,2,4,5], 'n': 5},$ {'arr': [1,3], 'n': 3}] arr = test cases[0]['arr'] n = test cases[0]['n'] print('arr:', arr, "\tn:", n, "\tMissing num:", missing number(arr, n)) arr = test cases[1]['arr'] n = test cases[1]['n'] print('arr:', arr, "\t\tn:", n, "\tMissing num:", missing_number(arr, n)) arr: [1, 2, 4, 5] n: 5 Missing num: 3 arr: [1, 3] n: 3 Missing num: 2 **Problem Statement 12: Union of Two Sorted Arrays** Given two sorted arrays, arr1, and arr2 of size n and m. Find the union of two sorted arrays. **Note:** Elements in the union should be in ascending order. Example 1: Input: arr1 = [1,2,3,4,5], arr2 = [2,3,4,4,5]Output: [1,2,3,4,5] Example 2: Input: arr1 = [1,2,3,4,5,6,7,8,9,10], arr2 = [2,3,4,4,5,11,12]Output: [1,2,3,4,5,6,7,8,9,10,11,12] In [33]: """ Better solution Time Complexity : O(2(n+m))Space Complexity : O(n+m) def find union BS(arr1, arr2): result = set() for num in arr1: result.add(num) for num in arr2: result.add(num) #Set to list: O(N) return list(result) In [34]: test cases = [{'arr1': [1,2,3,4,5], 'arr2': [2,3,4,4,5]}, {'arr1': [1,2,3,4,5,6,7,8,9,10], 'arr2': [2,3,4,4,5,11,12]}} arr1 = test cases[0]['arr1'] arr2 = test cases[0]['arr2'] print('arr1:', arr1, "\t\t arr2:", arr2, "\t Union:", find union BS(arr1, arr2)) arr1 = test cases[1]['arr1'] arr2 = test cases[1]['arr2'] print('arr1:', arr1, "arr2:", arr2, "Union:", find union BS(arr1, arr2)) arr1: [1, 2, 3, 4, 5] arr2: [2, 3, 4, 4, 5] Union: [1, 2, 3, 4, 5] arr1: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] arr2: [2, 3, 4, 4, 5, 11, 12] Union: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, In [35]: """ Optimal solution Time Complexity : O(n+m) Space Complexity : 0(1) def find union OS(arr1, arr2): i = j = 0n, m = len(arr1), len(arr2)result = [] while i < n and j < m:</pre> if arr1[i] <= arr2[j]:</pre> if len(result) == 0 or result[-1] != arr1[i]: result.append(arr1[i]) i += 1 else: if len(result) == 0 or result[-1] != arr2[j]: result.append(arr2[j]) j **+=** 1 while i < n:</pre> if len(result) == 0 or result[-1] != arr1[i]: result.append(arr1[i]) i += 1 while j < m:</pre> if len(result) == 0 or result[-1] != arr2[j]: result.append(arr2[j]) j **+=** 1 return result In [36]: test cases = [{'arr1': [1,2,3,4,5], 'arr2': [2,3,4,4,5]}, {'arr1': [1,2,3,4,5,6,7,8,9,10], 'arr2': [2,3,4,4,5,11,12]}] arr1 = test cases[0]['arr1'] arr2 = test cases[0]['arr2'] print('arr1:', arr1, "\t\t arr2:", arr2, "\t Union:", find union OS(arr1, arr2)) arr1 = test cases[1]['arr1'] arr2 = test cases[1]['arr2'] print('arr1:', arr1, "arr2:", arr2, "Union:", find union OS(arr1, arr2)) arr2: [2, 3, 4, 4, 5] Union: [1, 2, 3, 4, 5] arr1: [1, 2, 3, 4, 5] arr1: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] arr2: [2, 3, 4, 4, 5, 11, 12] Union: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 121 Problem Statement 13: Longest Subarray with sum K Given an array and a sum k, we need to print the length of the longest subarray that sums to k. Example 1: Input: arr = [2,3,5], k = 5Result: 2 Explanation: The longest subarray with sum 5 is [2, 3]. And its length is 2. Example 2: Input: arr = [2,3,5,1,9], k = 10Result: 3 Explanation: The longest subarray with sum 10 is [2, 3, 5]. And its length is 3. Example 3: Input: arr = [-1, 1, 1], k = 1Result: 3 Explanation: The longest subarray with sum 1 is [-1, 1, 1]. And its length is 3. In [37]: Brute force solution Time Complexity : $O(n^2)$ Space Complexity : O(1) def find longest subarr len BFS(arr, k): n = len(arr)longest subarr len = float('-inf') for i in range(0, n): running sum = 0for j in range(i, n): running sum += arr[j] if running sum == k: length = j - i + 1longest subarr len = max(length, longest subarr len) return longest subarr len In [38]: test cases = $[{'k': 5, 'arr': [2,3,5]},$ {'k': 10, 'arr': [2,3,5,1,9]}, {'k': 1, 'arr': [-1,1,1]}, {'k': 3, 'arr': [1,2,3,1,1,1,1,4,2,3]}, {'k': 0, 'arr': [1,2,-3,1,0,-4,1,4,0,1]}] for tc in test cases: arr = tc['arr'] k = tc['k']print(find longest subarr len BFS(arr, k)) 2 3 3 3 8

In [39]: """ Better solution Note: If arr has zero & +ev numbers, this is the better solution. If arr has zero, +ev & -ev numbers, this is the optimal solution. Time Complexity : O(n) Space Complexity : O(n) def find_longest_subarr_len_BS(arr, k): n = len(arr)longest subarr len = float('-inf') running_sum = 0 running_sum_map = dict() for i in range(0, n): running_sum += arr[i] if running_sum == k: length = i+1longest_subarr_len = max(length, longest subarr len) remainder = running sum - k if remainder in running_sum_map: length = i - running_sum_map[remainder] longest_subarr_len = max(length, longest_subarr_len) if running sum not in running sum map: running_sum_map[running_sum] = i return longest subarr len In [40]: test cases = $[{'k': 3, 'arr': [1,2,-3]},$ {'k': 5, 'arr': [2,3,5]}, {'k': 10, 'arr': [2,3,5,1,9]}, {'k': 0, 'arr': [-1,1,1]}, {'k': 3, 'arr': [1,2,3,1,1,1,1,4,2,3]}, {'k': 7, 'arr': [1,2,-3,1,0,-4,1,4,0,1,0,4,3]}, {'k': 0, 'arr': [-1,0,1,1,-1,-1,0]}] for tc in test cases: arr = tc['arr'] k = tc['k']print(find longest subarr len BS(arr, k)) 2 2 3 2 3 In [41]: """ Optimal solution If arr has zero & +ev numbers, this is the optimal solution. Time Complexity : O(2n) Space Complexity : O(1) def find_longest_subarr_len_OS(arr, k): n = len(arr)longest subarr len = float('-inf') flexi sum = arr[0]i = j = 0while j < n: while i <= j and flexi sum > k: flexi sum -= arr[i] if flexi sum == k: length = j - i + 1longest subarr len = max(length, longest subarr len) j **+=** 1 **if** j < n: flexi_sum += arr[j] return longest subarr len In [42]: test cases = $[\#\{'k': 0, 'arr': [-1,0,1,1,-1,-1,0]\},$ {'k': 3, 'arr': [1,2,3,1,1,1,1,4,2,3]}] for tc in test_cases: arr = tc['arr'] k = tc['k']print(find longest subarr len OS(arr, k)) 3 Problem Statement 14: Count Subarray sum Equals K Given an array of integers and an integer k, return the total number of subarrays whose sum equals k. Note: A subarray is a contiguous non-empty sequence of elements within an array. Example 1: Input: arr = [3, 1, 2, 4], k = 6Output: 2 Explanation: The subarrays that sum up to 6 are [3, 1, 2] and [2, 4]. Example 2: Input: arr = [1,2,3], k = 3Output: 2 Explanation: The subarrays that sum up to 3 are [1, 2], and [3]. In [43]: """ Brute force solution Time Complexity : $O(n^2)$ Space Complexity : O(1) def find_all_subarr_with_given_sum_BFS(arr, k): n = len(arr)subarr_counter = 0 for i in range(0, n): rsum = 0for j in range(i, n): rsum += arr[j] if rsum == k: subarr counter += 1 return subarr_counter In [44]: test_cases = [{'k': 3, 'arr': [1,2,3,-3,1,1,1,4,2,-3]}, {'k': 5, 'arr': [2,3,5]}, {'k': 10, 'arr': [2,3,5,1,9]}, {'k': 1, 'arr': [-1,1,1]}, {'k': 3, 'arr': [1,2,3,1,1,1,1,4,2,3]}, {'k': 0, 'arr': [1,2,-3,1,0,-4,1,4,0,1]}] for tc in test cases: arr = tc['arr'] k = tc['k']print(find all subarr with given sum BFS(arr, k)) 8 2 2 3 5 In [45]: """ Optimal solution Note: If arr has zero, +ev & -ev numbers, this is the optimal solution. Time Complexity : O(n)Space Complexity : O(n) def find_all_subarr_with_given_sum_OS(arr, k): n = len(arr)rsum = 0 $rsum\ map = \{0:1\}$ subarr_counter = 0 for i in range(n): rsum += arr[i] rem = rsum - ksubarr counter += rsum map.get(rem, 0) rsum_map[rsum] = rsum_map.get(rsum, 0) + 1 return subarr_counter test_cases = [{'k': 3, 'arr': [1,2,3,-3,1,1,1,4,2,-3]}, In [46]: {'k': 5, 'arr': [2,3,5]}, {'k': 10, 'arr': [2,3,5,1,9]}, {'k': 1, 'arr': [-1,1,1]}, {'k': 3, 'arr': [1,2,3,1,1,1,1,4,2,3]}, {'k': 0, 'arr': [1,2,-3,1,0,-4,1,4,0,1]}] for tc in test_cases: arr = tc['arr'] k = tc['k']print(find_all_subarr_with_given_sum_OS(arr, k)) 8 2 2 3 5 6 Problem Statement 15: Maximum Subarray Sum in an Array (Kadane's Algorithm) Given an integer array arr, find the contiguous subarray (containing at least one number) which has the largest sum and returns its sum and prints the subarray. Example 1: Input: arr = [-2,1,-3,4,-1,2,1,-5,4]Output: 6 Explanation: [4,-1,2,1] has the largest sum = 6. Examples 2: Input: arr = [1] Output: 1 Explanation: Array has only one element and which is giving positive sum of 1. In [47]: Brute force solution Time Complexity : $O(n^2)$ Space Complexity : O(1) def find_max_subarr_sum_BFS(arr): n = len(arr)max_subarr_sum = 0 for i in range(0,n): rsum = 0for j in range(i,n): rsum += arr[j] max_subarr_sum = max(rsum, max_subarr_sum) return max_subarr_sum In [48]: test_cases = [{'arr': [-2,1,-3,4,-1,2,1,-5,4]}, {'arr': [-2,-3,4,-1,-2,1,5,-3]}, {'arr': [1]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, '\tMax sub arr sum:', find_max_subarr_sum_BFS(arr)) arr: [-2, 1, -3, 4, -1, 2, 1, -5, 4] Max sub arr sum: 6 arr: [-2, -3, 4, -1, -2, 1, 5, -3] Max sub arr sum: 7 Max sub arr sum: 1 In [49]: """ Optimal solution (Kadane's Algorithm) Time Complexity : O(n)Space Complexity : O(1) def find_max_subarr_sum_OS(arr): n = len(arr)max subarr_sum = curr_sum = arr[0] for i in range(1, n): curr_sum = max(arr[i], curr_sum + arr[i]) max_subarr_sum = max(curr_sum, max_subarr_sum) return max_subarr_sum In [50]: test_cases = [{'arr': [-2,1,-3,4,-1,2,1,-5,4]}, {'arr': [-2,-3,4,-1,-2,1,5,-3]}, {'arr': [1]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, '\tMax sub arr sum:', find_max_subarr_sum_OS(arr)) arr: [-2, 1, -3, 4, -1, 2, 1, -5, 4] Max sub arr sum: 6 arr: [-2, -3, 4, -1, -2, 1, 5, -3] Max sub arr sum: 7 Max sub arr sum: 1 arr: [1] In [51]: """ Optimal solution (Kadane's Algorithm) Time Complexity : O(n) Space Complexity : O(1) def find_max_subarr_sum_OS2(arr): n = len(arr)curr_sum = arr[0] curr_sidx = curr_eidx = 0 max subarr sum = arr[0] max_subarr_sidx = max_subarr_eidx = 0 for i in range(1, n): if arr[i] > curr_sum + arr[i]: curr_sum = arr[i] curr_sidx = curr_eidx = i else: curr_sum = curr_sum + arr[i] curr_eidx = i if curr_sum > max_subarr_sum: max subarr sum = curr sum max subarr sidx = curr sidx max subarr eidx = curr eidx return max_subarr_sum, arr[max_subarr_sidx : max_subarr_eidx + 1] In [52]: test_cases = [{'arr': [-2,1,-3,4,-1,2,1,-5,4]}, {'arr': [-2,-3,4,-1,-2,1,5,-3]}, { 'arr': [1] }] for tc in test cases: arr = tc['arr'] print('arr:', arr, '\tMax sub arr:', *find_max_subarr_sum_OS2(arr)) arr: [-2, 1, -3, 4, -1, 2, 1, -5, 4] Max sub arr: 6 [4, -1, 2, 1] arr: [-2, -3, 4, -1, -2, 1, 5, -3] Max sub arr: 7 [4, -1, -2, 1, 5] arr: [1] Max sub arr: 1 [1] Problem Statement 16: Two Sum - Check if a pair with given sum exists in Array Given an array of integers and an integer target. • 1st variant: Return YES if there exist two numbers such that their sum is equal to the target. Otherwise, return NO. • 2nd variant: Return indices of the two numbers such that their sum is equal to the target. Otherwise, we will return {-1, Note: You are not allowed to use the same element twice. Example: If the target is equal to 6 and num[1] = 3, then nums[1] + nums[1] = target is not a solution. Example 1: Input: arr = [2,6,5,8,11], target = 14Output: YES (for 1st variant) [1, 3] (for 2nd variant) Example 2: Input: arr = [2,6,5,8,11], target = 15Result: NO (for 1st variant) [-1, -1] (for 2nd variant) In [53]: """ Better solution Time Complexity : O(n)Space Complexity : O(n) def two_sum_BS(arr, target): n = len(arr)hashmap = dict() for i in range(0, n): rem = target - arr[i] if rem in hashmap: return hashmap[rem], i hashmap[arr[i]] = i return -1, -1 In [54]: test_cases = [{'arr': [2,6,5,8,11], 'target': 14}, {'arr': [2,6,5,8,11], 'target': 15}] for tc in test_cases: arr = tc['arr'] target = tc['target'] print('arr:', arr, 'target:', target, '2 Sum:', two_sum_BS(arr, target)) arr: [2, 6, 5, 8, 11] target: 14 2 Sum: (1, 3) arr: [2, 6, 5, 8, 11] target: 15 2 Sum: (-1, -1) In [55]: """ Optimal (space) solution Time Complexity : $O(n \log n)$ Space Complexity : O(1) def two_sum_OS(arr, target): arr = sorted(enumerate(arr), key = lambda x: x[1])n = len(arr)i, j = 0, n-1while i < j: if arr[i][1] + arr[j][1] == target: return arr[i][0], arr[j][0] elif arr[i][1] + arr[j][1] < target:</pre> i += 1 else: j -= 1 return (-1, -1) In [56]: test_cases = [{'arr': [2,6,5,8,11], 'target': 14}, {'arr': [2,6,5,8,11], 'target': 15}] for tc in test_cases: arr = tc['arr'] target = tc['target'] print('arr:', arr, 'target:', target, '2 Sum:', two_sum_OS(arr, target)) arr: [2, 6, 5, 8, 11] target: 14 2 Sum: (1, 3) arr: [2, 6, 5, 8, 11] target: 15 2 Sum: (-1, -1) Problem Statement 17: 3 Sum - Find triplets that add up to a zero Given an integer array nums, return all the triplets [nums[i], nums[j], nums[k]] such that i!=j, i!=k, and j!=k, and nums[i] + nums[j] + nums[k] == 0.Note: The solution set must not contain duplicate triplets. Example 1: Input: nums = [-1,0,1,2,-1,-4]Output: [[-1,-1,2],[-1,0,1]] Example 2: Input: nums = [-1,0,1,0]Output: [[-1,0,1]] In [57]: """ Optimal (space) solution Time Complexity : $O(n \log n) + O(n^2)$ Space Complexity : O(1) def three_sum(arr): arr.sort() n = len(arr)ans = []for i in range(n): if i != 0 and arr[i-1] == arr[i]: continue j = i+1k = n-1while j < k: total_sum = arr[i] + arr[j] + arr[k] if total_sum < 0:</pre> j += 1 elif total_sum > 0: k = 1else: ans.append((arr[i], arr[j], arr[k])) j += 1 k = 1while j < k and arr[j] == arr[j - 1]: j += 1 while j < k and arr[k] == arr[k + 1]: k -= 1return ans In [58]: test_cases = [{'arr': [-1,0,1,2,-1,-4]}, {'arr': [-1,0,1,0]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, '3 Sum:', three_sum(arr)) arr: [-4, -1, -1, 0, 1, 2] 3 Sum: [(-1, -1, 2), (-1, 0, 1)] arr: [-1, 0, 0, 1] 3 Sum: [(-1, 0, 1)] Problem Statement 18: 4 Sum - Find quads that add up to a target value Given an array of N integers, your task is to find unique quads that add up to give a target value. In short, you need to return an array of all the unique quadruplets [arr[a], arr[b], arr[c], arr[d]] such that their sum is equal to a given target. Note: The solution set must not contain duplicate quadruplets. Example 1: Input: arr = [1,0,-1,0,-2,2], target = 0Output: [[-2,-1,1,2],[-2,0,0,2],[-1,0,0,1]] Example 2: Input: arr = [4,3,3,4,4,2,1,2,1,1], target = 9Output: [[1,1,3,4],[1,2,2,4],[1,2,3,3]] In [59]: Optimal (space) solution Time Complexity : $O(n \log n) + O(n^3)$ Space Complexity : O(1) def four_sum(arr, target): arr.sort() n = len(arr)ans = []for i in range(0, n): if i != 0 and arr[i-1] == arr[i]: continue for j in range(i+1, n): if j != 1 and arr[j-1] == arr[j]: continue k = j+1while k < 1: target_sum = arr[i] + arr[j] + arr[k] + arr[1] if target_sum < target:</pre> $k \neq 1$ elif target_sum > target: 1 -= 1 else: ans.append([arr[i], arr[j], arr[k], arr[l]]) k += 11 -= 1 while k < 1 and arr[k-1] == arr[k]: $k \neq 1$ while k < 1 and arr[1] == arr[1+1]: return ans In [60]: test_cases = [{'arr': [1,0,-1,0,-2,2], 'target': 0}, {'arr': [4,3,3,4,4,2,1,2,1,1], 'target': 9}] for tc in test_cases: arr = tc['arr'] target = tc['target'] print('arr:', arr, '4 Sum:', four_sum(arr, target)) arr: [-2, -1, 0, 0, 1, 2] 4 Sum: [[-2, -1, 1, 2], [-2, 0, 0, 2], [-1, 0, 0, 1]] arr: [1, 1, 1, 2, 2, 3, 3, 4, 4, 4] 4 Sum: [[1, 1, 3, 4], [1, 2, 2, 4], [1, 2, 3, 3]] **Problem Statement 19: Buy And Sell Stocks** You are given an array of prices where prices[i] is the price of a given stock on an ith day. You want to maximize your profit by choosing a single day to buy one stock and choosing a different day in the future to sell that stock. Return the maximum profit you can achieve from this transaction. If you cannot achieve any profit, return 0. Example 1: Input: prices = [7,1,5,3,6,4]Explanation: Buy on day 2 (price = 1) and sell on day 5 (price = 6), profit = 6-1 = 5. Note: That buying on day 2 and selling on day 1 is not allowed because you must buy before you sell. Example 2: Input: prices = [7,6,4,3,1]Output: 0 Explanation: In this case, no transactions are done and the max profit = 0. In [61]: """ Time Complexity : O(n)Space Complexity : O(1) def find_max_profit(arr): n = len(arr)min_price = float('inf') max_profit = float('-inf') for i in range(0,n): min_price = min(arr[i], min_price) max_profit = max(arr[i] - min_price, max_profit) return max_profit In [62]: test_cases = [{'arr': [7,1,5,3,6,4]}, {'arr': [7,6,4,3,1]}] for tc in test cases: arr = tc['arr'] print('arr:', arr, 'Max profit:', find_max_profit(arr)) arr: [7, 1, 5, 3, 6, 4] Max profit: 5 arr: [7, 6, 4, 3, 1] Max profit: 0 Problem Statement 20: Leaders in an Array Given an array, print all the elements which are leaders. A Leader is an element that is greater than all of the elements on its right side in the array. Example 1: Input: arr = [4, 7, 1, 0]Output: [7, 1, 0] Explanation: Rightmost element is always a leader. 7 and 1 are greater than the elements in their right side. Example 2: Input: arr = [10, 22, 12, 3, 0, 6]Output: [22, 12, 6] Explanation: 6 is a leader. In addition to that, 12 is greater than all the elements in its right side (3, 0, 6), also 22 is greater than 12, 3, 0, 6. In [631: Time Complexity : O(2n) Space Complexity : O(1) def find_leaders(arr): n = len(arr)maxi = float('-inf') leaders = [] for i in range (n-1, -1, -1): if arr[i] > maxi: leaders.append(arr[i]) maxi = arr[i] inplace_reverse(leaders) return leaders In [64]: test_cases = [{'arr': [4, 7, 1, 0]}, {'arr': [10, 22, 12, 3, 0, 6]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Leaders:', find leaders(arr)) arr: [4, 7, 1, 0] Leaders: [7, 1, 0] arr: [10, 22, 12, 3, 0, 6] Leaders: [22, 12, 6] Problem Statement 21: Find the Majority Element (Moore's Voting Algorithm) Given an array of N integers, write a program to return an element that occurs more than N/2 times (majority element) in the given array. Return -1 if no such element exists in the array. Example 1: Input: arr = [3,2,3]Output: 3 Example 2: Input: arr = [2,2,1,1,1,2,2]Output: 2 Example 3: Input: arr = [4,4,2,4,3,4,4,3,2,4]Output: 4 In [65]: Brute force solution Time Complexity : $O(n \log n)$ Space Complexity : O(1) def find_majority_element_BFS(arr): arr.sort() n = len(arr)candidate = arr[n//2] counter = 0 for i in range(0, n): if arr[i] == candidate: counter += 1 return candidate if counter > n//2 else -1 In [66]: test cases = [{'arr': [3,2,3]}, {'arr': [2,2,1,1,1,2,2]}, {'arr': [4,4,2,4,3,4,4,3,2,4]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Majority element:', find majority element BFS(arr)) arr: [2, 3, 3] Majority element: 3 arr: [1, 1, 1, 2, 2, 2, 2] Majority element: 2 arr: [2, 2, 3, 3, 4, 4, 4, 4, 4] Majority element: 4 In [67]: Better solution Time Complexity : O(2n) Space Complexity : O(n) def find majority element BS(arr): n = len(arr)hashmap = dict() for i in range(0,n): hashmap[arr[i]] = hashmap.get(arr[i], 0) + 1 for n, f in hashmap.items(): if f > n//2: return n return -1 In [68]: test cases = [{'arr': [3,2,3]}, {'arr': [2,2,1,1,1,2,2]}, {'arr': [4,4,2,4,3,4,4,3,2,4]}] for tc in test cases: arr = tc['arr'] print('arr:', arr, 'Majority element:', find_majority_element BS(arr)) arr: [3, 2, 3] Majority element: 3 arr: [2, 2, 1, 1, 1, 2, 2] Majority element: 2 arr: [4, 4, 2, 4, 3, 4, 4, 3, 2, 4] Majority element: 4 In [69]: """ Optimal solution (Moore's Voting Algorithm) Time Complexity : O(2n) Space Complexity : O(1) def find_majority_element_OS(arr): n = len(arr)candidate = None count = 0for i in range(0,n): if count == 0: candidate = arr[i] count = 1 elif arr[i] == candidate: count += 1 else: count -= 1 count = 0for i in range(0,n): if arr[i] == candidate: count += 1 return candidate if count > n//2 else -1 In [70]: test_cases = [{'arr': [3,2,3]}, {'arr': [2,2,1,1,1,2,2]}, {'arr': [4,4,2,4,3,4,4,3,2,4]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Majority element:', find_majority_element_OS(arr)) arr: [3, 2, 3] Majority element: 3 arr: [2, 2, 1, 1, 1, 2, 2] Majority element: 2 arr: [4, 4, 2, 4, 3, 4, 4, 3, 2, 4] Majority element: 4 Problem Statement 22: Find the Majority Element II (Moore's Voting Algorithm) Given an array of N integers, write a program to return the element(s) that occurs more than N/3 times (majority element) in the given array. Return [] if no such element exists in the array. Example 1: Input: arr = [1,2,2,3,2]**Output:** [2] Explanation: Here we can see that the Count(1) = 1, Count(2) = 3 and Count(3) = 1. Therefore, the count of 2 is greater than N/3 times. Hence, 2 is the answer. Example 2: Input: arr = [11,33,33,11,33,11] Output: [11, 33] Explanation: Here we can see that the Count(11) = 3 and Count(33) = 3. Therefore, the count of both 11 and 33 is greater than N/3 times. Hence, 11 and 33 is the answer. In [71]: """ Better solution Time Complexity : O(n)Space Complexity : O(n) def find_majority_element_2_BS(arr): n = len(arr)majority_elements = [] num_freq_map = dict() for i in range(0,n): num_freq_map[arr[i]] = num_freq_map.get(arr[i], 0) + 1 if $num_freq_map[arr[i]] == n//3+1$: majority_elements.append(arr[i]) if len(majority_elements) == 2: return majority_elements In [72]: test_cases = [{'arr': [1,2,2,3,2]}, {'arr': [11,33,33,11,33,11]}, {'arr': [2,1,1,3,1,4,5,6]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Majority element:', find_majority_element_2_BS(arr)) arr: [1, 2, 2, 3, 2] Majority element: [2] arr: [11, 33, 33, 11, 33, 11] Majority element: [33, 11] arr: [2, 1, 1, 3, 1, 4, 5, 6] Majority element: [1] In [73]: """ Optimal solution (Moore's Voting Algorithm) Time Complexity : O(2n) Space Complexity : O(1) def find_majority_element_2_OS(arr): n = len(arr)majority_elements = [] candidate1 = candidate2 = None counter1 = counter2 = 0 for i in range(0,n): if counter1 == 0 and arr[i] != candidate2: candidate1 = arr[i] counter1 = 1elif counter2 == 0 and arr[i] != candidate1: candidate2 = arr[i] counter2 = 1elif arr[i] == candidate1: counter1 += 1 elif arr[i] == candidate2: counter2 += 1 else: counter1 -= 1 counter2 -= 1 counter1 = counter2 = 0 for i in range(0, n): if arr[i] == candidate1: counter1 += 1 if arr[i] == candidate2: counter2 += 1 if counter1 > n//3: majority_elements.append(candidate1) if counter2 > n//3: majority_elements.append(candidate2) return majority_elements In [74]: test_cases = [{'arr': [1,2,2,3,2]}, {'arr': [11,33,33,11,33,11]}, {'arr': [2,1,1,3,1,4,5,6]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Majority element:', find_majority_element_2_OS(arr)) arr: [1, 2, 2, 3, 2] Majority element: [2] arr: [11, 33, 33, 11, 33, 11] Majority element: [11, 33] arr: [2, 1, 1, 3, 1, 4, 5, 6] Majority element: [1]

Problem Statement 23: Sort an array of 0s, 1s and 2s (Dutch National Flag Sorting Algorithm) Given an array consisting of only 0s, 1s, and 2s. Write a program to in-place sort the array without using inbuilt sort functions. (Expected: Single pass-O(N) and constant space) Input: nums = [2,0,2,1,1,0]Output: [0,0,1,1,2,2] Input: nums = [2,0,1]Output: [0,1,2] Input: nums = [0]**Output:** [0] In [75]: mmmNote: [1] if mid = 0, swap(low, mid); low ++; mid ++ [2] if mid = 1, mid ++ [3] if mid = 2, swap(high, mid); high--Time Complexity : O(n)Space Complexity : O(1) def dnf_sort(arr): n = len(arr)low = 0mid = 0high = n-1while mid <= high:</pre> if arr[mid] == 0: arr[low], arr[mid] = arr[mid], arr[low] mid += 1low += 1elif arr[mid] == 1: mid += 1else: arr[mid], arr[high] = arr[high], arr[mid] high -= 1 test cases = [{'arr': [2,0,2,1,1,0]}, In [76]: {'arr': [2,0,1]}, {'arr': [0]}, {'arr': [1,1,2,0,0,1,2,2,1,0]}] for tc in test_cases: arr = tc['arr'] dnf_sort(arr) print('arr:', arr) arr: [0, 0, 1, 1, 2, 2] arr: [0, 1, 2] arr: [0] arr: [0, 0, 0, 1, 1, 1, 1, 2, 2, 2] Problem Statement 24: Rearrange Array Elements by Sign There's an array 'A' of size 'N' with an equal number of positive and negative elements. Without altering the relative order of positive and negative elements, you must return an array of alternately positive and negative values. Note: Start the array with positive elements. Example 1: Input: arr = [1,2,-4,-5]Output: [1, -4, 2, -5] Example 2: Input: arr = [1,2,-3,-1,-2,3]Output: [1, -3, 2, -1, 3, -2] In [77]: """ Time Complexity : O(n)Space Complexity : O(1) def rearrange_by_sign(arr): n = len(arr) pos_idx , $neg_idx = 0$, 1 result = [0] * nfor i in range(0,n): if arr[i] >= 0: result[pos_idx] = arr[i] pos_idx += 2 else: result[neg_idx] = arr[i] $neg_idx += 2$ return result In [78]: test_cases = [{'arr': [1,2,-4,-5]}, {'arr': [1,2,-3,-1,-2,3]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Re-arranged arr:', rearrange_by_sign(arr)) arr: [1, 2, -4, -5] Re-arranged arr: [1, -4, 2, -5] arr: [1, 2, -3, -1, -2, 3] Re-arranged arr: [1, -3, 2, -1, 3, -2] Problem Statement 25: Longest Consecutive Sequence in an Array You are given an array of 'N' integers. You need to find the length of the longest sequence which contains the consecutive elements. Example 1: Input: [100, 200, 1, 3, 2, 4] Output: 4 Explanation: The longest consecutive subsequence is 1, 2, 3, and 4. Example 2: Input: [3, 8, 5, 7, 6] Output: 4 Explanation: The longest consecutive subsequence is 5, 6, 7, and 8. In [79]: """ Optimal Solution Time Complexity : $O(n \log n) + O(n)$ Space Complexity : O(1) def longest_successive_elements_OS1(arr): arr.sort() n = len(arr)last_smallest = float('-inf') counter = longest = 0 for i in range(0, n): if (arr[i] - 1) == last_smallest: counter += 1 last_smallest = arr[i] elif arr[i] != last_smallest: counter = 1 last_smallest = arr[i] longest = max(counter, longest) return longest In [80]: test_cases = [{'arr': [100,200,1,3,2,4]}, {'arr': [3,8,5,7,6]}, {'arr': [102,4,100,1,101,3,2,1,1]}, {'arr': [100,102,100,101,101,4,3,2,3,2,1,1,1,2]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Longest successive elements count:', longest_successive_elements_OS1(arr)) arr: [1, 2, 3, 4, 100, 200] Longest successive elements count: 4 arr: [3, 5, 6, 7, 8] Longest successive elements count: 4 arr: [1, 1, 1, 2, 3, 4, 100, 101, 102] Longest successive elements count: 4 arr: [1, 1, 1, 2, 2, 2, 3, 3, 4, 100, 100, 101, 101, 102] Longest successive elements count: 4 In [81]: """ Optimal Solution Time Complexity : O(3n) Space Complexity : O(n) def longest_successive_elements_OS2(arr): n = len(arr)unique_arr = set() for num in arr: unique_arr.add(num) longest = 0for num in unique_arr: if (num - 1) not in unique_arr: tmp = num counter = 1 while tmp+1 in unique arr: counter += 1 tmp += 1 longest = max(counter, longest) return longest In [82]: test_cases = [{'arr': [100,200,1,3,2,4]}, {'arr': [3,8,5,7,6]}, {'arr': [102,4,100,1,101,3,2,1,1]}, {'arr': [100,102,100,101,101,4,3,2,3,2,1,1,1,2]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, 'Longest successive elements count:', longest_successive_elements_OS2(arr)) arr: [100, 200, 1, 3, 2, 4] Longest successive elements count: 4 arr: [3, 8, 5, 7, 6] Longest successive elements count: 4 arr: [102, 4, 100, 1, 101, 3, 2, 1, 1] Longest successive elements count: 4 arr: [100, 102, 100, 101, 101, 4, 3, 2, 3, 2, 1, 1, 1, 2] Longest successive elements count: 4 **Problem Statement 26: Find next permutation** Given an array of integers, rearrange the numbers of the given array into the lexicographically next greater permutation of numbers. If such an arrangement is not possible, it must rearrange to the lowest possible order (i.e., sorted in ascending order). Eample 1: Input: arr = [1,3,2]Output: arr = [2,1,3]Explanation: All permutations of [1,2,3] are [[1,2,3], [1,3,2], [2,1,3], [2,3,1], [3,1,2], [3,2,1]]. So, the next permutation just after [1,3,2] is [2,1,3]. Eample 2: Input: arr = [3,2,1]Output: arr = [1,2,3]Explanation: As we see all permutations of [1,2,3], we find [3,2,1] at the last position. So, we have to return the topmost permutation. In [83]: Time Complexity : O(3n) Space Complexity : O(1) def reverse_inplace(arr, i, j): while i < j: arr[i], arr[j] = arr[j], arr[i] *i += 1* j -= 1 def next_greater_permutation(arr): n = len(arr)#Step 1: Find the break point idx = -1for i in range (n-2, -1, -1): if arr[i] < arr[i+1]:</pre> idx = ibreak else: #If break point does not exist, reverse the whole array and return reverse_inplace(arr, 0, n-1) return arr #Step 2: Find the next greater element and swap it with arr[idx] for i in range (n-1, idx, -1): if arr[i] > arr[idx]: arr[i], arr[idx] = arr[idx], arr[i] break # Step 3: reverse the right half reverse_inplace(arr, idx+1, n-1) return arr In [84]: test_cases = [{'arr': [1,3,2]}, {'arr': [3,2,1]}] for tc in test_cases: arr = tc['arr'] print('arr:', arr, end='') print('', 'Next Permutation:', next_greater_permutation(arr)) arr: [1, 3, 2] Next Permutation: [2, 1, 3] arr: [3, 2, 1] Next Permutation: [1, 2, 3] **Problem Statement 27: Set Matrix Zero** Given a matrix if an element in the matrix is 0 then you will have to set its entire column and row to 0 and then return the matrix. Example 1: Input: matrix = [[1,1,1],[1,0,1], [1,1,1]Output: matrix = [[1,0,1],[0,0,0], [1,0,1]] Explanation: Since matrix[2][2]=0. Therfore the 2nd column and 2nd row wil be set to 0. Example 2: Input: matrix = [[0,1,2,0],[3,4,5,2], [1,3,1,5]] Output: matrix = [[0,0,0,0],[0,4,5,0], [0,3,1,0]] Explanation: Since matrix[0][0]=0 and matrix[0][3]=0. Therefore 1st row, 1st column and 4th column will be set to 0 In [85]: """ Better solution Time Complexity : O(2rc) Space Complexity : O(r) + O(c)def set_zeroes_BS(matrix): rows, columns = len(matrix), len(matrix[0]) row_flag = [False] * rows col_flag = [False] * columns for r in range(rows): for c in range(columns): if matrix[r][c] == 0: row_flag[r] = True col flag[c] = True for r in range(rows): for c in range(columns): if row_flag[r] or col_flag[c]: matrix[r][c] = 0# Not gonna count this for r in range(rows): print('\n') for c in range(columns): print(matrix[r][c], ' ', end='') In [86]: test_cases = [{'matrix': [[1,1,1], [1,0,1], [1,1,1]]}, { 'matrix': [[0,1,2,0], [3,4,5,2], [1,3,1,5]]}, {'matrix': [[1,1,1,1], [1,0,1,1], [1,1,0,1], [0,1,1,1]]}] for tc in test_cases: matrix = tc['matrix'] set_zeroes_BS(matrix) print('\n', '#'*100, sep='') 1 0 1 0 0 0 0 0 0 0 0 4 5 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 In [87]: """ Optimal solution Time Complexity : O(2rc) Space Complexity : O(1) def set zeroes OS(matrix): rows, columns = len(matrix), len(matrix[0]) first_row_zero_flag = False #Step 1: Traverse the matrix and mark 1st row & col accordingly for r in range(rows): for c in range(columns): if matrix[r][c] == 0: matrix[0][c] = 0if r == 0: first_row_zero_flag = True else: matrix[r][0] = 0#Step 2: Mark with 0 from (1,1) to (n-1, m-1)for r in range(1, rows): for c in range(1, columns): if matrix[0][c] == 0 or matrix[r][0] == 0: matrix[r][c] = 0#Step 3: Mark the 1st col as 0s if [0][0] is 0 if matrix[0][0] == 0: for r in range(rows): matrix[r][0] = 0#Step 4: Mark the 1st row as 0s if first_row_zero_flag is True if first_row_zero_flag == True: for c in range(1, columns): matrix[0][c] = 0# Not gonna count this for r in range(rows): print('\n') for c in range(columns): print(matrix[r][c], ' ', end='') In [88]: test_cases = [{'matrix': [[1,1,1], [1,0,1], [1,1,1]]}, { 'matrix': [[0,1,2,0], [3,4,5,2], [1,3,1,5]]}, { 'matrix': [[1,1,1,1], [1,0,1,1], [1,1,0,1], [0,1,1,1]]}, {'matrix': [[1, 2, 3, 4], [5, 0, 7, 8], [0,10,11,12], [13,14,15, 0]]}] for tc in test_cases: matrix = tc['matrix'] set_zeroes_OS (matrix) print('\n', '#'*100, sep='') 1 0 1 0 0 0 1 0 1 0 0 0 0 0 4 5 0 0 3 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 3 0 0 0 0 0 0 0 0 0 0 0 0 0 Problem Statement 28: Rotate Image by 90 degree Given a matrix, your task is to rotate the matrix 90 degrees clockwise. Example 1: Input: [[1,2,3], [4,5,6], [7,8,9]] Output: [[7,4,1], [8,5,2], [9,6,3]] Example 2: Input: [[5, 1, 9,11], [2, 4, 8, 10], [13, 3, 6, 7], [15,14,12,16]] Output: [[15,13, 2, 5], [14, 3, 4, 1], [12, 6, 8, 9], [16, 7,10,11]] In [89]: """ Time Complexity : O(rc + rc/2)Space Complexity : O(1) def reverse (arr): n = len(arr)i, j = 0, n-1while i < j: arr[i], arr[j] = arr[j], arr[i] i += 1 j -= 1 def rotate(matrix, direction): rows, columns = len(matrix), len(matrix[0]) if direction == 'LEFT': for r in range(rows): reverse (matrix[r]) for r in range(rows): for c in range(r+1, columns): matrix[r][c], matrix[c][r] = matrix[c][r], matrix[r][c] for r in range (rows): for c in range(r+1, columns): matrix[r][c], matrix[c][r] = matrix[c][r], matrix[r][c] for r in range (rows): reverse(matrix[r]) # Not gonna count this for r in range(rows): print('\n') for c in range(columns): print(matrix[r][c], ' ', end='') In [90]: test_cases = [{'matrix': [[1,2,3], [7,8,9]], 'direction': 'LEFT'}, { 'matrix': [[1,2,3], [4,5,6], [7,8,9]], 'direction': 'RIGHT'},] for tc in test_cases: matrix = tc['matrix'] direction = tc['direction'] rotate (matrix, direction) print('\n', '#'*100, sep='') 3 6 9 2 5 8 1 4 7 7 4 1 8 5 2 **Problem Statement 29: Spiral Traversal of Matrix** Given a Matrix, print the given matrix in spiral order. Example 1: L Input: $matrix = T [[01 \ 02 \ 03 \ 04 \ 05],$ [14 15 16 17 06], [13 20 19 18 07], B [12 11 10 09 08]] Outhput: 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 In [91]: """ Time Complexity : O(rc) Space Complexity : O(1) def print_spiral(matrix): rows, columns = len(matrix), len(matrix[0]) top, bottom = 0, rows-1 left, right = 0, columns-1 result = []while top <= bottom and left <= right: for i in range(left, right+1): result.append(matrix[top][i]) top += 1 for i in range(top, bottom+1): result.append(matrix[i][right]) right -= 1 if top <= bottom:</pre> for i in range(right, left-1, -1): result.append(matrix[bottom][i]) bottom -= 1 if left <= right:</pre> for i in range(bottom, top-1, -1): result.append(matrix[i][left]) left += 1 return result In [92]: test_cases = [{'matrix': [[1, 2, 3, 4, 5], [14, 15, 16, 17, 6], [13, 20, 19, 18, 7], [12, 11, 10, 9, 8]]}] for tc in test_cases: matrix = tc['matrix'] print(print_spiral(matrix)) [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20] **Problem Statement 30: Pascal's Triangle** This problem has 3 variations. They are stated below: Variation 1: Given row number r and column number c. Print the element at position (r, c) in Pascal's triangle. Variation 2: Given the row number n. Print the n-th row of Pascal's triangle. Variation 3: Given the number of rows n. Print the first n rows of Pascal's triangle. Example 1: Input: r = 5, c = 3Output: (for variation 1) -> 6 (for variation 2) -> 1 4 6 4 1 (for variation 3) -> 1 1 1 1 2 1 1 3 3 1 1 4 6 4 1 Example 2: Input: r = 1, c = 1Output: (for variation 1) -> 1 (for variation 2) -> 1 (for variation 3) -> 1 In [93]: # note: # nCr = $n! = n \times (n-1) \times (n-2) \times ... \times (n-r)! = n \times (n-1) \times (n-2) \times ...$ ______ r! x (n-r)! r! x (n-r)! r! Time Complexity : O(r)Space Complexity : O(1) def nCr(n, r): numerator = denominator = 1 for i in range(1, r+1): numerator *= n denominator *= i n = 1return int(numerator / denominator) In [94]: """ Variation 1 (Optimal solution) Time Complexity : O(col_num) Space Complexity : O(1) def pascals triangle v1 (row num, col num): return nCr(row_num-1, col_num-1) In [95]: test_cases = [{'row_num': 1, 'col_num': 1}, {'row_num': 2, 'col_num': 2}, {'row_num': 5, 'col_num': 3}, {'row_num': 6, 'col_num': 4}, {'row_num': 12, 'col_num': 6}] for tc in test_cases: row_num, col_num = tc['row_num'], tc['col_num'] print(f"row_num: {row_num}\tcol_num: {row_num}\tPascal's Triangle Element: {pascals_triangle_v1(row_num, co. row num: 1 col_num: 1 Pascal's Triangle Element: 1 row num: 2 col num: 2 Pascal's Triangle Element: 1 row num: 5 col num: 5 Pascal's Triangle Element: 6 row num: 6 col num: 6 Pascal's Triangle Element: 10 col_num: 12 Pascal's Triangle Element: 462 row_num: 12 In [96]: """ Variation 2 (Brute force solution) Time Complexity : $O(r(r+1)/2) \sim O(r^2)$ Space Complexity : O(1) def pascals_triangle_v2_BFS(row_num): result = [] for col_num in range(1, row_num+1): result.append(nCr(row_num-1, col_num-1)) return result In [97]: test_cases = [{'row_num': 1}, {'row num': 2}, {'row num': 5}, {'row num': 6}, {'row_num': 12}] for tc in test cases: row num = tc['row num'] print(f"row_num: {row_num}\tPascal's Triangle Row: {pascals_triangle_v2_BFS(row_num)}") row_num: 1 Pascal's Triangle Row: [1] row_num: 2 Pascal's Triangle Row: [1, 1] row_num: 5 Pascal's Triangle Row: [1, 4, 6, 4, 1] row_num: 6 Pascal's Triangle Row: [1, 5, 10, 10, 5, 1] row num: 12 Pascal's Triangle Row: [1, 11, 55, 165, 330, 462, 462, 330, 165, 55, 11, 1] In [98]: """ Variation 2 (Optimal solution) Time Complexity : O(r)Space Complexity : O(1) def pascals_triangle_v2_OS(row_num): result = [] prev_row_num = row_num - 1 numerator = denominator = 1 for col_num in range(0, row_num): if col_num == 0 or col_num == row_num-1: result.append(1) else: numerator *= prev_row_num denominator *= col_num prev_row_num -= 1 result.append(int(numerator / denominator)) return result In [99]: test_cases = [{'row_num': 1}, {'row_num': 2}, {'row_num': 5}, {'row num': 6}, {'row num': 12}] for tc in test_cases: row_num = tc['row_num'] print(f"row_num: {row_num}\tPascal's Triangle Row: {pascals_triangle_v2_OS(row_num)}") Pascal's Triangle Row: [1] row_num: 1 Pascal's Triangle Row: [1, 1] row_num: 2 Pascal's Triangle Row: [1, 4, 6, 4, 1] row_num: 5 Pascal's Triangle Row: [1, 5, 10, 10, 5, 1] row_num: 6 Pascal's Triangle Row: [1, 11, 55, 165, 330, 462, 462, 330, 165, 55, 11, 1] row_num: 12 In [100... Variation 3 (Brute force solution) Time Complexity : $O(\sum[1,r](r(r+1)/2)) = O(r(r+1)(2r+1)/6) \sim O(r^3)$ Space Complexity : O(1) def pascals_triangle_v3_BFS(row_num): result = [] for row in range(1, row_num+1): result_row = [] for col in range(1, row+1): result_row.append(nCr(row-1, col-1)) result.append(result_row) return result In [101... test_cases = [{'row_num': 1}, {'row_num': 2}, {'row_num': 5}, {'row num': 6}, {'row_num': 12}] for tc in test_cases: row_num = tc['row_num'] pt = pascals_triangle_v3_BFS(row_num) for row in pt: print(row) print('#'*100) [1] [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] [1] [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] [1, 5, 10, 10, 5, 1] [1] [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] [1, 5, 10, 10, 5, 1] [1, 6, 15, 20, 15, 6, 1] [1, 7, 21, 35, 35, 21, 7, 1] [1, 8, 28, 56, 70, 56, 28, 8, 1] [1, 9, 36, 84, 126, 126, 84, 36, 9, 1] [1, 10, 45, 120, 210, 252, 210, 120, 45, 10, 1] [1, 11, 55, 165, 330, 462, 462, 330, 165, 55, 11, 1] 11 11 11 In [102... Variation 3 (Optimal solution) Time Complexity : $O(r^2)$ Space Complexity : O(1) def pascals_triangle_v3_OS(row_num): result = []for row in range(1, row num+1): result.append(pascals_triangle_v2_OS(row)) return result In [103... test_cases = [{'row_num': 1}, {'row_num': 2}, {'row_num': 5}, {'row_num': 6}, {'row_num': 12}] for tc in test_cases: row_num = tc['row_num'] pt = pascals_triangle_v3_OS(row_num) for row in pt: print(row) print('#'*100) *[11]* [1, 1] [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] *[11]* [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] [1, 5, 10, 10, 5, 1] *Γ11* [1, 1] [1, 2, 1] [1, 3, 3, 1] [1, 4, 6, 4, 1] [1, 5, 10, 10, 5, 1] [1, 6, 15, 20, 15, 6, 1] [1, 7, 21, 35, 35, 21, 7, 1] [1, 8, 28, 56, 70, 56, 28, 8, 1] [1, 9, 36, 84, 126, 126, 84, 36, 9, 1] [1, 10, 45, 120, 210, 252, 210, 120, 45, 10, 1] [1, 11, 55, 165, 330, 462, 462, 330, 165, 55, 11, 1]

In []: