

## Arrays

### Problem

Given an array, and an element num the task is to find the element or print -1.

Input: arr[] = 1 2 3 4 5, num = 3  
Output: 2  
Explanation: 3 is present in the 2nd index

Example 2:

```

Output: 0
Explanation: 5 is present in the 0th index

'''
Time Complexity : O(n)
Space Complexity : O(1)
'''
def linear_search(arr, num):
    n = len(arr)
    for i in range(0, n):
        if arr[i] == num:
            return i
    return -1

test_cases = [['arr',[1,2,3,4,5], 'num': 3],
               ['arr',[5,4,3,2,1], 'num': 3],
               ['arr',[5,4,3,2,1], 'num': 7]]

for to in test_cases:
    arr = to['arr']

```

## Problem Statement 2: Check if an Array is Sorted

Given an array of size  $n$ , write a program to check if the given array is sorted in (asc or desc). If the array is sorted then return True, Else return False.

**Note:** Two consecutive equal values are considered to be sorted.

**Example 1:**  
Input: N = 5, array[] = {1,2,3,4,5}  
Output: True.  
Explanation: The given array is sorted.

**Example 2:**  
Input: N = 5, array[] = {5,4,6,7,8}  
Output: False.  
Explanation: The given array is not sorted. Element 5 is not elements.

```
"""
Time Complexity : O(n)
Space Complexity : O(1)
"""
def is_sorted(arr):
    n = len(arr)

    for i in range(1, n):
        if arr[i-1] > arr[i]:
            return False

    return True

test_cases = [[{'arr': [1,2,3,4,5],
                'isarr': [4,6,5,7,8]}]]

for i in test_cases:
    arr = i['arr']
    print('arr:', arr, 'is_sorted:', is_sorted(arr))

arr = [1, 2, 3, 4, 5]
is_sorted = True
arr = [4, 6, 5, 7, 8]
is_sorted = False
```

Given an array, find the largest and the smallest elements in the array

**Example 1:**

```
Input: arr[] = {2,3,1,5,0};
Output: (0, 5)

Example2:
Input: arr[] = {8,10,5,7,9};
Output: (5, 10)
```

```
Time Complexity : O( n )
Space Complexity : O( 1 )
```

```
def find_min_max(arr):
    mini = maxi = arr[0]
    n = len(arr)
    for i in range(1, n):
        mini = min(arr[i], mini)
        maxi = max(arr[i], maxi)
    return mini, maxi

test_cases = [{'arr': [2,5,1,3,0]},
               {'arr': [8,10,5,7,9]}]

for tc in test_cases:
    arr = tc['arr']
    print('arr:', arr, '(min, max):', find_min_max(arr))

arr: [2, 5, 1, 3, 0] (min, max): (0, 5)
arr: [8, 10, 5, 7, 9] (min, max): (5, 10)
```

```

Example 1:
Input: [1,2,4,7,7,5]
Output: (2, 5)

Example 2:
Input: [1]
Output: (-1, -1)

```

---

```

"""
Brute force solution

Time Complexity : O(n log n) (For sorting the array)
Space Complexity : O(1)
"""
def find_2nd_min_maxi_SFBS(arr):
    arr.sort()

    #It is guaranteed that the array has no duplicates
    return arr[1], arr[-2]

mini = float('inf')
maxi = float('inf')
n = len(arr)

for i in range(0, n):
    if arr[i] != arr[0]:
        mini = min(arr[i], mini)

    if arr[i] != arr[-1]:
        maxi = max(arr[i], maxi)

mini = -1 if mini == float('inf') else mini
maxi = -1 if maxi == float('inf') else maxi

return mini, maxi

```

---

```

test_cases = [{"arr": [1]},
               [{"arr": [1,1,1,1,1]}],

```

```

        'arr': [1,2,4,7,5,1],
        'arr': [5,10,5,7,9,1])

print('arr:', test_cases[0]['arr'], '\n\t\t(min, max):')
print('arr:', test_cases[1]['arr'], '\n\t\t(min, max):')
print('arr:', test_cases[2]['arr'], '\n\t\t(min, max):')
print('arr:', test_cases[3]['arr'], '\n\t\t(min, max):')
print('arr:', test_cases[4]['arr'], '\n\t\t(min, max):')

arr: [1]                                (min, max): (-1, -1)
arr: [1, 1, 1, 1, 1, 1]                (min, max): (-1, -1)
arr: [1, 1, 1, 3]                      (min, max): (3, 1)
arr: [1, 2, 4, 5, 7, 7]                (min, max): (2, 5)
arr: [5, 7, 8, 9, 10]                  (min, max): (7, 9)

===
Setter solution

Time Complexity : O(2n)
Space Complexity : O(1)

def find_2nd_mini_maxi_88(arr):
    n = len(arr)

    mini = maxi = arr[0]
    for i in range(1, n):
        mini = min(arr[i], mini)
        maxi = max(arr[i], maxi)

    second_mini = float('inf')
    second_maxi = float('-inf')
    for i in range(0, n):
        if arr[i] != mini:
            second_mini = min(arr[i], second_mini)

        if arr[i] != maxi:
            second_maxi = max(arr[i], second_maxi)

    second_mini = -1 if second_mini == float('inf') else second_mini
    second_maxi = -1 if second_maxi == float('-inf') else second_maxi

    return second_mini, second_maxi

```

```

test_cases = [{ 'arr': [1],
                 {'arr': [1,1,1,1,1,1],
                  {'arr': [1,1,3],
                   {'arr': [1,2,4,7,7,5],
                    {'arr': [8,10,5,7,9]}

print('arr:', test_cases[0]['arr'], '\t\t\t(min, max)', find_2nd_mini_maxi_B8(arr = test_cases[0]['arr'])
print('arr:', test_cases[1]['arr'], '\t\t\t(min, max)', find_2nd_mini_maxi_B8(arr = test_cases[1]['arr'])
print('arr:', test_cases[2]['arr'], '\t\t\t(min, max)', find_2nd_mini_maxi_B8(arr = test_cases[2]['arr'])
print('arr:', test_cases[3]['arr'], '\t\t\t(min, max)', find_2nd_mini_maxi_B8(arr = test_cases[3]['arr'])
print('arr:', test_cases[4]['arr'], '\t\t\t(min, max)', find_2nd_mini_maxi_B8(arr = test_cases[4]['arr'])

arr: [1] (min, max): (-1, -1)
arr: [1, 1, 1, 1, 1, 1] (min, max): (-1, -1)
arr: [1, 1, 3] (min, max): (3, 1)
arr: [1, 2, 4, 7, 7, 5] (min, max): (3, 5)
arr: [8, 10, 5, 7, 9] (min, max): (7, 9)

new
Optimal solution

Time Complexity : O (n )
Space Complexity : O ( 1 )

```

```
def find_2nd_mini_maxi_OS(arr):  
    n = len(arr)  
  
    mini, second_mini = arr[0], float('inf')
```

```
for i in range(1, n):
    #Finds the second smallest element
    if arr[i] < mini:
        second mini = mini
        mini = arr[i]
    elif (i > 1 and arr[i] < second mini):
```

```

        second_min1 = arr[i]

        #Finds the second largest element
        if arr[i] > maxi:
            second_maxi = maxi
            maxi = arr[i]
        elif arr[i] < maxi and arr[i] > second_maxi:
            second_maxi = arr[i]

    second_min1 = -1 if second_min1 == float('inf') else second_min1
    second_maxi = -1 if second_maxi == float('-inf') else second_maxi

    return second_min1, second_maxi

: test_cases = [['arr': [1]],
                 {'arr': [1,1,1,1,1,1]},
                 {'arr': [1,1,3]},
                 {'arr': [1,2,4,7,7,5]},
                 {'arr': [8,10,5,7,9]}]

print('arr1:', test_cases[0]['arr'], '\t\t\t(min, maxi):', find_2nd_min_maxi_08(arr = test_cases[0]['arr'])
print('arr1:', test_cases[1]['arr'], '\t\t\t(min, maxi):', find_2nd_min_maxi_08(arr = test_cases[1]['arr'])

```

```
print('arr:', test_cases[3]['arr'], '\n(min, max):', find_2nd_mini_maxi_08(arr = test_cases[3]['arr'])
print('arr:', test_cases[4]['arr'], '\n(min, max):', find_2nd_mini_maxi_08(arr = test_cases[4]['arr'])

arr: [[], (min, maxi): (-1, -1)
arr: [[1, 1, 1, 1, 1, 1], (min, maxi): (-1, -1)
arr: [[1, 1, 3], (min, maxi): (3, 1)
arr: [[1, 2, 4, 7, 7, 5], (min, maxi): (2, 5)
arr: [[7, 10, 5, 7, 9], (min, maxi): (7, 9)
```

```
Time Complexity : O(n)
Space Complexity : O(1)
"""
def inplace_reverse(arr):
    i = 0
    j = len(arr) - 1

    while i < j:
        arr[i], arr[j] = arr[j], arr[i]
        i += 1
        j -= 1

test_cases = [['arr': [1,2,4,7,7,5]],
               {'arr': [1]}]

for tc in test_cases:
    arr = tc['arr']
    inplace_reverse(arr)
    print("Reversed arr:", arr)

Reversed arr: [5, 7, 7, 4, 2, 1]
Reversed arr: [1]
```

### Problem Statement 6: Move all Zeros to the end of the array

You are given an array of integers, your task is to move all the zeros in the array to the end of the array and move non-negative integers to the front **by maintaining their order**.

**Example 1:**  
Input: 1,0,2,3,0,4,0,1  
Output: 1,2,3,4,1,0,0,0  
Explanation: All the zeros are moved to the end and non-negative integers are moved to front by maintaining order

**Example 2:**  
Input: 1,2,0,1,0,4,0  
Output: 1,2,1,4,0,0,0  
Explanation: All the zeros are moved to the end and non-negative integers are moved to front by maintaining order

```

:
:
:
Time Complexity : O(n)
Space Complexity :
```

```
def move_zeroes(arr):
    n = len(arr)

    for i in range(0, n):
        if arr[i] == 0:
            j = i
            break

    for i in range(j+1, n):
        if arr[i] != 0:
            arr[i], arr[j] = arr[j], arr[i]
            j += 1

: test_cases = [{'arr': [1,0,2,3,0,4,0,1]},
                 {'arr': [1,2,0,1,0,4,0,0]}]

for i in test_cases:
    arr = test_cases[i]['arr']
    move_zeroes(arr)
    print("New arr:", arr)

New arr: [1, 2, 3, 4, 1, 0, 0, 0]
New arr: [1, 2, 1, 4, 0, 0, 0, 0]
```

### Problem Statement 7: Remove duplicates in-place from Sorted Array

Given an integer array sorted in **ascending order**, remove the duplicates in place such that each unique element appears only once. **The relative order of the elements should be kept the same.**

If there are  $k$  elements after removing the duplicates, then the first  $k$  elements of the array should hold the final result. It does not matter what you leave beyond the first  $k$  elements.

**Note:** Return  $k$  after placing the final result in the first  $k$  slots of the array.

**Example 1:**  
Input: arr [1,1,2,2,2,3,3]  
Output: arr [1,2,3,3,3,3,3]  
Explanation: Total number of unique elements are 3, i.e [1,2,3] and Therefore return 3 after assigning [1,2,3] in the beginning of the array.

**Example 2:**  
Input: arr [1,1,1,2,2,2,3,3,3,4,4]

```
def remove_duplicates(arr):
    n = len(arr)
    j = 0
    for i in range(0, n):
        if arr[i] != arr[j]:
            j += 1
            arr[i], arr[j] = arr[j], arr[i]
    return j+1

test_cases = [{'arr': [1,1,2,2,2,3,3]},
               {'arr': [1,1,1,2,2,2,3,3,3,4,4]}]

arr = test_cases[0]['arr']
print(f"arr: {arr}\tUnique Elements: (remove_duplicates(arr))\tNew arr: {arr}")
arr = test_cases[1]['arr']
print(f"arr: {arr}\tUnique Elements: (remove_duplicates(arr))\tNew arr: {arr}")
```

### Problem Statement 8: Rotate array by K elements

Given an array of integers, rotating array of elements by k elements either left or right.

**Example 1:**  
Input: arr = [1,2,3,4,5,6,7], k = 2, right  
Output: arr = [6,7,1,2,3,4,5]  
Explanation: array is rotated to right by 2 position.

**Example 2:**  
Input: arr = [3,7,8,9,10,11], k = 3, left  
Output: arr = [9,10,11,3,7,8]  
Explanation: Array is rotated to right by 3 position.

```
"""
Better solution
Time Complexity : O(n)
```

```

def rotate_90(arr, k, direction):
    n = len(arr)
    k = k % n

    if direction == 'LEFT':
        tmp_arr = arr[:k]
        for i in range(k, n):
            arr[i - k] = arr[i]
        for i in range(n - k, n):
            arr[i] = tmp_arr[i - k]
    else:
        tmp_arr = arr[n-k:]
        for i in range(n - k - 1, -1, -1):
            arr[i + k] = arr[i]
        for i in range(0, k):
            arr[i] = tmp_arr[i]

# test cases = [{"arr": [1,2,3,4,5,6,7], 'k': 2, 'direction': 'RIGHT'},

```

```
for to in test_cases:
    print("**** tc:['{arr}']\t\tk: {to['k']}\tdirection: [{to['direction']}]\t\t", end='')
    rotate_BS(arr=tc['arr'], k=tc['k'], direction=tc['direction'])
    print("\nNew arr: [{arr}]")

arr: [1, 2, 3, 4, 5, 6, 7]          k: 2       direction: RIGHT      New arr: [6, 7, 1, 2, 3, 4, 5]
arr: [3, 9, 8, 9, 10, 11]         k: 3       direction: LEFT       New arr: [9, 10, 11, 3, 7, 8]
```

====

#### Optimal solution

Time Complexity : O(2n)  
Space Complexity : O(1)

=====

```
def reverse_inplace(arr, i, j):
    while i < j:
        arr[i], arr[j] = arr[j], arr[i]
        i += 1
        j -= 1

def rotate_08(arr, k, direction):
```

```

k = k ^ n

if direction == 'LEFT':
    reverse_inplace(arr, 0, k-1)
    reverse_inplace(arr, k, n-1)
    reverse_inplace(arr, 0, n-1)
else:
    reverse_inplace(arr, 0, n-k-1)
    reverse_inplace(arr, n-k, n-1)
    reverse_inplace(arr, 0, n-1)

test_cases = [['arr': [1,2,3,4,5,6,7], 'k': 2, 'direction': 'RIGHT'],
               ['arr': [3,7,8,9,10,11], 'k': 3, 'direction': 'LEFT']]

for i in test_cases:
    print(f"arr: {tc['arr']} | k: {tc['k']} | direction: {tc['direction']} | tc: {i}, end="")
    rotate_O8(arr=tc['arr'], k=tc['k'], direction=tc['direction'])
    print(f"New arr: {tc['arr']}")

arr: [1, 2, 3, 4, 5, 6, 7]      k: 2      direction: RIGHT      New arr: [6, 7, 1, 2, 3, 4, 5]
arr: [3, 7, 8, 9, 10, 11]     k: 3      direction: LEFT       New arr: [9, 10, 11, 3, 7, 8]

```

Given an array that contains only 1's and 0's, return the count of maximum consecutive 1's in the array.

**Example 1:**  
Input: arr = [1, 1, 0, 1, 1, 1]  
Output: 3  
Explanation: There are 2 consecutive 1's and 3 consecutive 1's in the array out of which maximum is 3.

**Example 2:**  
Input: arr = [1, 0, 1, 1, 0, 1]  
Output: 2  
Explanation: There are 2 consecutive 1's in the array.

```
"""
Time Complexity : O(n)
Space Complexity : O(1)
"""
def find_max_consecutive_ones(arr):
    n = len(arr)
    one_count = 0
```

```

for i in range(0, n):
    if arr[i] == 1:
        one_count += 1
    else:
        one_count = 0

max_one_count = max(one_count, max_one_count)

return max_one_count

```

```

: test_cases = [{'arr': [1,1,0,1,1,1]},
:               {'arr': [1,0,1,1,0,1]}]

for tc in test_cases:
    print(tc['arr'], "Max consecutive 1's:", find_max_consecutive_ones(arr = tc['arr']))

arr: [1, 1, 0, 1, 1, 1] Max consecutive 1's: 3
arr: [1, 0, 1, 1, 0, 1] Max consecutive 1's: 2

```

**Problem Statement 10:** Find the number that appears once, while others appear twice

```

Given a non-empty array of integers, every element appears twice except for one. Find that single one.

Example 1:
Input Format: arr = [2,2,1]
Result: 1
Explanation: In this array, only the element 1 appear once and so it is the answer.

Example 2:
Input Format: arr = [4,1,2,1,2]
Result: 4
Explanation: In this array, only element 4 appear once and the other elements appear twice.

```

---

```

"""
Better solution

Time Complexity : O(n + n/2 + 1) ~ O(n)
Space Complexity : O(n/2 + 1) ~ O(n)
"""
def get_single_element_B0(arr):
    n = len(arr)
    freq_map = dict()

```

```

        freq_map[arr[i]] = freq_map.get(arr[i], 0) + 1

    for num, freq in freq_map.items():
        if freq == 1:
            return num

    return -1

test_cases = [{"arr": [2,2,1]},
               {"arr": [4,1,2,1,2]}]

print('arr:', test_cases[0]['arr'], "\t\tNum that appears once:", get_single_element_BS(arr = test_cases[0]['arr'], test_cases[0]['arr']), "\t\tNum that appears once:", get_single_element_BS(arr = test_cases[1]['arr'], test_cases[1]['arr']))

arr: [2, 2, 1]           Num that appears once: 1
arr: [4, 1, 2, 1, 2]    Num that appears once: 4

===
Optimal solution

Note:
XOR Property 1: a ^ a = 0

```

```

Time Complexity : O(n)
Space Complexity : O(1)
"""
def get_single_element_Q3(arr):
    n = len(arr)
    result = 0

    for i in range(0, n):
        result = result ^ arr[i]

    return result

:
test_cases = [{'arr': [2,2,1]},
               {'arr': [4,1,2,1,2]}]

print('arr:', test_cases[0]['arr'], "\tNum that appears once:", get_single_element_Q3(arr = test_cases[0]['arr']))
print('arr:', test_cases[1]['arr'], "\tNum that appears once:", get_single_element_Q3(arr = test_cases[1]['arr']))

arr: [2, 2, 1]          Num that appears once: 1
arr: [4, 1, 2, 1, 2]   Num that appears once: 4

```

### Problem Statement 11: Find the missing number in an array

Given an integer N and an array of size N-1 containing N-1 numbers between 1 to N. Find the number (between 1 to N), that is not present in the given array.

**Example 1:**  
Input Format: N = 5, arr = [1,2,4,5]  
Result: 3  
Explanation: In the given array, number 3 is missing. So, 3 is the answer.

**Example 2:**  
Input Format: N = 3, arr = [1,3]  
Result: 2  
Explanation: In the given array, number 2 is missing. So, 2 is the answer.

```
"""
Time Complexity : O(n) [For summing the array]
Space Complexity : O(1)
"""
def missing_number(arr, n):
    return (n*(n+1)/2) - sum(arr)
```

```

test_cases = [{'arr': [1,4,5], 'n': 5},
               {'arr': [1,3], 'n': 3}]

arr = test_cases[0]['arr']
n = test_cases[0]['n']
print('arr:', arr, "\tn:", n, "\tMissing num:", missing_number(arr, n))

arr = test_cases[1]['arr']
n = test_cases[1]['n']
print('arr:', arr, "\tn:", n, "\tMissing num:", missing_number(arr, n))

arr: [1, 2, 4, 5]           n: 5   Missing num: 3
arr: [1, 3]                n: 3   Missing num: 2

"""
Note:
    XOR Property 1:  $a \oplus a = 0$ 
    XOR Property 2:  $0 \oplus a = a$ 

Time Complexity : O(n)
Space Complexity : O(1)
"""
def missing_number(arr, n):

```

```
xor2 = 0

for i in range(0, n-1):
    xor1 ^= arr[i]
    xor2 ^= i+1

xor2 ^= n
return xor1 ^ xor2
```

```
test_cases = [{'arr': [1,2,4,5], 'n': 5},
               {'arr': [1,3], 'n': 3}]

arr = test_cases[0]['arr']
n = test_cases[0]['n']
print('arr:', arr, "\tn:", n, "\tMissing num:", missing_number(arr, n))

arr = test_cases[1]['arr']
n = test_cases[1]['n']
print('arr:', arr, "\tn:", n, "\tMissing num:", missing_number(arr, n))

arr: [1, 2, 4, 5]      n: 5   Missing num: 3
arr: [1, 3]           n: 3   Missing num: 2
```

## Problem Statement 12: Union of Two Sorted Arrays

Given two sorted arrays, arr1, and arr2 of size n and m. Find the union of two sorted arrays.

**Note:** Elements in the union should be in ascending order.

**Example 1:**  
Input: arr1 = [1,2,3,4,5], arr2 = [2,3,4,4,5]  
Output: [1,2,3,4,5]

**Example 2:**  
Input: arr1 = [1,2,3,4,5,6,7,8,9,10], arr2 = [2,3,4,4,5,11,12]  
Output: [1,2,3,4,5,6,7,8,9,10,11,12]

```
'''
Setter solution

Time Complexity : O(2(n+m))
Space Complexity : O(n+m)
'''
```

[illegible]

```

12]
'''
Optimal solution

Time Complexity : O(n*m)
Space Complexity : O(1)
'''
def find_union_CS(arr1, arr2):
    i = j = 0
    n, m = len(arr1), len(arr2)
    result = []

    while i < n and j < m:
        if arr1[i] <= arr2[j]:
            if len(result) == 0 or result[-1] != arr1[i]:
                result.append(arr1[i])
            i += 1
        else:
            if len(result) == 0 or result[-1] != arr2[j]:
                result.append(arr2[j])
            j += 1

    while i < n:

```

```

1 arr1 = arr1[-1] == arr1[-1]
2     result.append(arr1[-1])
3     i += 1
4
5 while j < m:
6     if len(result) == 0 or result[-1] != arr2[j]:
7         result.append(arr2[j])
8     j += 1
9
10 return result

```

```

: test_cases = [{"arr1": [1,2,3,4,5], "arr2": [2,3,4,5,1],
:               {"arr1": [1,2,3,4,5,6,7,8,9,10], "arr2": [2,3,4,4,5,11,12]}]

```

```

arr1 = test_cases[0]["arr1"]
arr2 = test_cases[0]["arr2"]
print("arr1:", arr1, "\t\t\t arr2:", arr2, "\t\t Union:", find_union_OS(arr1, arr2))

arr1 = test_cases[1]["arr1"]
arr2 = test_cases[1]["arr2"]
print("arr1:", arr1, "\t\t\t arr2:", arr2, "\t\t Union:", find_union_OS(arr1, arr2))

```

```

arr1: [1, 2, 3, 4, 5] arr2: [2, 3, 4, 4, 5] Union: [1, 2, 3, 4, 5]
arr1: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] arr2: [1, 2, 3, 4, 5, 11, 12] Union: [1, 2, 3, 4, 5, 6, 7, 8, 9, 10,

```

### Problem Statement 13: Longest Subarray with sum K

Given an array and a sum k, we need to print the length of the longest subarray that sums to k.

**Example 1:**  
Input: arr = [2,3,5], k = 5  
Result: 2  
Explanation: The longest subarray with sum 5 is [2, 3]. And its length is 2.

**Example 2:**  
Input: arr = [2,3,5,1,9], k = 10  
Result: 3  
Explanation: The longest subarray with sum 10 is [2, 3, 5]. And its length is 3.

**Example 3:**  
Input: arr = [-1, 1, 1], k = 1  
Result: 3  
Explanation: The longest subarray with sum 1 is [-1, 1, 1]. And its length is 3.

```

"""
Brute force solution

Time Complexity : O(n^2)
Space Complexity : O(1)
"""
def find_longest_subarr_len_BFS(arr, k):
    n = len(arr)
    longest_subarr_len = float('-inf')

    for i in range(0, n):
        running_sum = 0

        for j in range(i, n):
            running_sum += arr[j]

            if running_sum == k:
                length = j - i + 1
                longest_subarr_len = max(length, longest_subarr_len)

    return longest_subarr_len

# Test cases
test_cases = [{"k": 5, "arr": [2,3,5]}]

```



```
In [39]: """
Better solution

Note:
    If arr has zero & +ve numbers, this is the better solution.
    If arr has zero, +ve & -ve numbers, this is the optimal solution.

Time Complexity : O( n )
Space Complexity : O( 1 )
"""
def find_longest_subarr_len_BS(arr, k):
    n = len(arr)
    longest_subarr_len = float("-inf")
    running_sum = 0
    running_sum_map = dict()

    for i in range(0, n):
        running_sum += arr[i]

        if running_sum == k:
            length = i + 1
            longest_subarr_len = max(length, longest_subarr_len)

        remainder = running_sum - k
        if remainder in running_sum_map:
            length = i - running_sum_map[remainder]
            longest_subarr_len = max(length, longest_subarr_len)

        if running_sum not in running_sum_map:
            running_sum_map[running_sum] = i

    return longest_subarr_len

In [40]: test_cases = [{'k': 3, 'arr': [1,2,-3]},
                        {'k': 5, 'arr': [2,3,5]},
                        {'k': 10, 'arr': [2,3,5,1,9]},
                        {'k': 0, 'arr': [-1,1,1]},
                        {'k': 3, 'arr': [1,2,3,1,1,1,4,2,3]},
                        {'k': 7, 'arr': [1,2,-3,1,0,-4,1,4,0,1,0,4,3]},
                        {'k': 0, 'arr': [-3,0,1,1,-1,0]}]

for to in test_cases:
    arr = to['arr']
    k = to['k']
    print(find_longest_subarr_len_BS(arr, k))

2
2
3
2
3
12
6
```

```
In [41]: """
Optimal solution

Note:
    If arr has zero & +ve numbers, this is the optimal solution.

Time Complexity : O( 2n )
Space Complexity : O( 1 )
"""
def find_longest_subarr_len_OS(arr, k):
    n = len(arr)
    longest_subarr_len = float("-inf")
    flexi_sum = arr[0]
    i = j = 0

    while i < n & j <= j and flexi_sum > k:
        flexi_sum -= arr[i]
        i += 1

    if flexi_sum == k:
        length = j - i + 1
        longest_subarr_len = max(length, longest_subarr_len)
        j += 1

    if j < n:
        flexi_sum += arr[j]

    return longest_subarr_len

In [42]: test_cases = [{'k': 3, 'arr': [-2,0,1,1,-1,-1,0]},
                        {'k': 3, 'arr': [1,2,3,1,1,1,4,2,3]}]

for to in test_cases:
    arr = to['arr']
    k = to['k']
    print(find_longest_subarr_len_OS(arr, k))

3
```

## Problem Statement 14: Count Subarray sum Equals K

Given an array of integers and an integer k, return the total number of subarrays whose sum equals k.

**Note:** A subarray is a contiguous non-empty sequence of elements within an array.

**Example 1:**  
Input: arr = [3, 1, 2, 4], k = 6  
Output: 2  
Explanation: The subarrays that sum up to 6 are [3, 1, 2] and [2, 4].

**Example 2:**  
Input: arr = [1, 2, 3], k = 3  
Output: 2  
Explanation: The subarrays that sum up to 3 are [1, 2], and [3].

```
In [43]: """
Brute force solution

Time Complexity : O( n^2 )
Space Complexity : O( 1 )
"""
def find_all_subarr_with_given_sum_BFS(arr, k):
    n = len(arr)
    subarr_counter = 0

    for i in range(0, n):
        rsum = 0

        for j in range(i, n):
            rsum += arr[j]

            if rsum == k:
                subarr_counter += 1

    return subarr_counter

In [44]: test_cases = [{'k': 3, 'arr': [1,2,3,-3,1,1,4,2,-3]},
                        {'k': 5, 'arr': [2,3,5]},
                        {'k': 10, 'arr': [2,3,5,1,9]},
                        {'k': 1, 'arr': [-1,1,1]},
                        {'k': 3, 'arr': [1,2,3,1,1,1,4,2,3]},
                        {'k': 0, 'arr': [1,2,-3,1,0,-4,1,4,0,1]}]

for to in test_cases:
    arr = to['arr']
    k = to['k']
    print(find_all_subarr_with_given_sum_BFS(arr, k))

8
2
2
3
5
6

In [45]: """
Optimal solution

Note:
    If arr has zero, +ve & -ve numbers, this is the optimal solution.

Time Complexity : O( n )
Space Complexity : O( n )
"""
def find_all_subarr_with_given_sum_OS(arr, k):
    n = len(arr)
    rsum = 0
    rsum_map = {0:1}
    subarr_counter = 0

    for i in range(n):
        rsum += arr[i]

        rem = rsum - k

        subarr_counter += rsum_map.get(rem, 0)
        rsum_map[rsum] = rsum_map.get(rsum, 0) + 1

    return subarr_counter

In [46]: test_cases = [{'k': 3, 'arr': [1,2,3,-3,1,1,4,2,-3]},
                        {'k': 5, 'arr': [2,3,5]},
                        {'k': 10, 'arr': [2,3,5,1,9]},
                        {'k': 1, 'arr': [-1,1,1]},
                        {'k': 3, 'arr': [1,2,3,1,1,1,4,2,3]},
                        {'k': 0, 'arr': [1,2,-3,1,0,-4,1,4,0,1]}]

for to in test_cases:
    arr = to['arr']
    k = to['k']
    print(find_all_subarr_with_given_sum_OS(arr, k))

8
2
2
3
5
6
```

## Problem Statement 15: Maximum Subarray Sum in an Array (Kadane's Algorithm)

Given an integer array arr, find the contiguous subarray (containing at least one number) which has the largest sum and returns its sum and prints the subarray.

**Example 1:**  
Input: arr = [-2,-1,-3,4,-1,2,1,-5,4]  
Output: 6  
Explanation: [4,-1,2,1] has the largest sum = 6.

**Example 2:**  
Input: arr = [1]  
Output: 1  
Explanation: Array has only one element and which is giving positive sum of 1.

```
In [47]: """
Brute force solution

Time Complexity : O( n^2 )
Space Complexity : O( 1 )
"""
def find_max_subarr_sum_BFS(arr):
    n = len(arr)
    max_subarr_sum = 0

    for i in range(0, n):
        rsum = 0

        for j in range(i, n):
            rsum += arr[j]

            max_subarr_sum = max(rsum, max_subarr_sum)

    return max_subarr_sum

In [48]: test_cases = [{'arr': [-2,-1,-3,4,-1,2,1,-5,4]},
                        {'arr': [-2,-3,4,-1,-2,1,5,-3]},
                        {'arr': [1]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, '\tMax sub arr sum:', find_max_subarr_sum_BFS(arr))

arr: [-2, -1, -3, 4, -1, 2, 1, -5, 4]    Max sub arr sum: 6
arr: [-2, -3, 4, -1, -2, 1, 5, -3]    Max sub arr sum: 7
arr: [1]                               Max sub arr sum: 1

In [49]: """
Optimal solution (Kadane's Algorithm)

Time Complexity : O( n )
Space Complexity : O( 1 )
"""
def find_max_subarr_sum_OS(arr):
    n = len(arr)
    max_subarr_sum = arr[0]

    for i in range(1, n):
        curr_sum = max(arr[i], curr_sum + arr[i])

        max_subarr_sum = max(curr_sum, max_subarr_sum)

    return max_subarr_sum

In [50]: test_cases = [{'arr': [-2,-1,-3,4,-1,2,1,-5,4]},
                        {'arr': [-2,-3,4,-1,-2,1,5,-3]},
                        {'arr': [1]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, '\tMax sub arr:', find_max_subarr_sum_OS(arr))

arr: [-2, -1, -3, 4, -1, 2, 1, -5, 4]    Max sub arr sum: 6
arr: [-2, -3, 4, -1, -2, 1, 5, -3]    Max sub arr: 7
arr: [1]                               Max sub arr: 1

In [51]: """
Optimal solution (Kadane's Algorithm)

Time Complexity : O( n )
Space Complexity : O( 1 )
"""
def find_max_subarr_sum_OS2(arr):
    n = len(arr)
    curr_sum = arr[0]
    curr_idx = 0
    max_subarr_sum = curr_idx
    max_subarr_idx = max_subarr_idx = 0

    for i in range(1, n):
        if arr[i] > curr_sum + arr[i]:
            curr_sum = arr[i]
            curr_idx = i
        else:
            curr_sum = curr_sum + arr[i]
            curr_idx = i

        if curr_sum > max_subarr_sum:
            max_subarr_sum = curr_sum
            max_subarr_idx = curr_idx

    return max_subarr_sum, arr[max_subarr_idx : max_subarr_idx + 1]

In [52]: test_cases = [{'arr': [-2,-1,-3,4,-1,2,1,-5,4]},
                        {'arr': [-2,-3,4,-1,-2,1,5,-3]},
                        {'arr': [1]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, '\tMax sub arr:', find_max_subarr_sum_OS2(arr))

arr: [-2, -1, -3, 4, -1, 2, 1, -5, 4]    Max sub arr: 6 [-2, -1, 2, 1]
arr: [-2, -3, 4, -1, -2, 1, 5, -3]    Max sub arr: 7 [-2, -3, 4, -1, 2, 1, 5]
arr: [1]                               Max sub arr: 1 [1]
```

## Problem Statement 16: Two Sum - Check if a pair with given sum exists in Array

Given an array of integers and an integer target.

- 1st variant: Return YES if there exist two numbers such that their sum is equal to the target. Otherwise, return NO.
- 2nd variant: Return indices of the two numbers such that their sum is equal to the target. Otherwise, we will return [-1, -1].

**Note:** You are not allowed to use the same element twice. Example: If the target is equal to 6 and num[] = 3, then num[] + num[] = target is not a solution. </p>

**Example 1:**  
Input: arr = [2,6,5,8,11], target = 14  
Output: YES (for 1st variant)  
[1, 3] (for 2nd variant)

**Example 2:**  
Input: arr = [2,6,5,8,11], target = 15  
Result: NO (for 1st variant)  
[-1, -1] (for 2nd variant)

```
In [53]: """
Better solution

Time Complexity : O( n )
Space Complexity : O( n )
"""
def two_sum_BS(arr, target):
    n = len(arr)
    hashmap = dict()

    for i in range(0, n):
        rem = target - arr[i]

        if rem in hashmap:
            return hashmap[rem], i

        hashmap[arr[i]] = i

    return -1, -1

In [54]: test_cases = [{'arr': [2,6,5,8,11], 'target': 14},
                        {'arr': [2,6,5,8,11], 'target': 15}]

for to in test_cases:
    arr = to['arr']
    target = to['target']
    print('arr:', arr, 'target:', target, '2 Sum:', two_sum_BS(arr, target))

arr: [2, 6, 5, 8, 11] target: 14 2 Sum: (1, 3)
arr: [2, 6, 5, 8, 11] target: 15 2 Sum: (-1, -1)

In [55]: """
Optimal (space) solution

Time Complexity : O( n log n )
Space Complexity : O( 1 )
"""
def two_sum_OS(arr, target):
    arr = sorted(enumerate(arr), key = lambda x: x[1])
    n = len(arr)
    ans = []

    while i < j:
        if arr[i][1] + arr[j][1] == target:
            return arr[i][0], arr[j][0]
        elif arr[i][1] + arr[j][1] < target:
            i += 1
        else:
            j -= 1

    return (-1, -1)

In [56]: test_cases = [{'arr': [2,6,5,8,11], 'target': 14},
                        {'arr': [2,6,5,8,11], 'target': 15}]

for to in test_cases:
    arr = to['arr']
    target = to['target']
    print('arr:', arr, 'target:', target, '2 Sum:', two_sum_OS(arr, target))

arr: [2, 6, 5, 8, 11] target: 14 2 Sum: (1, 3)
arr: [2, 6, 5, 8, 11] target: 15 2 Sum: (-1, -1)
```

## Problem Statement 17: 3 Sum - Find triplets that add up to a zero

Given an integer array nums, return all the triplets (nums[i], nums[j], nums[k]) such that i!=j, i!=k, and j!=k, and nums[i] + nums[j] + nums[k] == 0.

**Note:** The solution set must not contain duplicate triplets.

**Example 1:**  
Input: nums = [-1,0,1,2,-1,-4]  
Output: [[-1,0,1],[-1,0,1]]

**Example 2:**  
Input: nums = [-1,0,1,0]  
Output: [[-1,0,1]]

```
In [57]: """
Optimal (space) solution

Time Complexity : O( n log n ) + O( n^2 )
Space Complexity : O( 1 )
"""
def three_sum(arr):
    n = len(arr)
    ans = []
    arr.sort()

    for i in range(n):
        if i != 0 and arr[i-1] == arr[i]:
            continue

        j = i+1
        k = n-1

        while j < k:
            total_sum = arr[i] + arr[j] + arr[k]

            if total_sum < 0:
                j += 1
            elif total_sum > 0:
                k -= 1
            else:
                ans.append( (arr[i], arr[j], arr[k]) )
                k -= 1

                while j < k and arr[j] == arr[j+1]:
                    j += 1

                while k < k and arr[k-1] == arr[k]:
                    k -= 1

        return ans

In [58]: test_cases = [{'arr': [-1,0,1,2,-1,-4]},
                        {'arr': [-1,0,1,0]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, '3 Sum:', three_sum(arr))

arr: [-1, 0, 0, 1, -1, 0, 1, 2] 3 Sum: [-1, -1, 2], [-2, 0, 2], [-1, 0, 0, 1]
arr: [-1, 0, 0, 1] 3 Sum: [-1, 0, 1]
```

## Problem Statement 18: 4 Sum - Find quads that add up to a target value

Given an array of N integers, your task is to find unique quads that add up to give a target value. In short, you need to return an array of all the unique quadruplets [arr[a], arr[b], arr[c], arr[d]] such that their sum is equal to a given target.

**Note:** The solution set must not contain duplicate quadruplets.

**Example 1:**  
Input: arr = [-1,0,-1,0,-2,2]  
Output: [[-2,-1,0,1],[2,0,0,2],[-1,0,0,1]]

**Example 2:**  
Input: arr = [4,3,3,4,4,2,1,2,1,1], target = 9  
Output: [[1,1,3,4],[1,2,2,4],[1,2,3,3]]

```
In [59]: """
Optimal (space) solution

Time Complexity : O( n log n ) + O( n^3 )
Space Complexity : O( 1 )
"""
def four_sum(arr, target):
    arr.sort()
    n = len(arr)
    ans = []

    for i in range(0, n):
        if i != 0 and arr[i-1] == arr[i]:
            continue

        for j in range(i+1, n):
            if j != i+1 and arr[j-1] == arr[j]:
                continue

            k = j+1
            l = n-1

            while k < l:
                target_sum = arr[i] + arr[j] + arr[k] + arr[l]

                if target_sum < target:
                    k += 1
                elif target_sum > target:
                    l -= 1
                else:
                    ans.append( (arr[i], arr[j], arr[k], arr[l]) )
                    k += 1
                    while k < l and arr[k] == arr[k+1]:
                        k += 1

                    while k < l and arr[l] == arr[l-1]:
                        l -= 1

        return ans

In [60]: test_cases = [{'arr': [1,0,-1,0,-2,2], 'target': 0},
                        {'arr': [4,3,3,4,4,2,1,2,1,1], 'target': 9}]

for to in test_cases:
    arr = to['arr']
    target = to['target']
    print('arr:', arr, '4 Sum:', four_sum(arr, target))

arr: [-2, -1, 0, 0, 1, 2] 4 Sum: [-2, -1, 1, 2], [-2, 0, 0, 2], [-1, 0, 0, 1]
arr: [1, 1, 1, 2, 2, 3, 3, 3, 4, 4] 4 Sum: [1, 1, 3, 4], [1, 2, 2, 4], [1, 2, 3, 3]
```

## Problem Statement 19: Buy And Sell Stocks

You are given an array of prices where prices[i] is the price of a given stock on an ith day. You want to maximize your profit by choosing a single day to buy one stock and choosing a different day in the future to sell that stock. Return the maximum profit you can achieve from this transaction. If you cannot achieve any profit, return 0.

**Example 1:**  
Input: prices = [7,1,5,3,6,4]  
Output: 5  
Explanation: Buy on day 2 (price = 1) and sell on day 5 (price = 6), profit = 6-1 = 5.  
Note: That buying on day 2 and selling on day 1 is not allowed because you must buy before you sell.

**Example 2:**  
Input: prices = [7,6,4,3,1]  
Output: 0  
Explanation: In this case, no transactions are done and the max profit = 0.

```
In [61]: """
Time Complexity : O( n )
Space Complexity : O( 1 )
"""
def find_max_profit(arr):
    n = len(arr)
    min_price = float("-inf")
    max_profit = float("-inf")

    for i in range(0, n):
        min_price = min(arr[i], min_price)
        max_profit = max(arr[i] - min_price, max_profit)

    return max_profit

In [62]: test_cases = [{'arr': [7,1,5,3,6,4]},
                        {'arr': [7,6,4,3,1]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, 'Max profit:', find_max_profit(arr))

arr: [7, 1, 5, 3, 6, 4] Max profit: 5
arr: [7, 6, 4, 3, 1] Max profit: 0
```

## Problem Statement 20: Leaders in an Array

Given an array, print all the elements which are leaders. A leader is an element that is greater than all of the elements on its right side in the array.

**Example 1:**  
Input: arr = [4, 7, 1, 0]  
Output: [7, 1, 0]  
Explanation: Rightmost element is always a leader. 7 and 1 are greater than the elements in their right side.

**Example 2:**  
Input: arr = [10, 22, 12, 3, 0, 6]  
Output: [22, 12, 6]  
Explanation: 6 is a leader. In addition to that, 12 is greater than all the elements in its right side [3, 0, 6], also 22 is greater than 12, 3, 0, 6.

```
In [63]: """
Time Complexity : O( 2n )
Space Complexity : O( 1 )
"""
def find_leaders(arr):
    maxi = float("-inf")
    leaders = []

    for i in range(n-1, -1, -1):
        if arr[i] > maxi:
            leaders.append(arr[i])
            maxi = arr[i]

    inplace_reverse(leaders)

    return leaders

In [64]: test_cases = [{'arr': [4, 7, 1, 0]},
                        {'arr': [10, 22, 12, 3, 0, 6]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, 'Leaders:', find_leaders(arr))

arr: [4, 7, 1, 0] Leaders: [7, 1, 0]
arr: [10, 22, 12, 3, 0, 6] Leaders: [22, 12, 6]
```

## Problem Statement 21: Find the Majority Element (Moore's Voting Algorithm)

Given an array of N integers, write a program to return the element(s) that occurs more than N/2 times (majority element) in the given array. Return -1 if no such element exists in the array.

**Example 1:**  
Input: arr = [3,2,3]  
Output: 3

**Example 2:**  
Input: arr = [2,2,1,1,2,2]  
Output: 2

**Example 3:**  
Input: arr = [4,4,2,4,3,4,3,2,4]  
Output: 4

```
In [65]: """
Brute force solution

Time Complexity : O( n log n )
Space Complexity : O( 1 )
"""
def find_majority_element_BFS(arr):
    arr.sort()

    n = len(arr)
    candidate = arr[n//2]
    counter = 0

    for i in range(0, n):
        if arr[i] == candidate:
            counter += 1
        else:
            counter -= 1

    return candidate if counter > n//2 else -1

In [66]: test_cases = [{'arr': [3,2,3]},
                        {'arr': [2,2,1,1,2,2]},
                        {'arr': [4,4,2,4,3,4,3,2,4]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, 'Majority element:', find_majority_element_BFS(arr))

arr: [2, 3, 3] Majority element: 3
arr: [1, 1, 1, 2, 2, 2, 2] Majority element: 2
arr: [2, 2, 3, 3, 4, 4, 4, 4, 4] Majority element: 4

In [67]: """
Better solution

Time Complexity : O( 2n )
Space Complexity : O( n )
"""
def find_majority_element_BS(arr):
    n = len(arr)
    hashmap = dict()

    for i in range(0, n):
        hashmap[arr[i]] = hashmap.get(arr[i], 0) + 1

    for n, f in hashmap.items():
        if f > n//2:
            return n

    return -1

In [68]: test_cases = [{'arr': [3,2,3]},
                        {'arr': [2,2,1,1,2,2]},
                        {'arr': [4,4,2,4,3,4,3,2,4]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, 'Majority element:', find_majority_element_BS(arr))

arr: [3, 2, 3] Majority element: 3
arr: [2, 2, 1, 1, 2, 2] Majority element: 2
arr: [4, 4, 2, 4, 3, 4, 3, 2, 4] Majority element: 4

In [69]: """
Optimal solution (Moore's Voting Algorithm)

Time Complexity : O( 2n )
Space Complexity : O( 1 )
"""
def find_majority_element_OS(arr):
    n = len(arr)
    candidate = None
    counter1 = counter2 = 0

    for i in range(0, n):
        if counter1 == 0 and arr[i] != candidate:
            candidate = arr[i]
            counter1 = 1
        elif arr[i] == candidate:
            counter1 += 1
        else:
            counter2 += 1

    counter1 = counter2 = 0

    for i in range(0, n):
        if arr[i] == candidate:
            counter1 += 1
        elif arr[i] == candidate:
            counter2 += 1
        else:
            counter1 -= 1
            counter2 -= 1

    counter1 = counter2 = 0

    for i in range(0, n):
        if arr[i] == candidate:
            counter1 += 1
        elif arr[i] == candidate:
            counter2 += 1
        else:
            counter1 -= 1
            counter2 -= 1

    if counter1 > n//2:
        majority_elements.append(candidate)
    if counter2 > n//3:
        majority_elements.append(candidate)

    return majority_elements

In [74]: test_cases = [{'arr': [1,2,2,3,2]},
                        {'arr': [11,33,33,11,33,11]},
                        {'arr': [2,1,3,1,4,5,6]}]

for to in test_cases:
    arr = to['arr']
    print('arr:', arr, 'Majority element:', find_majority_element_OS(arr))

arr: [1, 2, 2, 3, 2] Majority element: [2]
arr: [11, 33, 33, 11, 33, 11] Majority element: [11, 33]
arr: [2, 1, 3, 1, 4, 5, 6] Majority element: [1]
```







