Generalized Additive Models (GAMs) CMDA 4654 Project 2

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Replying to @millerdl

140 char vrsn

1 GAMs are just GLMs
2 GAMs fit wiggly terms
3 use + s(foo) not foo in frmla
4 use method = "REML"
5 gam.check()

2:37 PM · Mar 16, 2017 · TweetDeck

- Type of generalized linear model
- Response variable depends on smooth functions $f_i(x_i)$
- General structure of a GAM:

$$g(E(Y)) = \beta_0 + f_1(x_1) + f_2(x_2) + \cdots + f_n(x_n)$$

 Smooth functions can be many different things (polynomials, splines, weighted means, etc)

A Linear Model sums the linear terms

$$y_i = \beta_0 + \sum_j \beta_j x_{ji} + \epsilon_i$$

GAMs sums the smooth functions

$$y_i = \beta_0 + \sum_j s_j(x_{ji}) + \epsilon_i$$

where

$$\epsilon_i \sim N(0, \sigma^2), y_i \sim \text{Normal}$$

A *Spline* is a function made of up basis functions (the smoothing functions)

These simpler functions form a set of functions called the basis

When using a spline for GAMs, each basis function has a coefficient

The spline is formed by weighing the basis function and summing them at each value of \boldsymbol{x}

- Two options for packages, mgcv and gam
- mgcv is more commonly used and better supported

Description

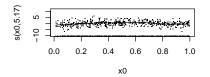
mgcv provides functions for generalized additive modelling (gam and bam) and generalized additive mixed modelling (gamm, and random,effects). The term GAM is taken to include any model dependent on unknown smooth functions of predictors and estimated by quadratically penalized (possibly quasi-) likelihood maximization. Available distributions are covered in family_mgcv and available smooths in smooth.terms.

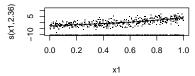
Particular features of the package are facilities for automatic smoothness selection (Wood, 2004, 2011), and the provision of a variety of smooths of more than one variable. User defined smooths can be added. A Bayesian approach to confidence/credible interval calculation is provided. Linear functionals of smooths, penalization of parametric model terms and linkage of smoothing parameters are all supported. Lower level routines for generalized ridge regression and penalized linearly constrained least squares are also available. In addition to the main modeling functions, squares are also available. In addition to the main modeling functions, squares are supported. Lower level routines for generalized ridge regression and provided facilities to ease the set up of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of models for use with JAGS, while squares are supported. Lower level of mailto: squares are

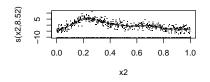
```
library(mgcv)
set.seed(0)
sim_data <- gamSim(1, n = 400, dist="normal", scale=2)</pre>
Gu & Wahba 4 term additive model
head(sim data)
                            x1 x2 x3
1 5.114211 0.8966972 0.1478457 0.34826473 0.04572472 7.962274 0.6377368
2 2.175828 0.2655087 0.6588776 0.85868745 0.36652658 5.514517 1.4814113
3 6.334878 0.3721239 0.1850700 0.03443876 0.74139303 3.576406 1.8407682
4 6.853276 0.5728534 0.9543781 0.97099715 0.93350625 8.692625 1.9478442
5 7.743879 0.9082078 0.8978485 0.74511014 0.67320995 8.752859 0.5687870
6 13.920886 0.2016819 0.9436971 0.27325524 0.70135711 16.190349 1.1841037
                    f2 f3
       f1
1 1 344055 5 980482e+00 0
2 3.735028 2.980780e-01 0
3 1.447937 2.877006e-01 0
4 6.744695 8.611364e-05 0
5 6.023672 2.160400e+00 0
6 6.602142 8.404104e+00 0
```

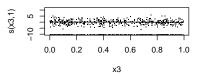
```
fit \leftarrow gam(v \sim s(x0) + s(x1) + s(x2) + s(x3), data = sim data)
summary(fit)
Family: gaussian
Link function: identity
Formula:
y \sim s(x0) + s(x1) + s(x2) + s(x3)
Parametric coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 7.9150 0.1049 75.44 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
       edf Ref.df F p-value
s(x0) 5.173 6.287 4.564 0.000134 ***
s(x1) 2.357 2.927 103.053 < 2e-16 ***
s(x2) 8.517 8.931 84.308 < 2e-16 ***
s(x3) 1.000 1.000 0.441 0.506929
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
R-sq.(adi) = 0.726 Deviance explained = 73.7%
GCV = 4.611 Scale est = 4.4029 n = 400
```

plot(fit, pages=1, residuals=TRUE)

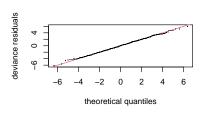




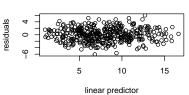




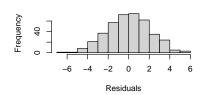
gam.check(fit)



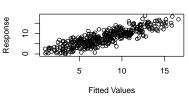
Resids vs. linear pred.



Histogram of residuals

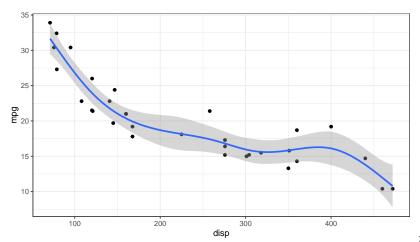


Response vs. Fitted Values

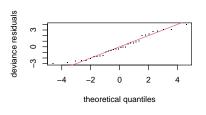


```
data("mtcars")
mtcars_gam <-
  gam(mpg ~ s(disp), data = mtcars, method = "REML")
summary(mtcars gam)
Family: gaussian
Link function: identity
Formula:
mpg ~ s(disp)
Parametric coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 20.0906 0.3788 53.04 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
         edf Ref.df F p-value
s(disp) 4.884 5.904 36.3 <2e-16 ***
---
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.874 Deviance explained = 89.4%
-REMI = 74 101 Scale est = 4.5918 n = 32
```

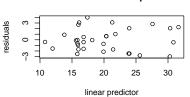
```
library(ggplot2)
ggplot(data = mtcars, aes(x = disp, y = mpg)) +
    theme_bw() + geom_point() +
geom_smooth(method = "gam", formula = y ~ s(x))
```



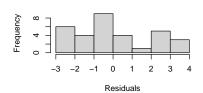
gam.check(mtcars_gam)



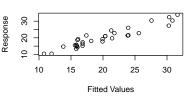
Resids vs. linear pred.



Histogram of residuals



Response vs. Fitted Values



data("iris")

```
df <- read.csv("estimated_inpatient.csv")</pre>
```

Conclusion

Conclusion

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References