Early Growth in a Perturbed Universe: Dark Matter Halo Properties in 2LPT and ZA Simulations

Ву

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This is where you thank the people that made your work possible: grant awarding agencies, advisers, your committee, mom and dad, whatever.

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CHAPTER I

Introduction

Text goes here. This is where we'll talk about the purpose of the project and the layout of this document.

The structure of this document is as follows: The remainder of this chapter, Chapter I, provides an introduction to the early universe and the processes that lead to galaxy-hosting dark matter halos, as well as the fundamentals of the computational theory for the numerical methods relevant to this discussion. Chapter II examines in more detail the specific numerical methods used for this work, with emphasis on the methodologies of the codes themselves, how they are implemented in the context of the overall simulation and analysis pipeline, and the results obtained at each step. Chapter III is a direct representation of the published paper which (more succinctly) presents an overview of the numerical methods and the main results in this work. Chapter IV is primarily the same material as previously submitted to fulfill the requirements of the Qualifying Exam, and is slightly edited to better suit the tone of this document. Chapter V concludes with a discussion of the results in this work and the greater implications to the overall field.

I.1 The Early Universe

Text goes here.

I.1.1 The CMB Epoch

Text goes here.

I.1.1.1 Recombination

I.1.1.2 The Cosmic Microwave Background

Text goes here.

I.1.2 Dark Matter Halo Formation

Text goes here.

I.1.2.1 Collapse

Text goes here.

I.1.2.2 Accretion

Text goes here.

I.1.2.3 Mergers

Text goes here.

I.1.2.4 Large-scale Structure

Text goes here.

I.1.3 Halo Properties

Text goes here.

I.1.3.1 Mass

There are a number of ways to define a halo's mass. This becomes significant for mass-sensitive studies, such as the halo mass function (Press & Schechter, 1974; Reed et al., 2007; Heitmann et al., 2006; Lukić et al., 2007), the number density of halos as a function of mass and a key probe of cosmology. For a review, see, e.g., White (2001) and references therein. Additionally, see Voit (2005) and references therein for a more observation-focused discussion.

I.1.3.2 Density and Concentration

The density profile of a DM halo is determined by radially binning the constituent particles into spherical shells, and determining the average density per shell, giving a characteristic $\rho(r)$. The most widely used model for the DM halo density profile is the NFW (Navarro et al., 1996) profile

$$\rho(r) = \frac{\rho_0}{\frac{r}{R_s} \left(1 + \frac{r}{R_s}\right)^2},\tag{I.1}$$

where ρ_0 is the characteristic density, and the scale radius R_s is the break radius between the inner $\sim r^{-1}$ and outer $\sim r^{-3}$ density profiles.

The halo density profile is quantified by the halo concentration $c \equiv R_{\rm vir}/R_s$, where $R_{\rm vir}$ is the halo virial radius. Generally, at low redshift, low mass halos are more dense than high mass halos (Navarro et al., 1997a), and concentration decreases with redshift and increases in dense environments (Bullock et al., 2001). Neto et al. (2007) additionally find that concentration decreases with halo mass. Various additional studies have explored concentration's dependence on characteristics of the power spectrum (Eke et al., 2001), cosmological model (Macciò et al., 2008), redshift (Gao et al., 2008; Muñoz-Cuartas et al., 2011), and halo merger and mass accretion histories (Wechsler et al., 2002; Zhao et al., 2003, 2009). For halos at high redshift, Klypin et al. (2011) find that concentration reverses and increases with mass for high mass halos, while Prada et al. (2012) find that concentration's dependence on mass and redshift is more complicated and is better described through $\sigma(M,z)$, the rms fluctuation amplitude of the linear density field.

I.1.3.3 Substructure and Environment

Text goes here.

I.1.4 Baryonic Processes

Early-forming dark matter halos provide an incubator for the baryonic processes that transform the surrounding space and allow galaxies to form. Initial gas accretion can lead to

the formation of the first Pop-III stars (Couchman & Rees, 1986; Tegmark et al., 1997; Abel et al., 2000, 2002), which, upon their death, can collapse into the seeds for supermassive black holes (SMBHs) (Madau & Rees, 2001; Islam et al., 2003; Alvarez et al., 2009; Jeon et al., 2012) or enrich the surrounding medium with metals through supernovae (Heger & Woosley, 2002; Heger et al., 2003). The radiation from these early quasars (Shapiro & Giroux, 1987; Madau et al., 1999; Fan et al., 2001), Pop-III stars (Gnedin & Ostriker, 1997; Venkatesan et al., 2003; Alvarez et al., 2006), and proto-galaxy stellar populations (Bouwens et al., 2012; Kuhlen & Faucher-Giguère, 2012) all play a key role in contributing to the re-ionizing the universe by around z = 6 (Barkana & Loeb, 2001). Additionally, halo mergers can drastically increase the temperature of halo gas through shock heating, increasing X-ray luminosity (Sinha & Holley-Bockelmann, 2009), and contribute to the unbinding of gas to form the warm-hot intergalactic medium (Bykov et al., 2008; Sinha & Holley-Bockelmann, 2010; Tanaka et al., 2012).

I.1.4.1 The First Stars

Text goes here.

I.1.4.2 Supermassive Black Holes

Text goes here.

I.1.4.3 Enrichment and the The Intergalactic Medium

Text goes here.

I.1.4.4 Reionization

Text goes here.

I.2 Computational Theory

I.2.1	Simulation Initialization

Text goes here.

I.2.1.1 Initial Conditions and the Surface of Last Scattering

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I.2.1.2 The Zel'dovich Approximation

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I.2.1.3 Second-order Lagrangian Perturbation Theory

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I.2.2 Dark Matter Halos in N-body Simulations

Text goes here.

I.2.2.1 Spherical Overdensity

Text goes here.

I.2.2.2 Friends-of-Friends

CHAPTER II

Numerical Methods

Text goes here. Here, we will discuss the computational tools used, their inner workings, and how they are implemented to accomplish their purpose in the pipeline.

II.1 Initialization Code

Text goes here.

II.1.1 Sampling the Power Spectrum

Text goes here.

II.1.1.1 Cosmological Parameters

Text goes here.

II.1.1.2 Sampling

Text goes here.

II.1.2 Particle Displacement with ZA

Text goes here.

II.1.3 Particle Displacement with 2LPT

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II.2 Simulations with GADGET-2

We use the massively parallel TreeSPH cosmological N-body simulation code GADGET-2 for the dark matter simulations presented in this work. In this section, we begin with

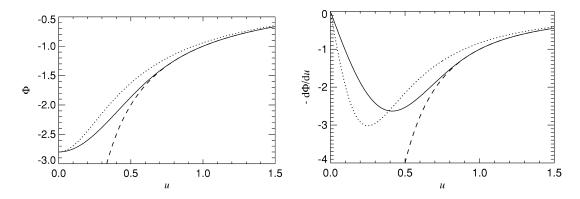


Figure II.1: Potential (left) and force (right) softening.

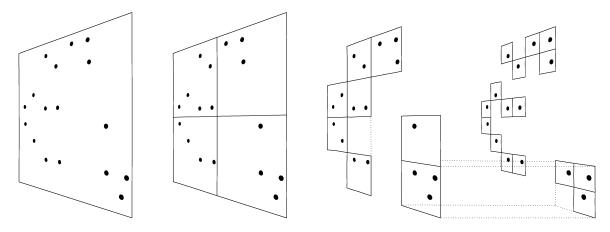


Figure II.2: Barns-Hut oct-tree in two dimensions.

a discussion of the fundamental concepts presented in the original GADGET code, then proceed to the improvements made in the GADGET-2 code.

II.2.1 GADGET-2

Text goes here.

II.2.1.1 Force Calculation and Softening

Text goes here.

II.2.1.2 The Tree Code

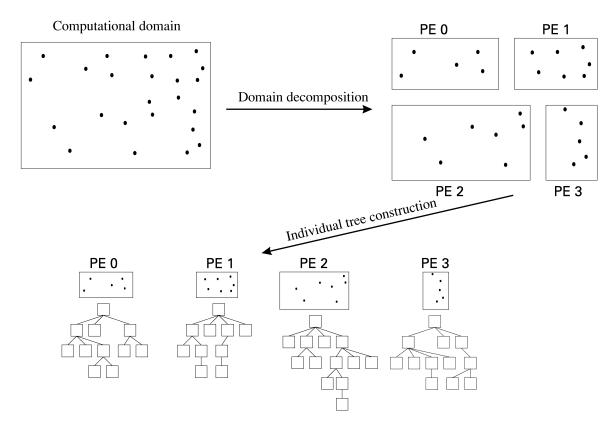


Figure II.3: Domain decomposition.

II.2.1.3 Parallelization

Text goes here.

II.2.1.4 Metrics

Text goes here.

II.2.2 Simulations

Text goes here.

II.3 Halo Finding with ROCKSTAR

Text goes here.

II.3.1 Halo Identification

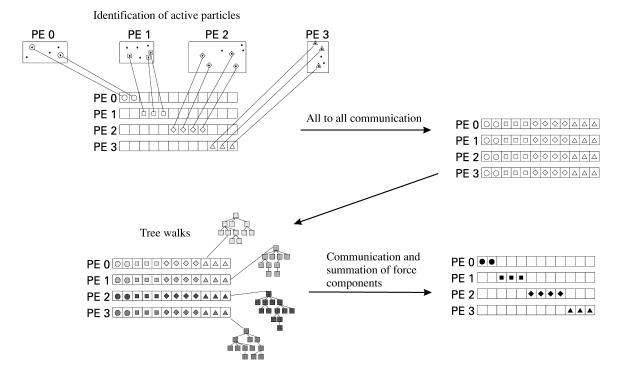


Figure II.4: Force parallelism.

II.3.2 Halo Properties

Text goes here.

II.3.2.1 Mass

Text goes here.

II.3.2.2 Concentration

Text goes here.

II.3.2.3 Relaxation Parameters

Text goes here.

II.3.3 Halo Catalogs

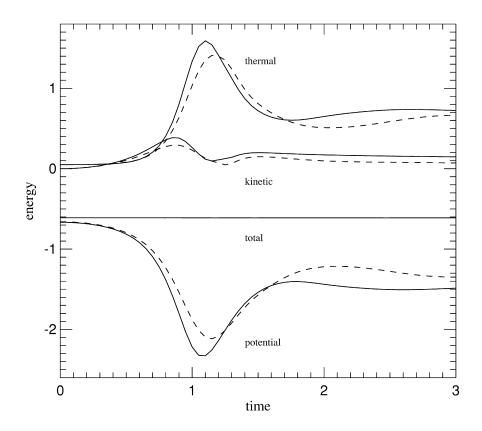


Figure II.5: Energy conservation for an initially isothermal gas sphere.

II.4 CROSSMATCH

Text goes here.

II.5 Analysis

In this section, we discuss the details of the pipeline used for this work, including the analysis and plotting codes, databases, and automation scripts. We also present an overview of the results obtained at each step. A more in depth discussion of the observed trends and interpretations of results are presented in Sections III.3 and III.4.

As a high-level overview, we gather snapshots from previously run 2LPT and ZA simulations, find halos in each snapshot with ROCKSTAR, match halos between simulations with CROSSMATCH, and compare the differences in various properties between corresponding 2LPT and ZA halos, primarily as functions of redshift and halo mass. The specific codes developed for and used in our analysis are provided in the Appendices, and are referenced

with the relevant discussions below.

II.5.1 Halo Properties

Halos are identified and measured with the ROCKSTAR halo finder (see Section II.3 for implementation details).

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II.5.1.1 Rockstar Output and Post-processing

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II.5.1.2 Spherical Overdensity Halo Particles

Text goes here.

II.5.2 Density Profile Fitting

While ROCKSTAR's output includes measurements for halo virial and scale radii, and thus concentration, we independently fit NFW density profiles to halos and measure concentration as a verification of ROCKSTAR's fitting. The full density profile python code is presented in Appendix D.

II.5.2.1 Density Profiles

For each halo, a list of constituent spherical overdensity particles is obtained from the post-processed BGC2 catalog from ROCKSTAR's output. For our purposes here, the relevant parameters are particle mass and position. We also use the values for each halo's center position and virial radius as found by ROCKSTAR.

Density profiles are then constructed by binning the particle positions in logarithmic radial bins from the resolution limit of the simulation to the halo virial radius and multiplying by particle mass. Before being passed to the fitting routine, density profiles are normalized to unity for both virial radius and maximum density.

II.5.2.2 Fitting

Halos are fit using the CurveFit routine from the SciPy Optimize library. It uses the Levenberg-Marquardt algorithm [citation needed] for non-linear least squares fitting.

CurveFit is called by providing a model function, independent variable, measured dependent variable, and optionally weights for the dependent variable and initial guesses for fit coefficients. Here, our fit function is the NFW dark matter density profile (see Equation III.1). The free parameters to be fit are the scale radius R_s and the characteristic density ρ_0 .

As the least squares algorithm is sensitive to local minima, care must be taken in choosing initial guesses for the fit coefficients. Additionally, large dynamic range in the fit parameters tended to produce poor results. We explored a number of solutions to improve solution stability, including fitting in logarithmic space and randomizing the initial guesses and picking the best solution. We found the best results were achieved by normalizing the data to unity for both radius and density, and choosing initial guesses within an order of magnitude for a typical halo, namely, normalized $R_s = 0.1$ and normalized $\rho_0 = 1.0$.

Some halos with irregular profiles presented the problem of the fitting algorithm choosing an unphysical scale radius larger than the virial radius of the halo. In order to heavily penalize this option from being chosen by the fitting algorithm, the dependent variable returned by the model function must differ from the input measured dependent variable as much as possible. However, we discovered that the transition must also be smooth, as a disjointed jump such as, say, returning a very large number for every value if $R_s > R_{\text{vir}}$ would cause the algorithm to fail. We achieve this smooth transition penalty by adding the term $(R_s - 1)e^r$ to the density returned by the model function if the fitting algorithm tries to guess a value of R_s larger than R_{vir} . However, while this did force halos to have definable concentrations, these halos often ended up with best fit scale radii equal to or just slightly less than the virial radii.

As we fit halos over a large range in redshift, we found low particle count halos to have

noisy density profiles that were inherently more difficult to properly fit. Throughout our analysis, we use a lower bound of 100 particles to define a halo. At high redshift, even the largest halos are just beginning to cross this threshold. With such few particles spread across the number of bins necessary to properly define a density profile, we are left with only a handful of particles per bin. In Figure II.6, we compare one of the largest halos at z = 14 with one of the largest halos at the end of the simulation at z = 6.

II.5.2.3 Characterization of Uncertainty

An initial motivation for finding our own concentration parameters independent from ROCK-STAR is that ROCKSTAR does not provide information about the quality of its density profile fits. We assign Poisson errors to the density in each bin such that $\sigma_{\rho} = \rho \sqrt{N}/N$, where ρ is the density and N is the number of particles in each bin. These uncertainties are then provided as weights to the CurveFit routine. Upon finding a best fit, the routine provides the fit parameters and an estimation of the uncertainty in those parameters via a covariance matrix, which we use to uncertainty in the concentration. Additionally, we find the χ^2 for the overall fit, which we use as an indicator of whether to accept or reject the fit for a given halo.

II.5.2.4 Mass Profiles

Text goes here. Mass profiles tested to avoid binning issues and the stats stuff Manodeep learned at the conference. Bad fitting results, so abandoned. Figure II.7.

II.5.2.5 Concentration Comparison to ROCKSTAR

Overall, we do not find good agreement with ROCKSTAR. Using a script (see Appendix H) to compare the concentrations derived from our fits with those from ROCKSTAR. At z=6, we find that only 26% of halos fit by our method have concentrations within 20% of concentrations as measured by ROCKSTAR. We have slightly more agreement with high mass halos, with 37% agreement if we only consider the most massive 10% of halos. Addition-

ally, we do not find good fits for every halo. If the distribution of particles would produce too few bins or the fitting routine exceeded a maximum number of iterations to find a stable solution, the halo is not fit. We also exclude halos with fits returned with very large χ^2 values. Because of the discrepancies in our results and the fact that we do not find acceptable fits for every halo, we use the more complete ROCKSTAR data for the final concentration measurements used in the remainder of our analysis.

II.5.3 Cross-matched Halo Catalog

With halo catalogs generated by ROCKSTAR for both 2LPT and ZA simulations, we need to be able to directly compare corresponding halos from the two suites of simulations. We match halos between simulations based on constituent particles with the CROSSMATCH code modified to import ROCKSTAR's BGC2 binary output files. Properties of the matched halos are then compiled into one large database per box for further filtering and analysis.

II.5.3.1 Cross-matching

Our simulations are initialized with identical particle ID schemes, and we are thus able to uniquely identify and track matching particles between simulations and match halos based on the largest number of shared particles. As the full implementation of the CROSSMATCH code is previously discussed in Section II.4, we only briefly summarize its place in our analysis pipeline here. The script in Appendix M.2 sets up the directory structure for the CROSSMATCH analysis and copies the CROSSMATCH parameter files (Appendices B.1 and B.2) to the appropriate run directories. CROSSMATCH is then run for each snapshot via the submission script in Appendix M.7, which is run for each simulation box.

Once caveat of the CROSSMATCH code is that matches are not necessarily unique. For each halo in the first simulation, only one best match halo will be selected from the second simulation. However, there may be other halos from the first simulation that also have the same halo from the second simulation selected as a best match. To counter this, we run CROSSMATCH in both directions—once matching ZA halos to 2LPT halos and once

matching 2LPT halos to ZA halos—and choose best match halos as those that are matched in both directions. This assures a unique one-to-one matching between 2LPT and ZA halos. The code and submission script that select the best matches from the 2LPT-first and ZA-first cross-matched halo lists are presented in Appendix E.1.

II.5.3.2 Aggregation

Text goes here.

II.5.3.3 Filtering

Text goes here.

II.5.4 Halo Comparison

Text goes here.

II.5.4.1 Match Verification

Text goes here.

II.5.4.2 Morphology

Text goes here.

II.5.4.3 Density Profiles

Text goes here.

II.5.5 Difference Distributions

Text goes here.

II.5.5.1 Histograms

II.5.5.2 Fitting

Text goes here.

II.5.5.3 Mass Quartiles

Text goes here.

II.5.6 Redshift Trends

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II.5.6.1 Mean and Standard Deviation

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II.5.6.2 Skew

Text goes here.

II.5.6.3 Kurtosis

Text goes here.

The standard deviation of a function $f(x_1, x_2, ..., x_n)$ is, in general, given by

$$s_f = \sqrt{\sum_{x} \left(\frac{\partial f}{\partial x}\right)^2 s_x^2} \tag{II.1}$$

with summation over all independent variables x. The generalized normal distribution

$$f(x) = \frac{\beta}{2\alpha\Gamma(1/\beta)}e^{-(|x-\mu|/\alpha)^{\beta}}$$
 (II.2)

with mean μ , scale parameter α , and shape parameter β , has excess kurtosis

$$\gamma_2 = \frac{\Gamma(5/\beta)\Gamma(1/\beta)}{\Gamma(3/\beta)^2} - 3. \tag{II.3}$$

The gamma function

$$\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt$$
 (II.4)

has the first derivative

$$\Gamma'(x) = \Gamma(x)\psi_0(x) \tag{II.5}$$

where the digamma function ψ_0 is the derivative of the logarithm of the gamma function and is given by

$$\psi_0(x) = \int_0^\infty \left(\frac{e^{-t}}{t} - \frac{e^{-xt}}{1 - e^{-t}} \right) dt$$
 (II.6)

if the real part of *x* is positive.

We now apply (II.1) to (III.13) to find the standard deviation of the excess kurtosis:

$$s_{\gamma_2} = \sqrt{\left(\frac{\mathrm{d}\gamma_2}{\mathrm{d}\beta}\right)^2 s_\beta^2} \tag{II.7}$$

$$= s_{\beta} \frac{\mathrm{d}\gamma_2}{\mathrm{d}\beta} \tag{II.8}$$

$$= s_{\beta} \frac{\mathrm{d}}{\mathrm{d}\beta} \left[\frac{\Gamma(5/\beta)\Gamma(1/\beta)}{\Gamma(3/\beta)^2} - 3 \right]. \tag{II.9}$$

Making the substitution $x = 1/\beta$ and $dx = -1/\beta^2 d\beta$, taking the derivative, and doing a bit

of algebra, we have:

$$s_{\gamma_2} = s_\beta \frac{\mathrm{d}\gamma_2}{\mathrm{d}x} \frac{\mathrm{d}x}{\mathrm{d}\beta} \tag{II.10}$$

$$= s_{\beta} \left(-\frac{1}{\beta^2} \right) \frac{\mathrm{d}}{\mathrm{d}x} \left[\frac{\Gamma(5x)\Gamma(x)}{\Gamma(3x)} - 3 \right] \tag{II.11}$$

$$= -s_{\beta}x^{2} \left\{ \frac{\Gamma(3x)^{2} \frac{\mathrm{d}}{\mathrm{d}x} [\Gamma(5x)\Gamma(x)] - \Gamma(5x)\Gamma(x) \frac{\mathrm{d}}{\mathrm{d}x} [\Gamma(3x)^{2}]}{\Gamma(3x)^{4}} \right\}$$
(II.12)

$$= -s_{\beta} \frac{x^2}{\Gamma(3x)^4} \left\{ \Gamma(3x)^2 [5\Gamma(5x)\psi_0(5x)\Gamma(x) + \Gamma(5x)\Gamma(x)\psi_0(x)] - \Gamma(5x)\Gamma(x)[6\Gamma(3x)^2\psi_0(3x)] \right\}$$

 $= s_{\beta} \frac{x^2}{\Gamma(3x)^4} \left\{ 6\Gamma(5x)\Gamma(3x)^2\Gamma(x)\psi_0(3x) - \Gamma(5x)\Gamma(3x)^2\Gamma(x)[5\psi_0(5x) + \psi_0(x)] \right\}$

(II.14)

(II.13)

$$= s_{\beta} \frac{x^2}{\Gamma(3x)^4} \left\{ \Gamma(5x)\Gamma(3x)^2 \Gamma(x) \left[6\psi_0(3x) - 5\psi_0(5x) - \psi_0(x) \right] \right\}$$
 (II.15)

$$= s_{\beta} x^{2} \frac{\Gamma(5x)\Gamma(x)}{\Gamma(3x)^{2}} [6\psi_{0}(3x) - 5\psi_{0}(5x) - \psi_{0}(x)]. \tag{II.16}$$

Substituting back in for x and recognizing an occurance of γ_2 , we have the result

$$s_{\gamma_2} = s_{\beta} \frac{1}{\beta^2} (\gamma_2 + 3) \left[6\psi_0(3/\beta) - 5\psi_0(5/\beta) - \psi_0(1/\beta) \right]$$
 (II.17)

with which we can find the uncertainty in the kurtosis given the value and uncertainty of the shape parameter β .

II.5.7 2-D Histograms

Text goes here.

II.5.7.1 Binning and Plotting

II.5.7.2 Fitting

Text goes here.

II.5.8 Alternate Difference Distributions

Text goes here.

II.5.8.1 Equivalent Displacement

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II.5.8.2 Redshift Trends

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II.6 Automation

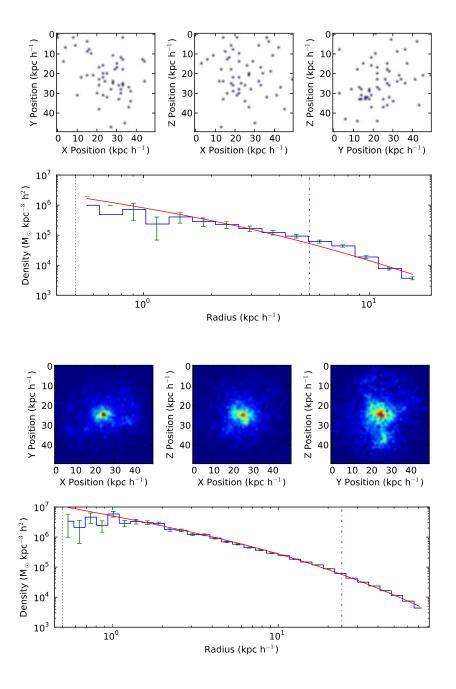


Figure II.6: Density profiles for two large halos at z = 14 and z = 6. Both halos are from the Box 1 2LPT simulation, and are the largest halos at their respective redshifts. (Get rid of density projections.)

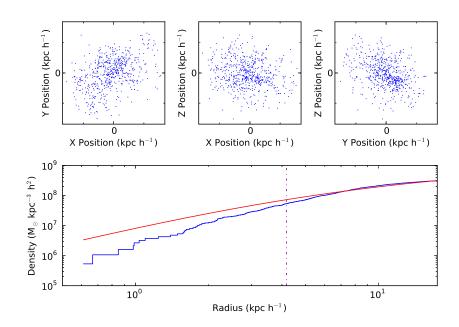


Figure II.7: Mass profiles for a large halo at z = 6. (Get rid of density projections.)

CHAPTER III

Exploring Dark Matter Halo Populations in 2LPT and ZA Simulations

We study the structure and evolution of dark matter halos from z=300 to z=6 for two cosmological N-body simulation initialization techniques. While the second order Lagrangian perturbation theory (2LPT) and the Zel'dovich approximation (ZA) both produce accurate present day halo mass functions, earlier collapse of dense regions in 2LPT can result in larger mass halos at high redshift. We explore the differences in dark matter halo mass and concentration due to initialization method through three 2LPT and three ZA initialized cosmological simulations. We find that 2LPT induces more rapid halo growth, resulting in more massive halos compared to ZA. This effect is most pronounced for high mass halos and at high redshift, with a fit to the mean normalized difference between 2LPT and ZA halos as a function of redshift of $\mu_{\Delta M_{\rm vir}} = (7.88 \pm 0.17) \times 10^3 z - (3.07 \pm 0.14) \times 10^{-2}$. Halo concentration is, on average, largely similar between 2LPT and ZA, but retains differences when viewed as a function of halo mass. For both mass and concentration, the difference between typical individual halos can be very large, even for symmetrically distributed quantities, highlighting the shortcomings of ZA-initialized simulations for high-z

III.1 Introduction

The pre-reionization epoch is a time of significant evolution of early structure in the universe. Rare density peaks in the otherwise smooth dark matter (DM) sea lead to the collapse and formation of the first dark matter halos. For example, at z=20, $10^7~\rm M_{\odot}$ halos are $\sim 4\sigma$ peaks, and $10^8~\rm M_{\odot}$ halos, candidates for hosting the first supermassive black hole seeds, are $\sim 5\sigma$ peaks.

These early-forming dark matter halos provide an incubator for the baryonic processes that transform the surrounding space and allow galaxies to form. Initial gas accretion can

lead to the formation of the first Pop-III stars (Couchman & Rees, 1986; Tegmark et al., 1997; Abel et al., 2000, 2002), which, upon their death, can collapse into the seeds for supermassive black holes (SMBHs) (Madau & Rees, 2001; Islam et al., 2003; Alvarez et al., 2009; Jeon et al., 2012) or enrich the surrounding medium with metals through supernovae (Heger & Woosley, 2002; Heger et al., 2003). The radiation from these early quasars (Shapiro & Giroux, 1987; Madau et al., 1999; Fan et al., 2001), Pop-III stars (Gnedin & Ostriker, 1997; Venkatesan et al., 2003; Alvarez et al., 2006), and proto-galaxy stellar populations (Bouwens et al., 2012; Kuhlen & Faucher-Giguère, 2012) all play a key role in contributing to the re-ionizing the universe by around z = 6 (Barkana & Loeb, 2001). Additionally, halo mergers can drastically increase the temperature of halo gas through shock heating, increasing X-ray luminosity (Sinha & Holley-Bockelmann, 2009), and contribute to the unbinding of gas to form the warm-hot intergalactic medium (Bykov et al., 2008; Sinha & Holley-Bockelmann, 2010; Tanaka et al., 2012).

While a number of parameters are required to fully characterize a DM halo, a first-order description can be obtained from its mass and density profile. There are a number of ways to define a halo's mass. This becomes significant for mass-sensitive studies, such as the halo mass function (Press & Schechter, 1974; Reed et al., 2007; Heitmann et al., 2006; Lukić et al., 2007), the number density of halos as a function of mass and a key probe of cosmology. For a review, see, e.g., White (2001) and references therein. Additionally, see Voit (2005) and references therein for a more observation-focused discussion.

From a simulation standpoint, the two most common ways to obtain halo mass are to define either spherical overdensity halos or friends-of-friends (FOF) halos. The spherical overdensity method identifies regions above a certain density threshold, either with respect to the critical density $\rho_c = 3H^2/8\pi G$ or the background density $\rho_b = \Omega_m \rho_c$, where Ω_m is the matter density of the universe. The mass is then the mass enclosed in a sphere of some radius with mean density $\Delta \rho_c$, where Δ commonly ranges from ~ 100 to ~ 500 . Alternatively, the FOF method finds particle neighbors and neighbors of neighbors defined

to be within some separation distance (Einasto et al., 1984; Davis et al., 1985). Halo mass, then, is simply the sum of the masses of the constituent particles.

The density profile of a DM halo is determined by radially binning the constituent particles into spherical shells, and determining the average density per shell, giving a characteristic $\rho(r)$. The most widely used model for the DM halo density profile is the NFW (Navarro et al., 1996) profile

$$\rho(r) = \frac{\rho_0}{\frac{r}{R_s} \left(1 + \frac{r}{R_s}\right)^2},\tag{III.1}$$

where ρ_0 is the characteristic density, and the scale radius R_s is the break radius between the inner $\sim r^{-1}$ and outer $\sim r^{-3}$ density profiles.

The halo density profile is quantified by the halo concentration $c \equiv R_{\rm vir}/R_s$, where $R_{\rm vir}$ is the halo virial radius. Generally, at low redshift, low mass halos are more dense than high mass halos (Navarro et al., 1997a), and concentration decreases with redshift and increases in dense environments (Bullock et al., 2001). Neto et al. (2007) additionally find that concentration decreases with halo mass. Various additional studies have explored concentration's dependence on characteristics of the power spectrum (Eke et al., 2001), cosmological model (Macciò et al., 2008), redshift (Gao et al., 2008; Muñoz-Cuartas et al., 2011), and halo merger and mass accretion histories (Wechsler et al., 2002; Zhao et al., 2003, 2009). For halos at high redshift, Klypin et al. (2011) find that concentration reverses and increases with mass for high mass halos, while Prada et al. (2012) find that concentration's dependence on mass and redshift is more complicated and is better described through $\sigma(M,z)$, the rms fluctuation amplitude of the linear density field.

The subtle $\mathcal{O}(10^{-5})$ density perturbations in place at the CMB epoch are vulnerable to numerical noise and intractable to simulate directly. Instead, a displacement field is applied to the particles to evolve them semi-analytically, nudging them from their initial positions to an approximation of where they should be at a more reasonable starting redshift for the numerical simulation. Starting at a later redshift saves computation time as well as avoiding

interpolation systematics and round-off errors (Lukić et al., 2007).

The Zel'dovich approximation (Zel'dovich, 1970) and 2nd-order Lagrangian Perturbation Theory (Buchert, 1994; Buchert et al., 1994; Bouchet et al., 1995; Scoccimarro, 1998) are the two canonical frameworks for the initial particle displacement involved in generating simulation initial conditions. Zel'dovich approximation (ZA, hereafter) initial conditions (Klypin & Shandarin, 1983; Efstathiou et al., 1985) displace initial particle positions and velocities via a linear field, while 2nd-order Linear Perturbation Theory (2LPT, hereafter) initial conditions (Scoccimarro, 1998; Sirko, 2005; Jenkins, 2010) add a second-order correction term to the expansion of the displacement field.

Following Jenkins (2010), we briefly outline the second-order Lagrangian perturbation theory and compare it to the Zel'dovich approximation. In 2LPT, a displacement field $\Psi(q)$ is applied to the initial positions q to yield the Eulerian final comoving positions

$$x = q + \Psi.$$
 (III.2)

The displacement field is given in terms of two potentials $\phi^{(1)}$ and $\phi^{(2)}$ by

$$x = q - D_1 \nabla_a \phi^{(1)} + D_2 \nabla_a \phi^{(2)}, \tag{III.3}$$

with linear growth factor D_1 and second-order growth factor $D_2 \approx -3D_1^2/7$. The subscripts q refer to partial derivatives with respect to the Lagrangian coordinates q. Likewise, the comoving velocities are given, to second order, by

$$v = -D_1 f_1 H \nabla_q \phi^{(1)} + D_2 f_2 H \nabla_q \phi^{(2)}, \tag{III.4}$$

with Hubble constant H and $f_i = d \ln D_i / d \ln a$, with expansion factor a. The relations $f_1 \approx \Omega^{5/9}$ and $f_2 \approx 2\Omega^{6/11}$, with matter density Ω , apply for flat models with a non-zero cosmological constant (Bouchet et al., 1995). The f_1 , f_2 , and D_2 approximations here are

very accurate for most actual Λ CDM initial conditions, as Ω is close to unity at high starting redshift (Jenkins, 2010). We may derive $\phi^{(1)}$ and $\phi^{(2)}$ by solving a pair of Poisson equations

$$\nabla_q^{(1)}(q) = \delta^{(1)}(q),$$
 (III.5)

with linear overdensity $\delta^{(1)}(q)$, and

$$\nabla_q^{(2)}(q) = \delta^{(2)}(q).$$
 (III.6)

The second order overdensity $\delta^{(2)}(q)$ is related to the linear overdensity field by

$$\delta^{(2)}(q) = \sum_{i>j} \left\{ \phi_{,ii}^{(1)}(q)\phi_{,jj}^{(1)}(q) - \left[\phi_{,ij}^{(1)}(q)\right]^2 \right\},\tag{III.7}$$

where $\phi_{,ij} \equiv \partial^2 \phi / \partial q_i \partial q_j$. For initial conditions from the Zel'dovich approximation, or first-order Lagrangian initial conditions, the $\phi^{(2)}$ terms of Equations III.3 and III.4 are ignored.

Cosmological simulations that follow the initial collapse of dark matter density peaks into virialized halos often neglect to consider the nuances of initialization method. Non-linear decaying modes, or transients, will be damped as 1/a in ZA. In 2LPT, however, transients are damped more quickly as $1/a^2$. It should be expected, then, that structure in 2LPT will be accurate after fewer e-folding times than in ZA (Scoccimarro, 1998; Crocce et al., 2006; Jenkins, 2010). The practical result is that high- σ DM density peaks at high redshift are suppressed in ZA compared with 2LPT for a given starting redshift (Crocce et al., 2006).

While differences in ensemble halo properties, such as the halo mass function, between simulation initialization methods are mostly washed away by z = 0 (Scoccimarro, 1998), trends at earlier redshifts are less studied (Lukić et al., 2007). In this paper, we explore the effects of ZA and 2LPT on the evolution of halo populations at high redshift. It is thought that 2LPT allows initial DM overdensities to get a "head start" compared with ZA, allowing

earlier structure formation, more rapid evolution, and larger possible high-mass halos for a given redshift. We explore this possibility by comparing halo properties in (otherwise identical) simulations initialized with ZA and 2LPT.

We discuss the simulations, halo finding, and analysis methods in Section III.2, results in Section III.3, implications, caveats, and future work in Section III.4, and finally summarize our results and conclude in Section III.5.

III.2 Numercial Methods

We use the Nbody tree/SPH code GADGET-2 (Springel et al., 2001; Springel, 2005) to evolve six dark matter–only cosmological volumes from $z_{start} = 300$ to z = 6 in a Λ CDM universe. Each simulation is initialized using WMAP-5 (Komatsu et al., 2009) parameters. For each of the three simulation pairs, we directly compare 2LPT and ZA by identically sampling the CMB transfer function and displacing the initial particle positions to the same starting redshift using 2LPT and ZA. The three sets of simulations differ only by the initial phase sampling random seed. Each volume contains 512³ particles in a 10 h^{-1} Mpc box. Full simulation details are discussed in Holley-Bockelmann et al. (2012).

One facet often overlooked when setting up an N-body simulation is an appropriate starting redshift, determined by box size and resolution (Lukić et al., 2007). Initialization with 2LPT allows for a later starting redshift compared with an equivalent ZA-initialized simulation. However, many ZA simulations do not take this into account, starting from too late of an initial redshift (Crocce et al., 2006; Jenkins, 2010). In order to characterize an appropriate starting redshift, the relation between the initial rms particle displacement and mean particle separation must be considered. The initial rms displacement Δ_{rms} is given by

$$\Delta_{\text{rms}}^2 = \frac{4\pi}{3} \int_{k_f}^{k_{\text{Ny}}} P(k, z_{\text{start}}) dk, \qquad (\text{III.8})$$

where $k_f = 2\pi/L_{\text{box}}$ is the fundamental mode, L_{box} is the simulation box size, $k_{\text{Ny}} = \frac{1}{2}Nk_f$ is the Nyquist frequency of an N^3 simulation, and $P(k, z_{\text{start}})$ is the power spectrum at

starting redshift $z_{\rm start}$. In order to avoid the "orbit crossings" that reduce the accuracy of the initial conditions, $\Delta_{\rm rms}$ must be some factor smaller than the mean particle separation $\Delta_p = L_{\rm box}/N$ (Holley-Bockelmann et al., 2012). For example, making orbit crossing a $\sim 10\sigma$ event imposes $\Delta_{\rm rms}/\Delta_p = 0.1$. However, for small-volume, high-resolution simulations, this quickly leads to impractical starting redshifts. Continuing our example, satisfying $\Delta_{\rm rms}/\Delta_p \sim 0.1$ for a $10h^{-1}$ Mpc, 512^3 simulation suggests $z_{\rm start} \approx 799$. Starting at such a high redshift places such a simulation well into the regime of introducing errors from numerical noise caused by roundoff errors dominating the smooth potential. A more relaxed requirement of $\Delta_{\rm rms}/\Delta_p = 0.25$ yields $z_{\rm start} = 300$, which we adopt for this work.

For each of our six simulations, we use the 6-D phase space halo finder code ROCKSTAR (Behroozi et al., 2013) to identify spherical overdensity halos at each timestep. ROCKSTAR follows an adaptive hierarchical refinement of friends-of-friends halos in 6-D phase space, allowing determination of halo properties such as halo mass, position, virial radius, internal energy, and number of subhalos. ROCKSTAR tracks halos down to a threshold of around 20 particles, but we use a more conservative 100 particle threshold for our analysis. We use all particles found within the virial radius to define our halos and their properties.

We identify matching halos based on the highest fraction of matching particles contained in each at any given timestep. We remove subhalo matches (i.e. a halo must not be contained within another halo) and halo pairs with fewer than 100 particles in either 2LPT or ZA. We are left with approximately 60,000 total halo pairs for our three boxes at z = 6. With halo catalogues matched between simulations, we can compare properties of individual corresponding halos. To mitigate the effects of cosmic variance on our small volumes, we "stack" the three simulation boxes for each initialization method, and combine the halos from each into one larger sample in our analysis.

Halo concentration is derived from ROCKSTAR's output for R_s and R_{vir} . Here, R_{vir} is the virial radius as defined by Bryan & Norman (1998). Figure III.1 makes evident the difficulty in fitting density profiles and obtaining concentration measurements for typical

realistic halos. Large substructure, as displayed by the ZA halo, can disrupt the radial symmetry of the halo and cause significant deviations in the density profile. Centering can also be an issue in these cases. Due to these complications, there are a number of approaches for finding halo concentrations (Prada et al., 2012), but for consistency, we use the values derived from ROCKSTAR's fitting for our concentration measurements.

At each simulation snapshot, we measure and compare a number of parameters for halos in both 2LPT and ZA simulations. For each quantity q, we create histograms of Δq , the normalized difference in q between halos in the 2LPT and ZA simulations, defined as

$$\Delta q = \frac{q_{\text{2LPT}} - q_{\text{ZA}}}{q_{\text{avg}}},\tag{III.9}$$

where $q_{\text{avg}} = \frac{1}{2}(q_{\text{2LPT}} + q_{\text{ZA}})$. For each of these, we fit the Δq histograms with a generalized normal distribution (Nadarajah, 2005) with the probability density function

$$f(x) = \frac{\beta}{2\alpha\Gamma(1/\beta)}e^{(|x-\mu|/\alpha)^{\beta}},$$
 (III.10)

where μ is the mean, α is the scale parameter, β is the shape parameter, and Γ is the gamma function

$$\Gamma(t) = \int_0^\infty x^{t-1} e^{-x} dx.$$
 (III.11)

The shape parameter β is restricted to $\beta \geq 1$. This allows the distribution to potentially vary from a Laplace distribution ($\beta = 1$) to a uniform distribution ($\beta = \infty$) and includes the normal distribution ($\beta = 2$). The distribution has variance

$$\sigma^2 = \frac{\alpha^2 \Gamma(3/\beta)}{\Gamma(1/\beta)}$$
 (III.12)

and excess kurtosis

$$\gamma_2 = \frac{\Gamma(5/\beta)\Gamma(1/\beta)}{\Gamma(3/\beta)^2} - 3. \tag{III.13}$$

The distribution is symmetric, and thus has no skewness by definition. As such, the values for skew presented below are measured directly from the data.

As our fitting distributions are symmetrical and skew must therefore be measured directly from the data, in order to derive uncertainties for skew, we measure the skew of the distributions for each of our three simulation boxes individually as well as for the single stacked data set. Uncertainty in skew is then simply the standard deviation of the mean of the skew of the three individual boxes.

Determining the uncertainty in the kurtosis is slightly more involved, as kurtosis is determined by a transformation of the generalized normal distribution's shape parameter β according to Equation III.13. Following the standard procedure for propagation of uncertainty, we calculate the standard deviation of the kurtosis as

$$s_{\gamma_2} = \sqrt{\left(\frac{\mathrm{d}\gamma_2}{\mathrm{d}\beta}\right)^2 s_\beta^2} \tag{III.14}$$

$$= s_{\beta} \frac{\mathrm{d}}{\mathrm{d}\beta} \left[\frac{\Gamma(5/\beta)\Gamma(1/\beta)}{\Gamma(3/\beta)^2} - 3 \right]. \tag{III.15}$$

The derivative of the gamma function is

$$\Gamma'(x) = \Gamma(x)\psi_0(x), \tag{III.16}$$

where the digamma function ψ_0 is the derivative of the logarithm of the gamma function and is given by

$$\psi_0(x) = \int_0^\infty \left(\frac{e^{-t}}{t} - \frac{e^{-xt}}{1 - e^{-t}} \right) dt$$
 (III.17)

if the real part of x is positive. Now, taking the derivative of γ_2 and doing a bit of algebra gives us

$$s_{\gamma_2} = s_{\beta} \frac{1}{\beta^2} (\gamma_2 + 3) \left[6\psi_0(3/\beta) - 5\psi_0(5/\beta) - \psi_0(1/\beta) \right], \tag{III.18}$$

with which we can find the uncertainty in the kurtosis given the value and uncertainty of

the shape parameter β estimated from the least squares fit routine.

In addition to distributions of Δq , we also consider distributions of

$$\Delta' q = \frac{q_{\text{2LPT}} - q_{\text{ZA}}}{q_{\text{ZA}}} \tag{III.19}$$

in order to better quantify the fraction of halos differing by a given amount between 2LPT and ZA simulations. This distribution is inherently non-symmetrical, and is only defined for $\Delta' q \ge -1$ for positive quantities like mass and concentration. In order to consider halo pairs that differ by a certain amount in either direction (e.g. pairs that differ by 10%, whether larger in 2LPT or ZA), a relation for equivalent displacement is required. Rearranging Equation III.19 yields

$$q_{\text{2LPT}} = (\Delta' q + 1)q_{\text{ZA}},\tag{III.20}$$

and making the substitution $x = \Delta' q + 1$ gives us

$$q_{2LPT} = xq_{ZA}. (III.21)$$

For a given x_1 , we want an x_2 such that $x_2 = 1/x_1$. Substituting now for x_1 and x_2 and rearranging gives us

$$\Delta' q_2 = \frac{1}{\Delta' q_1 + 1} - 1,$$
 (III.22)

the value for which a halo pair with a larger q in ZA would differ by the same factor as a halo pair with a larger q in 2LPT where $\Delta' q = \Delta' q_1$.

III.3 Results

With our catalog of matched dark matter halos, we directly compare differences in halo properties arising from initialization with 2LPT vs ZA. We consider halos on a pair-by-pair basis as well as the entire sample as a whole. Overall, we find 2LPT halos undergo more growth at a given redshift than their ZA counterparts.

III.3.1 Individual halo pairs

We compare large scale morphologies, density profiles, and various other halo properties for halo pairs on an individual halo-by-halo basis for several of the most massive halos. Morphologies appear similar for most halos, indicating good halo matches between simulations. However, many pairs display differences in central morphology, such as the number and separation of central density peaks. We interpret these cases to be examples of differences in merger epochs, in which case one halo may still be undergoing a major merger, while its companion is in a more relaxed post-merger state. We give an example of one such pair at z=6 in Figure III.1. The top two rows show density projections of the nuclear regions for a large 2LPT and matching ZA halo (first and second rows, respectively). We find the ZA halo to contain two distinct density peaks with a separation of ~ 10 kpc, while the 2LPT halo displays only a single core. On the third and fourth rows, we plot the density profiles of the same two halos (2LPT and ZA, respectively). Here, with nearly identical virial radii, it is readily seen that the 2LPT halo is more concentrated than the ZA halo.

III.3.2 Difference distributions of halo properties

For the halo population as a whole, we consider distributions of halo virial mass $M_{\rm vir}$ and concentration c. We plot histograms of $\Delta M_{\rm vir}$ and Δc in the left and right columns, respectively, of Figure III.2 for three representative timesteps at redshifts of z=14.7, z=10.3, and z=6.0. For each panel, the blue histogram features the entire halo sample, and the smaller gray-filled green histogram displays only the top 25% most massive halos, ordered by 2LPT mass. Fits to the primary histograms are overplotted as red dashed curves.

Throughout the simulation, we find a tendency for 2LPT halos to be more massive. At z=15, the mean of the ΔM_{vir} distribution is $(9.3\pm1.2)\times10^{-2}$. The mean is consistently positive (heavier 2LPT halos) and is most displaced from zero at high redshift. The peak of the distribution gradually moves closer to zero as we progress in redshift. We find the least difference between paired halos for the final snapshot at z=6, with $\mu_{\Delta M_{\text{vir}}}=$

$$(1.79 \pm 0.31) \times 10^{-2}$$
.

The higher-order moments of the $\Delta M_{\rm vir}$ distribution are of interest as well, as we find significant deviation from a Gaussian distribution. As we use the symmetrical generalized normal distribution as our fit function, the skewness of the data is unable to be measured from the fit itself. However, a qualitative deviation from symmetry can be readily observed. By z=6, we end up with a rather symmetrical distribution, with both sides of the histogram equally well described by our fit. However, at higher redshift, we note a marked increase in skewness and deviation from this symmetry. As redshift increases, we observe an increasing difference between the fit curve and the bins to the left of the histogram peak.

We find the distributions to be much closer to a Laplace distribution than a Gaussian, with shape parameter consistently sitting at or very close to $\beta = 1$. Compared to a Gaussian distribution, the larger excess kurtosis implies a narrower central peak and heavier outlying tails. Our fit constrains $\beta \geq 1$, so the kurtosis of the data itself could potentially be higher than the fit implies.

We find no no overall preference for more concentrated 2LPT or ZA halos. In contrast to the $\Delta M_{\rm vir}$ histograms, Δc shows very little deviation from symmetry about zero. Throughout the simulation, we find the distributions to have a mean close to zero and negligible skew. The widths of the distributions are much wider than those for $\Delta M_{\rm vir}$, with an order of magnitude difference by z=6. As with mass, concentration histograms are sharply peaked with heavy tails, implying a tendency for halo pairs to move towards the extremes of either very similar or very discrepant concentrations.

III.3.3 Trends with redshift

In Figure III.3, we more quantitatively assess the evolution of our various trends hinted at in Figure III.2. Here, we plot the mean, root mean square (RMS), standard deviation, skew, and kurtosis for $\Delta M_{\rm vir}$ and Δc as functions of redshift. Uncertainty in the mean is estimated directly by the least squares fitting routine.

Table III.1: Coefficients for linear least squares fits from Figure III.3.

	$\Delta M_{ m vir}$	Δc
A	$(7.88 \pm 0.17) \times 10^{-3}$	$(3.62 \pm 0.95) \times 10^{-3}$
В	$(-3.07 \pm 0.14) \times 10^{-2}$	$(-2.34 \pm 0.84) \times 10^{-2}$

The mean for $\Delta M_{\rm vir}$ is positive and highest at high redshift, trending toward zero by the end of the simulation. Distributions for Δc retain means close to and consistent with zero. Standard deviation decreases slightly for both $\Delta M_{\rm vir}$ and Δc . From z=15 to z=6, standard deviation falls from $(9.0\pm1.5)\times10^{-2}$ to $(6.08\pm0.31)\times10^{-2}$ for $\Delta M_{\rm vir}$ and from 0.73 ± 0.11 to 0.551 ± 0.026 for Δc .

We find least square linear fits for both mean $\Delta M_{\rm vir}$ vs z and mean Δc vs z. Coefficients for slope A and y-intercept B for the fit equation $\mu = Az + B$ are given in Table III.1 for both cases. We find a significant trend for $\Delta M_{\rm vir}$, with a slope $\sim 46\sigma$ from zero. Conversely, the slope for Δc is much smaller and, considering the larger spread of the underlying distributions, can be considered negligible. For $\Delta M_{\rm vir}$, the y-intercept coefficient B likely has little meaning in terms of the actual behavior at z=0, as we expect the trend to level out at later redshift.

We do note, however, that the mean can be deceiving as an indicator of total difference between halo populations, especially when it is close to zero as with concentration. It should be noted that while the mean can indicate a lack of average difference between the whole sample of 2LPT and ZA halos, there can still be very large discrepancies between many individually paired halos. We visualize this by plotting the RMS of $\Delta M_{\rm vir}$ and Δc , which is plotted as a green dotted line. Unlike the mean, standard deviation, and kurtosis, which are measured from fits to the histograms, RMS is measured directly from the data and is not dependent on fitting. The large RMS values are indicative of how much overall difference can arise between 2LPT and ZA halos, even though the differences may average to zero when considering the entire population. The RMS for both $\Delta M_{\rm vir}$ and Δc starts highest at high redshift—0.19 for $\Delta M_{\rm vir}$ and 0.57 for Δc at z=15—and steadily decreases

throughout the simulation, reaching minimums of 0.11 for $\Delta M_{\rm vir}$ and 0.45 for Δc by z=6.

Additionally, it is of interest to consider the percentage of halo pairs that are "wrong" at some given time, regardless of whether the quantity is higher in 2LPT or ZA. For example, if we count halos outside a slit of $\varepsilon = 10\%$ around $\Delta q = 0$, we find that by z = 6, 14.6% of halo pairs still have substantially mismatched masses, and 74.3% have mismatched concentrations. It is evident that a substantial percentage of halo pairs can have markedly different growth histories, even when there is little or no offset in the ensemble halo population average.

Kurtosis is consistently large for both mass and concentration, with a slight increasing trend throughout the simulation for concentration. It reaches maximum values of 17.5 ± 2.4 at redshift 10 for $\Delta M_{\rm vir}$ and 15.4 ± 1.0 at the end of the simulation at redshift 6 for Δc . Skew is positive for much of the simulation for mass, but is much smaller for concentration. We find average skews of 0.39 ± 0.29 for $\Delta M_{\rm vir}$ and 0.045 ± 0.028 for Δc . These higher moment deviations from Gaussianity hint at the non-linear dynamics at play in halo formation.

The narrow peak and heavy tails of the distribution may indicate a fair amount of sensitivity to initial differences in halo properties, in that halo pairs that start out within a certain range of the mean are more likely move closer to the mean, while pairs that are initially discrepant will diverge even further in their characteristics. This is indicative of the non-linear gravitational influence present during halo evolution, and is further supported by a kurtosis that increases with time.

The skew at high redshift for $\Delta M_{\rm vir}$ may give another hint at the non-linear halo formation process. Runaway halo growth causes more massive halos to favor faster mass accretion and growth. The positively skewed distributions show a picture of 2LPT halo growth in which initial differences in mass are amplified the most readily in the earliest forming and most massive halos, again indicating the extra kick-start to halo growth provided by 2LPT initialization. While the slight decrease in skew with redshift may be counter-intuitive to this notion, it is likely that the large number of newly formed halos begin to mask the signal

from the smaller number of large halos displaying this effect.

III.3.4 Trends with halo mass

We consider $\Delta M_{\rm vir}$ and Δc as a function of average halo mass $M_{\rm vir,avg} = (M_{\rm vir,2LPT} + M_{\rm vir,ZA})/2$ in Figure III.4. The data is binned on a 2-D grid with a logarithmic color map for three representative timesteps. A linear fit to the data is overplotted in red, and a dotted blue line is provided at $\Delta M_{\rm vir} = 0$ and $\Delta c = 0$ to guide the eye.

We find that $\Delta M_{\rm vir}$ tends to increase with increasing $M_{\rm vir,avg}$, a trend that is, again, most pronounced at high redshift. 2LPT halos are consistently more massive than their ZA counterparts, with the difference increasing with average halo mass. While less massive halo pairs have a larger spread in the difference in 2LPT and ZA mass, more massive halo pairs are consistently heavier in 2LPT than in ZA. At redshift 15, the least squares fit to the data produces the fit equation $\Delta M_{\rm vir} = 5.6 \times 10^{-2} M_{\rm vir,avg} - 0.33$. The slope of the fit line trends towards zero as we progress in redshift, with little average mass dependence and a fit of $\Delta M_{\rm vir} = 6.4 \times 10^{-3} M_{\rm vir,avg} - 2.5 \times 10^{-2}$ by z = 6.

We find a small trend for more massive halo pairs to be more concentrated in ZA, but this trend is weaker than for $\Delta M_{\rm vir}$. The fit equations for z=15 and z=6 are $\Delta c=-5.3\times 10^{-2}M_{\rm vir,avg}-0.45$ and $\Delta c=-9.3\times 10^{-3}M_{\rm vir,avg}-8.9\times 10^{-2}$, respectively. The negative slope might be expected, as halo concentration is expected to decrease with increasing mass, at least at later redshift (Neto et al., 2007), and we find high mass halos to be more massive in 2LPT than in ZA. However, the dependence of concentration on mass and redshift at high redshift is more complicated (Klypin et al., 2011; Prada et al., 2012). The data have a larger variance than $\Delta M_{\rm vir}$, and fits have and overall shallower slope. Mass dependence all but disappears by z=6. To reconcile these trends with the symmetrical concentration distributions of Figure III.2, we note that the trends in mass may be hidden by integration across the entire mass range and still result in overall Δc distributions symmetric about zero.

III.3.5 Alternate fractional difference distributions

In Figure III.5, we plot, as functions of redshift, statistics derived from the alternate fractional difference distributions $\Delta' M_{\rm vir}$ and $\Delta' c$ (see Equation III.19). In the left column, we plot the $\Delta' q$ of the peak of the distribution along with the $\Delta' q$ where various percentages of the halo pairs fall at or above $\Delta' q$.

As the $\Delta'q$ value of peak of the distribution is the location of the mode, it represents the most typical halo pair. While concentration differences remain close to zero throughout the simulation, mass difference peak moves from a $\Delta' M_{\rm vir}$ of 8.7×10^{-2} at z=15 to 2.9×10^{-2} at z=6. The 1% of halo pairs with the largest excess 2LPT mass are at least 1.97 times ZA mass at z=15 and 1.45 times ZA mass at z=6. For concentration, the 1% most 2LPT concentrated halo pairs differ by at least a factor of 6.00 at z=15 and 3.73 at z=6.

In the right column of Figure III.5, we plot the fraction of halos f_h that fall outside various $\Delta'q$ values. The solid lines represent halo pairs that have $\Delta'q$ greater than or equal to the listed values, i.e., the fraction of halo pairs where the 2LPT halo has a virial mass or concentration that is at least 1.1, 1.5, 2.0, or 5.0 times that of it's corresponding ZA halo. The dashed lines additionally count halos with $\Delta'q$ at or below the corresponding equivalent displacement (see Equation III.22) and represent the fraction of halo pairs where one halo has a virial mass or concentration at least 1.1, 1.5, 2.0, or 5.0 times that of it's companion, regardless of whether the 2LPT or ZA value is higher.

We find that 50% of halo pairs are at least 10% more massive in 2LPT at z=15. By z=6, this has fallen to 10%. Furthermore, 0.81% are at least twice as massive in 2LPT at z=15, and by z=6, this has only reduced to 0.26%. Halos in 2LPT are at least twice as concentrated as their ZA counterparts for at least 12% of the halo population at z=15 and at least 7.8% of the population by z=6. Halo pairs that are at least 5 times as concentrated in 2LPT make up 1.3% at z=15 and 0.26% at z=6.

When we additionally consider halo pairs that are less than or equal to the equivalent displacement, i.e. pairs where either the 2LPT or ZA halos has the higher mass or concen-

tration, we include an even larger percentage of the population. We find 54% of the halo pairs differ in mass by at least 10% at z=15, with 16% differing by z=6. Halos that are at least twice as massive in either 2LPT or ZA account for 1.1% at z=15 and 0.46% at z=6. Halos that are at least twice as concentrated in either 2LPT or ZA account for 25% at z=15 and 15% at z=6.

III.4 Discussion

As we evolve our DM halo population from our initial redshift to z=6, we find that simulation initialization with 2LPT can have a significant effect on halo population compared to initialization with ZA. The second order displacement boost of 2LPT provides a head start on the initial collapse and formation of DM halos. This head start manifests itself further along in a halo's evolution as more rapid growth and earlier mergers. 2LPT halos are, on average, more massive than their ZA counterparts, with a maximum mean $\Delta M_{\rm vir}$ of $(9.3\pm1.2)\times10^{-2}$ at z=15. The larger mass for 2LPT halos is more pronounced for higher mass pairs, while 2LPT halo concentration is larger on the small mass end. Both mass and concentration differences trend towards symmetry about zero as halos evolve in time, with the smallest difference observed at the end of the simulations at z=6, with a mean $\Delta M_{\rm vir}$ of $(1.79\pm0.31)\times10^{-2}$. Casual extrapolation of our observed trends with redshift to today would indicate that, barring structure like massive clusters that form at high redshift, 2LPT and ZA would produce very similar halo populations by z=0. However, the larger differences at high redshift should not be ignored.

The earlier formation times and larger masses of halos seen in 2LPT-initialized simulations could have significant implications with respect to early halo life during the Dark Ages. Earlier forming, larger halos affect the formation of Pop-III stars, and cause SMBHs to grow more rapidly during their infancy (Holley-Bockelmann et al., 2012). The epoch of peak star formation may also be shifted earlier. This could additionally affect the contribution of SMBHs and early star populations to re-ionization. Larger halos may also influence

studies of the high-z halo mass function, abundance matching, gas dynamics, AGN, clustering, and large scale structure formation.

In these discussions, it is important to note that it is wrong to assume that the ZA halo properties are the "correct" halo properties, even in a statistical sense. While halo mass suggests the most obvious shortcoming of ZA simulations, even properties such as concentration—that show little difference on average between 2LPT and ZA—can have large discrepancies on an individual halo basis. Failure to consider uncertainties in halo properties for high z halos in ZA simulations can lead to catastrophic errors.

We note a few caveats with our simulations and analysis. We did not exclude substructure when determining the properties of a halo, and although this would not change the broad conclusions herein, care must be taken when comparing to works which remove subhalo particles in determining halo mass and concentration. Halo matching is not perfect, as it is based on one snapshot at a time, and may miss count halos due to merger activity and differences in merger epochs. However, we believe this effect to be minor. While we compared ROCKSTAR's output with our own fitting routines and found them to be in good agreement, ROCKSTAR does not provide goodness of fit parameters for its NFW profile fitting and R_s measurements. It also may be debated whether it makes sense to even consider concentration of halos at high redshift which are not necessarily fully virialized.

ROCKSTAR does not provide goodness-of-fit parameters for its internal density profile measurements used to derive concentration, so error estimates for concentration values of individual halos are unknown. Additionally, proper density profile fitting is non-trivial, as the non-linear interactions of numerical simulations rarely result in simple spherical halos that can be well described using spherical bins.

We use a simulation box size of only (10 Mpc)³. This is too small to effectively capture very large outlier density peaks. We would, however, expect these large uncaptured peaks to most affected by 2LPT initialization, so the effects presented here may even be dramatically underestimated. Additionally, a larger particle number would allow us to consider smaller

mass halos than we were able to here, and to better resolve all existing structure. A higher starting redshift could probe the regime where 2LPT initialization contributes the most. It would also be of interest to evolve our halo population all the way to z=0. The addition of baryons in a fully hydrodynamical simulation could also affect halo properties. These points may be address in future studies.

III.5 Conclusion

We analyzed three 2LPT and ZA simulation pairs and tracked the spherical overdensity dark matter halos therein with the 6-D phase space halo finder code ROCKSTAR to compare the effect of initialization technique on properties of particle—matched dark matter halos. This approach allowed us to directly compare matching halos between simulations and isolate the effect of using 2LPT over ZA. In summary, we found the following:

- 2LPT halos get a head start in the formation process and grow faster than their ZA counterparts. Companion halos in 2LPT and ZA simulations may have offset merger epochs and differing nuclear morphologies.
- 2LPT halos are, on average, more massive than ZA halos. At z=15, the mean of the $\Delta M_{\rm vir}$ distribution is $(9.3\pm1.2)\times10^{-2}$, and 50% of 2LPT halos are at least 10% more massive than their ZA companions. By z=6, the mean $\Delta M_{\rm vir}$ is $(1.79\pm0.31)\times10^{-2}$, and 10% of 2LPT halos are at least 10% more massive.
- This preference for more massive 2LPT halos is dependent on redshift, with the effect most pronounced at high z. This trend is best fit by $\Delta M_{\rm vir} = (7.88 \pm 0.17) \times 10^{-3} z (3.07 \pm 0.14) \times 10^{-2}$.
- Earlier collapse of the largest initial density peaks causes the tendency for more massive 2LPT halos to be most pronounced for the most massive halos, especially at high z. We find a trend of $\Delta M_{\rm vir} = 5.6 \times 10^{-2} M_{\rm vir,avg} 0.33$ for z = 15. By z = 6, this has flattened to $\Delta M_{\rm vir} = 6.4 \times 10^{-3} M_{\rm vir,avg} 2.5 \times 10^{-2}$.

- Halo concentration, on average, is similar for 2LPT and ZA halos. However, even by the end of the dark ages, the width of the Δc distribution— $\sigma_{\Delta c} = 0.551 \pm 0.026$ at z = 6—is large and indicative of a significant percentage of halos with drastically mismatched concentrations, despite the symmetrical distribution of Δc . At z = 15, 25% of halo pairs have at least a factor of 2 concentration difference, with this falling to 15% by z = 6.
- There is a slight trend for ZA halos to be more concentrated than 2LPT halos at high mass. We find $\Delta c = -5.3 \times 10^{-2} M_{\rm vir,avg} 0.45$ at z = 15 and $\Delta c = -9.3 \times 10^{-3} M_{\rm vir,avg} 8.9 \times 10^{-2}$ at z = 6. This is not visible in the symmetrical Δc distributions, as the trends are roughly centered about zero and are washed away when integrated across the entire mass range.

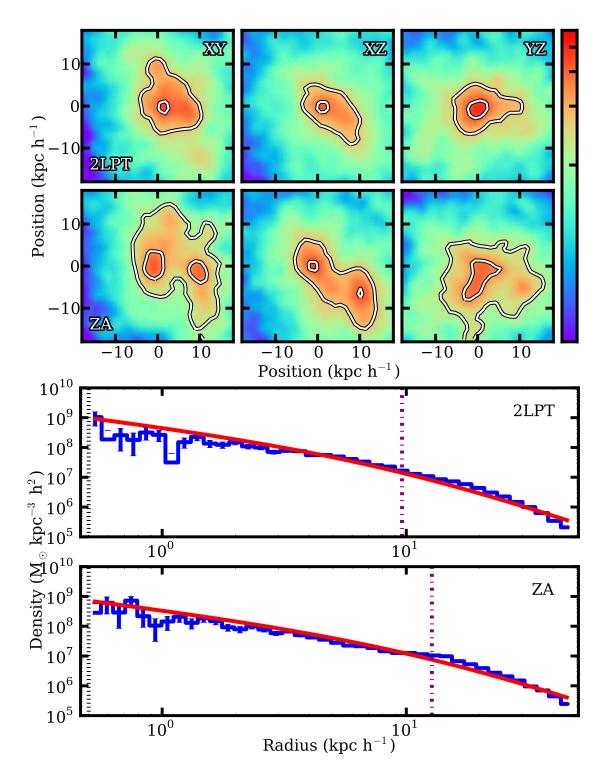


Figure III.1: *Top two rows:* Density projections for two matching halos at z=6. The first and second row are 2LPT and ZA, respectively. The halos appear to be either undergoing or have recently undergone a major merger. The 2LPT halo appears to be more relaxed and further along in the merger process, while the ZA halo lags behind, still displaying two distinct cores. The halos have masses of $5.95 \times 10^9 M_{\odot}$ for 2LPT and $5.85 \times 10^9 M_{\odot}$ for ZA. *Bottom two rows:* Density profiles for the same two halos as above. NFW profiles are fit to logarithmic radial bins of particle position and are overplotted as red curves. The purple dot–dash lines mark the scale radii. The black dotted lines mark the resolution limit of the simulations.

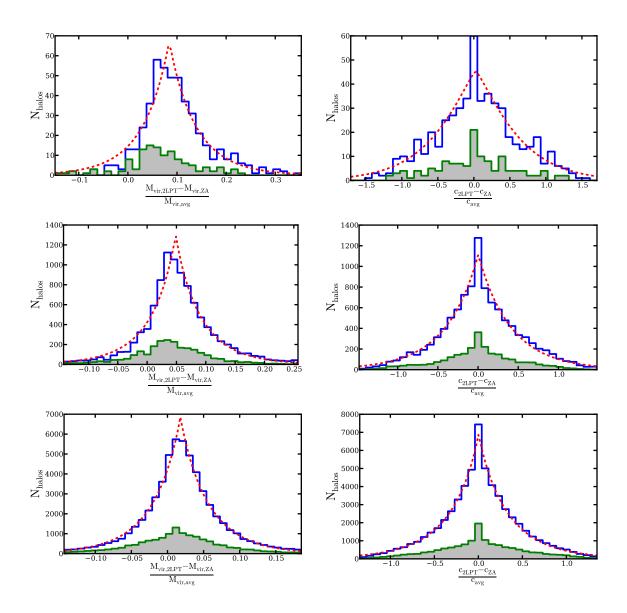


Figure III.2: Histograms of $\Delta M_{\rm vir}$ (left column) and Δc (right column) for snapshots at z=14.7, z=10.3, and z=6.0 (top, middle, and bottom panels, respectively). The small gray-filled histograms count only the top 25% most massive halos. The main histograms are fit with a generalized normal distribution with parameters for mean, scale, and shape, overplotted as the red dashed line (see Equation III.10). The distributions for $\Delta M_{\rm vir}$ have positive means and heavier 2LPT halos, with the most pronounced difference at high redshift. The distributions shown here have means of $(8.4\pm1.8)\times10^{-2}$, $(4.87\pm0.87)\times10^{-2}$, and $(1.79\pm0.31)\times10^{-2}$, respectively. The skew of the distribution is also the most positive at high redshift, and shifts toward symmetry by z=6. The Δc distributions remain symmetric about zero and have negligible skew. The means are consistent with zero, at $(2.6\pm2.7)\times10^{-2}$, $(0.2\pm2.6)\times10^{-2}$, and $(0.3\pm1.1)\times10^{-2}$, respectively. Both distributions have excess kurtosis consistently larger than that of a standard Gaussian distribution, with a sharp peak and heavy tails.

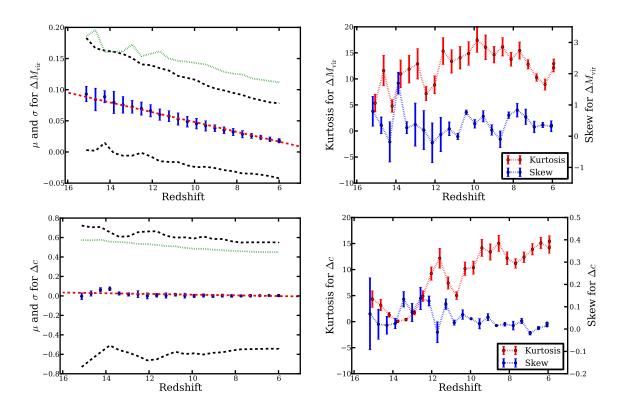


Figure III.3: Mean, standard deviation, and RMS (*left column*) and skew and excess kurtosis (*right column*) as functions of redshift for $\Delta M_{\rm vir}$ (*top row*) and Δc (*bottom row*). In the left column, μ is plotted as blue points, and $\mu \pm \sigma$ is plotted as the black dashed line, and RMS values are plotted as a green dotted line. The red dashed line is a linear fit to the mean. We find a significant trend for μ for $\Delta M_{\rm vir}$ to be more positive at higher redshift and gradually shift toward zero as the simulation progresses, with a fit function of $\mu_{\Delta M_{\rm vir}} = (7.88 \pm 0.17) \times 10^{-3} z - (3.07 \pm 0.14) \times 10^{-2}$. The mean for Δc , however, remains at or very near zero for most of the simulation and is fit by $\mu_{\Delta c} = (3.62 \pm 0.95) \times 10^{-3} z - (2.34 \pm 0.84) \times 10^{-2}$. The $\Delta M_{\rm vir}$ and Δc distributions narrow over time, with a slight decrease in σ . In the right column, we plot skew (blue line) and excess kurtosis (red line). Skew is positive for much of the simulation for $\Delta M_{\rm vir}$, but is much smaller for Δc . Kurtosis is large (much more peaked than Gaussian) for both $\Delta M_{\rm vir}$ and Δc throughout much of the simulation, and especially at later redshift.

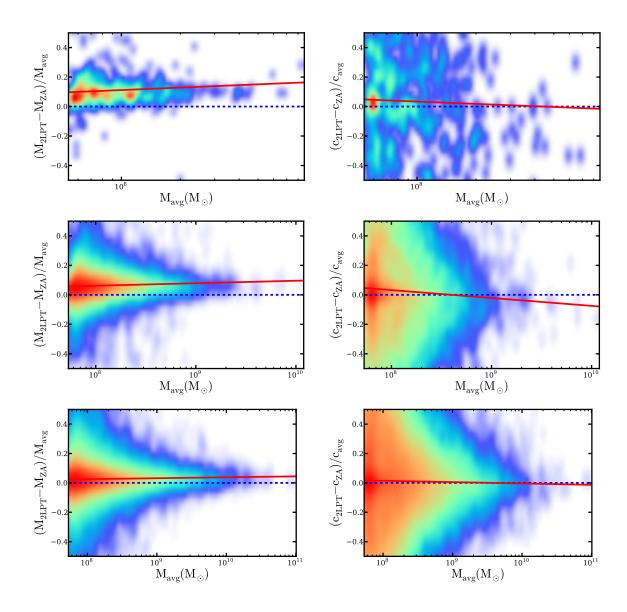


Figure III.4: $\Delta M_{\rm vir}$ (left column) and Δc (right column) as functions of $M_{\rm vir,avg}$. Halos are counted in 2-D rectangular bins and smoothed with a Gaussian kernel with a logarithmic color scale. The red line is the least-squares best fit to the data. The blue dashed line at zero is provided to guide the eye. The three rows again correspond to snapshots at z=14.7, z=10.3, and z=6.0. We again see the overall offset for positive $\Delta M_{\rm vir}$ as before, and additionally find that more massive halo pairs are more likely to have even larger $\Delta M_{\rm vir}$, especially at high redshift. Fit equations for the left column panels are $\Delta M_{\rm vir}=5.6\times10^{-2}M_{\rm vir,avg}-0.33$, $\Delta M_{\rm vir}=1.7\times10^{-2}M_{\rm vir,avg}-7.3\times10^{-2}$, and $\Delta M_{\rm vir}=6.4\times10^{-3}M_{\rm vir,avg}-2.5\times10^{-2}$, respectively. Concentration show a small but opposite trend for more massive halos to be more concentrated in ZA than in 2LPT. The right column panels have fit equations $\Delta c=-5.3\times10^{-2}M_{\rm vir,avg}+0.46$, $\Delta c=-4.5\times10^{-2}M_{\rm vir,avg}+0.46$, and $\Delta c=-9.3\times10^{-3}M_{\rm vir,avg}+8.9\times10^{-2}$, respectively.

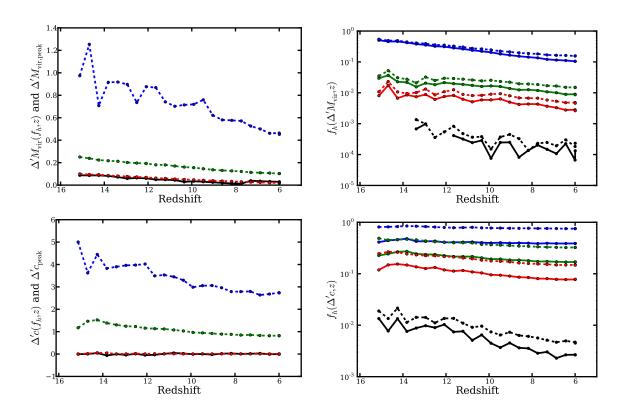


Figure III.5: Fractional error distributions statistics for $\Delta' M_{\rm vir}$ (top row) and $\Delta' c$ (bottom row) as functions of redshift. Left column: The $\Delta' q$ of the peak of the distribution (black line), and the $\Delta' q$ where 50% (red dashed line), 10% (green dashed line), and 1% (blue dashed line) of the halos fall at or above $\Delta' q$. As with distributions of $\Delta M_{\rm vir}$, $\Delta' M_{\rm vir}$ has the largest positive displacement at high redshift and steadily decreases throughout the simulation. Additionally, $\Delta' c$ maintains a peak near zero and has a spread much larger than that of $\Delta' M_{\rm vir}$. Right column: The fraction of halos with $\Delta' q$ greater than 0.10 (solid blue line), 0.50 (solid green line), 1.00 (solid red line), and 4.00 (solid black line). The dashed lines additionally count halo pairs with $\Delta' q$ lower than the corresponding equivalent displacements of -0.09, -0.33, -0.50, and -0.80, respectively (see Equation III.22). We find that 50% of 2LPT halos are at least 10% more massive than their ZA companions at z = 15, reducing to 10% by z = 6. Halos in 2LPT are at least twice as concentrated for 12% of halos at z = 15 and 7.8% of halos at z = 6.

CHAPTER IV

Supermassive Black Holes and Their Hosts

IV.1 Introduction

The study of the evolution of galaxies and the growth of the supermassive black holes at their cores go hand in hand. Although the typical length scales for the two can vary by many orders of magnitude, they seem inexorably linked. Observational correlations between galaxy and supermassive black hole properties hint at an underlying co-evolution driven by shared mechanisms.

IV.1.1 Galaxy Properties

How do we describe a galaxy? Being extended, resolvable objects, galaxies provide a unique wealth of observable characteristics not obtainable from point sources such as stars. While many characteristics can be deduced about point sources, the actual observations themselves come down to measuring position on the sky and measuring flux as a function of frequency and time. From this information, all that we know about stars and other point sources, such as temperature, age, size, and composition, can be inferred. However, for extended objects like galaxies, we are given more to work with.

IV.1.1.1 Color

A galaxy's color is determined by its stellar component. While a galaxy in itself may be resolvable, for all but the most nearby of galaxies, individual stars are not. What we see when looking at a particular small section of a galaxy is the averaged-together light from stars in that section.

Broadly, bluer late-type spirals have a u-r color of around 1.3-2.0, while redder early-type galaxies have a u-r color of around 2.3-2.7. The color of a galaxy can be a good indicator for its age and evolutionary stage. Star formation processes generally tend

to produce many smaller, cooler, redder stars and fewer larger, hotter, bluer stars. These small, cool stars are much longer-lived than their massive counterparts, while the large, warm stars are much brighter. After star formation turns off, the short-lived blue stars begin to die off, and the galaxy becomes redder, as more of the fraction of total light comes from the red end of the population.

IV.1.1.2 Morphology

The extended nature of galaxies allows us to observe their morphology. The classification scheme originally devised by Hubble (1926) places galaxies into the four broad categories: elliptical, spiral, lenticular, and irregular. Elliptical galaxies tend to be larger, redder, have less gas, and dominated by more radial orbits. Spiral galaxies tend to be smaller, bluer, have more gas, and have more of a disk component. Spirals can have a number or arms, a central bulge, and a central bar. Lenticular galaxies are middle-of-the-road galaxies, with both a strong central bulge like an elliptical, and an extended disk like a spiral, however without spiral arms. Irregular galaxies tend to defy this simple classification scheme, and can be found in any number of configurations.

Figure IV.1 is a cartoon of the classification scheme. To the left of the diagram are elliptical galaxies. The subcategories are an indication of the shape of the galaxy, with the most spherical on the left and progressing to more flattened shapes to the right. On the right of the diagram are spiral galaxies. These are broken into two branches, based on whether or not the galaxy contains a central bar. Moving from right to left, the spiral arms of the galaxies become more tightly wound, and the central bulges become more dominant. At the center of the diagram where the spiral fork meets the elliptical line, lie lenticular galaxies. Irregular galaxies are, as the name would imply, irregular and do not fall on the diagram.

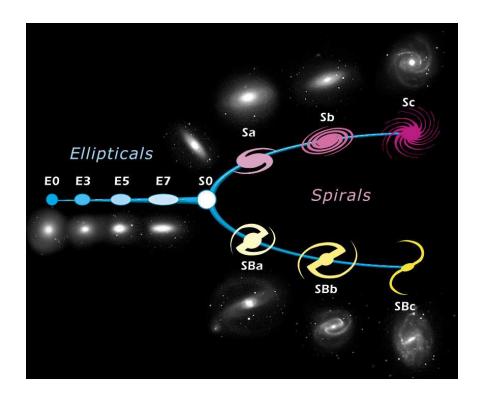


Figure IV.1: The Hubble tuning fork. On the left of the diagram are elliptical galaxies. E0 galaxies are the most spherical, while E7 are the most flattened or elongated. S0 are lenticular galaxies. The top branch on the right are spiral galaxies with no bar, while the bottom right branch are spiral galaxies with a bar. Both progress from tightly wound spiral arms and large bulges to loosely wound spiral arms and small to no bulges, going from Sa to Sc or SBa to SBc.

IV.1.2 Supermassive Black Hole Properties

A non-merging black hole, much like an elementary particle, can be described simply by its mass, charge, and spin. Its effect on its local spacetime, infalling matter, and surrounding environment all come back to these three parameters. However, determination of these parameters and the study of how black holes interact with their surroundings can be quite involved.

Black holes are, by their very nature, black, and difficult to observe. We cannot see light emitted directly from a black hole as we would a star, since a black hole is defined as an object massive and compact enough to not allow light within its event horizon to escape. We are forced, therefore, to employ other methods of measuring black holes.

Thus far, the majority of progress in the measurement of black hole properties has been in measuring mass. There are a number of ways to measure the mass of a black hole. Here, we will briefly discuss masers, stellar dynamics, gas dynamics, and reverberation mapping as methods of measuring a supermassive black hole's mass.

Astrophysical masers are sources of stimulated spectral line emission in the microwave band formed in regions of high-density gas comprised of molecules such as hydroxyl, formaldehyde, and water (Lo, 2005). Since the emission frequencies of these sources are very well constrained, high-accuracy Doppler shifts can be determined. These Doppler shifts can then be used to determine velocities for the masers, and thus how much mass is enclosed by their orbits. If these masers lie very close to the supermassive black hole (SMBH) in the center of their galaxy, the enclosed mass can be constrained to be primarily that of the SMBH.



Figure IV.2: Maser orbits fit to a warped disk for NGC4258. Masers can also be useful for distance determinations. Here, the positions and velocities of water masers are able to be fit to a warped disk model surrounding a supermassive black hole. This allows the interpolation of physical radii away from the black hole, giving us both the black hole mass and an standard ruler to allow precise determination of the distance to NGC4258. (Herrnstein et al., 1999)

Stellar dynamics and gas dynamics both probe light coming from matter near the black hole. The width of broadened spectral lines from either the stars or gas can be used to determine a velocity dispersion for the matter local to the SMBH. This velocity dispersion, therefore, can then be used to determine the potential through which the matter is traveling, and thus the mass of the black hole.

A special case of stellar dynamics for which the orbits of the constituent stars can be resolved—namely, for the case of our own Milky Way—adds another dimension to our knowledge of the stellar orbits. Over time, we can observe the proper motion on the sky for these orbits. Combining these measurements with Doppler measurements for radial

velocity yields full orbital solutions. Then, it simply requires Kepler's laws to determine the mass of the SMBH.

Reverberation mapping can be thought of as "echo-mapping" the gas disk around a SMBH. Continuum emission very near the black hole travels outward and stimulates broad line emission in surrounding gas. Any changes in the continuum emission will take time to propagate to the broad line region, since the speed of light is finite. By measuring the timing difference in the change in continuum emission and change in stimulated broad line emission, the physical distance from the SMBH to the broad line region can be inferred. With this radius, and the velocity of the gas in the broad line region measured by the width of the broadened lines, a black hole mass can be determined (Blandford & McKee, 1982).

IV.1.3 Correlations

Correlations between varying properties of galaxies and black holes can provide much deeper insight into the dynamics that shape the evolution of both. Of particular interest here are the fundamental plane of elliptical galaxies, the $M-\sigma$ relation, and the green valley-AGN relation.

IV.1.3.1 The M-Sigma Relation

If we consider the all the observable properties of a galaxy and compare them to the mass of its SMBH, the tightest correlation can be found with the velocity dispersion σ of the galaxy's bulge. Such a tight correlation is surprising, as the sphere of influence of a typical SMBH does not extend much past order a few pc, while bulges exist on scales of a kpc or greater. In essence, the supermassive black hole and the outer edges of the bulge shouldn't "feel" each other. Nevertheless, the correlation is indeed there, suggesting some mechanism that influences—or is influenced by—both of them. Gültekin et al. (2009) use a sample of 49 M_{BH} measurements and 19 upper limits to measure this correlation, and find $\log(M_{BH}/M_{\odot}) = \alpha + \beta \log(\sigma/200 \text{ km s}^{-1})$ with $(\alpha, \beta, \varepsilon_0) = (8.12 \pm 0.08 M_{\odot}, 4.24 \pm 0.41 M_{\odot}, 0.44 \pm 0.06 M_{\odot})$ for all galaxies and $(\alpha, \beta, \varepsilon_0) = (8.23 \pm 0.08 M_{\odot}, 3.96 \pm 0.42 M_{\odot}, 0.31 \pm 0.08 M_{\odot})$

$0.06M_{\odot}$) for ellipticals, where ε_0 is the intrinsic scatter in the relation.

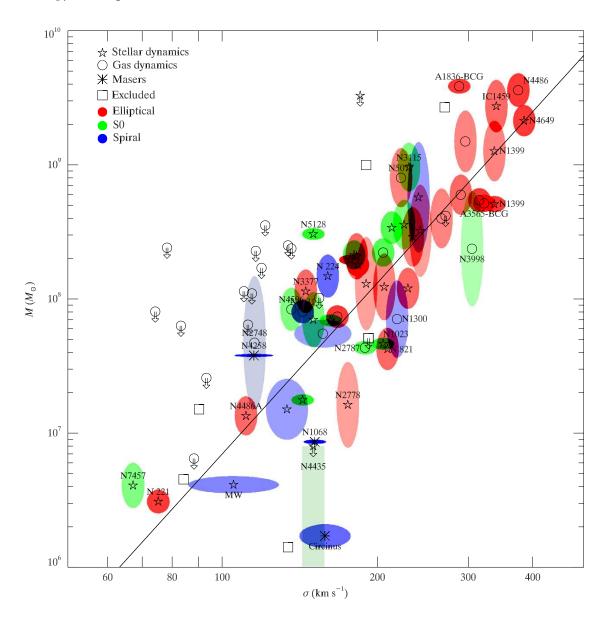


Figure IV.3: The M- σ relation for galaxies with dynamical measurements. Black hole mass is plotted vs velocity dispersion of its host spheroid. The symbols represent the method by which the black hole mass was measured: pentagrams for stellar dynamics, circles for gas dynamics, and asterisks for masers. Upper limits are given by arrows. Error ellipses are colored by galaxy type, with red for ellipticals galaxies, green for lenticular galaxies, and blue for spiral galaxies. The saturation of the color is inversely proportional to the area of the ellipse. For this sample, the best fit relation is $M_{BH} = 10^{8.12} \text{ M}_{\odot} (\sigma/200 \text{ km s}^{-1})^{4.24}$. Galaxies not included in this fit are labeled as squares. (Gültekin et al., 2009)

IV.1.3.2 The Fundamental Plane

While not a direct correlation with the properties of supermassive black holes, the fundamental plane of elliptical galaxies offers insight into the characteristics of their hosts. The fundamental plane is a three-parameter correlation between properties of elliptical galaxies: velocity dispersion, effective radius, and surface brightness. This correlation (Figure IV.4) between these three parameters is tighter than the combination of any two alone (Djorgovski & Davis, 1987). The fit for this correlation can be given as $\log R_e = 0.36(\langle I \rangle_e/\mu_B) + 1.4\log \sigma_0$, where R_e is the effective radius in kpc, $\langle I \rangle_e$ is the mean surface brightness interior to R_e in units of μ_B , and σ_0 is the velocity dispersion in km s⁻¹ (Binney & Merrifield, 1998).

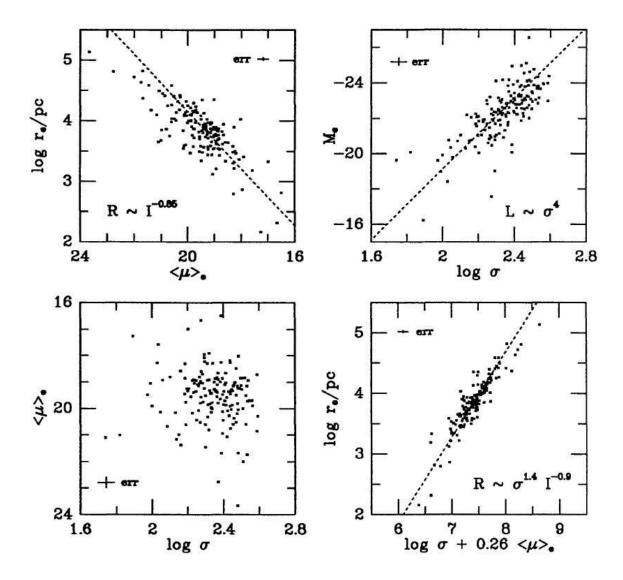


Figure IV.4: The fundamental plane for elliptical galaxies. *Top panels:* The top panels show the one-parameter scaling relations, with the relation between radius and mean surface brightness on the left and the relation between luminosity and velocity dispersion (the Faber-Jackson relation) on the right. *Bottom left:* The relation between the surface brightness and velocity dispersion. This is an almost face-on view of the fundamental plane. *Bottom right:* The relation between the effective radius and the combination of surface brightness and velocity dispersion. This is the edge-on view of the fundamental plane. (Kormendy & Djorgovski, 1989)

IV.1.3.3 The Green Valley

When considering both the color and stellar mass of a galaxies, a correlation emerges where many galaxies lie in either the "blue cloud" of bluer, lower mass galaxies, or the "red sequence" of redder, generally higher mass galaxies. The area between these two is known as the "green valley" and, while not as populated as the blue cloud or red sequence, holds special interest when active galactic nuclei (AGN) are considered. AGN are very luminous regions at the centers of some galaxies. Schawinski et al. (2010) show that galaxies falling on the green valley are much more likely to host AGN than galaxies on the blue cloud or red sequence, hinting at an underlying link between the evolution of galaxies, and the activity at their centers.

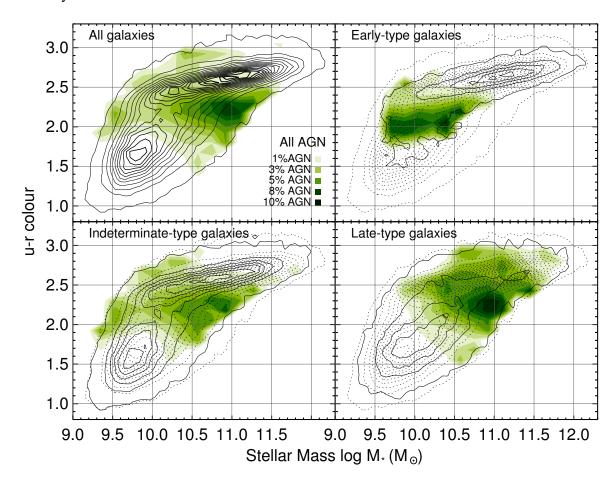


Figure IV.5: Distribution of the fraction of galaxies containing AGN. Galaxy color in u-r is plotted vs stellar mass. The contours are the galaxy population for all galaxies (top-left), early-type galaxies (top right), intermediate-type galaxies (bottom left), and late type galaxies (bottom right). For the three sub-samples, dotted contours represent the full sample for comparison. The green shaded contours represent the fraction of galaxies in that subsample that contain active galactic nuclei. It can be clearly seen that the AGN fraction is highest for galaxies falling within the green valley. (Schawinski et al., 2010)

IV.2 Galaxy Evolution

IV.2.1 Dark Matter Halos

Every galaxy resides inside a dark matter halo. Often about an order of magnitude larger in both radius and mass than the baryonic component, dark mater halos dominate the large-scale behavior of galaxies. Dark matter is matter that is thought to interact very weakly or not at all with light and ordinary matter, except gravitationally. Evidence for dark matter comes from a number of sources, including the relatively flat rotational velocity curve of galaxies, the velocity dispersion of galaxies, gravitational lensing measurements, galaxy clustering, and the offset between the gas and dominant mass measured in the Bullet cluster. Here we will briefly discuss the evidence from flat rotation curves.

If there were no dark matter component and only the baryonic components (i.e. stars and gas) contributed to the galactic potential, we would expect the rotational velocity of galaxies to fall off with radius. However, observations show that the rotation curve remains relatively flat (Rubin et al., 1980). Figure IV.6 shows several observed rotation curves.

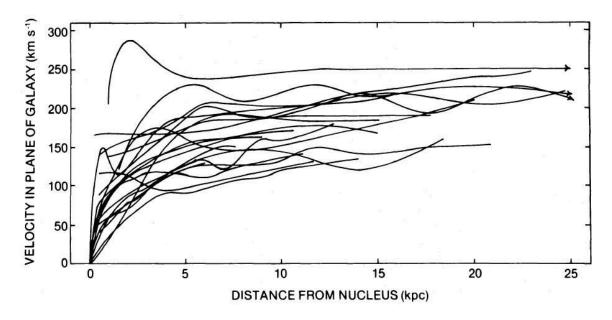


Figure IV.6: Rotation curves for 21 Sc galaxies. It is readily identifiable that the rotation curves do not fall off as would be expected for galaxies without a dark matter component. (Rubin et al., 1980)

Navarro et al. (1997b) found that dark matter halos generally follow the same density

profile, regardless of mass. This universal dark matter density profile can be given as

$$\rho(r) \propto \frac{1}{(r/a)(1+r/a)^2},\tag{IV.1}$$

where a is the radius where the profile transitions from an r^{-1} power law to an r^{-3} power law.

IV.2.2 Galaxy Mergers

Galaxy mergers are the fundamental mechanism by which galaxies grow and evolve. Collisions between galaxies trigger processes that can alter nearly all the properties of the galaxies. Naturally, mergers increase the mass of galaxies. Starting from small perturbations in the early universe, gravity slowly pulls matter together to form larger and larger clumps. These clumps of gas and dark matter eventually form stars, beginning what we think of as typical galaxies, and over time, these galaxies merge together into larger and larger galaxies.

Mergers affect many other properties of galaxies as well. Mergers distort the shapes of galaxies, causing long tidal tails to form and the entire morphology to appear irregular. The disk structures of spiral galaxies that form from the settling of the rotational component are distorted and "puffed up" into components with ever increasing bulge-like properties.

Mergers can trigger wide-scale starburst events, where a large portion of gas goes into the formation of stars. Much of the gas component of the galaxy can subsequently be blown out by the winds from the supernovae of short-lived O and B stars. This shuts off star formation, and as the stellar population is no longer replenished with new high-mass stars, the galaxy becomes progressively redder as large stars die.

The general trend is for mergers to move galaxies from the right side of the Hubble tuning fork towards the left, turning blue, gas rich spirals into red, gas poor ellipticals. This process is aided by the AGN feedback also triggered during galaxy mergers, as we discuss in the following section.

IV.3 Supermassive Black Hole Growth

Supermassive black holes grow by two primary mechanisms, binary mergers and gas accretion. Through a combination of these, black holes can grow to as large as $\sim 10^9$ – $10^{10}~{\rm M}_{\odot}$ by z=0.

IV.3.1 Binary Mergers

When two galaxies merge, the supermassive black holes at their hearts begin a process that will eventually lead to their coalescence. There are generally thought to be three stages to this journey. First, the black holes sink towards the center of the merged galaxy through mass segregation and dynamical friction until they form a bound orbit with each other. Then, the black holes tighten their orbit through three-body scattering of nearby stars. Finally, as the black holes become close enough together for general relativistic effects to come into play, gravitational waves are emitted and radiate away the remaining orbital energy until the binary coalesces.

IV.3.1.1 Dynamical Friction and Inspiral

During the majority of the inspiral process, the black holes do not "feel" each other's gravitational pull. Instead, interactions with the galaxy itself push the holes together.

As it travels through a galaxy, a black hole—or any massive body—is slowed by the surrounding field of matter. Gravitational attraction pulls surrounding matter toward the black hole. However, as the black hole is moving with respect to the local medium, the attracted particles will tend to fall behind the black hole. This creates a wake of overdensity that gravitationally attracts the black hole from behind and slows its velocity. Chandrasekhar (1943) develops this notion of dynamical friction for the motion of a star through a sea of other stars. If the distribution of velocities of the surrounding particles is Maxwellian, the acceleration on the black hole can be written as

$$\frac{d\mathbf{v}_{M}}{dt} = -\frac{4\pi G^{2}M\rho \ln \Lambda}{v_{M}^{3}} \left[\operatorname{erf}(X) - \frac{2X}{\sqrt{\pi}} e^{-X^{2}} \right] \mathbf{v}_{M}, \tag{IV.2}$$

where \mathbf{v}_M is the velocity of the black hole, M is it's mass, ρ is the density of surrounding matter, erf is the error function, $\ln \Lambda$ is the Coulomb logarithm, and $X \equiv v_M/(\sqrt{2}\sigma)$ where σ is the velocity dispersion of the surrounding medium (Binney & Tremaine, 1988). As the black hole is slowed by dynamical friction, it loses angular momentum and sinks towards the center of the galaxy's potential well.

IV.3.1.2 The Final Parsec Problem

Dynamical friction and mass segregation can only take us so far. Once the black holes are close enough together, they form a bound binary orbit. This generally occurs for separations of around a few to tens of parsecs. This presents a problem, however, since the orbit needs to shrink to around 10^{-2} – 10^{-3} pc in order for gravitational wave emission to remove energy from the orbit in a significant amount. The orbit can be tightened with three-body scattering of stars that wander through the orbit of the binary, however, in the spherical galaxies where mergers often take place, there is a depletion of stars with orbits that intersect the binary. Khan et al. (2011), however, show that the non-spherical, triaxial potential typical of postmerger galaxy remnants can efficiently funnel stars through the orbit of the black hole binary with sufficient intensity to tighten the binary orbit to the gravitational wave regime.

IV.3.1.3 Gravitational Waves and Recoil Kicks

Once the black hole binary separation reaches the point where strong field general relativistic effects come into play, we no longer require external influences to nudge the black holes together. In the final plunge toward coalescence, the black hole binary sheds energy through emission of gravitational radiation. As energy is radiated away, the binary tightens its orbit until the two black holes merge into one. Following this coalescence, the resultant black hole undergoes a "ringdown" phase, in which the distorted space time settles back down into a black hole that can again be simply described by mass, charge, and spin.

The emission of gravitational waves has two interesting consequences. First, the radiation from two merging supermassive black holes is extremely loud, and can potentially provide an observational signature of the process for gravitational wave observatories. Second, the gravitational waves carry linear momentum, leading to a recoil "kick" imparted to the black hole merger remnant.

Recent advances in numerical relativity simulations have provided a much deeper insight into the black hole binary merger process than has been previously available. Waveforms produced from these simulations (Figure IV.7) can be used to predict what gravitational wave observatories such as LIGO and LISA would expect to observe for signals originating from merging supermassive black hole binaries. Having these waveforms as templates for comparison to data can greatly increase the signal to noise ratio for these detectors, potentially allowing the gravitational wave events to be seen among the sea of noise. These waveforms produced from simulations of the last few orbits of inspiral through the merger and ringdown can be combined with waveforms suggested from post-Newtonian approximations for the longer duration inspiral to provide a complete extended signal to match against.

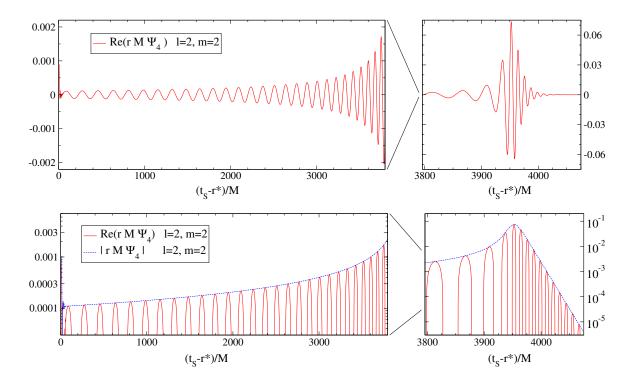


Figure IV.7: Gravitational waveform for an equal-mass, non-spinning black hole binary merger. This is the final waveform, extrapolated to infinity, from the numerical relativity simulation of Scheel et al. (2009). The waveform is shown on the top panel with a linear y-axis and on the bottom panel with a logarithmic y-axis. The left panels are the earlier stages of inspiral, and the right panels show the merger and ringdown stages.

For asymmetric mergers, gravitational radiation is emitted anisotropically. This causes a recoil kick, in which the gravitational waves impart a net velocity to the final black hole with respect to the original center of mass. The magnitude and direction of this kick are dependent on the mass ratio of the binary and the spins of the two black holes—in all, a 7-dimensional parameter space. This large parameter space has been largely explored with numerical relativistic simulations, and analytic equations can be fit to the data to predict the recoil from a given merger configuration. Holley-Bockelmann et al. (2008), give these equations as

$$\mathbf{v}_{kick} = (1+e) \left[\hat{\mathbf{x}} \left(v_m + v_{\perp} \cos \xi \right) + \hat{\mathbf{y}} v_{\perp} \sin \xi + \hat{\mathbf{z}} v_{\parallel} \right], \tag{IV.3}$$

where

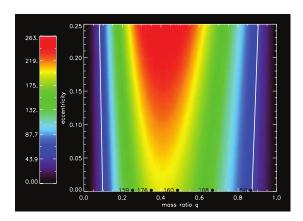
$$v_m = A \frac{q^2 (1-q)}{(1+q)^5} \left[1 + B \frac{q}{(1+q)^2} \right],$$
 (IV.4)

$$v_{\perp} = H \frac{q^2}{(1+q)^5} \left(\alpha_2^{\parallel} - q \alpha_1^{\parallel} \right),$$
 (IV.5)

$$v_{\parallel} = K\cos\left(\Theta - \Theta_0\right) \frac{q^2}{\left(1 + q\right)^5} \left(\alpha_2^{\perp} - q\alpha_1^{\perp}\right). \tag{IV.6}$$

Here, the fitting constants are $A=1.2\times 10^4$ km s⁻¹, B=-0.93, $H=(7.3\pm 0.3)\times 10^3$ km s⁻¹, and $K=(6.0\pm 0.1)\times 10^4$ km s⁻¹. The \hat{z} unit vector is in the direction of the orbital angular momentum, and \bot and \Vert refer to components perpendicular and parallel to \hat{z} , respectively. The fitting parameters are the eccentricity e, the mass ratio $q\equiv M_2/M_1$, and the reduced spin parameters $\alpha_i\equiv S_i/M_i^2$ where S is the spin angular momentum. The orientation of the merger is given by the angles Θ , Θ_0 , and ξ (Holley-Bockelmann et al., 2008).

Slices through this parameter space are shown in Figure IV.8. For certain configurations of the merger, the recoil velocity can be very high. Very asymmetric mergers can produce recoils as high as $\sim 4000 \ \rm km \ s^{-1}$. These large recoils can be enough for the black hole to escape the potential well of its host galaxy and be ejected. Even less extreme recoil kicks can affect the evolution of black holes, as the kicked black hole can oscillate about its host's center, potentially changing its local gas environment and accretion rate.



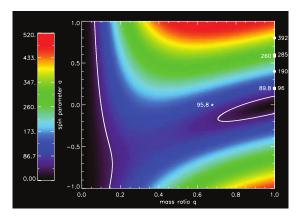


Figure IV.8: *Left:* Gravitaional wave recoil velocity from a merger of nonspinning black holes as a function of eccentricity and mass ratio. Data from numerical relativity simulations (González et al., 2007) are overlaid along the zero eccentricity line. The overlaid white contours are the escape velocity of a typical globular cluster, 50 km s⁻¹. *Right:* Gravitational wave recoil kick velocity as a function of spin parameter and mass ratio for a merger of spinning black holes on a circular orbit with spins perpendicular to the orbital plane of the binary and anti-aligned with each other. Again, the 50 km s⁻¹ escape velocity of a globular cluster is overlaid as white contours. Results from numerical relativity simulations are over-plotted: squares for Koppitz et al. (2007), cirlces for Herrmann et al. (2007), and star for Brügmann et al. (2004). (Holley-Bockelmann et al., 2008)

IV.3.2 Accretion

Although mergers play an important role in the evolution of supermassive black holes, gas accretion can often dominate in terms of mass growth. Gas can fall into a black hole in a number of ways. Here, we will discuss accretion onto a moving black hole, spherical accretion onto a stationary black hole, and disk accretion onto a stationary black hole.

IV.3.2.1 Bondi-Hoyle-Lyttleton Accretion

Let us first consider a massive object, in this case our black hole, moving through a uniform density gas medium. Just as in the case of dynamical friction, particles close enough to the black hole will feel a gravitational attraction, causing them to move toward the black hole. As they move closer, the black hole is also moving through the medium, causing the gas particles to focus behind the black hole. As the particle stream reaches the wake directly

behind the black hole, it collides with opposing streams, causing the angular momentum to go to zero. If these particles are bound, they will proceed to fall onto the black hole. Hoyle & Lyttleton (1939) derive an impact parameter for which particles will be accreted,

$$\sigma < \sigma_{HL} = \frac{2GM}{v_{\infty}^2},\tag{IV.7}$$

and a mass accretion from the wake column at a rate of

$$\dot{M}_{HL} = \pi \sigma_{HL}^2 v_{\infty} \rho_{\infty} = \frac{4\pi G^2 M^2 \rho_{\infty}}{v_{\infty}^3},\tag{IV.8}$$

where v_{∞} and ρ_{∞} are the velocity and density far away from the black hole, respectively. Expanding upon this analysis, Bondi & Hoyle (1944) suggest that the accretion rate should rather be

$$\dot{M}_{BH} = \frac{2\alpha\pi G^2 M^2 \rho_{\infty}}{v_{\infty}^3},\tag{IV.9}$$

where α is a constant between 1 and 2, with a typical value of around 1.25.

For an accretor at rest in an isotropic gas medium, one would expect accretion to be a spherical process. Bondi (1952) considers this configuration, and finds the accretion rate for this "temperature-limited" case to be

$$\dot{M}_{Bondi} = \frac{2\pi G^2 M^2 \rho_{\infty}}{c_{s,\infty}^3},\tag{IV.10}$$

where $c_{s,\infty}$ is the speed of sound far away from the black hole.

Extrapolating between this result and the "velocity-limited" case of Equation IV.9 suggests (Bondi, 1952)

$$\dot{M}_{BH} = \frac{2\pi G^2 M^2 \rho_{\infty}}{\left(c_{s,\infty}^2 + v_{\infty}^2\right)^{3/2}}$$
(IV.11)

as an order of magnitude estimate of the more general case of accretion. Numerical simulations (Shima et al., 1985) suggest an additional factor of 2 is needed for better agreement

with simulation results, giving us a generally applicable from for the accretion rate,

$$\dot{M}_{BH} = \frac{4\pi G^2 M^2 \rho_{\infty}}{\left(c_{s,\infty}^2 + v_{\infty}^2\right)^{3/2}}.$$
 (IV.12)

IV.3.2.2 Disk Accretion and Active Galactic Nuclei

Active galactic nuclei play a fundamental role in the evolution of both supermassive black holes and their host galaxies. As gas falls in to a black hole in the center of a galaxy, its angular momentum forces it into an accretion disk. As matter moves towards the SMBH, it transfers its gravitational potential energy to thermal energy. For accretion disks around supermassive black holes, this can cause the disk to emit large amounts of electromagnetic radiation (Lin & Papaloizou, 1996).

This emitted radiation is important in a number of ways. Most critical to the SMBH itself is the radiation pressure exerted on infalling matter. This radiation pressure sets an upper limit on the rate of accretion, as there is a point where the force from emitted radiation balances the force of gravity for infalling gas (Rybicki & Lightman, 1979). This limit, known as the Eddington limit, is given by

$$L_{Edd} = 4\pi GM cm_H/\sigma_T = 1.25 \times 10^{38} \text{erg s}^{-1} (M/M_{\odot}),$$
 (IV.13)

where c is the speed of light, m_H is the mass of hydrogen, and σ_T is the Thompson cross section.

The radiation given off by the accretion disk affects galactic properties as well. Powerful AGN can strip away gas from the center of the galaxy, halting star formation. This can quickly change a galaxy from a blue, gaseous, star forming galaxy into one that is red, dry, and dead.

IV.4 Conclusion

We have seen that galaxies and the supermassive black holes at their centers both have their most dramatic periods of evolution around the same time. Galaxy mergers grow both the galaxy and the SMBH. Galaxies grow and become more elliptical as mergers bring in additional mass on orbits that can disrupt their gaseous disks. These mergers also bring in counterpart supermassive black holes that fall toward the center of the galaxy and merge with the central SMBH, while also triggering accretion events and AGN feedback that pump energy back into the galaxy, shutting off star formation.

IV.4.1 Correlations

In light of these shared growth mechanisms, the correlations mentioned in Section IV.1 begin to move from a purely observational coincidence to a natural result of co-evolution. The $M-\sigma$ relation is a natural byproduct of the simultaneous growth of supermassive black holes and their galaxies during merger events. The mass of the SMBH increases due to the merging of binary companions and increased levels of accretion, while the host mass, and thus velocity dispersion, increases due to the infalling galaxy itself. Likewise, the overabundance of AGN in galaxies lying in the green valley is the consequence of simultaneous change. Mergers both trigger highly luminous AGN feedback and cause an inexorable shift from the blue cloud, through the green valley, to the red sequence. Even the increase in scatter of the $M-\sigma$ relation at low masses can be explained by the galaxies having lower mass, and therefore being more likely to allow a gravitational wave recoil kicked black hole of a given velocity to escape.

IV.4.2 Open Questions

In the end, there remain a number of open questions. How can very large supermassive black holes form so early? What is dark matter actually made of? How do galaxies retain their black holes if merger recoils can kick them with velocities greater than the escape velocity of the galaxy? Over what range are our correlations truly valid? These are just

some of the questions that are currently being investigated, and promise to provide a rich field of study for years to come.

CHAPTER V

Conclusion

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Appendices

Appendix A

ROCKSTAR Configuration and Execution

A.1 Single Node Configuration File (Text)

```
2 #Parallel config file for multi-cpu, multi-snapshot halo finding
3 #Note that periodic boundary conditions are assumed for NUM_WRITERS > 1.
4 #See README for details.
 6 #Once compiled ("make"), run Rockstar server as
 7 # ./rockstar -c parallel.cfg
8 #Then launch the reading/analysis tasks with:
9 # ./rockstar -c auto-rockstar.cfg
10 #You will have to launch at least NUM_BLOCKS+NUM_WRITERS processes.
12 FILE_FORMAT = "GADGET2" # or "ART" or "ASCII"
13 PARTICLE_MASS = 0
                                 # must specify (in Msun/h) for ART or ASCII
15 # You should specify cosmology parameters only for ASCII formats
16 # For GADGET2 and ART, these parameters will be replaced with values from the
17 # particle data file
18 SCALE_NOW = 1
19 h0 = 0.7
20 01 = 0.73
21 \text{ Om} = 0.27
# For GADGET2, you may need to specify conversion parameters.

4 # Rockstar's internal units are Mpc/h (lengths) and Msun/h (masses)

5 GADGET_LENGTH_CONVERSION = 1e-3
26 GADGET_MASS_CONVERSION = 1e+10
28 # This specifies the use of multiple processors:
31 # Output full particle information as well as halos for N number of procs 32 FULL_PARTICLE_CHUNKS = 0
34 # This should be less than 1/5 of BOXSIZE
35 OVERLAP_LENGTH = 1.5
37 # This specifies how many CPUs you want to analyze the particles:
38 NUM_WRITERS = 8
40 # Calculate radii and other halo properties using unbound (0) or only bound (1) particles (default 1)
41 \quad BOUND_PROPS = 0
43 # This sets the virial radius/mass definition ("vir", "XXXc", or "XXXb")
44 MASS_DEFINITION = "vir"
46 # This specifies the I/O filenames:
47 OUTBASE = "halos"
48 INBASE = "particles"
49 NUM_SNAPS = 1
50 NUM_BLOCKS = 1
51 #BGC2_SNAPNAMES = "snapnames.lst"
52 #FILENAME = "particles_<snap>.<block>.dat"
```

A.2 PBS Submission Script (Bash)

```
1 #!/bin/sh
2 #PBS -M djsissom@gmail.com
3 #PBS -m bae
4 #PBS -l nodes=1:ppn=10
5 #PBS -l pmem=3000mb
6 #PBS -l mem=3000mb
7 #PBS -l walltime=0:30:00
8 #PBS -o out.log
9 #PBS -j oe
10
11 # Change to working directory
12 echo $PBS_NODEFILE
13 cd $PBS_O_WORKDIR
14
15 # Start the server
16 rockstar -c onenode.cfg &> server.out &
17
18 # Wait for auto-rockstar.cfg to be created
19 perl -e 'sleep 1 while (!(-e "halos/auto-rockstar.cfg"))'
20 mv halos/auto-rockstar.cfg .
21
22 # Execute the reader processes
23 mpiexec -verbose -n 1 rockstar -c auto-rockstar.cfg >> clients.out 2>&1 & sleep 20
```

```
25
26 # Execute the analysis processes
27 mpiexec -verbose -n 8 rockstar -c auto-rockstar.cfg >> clients.out 2>&1
28
29 # - end of script
```

A.3 Post-Processing Script (Bash)

```
1 #!/bin/bash
 2
3 echo 'running finish_bgc2...'
4 ~/projects/programs/nbody/rockstar/Rockstar-0.99.9/util/finish_bgc2 -c onenode.cfg -s 0
 6 echo 'running bgc2_to_ascii...'
7 ~/projects/programs/nbody/rockstar/Rockstar-0.99.9/util/bgc2_to_ascii -c onenode.cfg -s 0 > halos/all_halos.bgc2.
           ascii
ascii
8
9 echo 'running find_parents...'
10 "/projects/programs/nbody/rockstar/Rockstar-0.99.9/util/find_parents halos/out_0.list 10.0 > halos/out_0.list.
parents
...
11
12 echo 'finished'
```

76

Appendix B

CROSSMATCH Modifications and Configuration

B.1 2LPT First Configuration File (Text)

B.2 ZA First Configuration File (Text)

Appendix C

BGC2 Import Code (Python)

```
1 #!/usr/bin/env python
 3 import sys
 4 import struct
 6 def read_bgc2(filename):
      offset = 4
      groupoffset = 8
      particleoffset = 8
      headersize = 1024
groupsize = 4*8 + 10*4
particlesize = 1*8 + 6*4
11
      \begin{array}{lll} \text{headerformat} &=& \text{`=Q}_{\sqcup} 16\, q_{\sqcup} 19\, d\, \text{`}\\ \text{groupformat} &=& \text{`=Q}_{\sqcup} 2\, Q_{\sqcup} 10\, f\, \text{`}\\ \text{particleformat} &=& \text{`=q}_{\sqcup} 6\, f\, \text{`} \end{array}
      print "Reading_"+filename+"..."
fd = open(filename, 'rb')
bin_string = fd.read()
20
22
23
      fd.close()
print "Finishedureadingufile."
       bin_string = bin_string[offset:]
       # Header stuff
      header_bin = bin_string[:headersize]
header_pad = headersize - 36*8
header = list(struct.unpack(headerformat, header_bin[:-header_pad]))
      31
32
        group.append(list(struct.unpack(groupformat, group_bin[i*groupsize:(i+1)*groupsize])))
      particlestart = headersize + groupoffset + ngroups*groupsize + particleoffset
particle_bin = bin_string[particlestart:]
      particle = []
p_start = 0
for i in range(ngroups):
        npart = group[i][2]
48
         particle.append([])
for j in range(npart):
50
          particle[i].append(list(struct.unpack(particleformat, particle_bin[p_start:p_start+particlesize])))
51
        p_start += particlesize
p_start += particleoffset
53
      print "Finisheduparsingubgc2ufile"
       return header, group, particle
59
      header, group, particle = read_bgc2(sys.argv[1])
       print 'Header contents:'
      for value in header:
print value
64
65
       print 'Group[0] contents:'
67
       for value in group[0]:
      print value
68
71
72
73
74
75
76
77
       print part
       print 'Group[1] contents:'
for value in group[1]:
      print value
      print 'Particles_in_group[1]:'
for part in particle[1]:
```

Appendix D

Density Profile Code (Python)

```
1 #!/usr/bin/env python
 3 import sys
 4 import bgc2
5 import numpy as np
 6 import matplotlib.pyplot as plt
 7 from matplotlib.ticker import MultipleLocator
8 from scipy.optimize import curve_fit
 9 from scipy.stats import chisquare
11 #read_mode = 'ascii2'
12 read_mode = 'bgc2'
14 if read_mode == 'bgc2':
15  use_bgc2 = True
16  use_all = False
       individual_masses = False
halo_id = 146289
nbins = 50
nfit = 500
20
        ooms = 3.0
22
23
       mass_scale = 1.0
common_mass = 5.33423e5
       dist_scale = 1.0e3
#res_limit = 0.488
       #res_limit = 4.0
26
       res_limit = 0.5
#res_limit = 10.0
draw_frac = 0.1
29
        tick_base_major = 100.0
31
       tick_base_minor = 10.0
find_com = False
33 elif read_mode == 'ascii':
       use_bgc2 = False
use_all = True
        individual_masses = True
       halo_id = 0
nbins = 100
nfit = 500
ooms = 5.0
37
39
40
        mass_scale = 1.0e12
       dist_scale = 200.0
res_limit = 1.0e-2
draw_frac = 2.0e-4
       tick_base_major = 80.0
tick_base_minor = 20.0
45
        find_com = True
48 elif read_mode == 'ascii2':
49  use_bgc2 = False
50  use_all = True
51
        individual_masses = True
       individual_r
halo_id = 0
nbins = 100
nfit = 500
ooms = 3.5
53
54
       mass_scale = 1.0e10
dist_scale = 1.0
        #res_limit = 3.0e-1
       res_limit = 1.0
draw_frac = 1.0e-2
59
       tick_base_major = 200.0
tick_base_minor = 40.0
find_com = True
62
64 else:
       sys.exit(98712)
67 #outfile = 'asciitest_halo_properties.txt'
68 outfile = 'asclitest_nalo_properties
69 comfile = 'density_profile_halos.dat'
69 comfile = 'center_of_mass.txt'
71 make_plot = False
     #make_plot = True
78 xlabel_proj = [r'XuPositionu(%suh$^{-1}$)' % (dist_units), r'XuPositionu(%suh$^{-1}$)' % (dist_units), r'Yu
Positionu(%suh$^{-1}$)' % (dist_units)]
79 ylabel_proj = [r'YuPositionu(%suh$^{-1}$)' % (dist_units), r'ZuPositionu(%suh$^{-1}$)' % (dist_units), r'Zu

Position_(%s_h$^{-1}$), % (dist_units)]
80 xlabel_prof = r'Radius_(%s_h$^{-1}$), % (dist_units)
```

```
81 ylabel_prof = r'Density_{\sqcup}(M^{-\{\cdot\}}_{\sqcup}/s^{-3})^{-3}_{\sqcup}h^{-\{2\}})' % (dist_units)
  82 npixels = 50
 84 #common_mass = 1.0e-7
  85 \text{ #common_mass} = 1.0e5
 86 \text{ mass\_col} = 0
 87 pos_cols = (1,2,3)
88 vel_cols = (4,5,6)
 89 halo_id_col = 0
 91 grav_const = 4.3e-6 # kpc M_sol^-1 (km/s)^2
 94 def read files(files):
            data = 0
for file in files:
    print 'Reading_file_\%s...' % (file)
    if data == 0:
 95
 97
 99
                       data = np.genfromtxt(file, comments='#')
100
                       data = np.append(data, np.genfromtxt(file, comments='#'), axis=0)
            print 'Finished reading files
102
103
             return data
105
106 def my_chisq(ydata,ymod,deg=2,sd=None):
108 \ \texttt{Returns} \bot \texttt{the} \bot \texttt{reduced} \bot \texttt{chi-square} \bot \texttt{error} \bot \texttt{statistic} \bot \texttt{for} \bot \texttt{an} \bot \texttt{arbitrary} \bot \texttt{model} \texttt{,}
109 {\rm chisq/nu}, {\rm uwhere} {\rm unu} {\rm is} {\rm uthe} {\rm number} {\rm uof} {\rm degrees} {\rm uof} {\rm ufreedom} . {\rm uIf} {\rm uindividual} 110 {\rm standard} {\rm deviations} {\rm uorate} {\rm uora
111 \quad statistic \\ \sqcup is \\ \sqcup computed \\ \sqcup as \\ \sqcup the \\ \sqcup sum \\ \sqcup of \\ \sqcup squared \\ \sqcup errors \\ \sqcup divided \\ \sqcup by \\ \sqcup the \\ \sqcup standard
112 deviations. ||See|http://en.wikipedia.org/wiki/Goodness_of_fit||for||reference
114 ydata, ymod, sd_assumed_to_be_Numpy_arrays._deg_integer.
116 Usage:
117 >>>_{\sqcup}chisq=redchisqg(ydata,ymod,n,sd) 118 where
119 ydata⊔:⊔data
120 ymodu:umodeluevaluateduatutheusameuxupointsuasuydata
121 nu:unumberuofufreeuparametersuinutheumodel
122 sdu: uncertainties in ydata
124 Rodrigo_Nemmen
125 http://goo.gl/8S10o
126 шшш
              # Chi-square statistic
128
            if sd==None:
                 chisq=np.sum((ydata-ymod)**2)
129
130
                 chisq=np.sum( ((ydata-ymod)/sd)**2 )
133
            \mbox{\tt\#} Number of degrees of freedom assuming 2 free parameters
134
            nu=ydata.size-1-deg
             return chisq/nu
135
136
138 def calc_m_enclosed(mass, pos):

139    r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)

140    r = np.sort(r)
141
             first_good_bin = 0
142
            for i in range(len(r)):
   if r[i] > res_limit:
144
                     first_good_bin = i
145
                      break
            print 'r1_=', r[first_good_bin-1]
            print 'r2<sub>U</sub>=', r[first_good_bin]
print 'r3<sub>U</sub>=', r[first_good_bin+1]
m_extra = mass[0] * first_good_bin
147
148
150
             r = r[first_good_bin:]
             #m_enclosed = np.zeros(len(r))
151
             #for i in range(len(r)):
            153
154
155
             return r, m_enclosed
156
158 def calc_density_profile(mass, pos):
           r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)
max_r = r.max()
#min_r = max_r / 10**ooms
min_r = res_limit
log_range = np.log10(max_r) - np.log10(min_r)
159
161
162
164
             #global nbins
165
166
             local_nbins = float(nbins + 1)
             #nbins = len(r) / 1000
167
             while True:
168
169
                  bins = np.arange(local_nbins)
bins = max_r * 10.0**(log_range * bins / (local_nbins-1.0) - log_range)
bin_mass, r_bins = np.histogram(r, bins, weights=mass)
170
                  if (bin_mass == 0.0).any():
```

```
local nbins -= 1
             continue
175
         else:
176
             break
        #print 'Binning particles using bin edges of \n', r\_bins
178
179
        rho = bin_mass / (sphere_vol(r_bins[1:]) - sphere_vol(r_bins[:-1]))
181
        N_bin, blah = np.histogram(r, bins)
183
       rho_err = poisson_error(N_bin) * rho
184
       return r_bins, rho, rho_err
186
187
188 def logbin(pos):
189
       r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)
       max_r = r.max()
min_r = max_r / 10**ooms
190
191
       log_range = np.log10(max_r) - np.log10(min_r)
192
194
        global nbins
       nbins = float(nbins + 1)
bins = np.arange(nbins)
195
197
        bins = max_r * 10.0**(log_range * bins / (nbins-1.0) - log_range)
198
        hist, bin_edges = np.histogram(r, bins)
       #print 'Binning particles using bin edges of \n', bin_edges
return hist, bin_edges
200
201
203
204 def poisson_error(N):
       err = np.sqrt(N) / N
return err
205
206
208
209 def sphere_vol(r):
210 volume = (4.0 / 3.0) * np.pi * r**3
211
       return volume
213 def get_rho_0(R_s, R_vir):

215 H = 70.0e-3 # km s^-1 kpc^-1

216 G = 4.3e-6 # kpc M_sol^-1 (km/s)^2

217 rho_crit = 3.0 * H**2 / (8.0 * np.pi * G)
218
       c = R_vir / R_s
220
       g = 1.0 / (np.log(1.0+c) - c/(1.0+c))

delta_char = v * c**3 * g / 3.0
       return rho_crit * delta_char
226
227 def nfw_fit_rho0(r, R_s, rho_0):
      if R<sub>s</sub> >= 1.0:

return (R<sub>s</sub> - 1.0) * np.exp(r) + rho_0 / (( r / R<sub>s</sub> ) * ( 1.0 + r / R<sub>s</sub> )**2)

return rho_0 / (( r / R<sub>s</sub> ) * ( 1.0 + r / R<sub>s</sub> )**2)
228
229
230
231
233 def nfw_fit_rho0_log(r, R_s, rho_0):
234
      r = 10.0**r
R_s = 10.0**R_s
       rbo_0 = 10.0**rho_0
profile = rho_0 / ((r / R_s ) * ( 1.0 + r / R_s ) **2)
return np.log10(profile)
236
239
240
241 def nfw_def_rho0(R_vir):
       def _nfw_def_rho0(r, R_s):
    rho_0 = get_rho_0(R_s, R_vir)
    return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
242
243
245
       return _nfw_def_rho0
247
248 def nfw_databin_rho0(rho_0):
       def _nfw_databin_rhoo(r, R_s):
    return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
250
251
       return _nfw_databin_rho0
253
254 def dm_profile_fit_rho0_log(r, R_s, rho_0, alpha):
255 r = 10.0**r
       R_s = 10.0**R_s
rho_0 = 10.0**rho_0
256
257
258
        alpha = 10.0**alpha
       rofile = rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**alpha)
return np.log10(profile)
259
261
263 def dm_profile_fit_rho0(r, R_s, rho_0, alpha):
264    return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s ) **alpha)
```

```
273
274 def dm_profile_databin_rho0(rho_0):
       def _dm_profile_databin_rho0(r, R_s, alpha):
    return rho_0 / ((r / R_s) * (1.0 + r / R_s) **alpha)
return _dm_profile_databin_rho0
275
276
278
279
280 def nfw_cdf(r, R_s, rho_0):
       r = 10.0**r
R_s = 10.0**R_s
281
282
283
       rho_0 = 10.0**rho_0
        profile = rho_0 * R_s * (np.log(1.0 + r / R_s) - 1.0 / (1.0 + r / R_s))
284
        return np.log10(profile)
286
287
288 def nfw_cdf_nolog(r, R_s, rho_0):
289 profile = rho_0 * R_s * (np.log(1.0 + r / R_s) - 1.0 / (1.0 + r / R_s))
290
        return profile
292
293 def mass_profile(s, c):

294  g = 1.0 / (np.log(1.0 + c) - c / (1.0 + c))

295  return g * (np.log(1.0 + c * s) - c * s / (1.0 + c * s))
296
297
298 def fit_mass_profile(s, m_enclosed, err=None, R_vir=None): 299 #for i in range(len(s)):
300
       # if s[i] > res_limit:
       # first_good_bin = i
# break
301
303
       first_good_bin = 0
304
       #popt, pcov = curve_fit(nfw_cdf, np.log10(r), np.log10(m_outside), sigma=np.log10(err))
306 # popt, pcov = curve_fit(nfw_cdf, np.log10(r), np.log10(m_outside))
307 # popt = 10.0**popt
308 # pcov = 10.0**pcov
309
       popt, pcov = curve_fit(mass_profile, s, m_enclosed)
310
       print 'fit_paramsu=', popt
print 'covarianceu=', pcov
nfw_r = np.linspace(s[0], s[-1], nfit)
311
313
       nfw_fit = mass_profile(nfw_r, popt[0])
chi2_fit = mass_profile(s, popt[0])
314
315
316
       chi2 = chisquare(np.log10(m_enclosed[first_good_bin:]), np.log10(chi2_fit[first_good_bin:]))
chi2_nolog = chisquare(m_enclosed[first_good_bin:], chi2_fit[first_good_bin:])
print 'chi_square_', chi2
print 'chi_square_nolog_'=', chi2_nolog
317
318
320
321
        return nfw_r, nfw_fit, popt, pcov, chi2[0]
323
324 def fit_profile(r, rho, err=None, R_vir=None):
325 first_good_bin = 0
326 # for i in range(len(r)):
327 # if r[i] > res_limit:
             rho_O_databin = rho[i]
first_good_bin = i
328 #
329 #
330 #
               break
331 # print 'first_good_bin =', first_good_bin
        #-----#
       #------
#popt, pcov = curve_fit(nfw_fit_rho0, r, rho, sigma=err)
#popt, pcov = curve_fit(nfw_def_rho0(R_vir), r, rho, p0=[10.0], sigma=err)
#popt, pcov = curve_fit(nfw_databin_rho0(rho_0_databin), r, rho, sigma=err)
blah = 3
334
338
        if blah == 0:
339
         for i in range(100):
           a = 2.0 * np.random.random() * 0.1 * r.max()
b = 2.0 * np.random.random() * 10.0
340
342
             c = 2.0 * np.random.random() * 2.0
343
             try:
                popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err)
345
             except RuntimeError:
346
                continue
             if (popt[0] < r.max()) and (popt[2] >= 0.0):
             break
elif i >= 99:
348
349
350
              print 'nougoodufitufounduforuthisuhalo...'
       return None, None, None, None, None elif blah == 1:
351 #
353
          #a = r.max() / 100.0

a = 0.001
354
          b = rho[first_good_bin]
c = 0.001
356
```

```
#popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, sigma=err)
359
          print 'rho_0_before_=', b
360
          #trv:
          #popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err, maxfev=1, xtol=100.0)
popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err, xtol=1.0e-1)
362
363
          #except RuntimeError:
364
          # print 'just checking for now...'
365
          print 'rho_0_{\square}after_{\square}=', popt[1]
366
          #sys.exit()
367
       elif blah == 2:
          #popt, pcov = curve_fit(dm_profile_fit_rho0_log, np.log10(r), np.log10(rho), sigma=np.log10(err))
popt, pcov = curve_fit(nfw_fit_rho0_log, np.log10(r), np.log10(rho), sigma=np.log10(err))
368
       popt = 10.0**popt
pcov = 10.0**pcov
elif blah == 3:
371
         popt, pcov = curve_fit(nfw_fit_rho0, r, rho, sigma=err, p0 = [0.1, 1.0])
375
       #popt, pcov = curve_fit(dm_profile_def_rho0(R_vir), r, rho, sigma=err)
376
       #popt, pcov = curve_fit(dm_profile_databin_rho0(rho_0_databin), r, rho, sigma=err)
378
       print 'fit_params<sub>□</sub>=', popt
print 'covariance<sub>□</sub>=', pcov
381
       nfw_r = np.linspace(r[0], r[-1], nfit)
382
                      choose one fitting type
       nfw_fit = nfw_fit_rho0(nfw_r, popt[0], popt[1])
384
385
       #nfw_fit = nfw_def_rho0(R_vir)(nfw_r, popt[0])
#nfw_fit = nfw_databin_rho0(rho_0_databin)(nfw_r, popt[0])
       #nfw_fit = dm_profile_fit_rho0(nfw_r, popt[0], popt[1])
#nfw_fit = dm_profile_def_rho0(R_vir)(nfw_r, popt[0], popt[1])
#nfw_fit = dm_profile_databin_rho0(rho_0_databin)(nfw_r, popt[0], popt[1])
387
388
389
390
                                                 #----- choose one fitting type -----
392
       chi2_fit = nfw_fit_rho0(r, popt[0], popt[1])
       #chi2_fit = nfw_def_rho0(R_vir)(r, popt[0])
#chi2_fit = nfw_databin_rho0(rho_0_databin)(r, popt[0])
393
       #chi2_fit = dm_profile_fit_rho0(r, popt[0], popt[1], popt[2])
#chi2_fit = dm_profile_def_rho0(R_vir)(r, popt[0], popt[1])
#chi2_fit = dm_profile_databin_rho0(rho_0_databin)(r, popt[0], popt[1])
395
396
397
308
                                                 ----#
399
       #chi2 = my_chisq(rho, chi2_fit, 2, err)
chi2 = chisquare(rho, chi2_fit)
print 'chi_square_=', chi2
400
401
402
403
       chi2 = chi2[0]
404
       return nfw_r, nfw_fit, popt, pcov, chi2
406
407
408 def draw_projection(fig, place, plot_lim, x, y):
      ax = plt.subplot(2,3,place+1, aspect='equal')
im = ax.plot(x, y, linestyle='', marker='.', markersize=1, markeredgecolor='blue')
ax.set_xlabel(xlabel_proj[place])
409
410
412
       ax.set_ylabel(ylabel_proj[place])
413
       ax.set_xlim(-plot_lim, plot_lim)
ax.set_ylim(-plot_lim, plot_lim)
414
415
       ax.xaxis.set_major_locator(MultipleLocator(tick_base_major))
       ax.xaxis.set_minor_locator(MultipleLocator(tick_base_minor))
417
       ax.yaxis.set_major_locator(MultipleLocator(tick_base_major))
418
       ax.yaxis.set_minor_locator(MultipleLocator(tick_base_minor))
       return fig
420
421
422 def draw_density_projection(fig, place, plot_lim, x, y)
423
       limits = [[-plot_lim, plot_lim], [-plot_lim, plot_lim]]
ax = plt.subplot(2,3,place+1, aspect='equal')
424
       #ax.set_xlim(-plot_lim, plot_lim)
426
       #ax.set_ylim(-plot_lim, plot_lim)
       #im = ax.plot(x, y, linestyle='', marker='.', markersize=1, markeredgecolor='blue')
z, xedges, yedges = np.histogram2d(x, y, bins = npixels, range = limits)
427
429
       \#z = np.log10(z)
       im = ax.imshow(z.T, extent=(-plot_lim, plot_lim, -plot_lim, plot_lim), interpolation='gaussian', origin='lower'
431
       ax.locator_params(nbins=6)
       ax.set_xlabel(xlabel_proj[place])
433
       ax.set_ylabel(ylabel_proj[place])
434 # ax.xaxis.set_major_locator(MultipleLocator(tick_base_major))
435 # ax.xaxis.set_minor_locator(MultipleLocator(tick_base_minor))
436 # ax.yaxis.set_major_locator(MultipleLocator(tick_base_major))
437 # ax.yaxis.set_minor_locator(MultipleLocator(tick_base_minor))
       return fig
439
441 def draw_density_profile(fig, r, rho, err=None):
       ax = plt.subplot(2,1,2)
im = ax.loglog(r, rho, linestyle='steps-mid-')
442
444
       line1 = ax.axvline(res_limit, color='black', linestyle=':')
       445
       ax.set_xlabel(xlabel_prof)
```

```
ax.set_ylabel(ylabel_prof)
       if err != None:
450
          err_bars = ax.errorbar(r, rho, yerr=err,linestyle='None')
451
       return fig, ax
453
454 def draw_nfw_profile(fig, ax, r, rho, R_s=None):
455 ax.loglog(r, rho, linestyle='-', color='red')
       if R_s != None:
   line = ax.axvline(R_s, color='purple', linestyle='-.')
456
458
       return fig
459
461 def calc_kinetic_energy(mass, vel):
      vsq = vel[:,0]**2 + vel[:,1]**2 + vel[:,2]**2
energy = 0.5 * np.sum(mass*vsq)
462
464
       return energy
465
466
467 def calc_potential_energy(mass, pos):
       local_sqrt = np.sqrt
partial_sum = 0.0
469
        for i in range(len(mass)):
   for j in range(len(mass)):
470
       if j != i:
    r_diff = local_sqrt((pos[i,0] - pos[j,0])**2 + (pos[i,1] - pos[j,1])**2 + (pos[i,2] - pos[j,2])**2)
    partial_sum = partial_sum - mass[i]*mass[j]/r_diff
energy = partial_sum * grav_const / 2.0
return energy
472
473
475
476
478
479 def calc_angular_momentum(mass, pos, vel):
480 ang_mom_x = np.sum(mass * (pos[:,1] * vel[:,2] - pos[:,2] * vel[:,1]))
481 ang_mom_y = np.sum(mass * (pos[:,2] * vel[:,0] - pos[:,0] * vel[:,2]))
482 ang_mom_z = np.sum(mass * (pos[:,1] * vel[:,2] - pos[:,2] * vel[:,1]))
483
       ang_mom = np.sqrt(ang_mom_x**2 + ang_mom_y**2 + ang_mom_z**2)
484
       return ang_mom
486
487 def main():
      with open(outfile, 'w') as fd:
488
         489
490
             _{\text{UUUUU}}nbins_{\text{UUUU}}N_partn,)
491 # with open(comfile, 'w') as fd:
492 # fd.write('#id mass dx dy dz\n')
493
494 # if use_bgc2 == True:
        header, halos, particles = bgc2.read_bgc2(sys.argv[1])
for i in range(len(halos)):
495 #
496 #
             if halos[i][halo_id_col] == halo_id:
498 #
                index = i
         halo_particles = np.asarray(particles[index])
pos = halo_particles[:,pos_cols[0]:pos_cols[0]+3] * dist_scale
r_vir = halos[index][4] * dist_scale
499 #
500 #
501 #
502 # else:
503 #
           # Read in particle files
504 #
           data = read_files(sys.argv[1:])
           # Select particles with a given halo ID and convert positions from Mpc to kpc
505 #
506 #
           if use_all == False:
507 #
           halo_particles = data[np.where(data[:,halo_id_col] == halo_id)]
if use_all == True:
509 #
             halo_particles = data
          del data
510 #
          pos = halo_particles[:,pos_cols[0]:pos_cols[0]+3] * dist_scale
511 #
512 #
          r_vir = 241.48
#r_vir = pos.max()
513 #
      for input_file in sys.argv[1:]:
   if use_bgc2 == True:
515
516
             #header, halos, particles = bgc2.read_bgc2(sys.argv[1])
            header, halos, particles = bgc2.read_bgc2(input_file)
halos = np.asarray(halos)
518
519
            indices = np.argsort(halos[:,2])
indices = indices[::-1]
520
                                                              # sort by number of particles
521
                                                               # start with the biggest
          else:
523
             data = read_files([input_file])
            # Select particles with a given halo ID and convert positions from Mpc to kpc if use_all == False:
524
            particles = [data[np.where(data[:,halo_id_col] == halo_id)]]
if use_all == True:
    particles = [data]
526
527
           del data
529
530
531
532
          itteration = 0
533
          #for index in range(len(halos)):
534
          #for index in range(1):
535
          #for index in indices[:10]:
          for index in indices:
             if ((len(particles[index]) >= 100) and (halos[index][1] == -1)):
```

```
538
540
                        halo_particles = np.asarray(particles[index])
pos = halo_particles[:,pos_cols[0]:pos_cols[0]+3] * dist_scale
541
                        vel = halo_particles[:,vel_cols[0]:vel_cols[0]+3]
543
544
                        if use_bgc2 == True:
                            rusir = halos[index][0]
r_vir = halos[index][4] * dist_scale
halo_mass = halos[index][5]
5/15
546
548
                            halo_pos = np.array([halos[index][6] * dist_scale, halos[index][7] * dist_scale, halos[index][8] *
                  dist_scale])
549
                            halo_vel = np.array([halos[index][9], halos[index][10], halos[index][11]])
                        else:
550
551
                             r_{vir} = 241.48
                           r_vir = 241.48
halo_id = 0
#halo_mass = mass[0] * len(halo_particles)
halo_pos = np.array([0.0, 0.0, 0.0])
halo_vel = np.array([0.0, 0.0, 0.0])
553
554
555
556
557
558
559
                        if individual_masses == True:
                            mass = halo_particles[:,mass_col] * mass_scale
560
                        else:
561
                            mass = np.ones(halo_particles.shape[0]) * common_mass * mass_scale
562
                        if use_bgc2 == False:
564
                            halo_mass = mass[0] * len(halo_particles) #fix placement of this for ascii test
565
566
                        print \ 'Using_{\sqcup} \% d_{\sqcup} particles_{\sqcup} in_{\sqcup} halo_{\sqcup} \% d. ' \ \% \ (halo\_particles.shape[0], \ halo\_id)
567
568
                        # Find center of mass
if find_com == True:
   mass_tot = mass.sum()
569
570
571
                             m_pos = mass.reshape(mass.shape[0],1) * pos
572
                             com = m_pos.sum(axis=0) / mass_tot
                            pos = pos - com
print 'Center_of_mass_=_(%g_||_%g_||_%g)' % (com[0], com[1], com[2])
573
575
                        else:
                            pos = pos - halo_pos
576
                             vel = vel - halo_vel
578
                        #with open(comfile, 'a') as fd:
579
580
                            fd.write("%d %g %g %g %g\n" % (halo_id, halo_mass, halo_pos[0] - com[0], halo_pos[1] - com[1],
                  halo_pos[2] - com[2]))
581
                       # Bin halo particles into logarithmic shells and compute density r\_bins, rho, rho\_err = calc\_density\_profile(mass, pos)
582
583
                        if len(r_bins) < 5:</pre>
585
586
                             print 'Tooufewubins.uuSkippinguthisuhalo.'
                  with open(outfile, 'a') as fd:
    fd.write("%8du%16.12guu%14.10guu%14.10guu%14.10guu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14du+-u%14duu%14duu%14du+-u%14duu%14duu%14du+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%14duu&+-u%
588
589
                            continue
590
591
                    # hist, r_bins = logbin(pos)
592
                    # err = poisson_error(hist)
# rho = mass * hist / (sphere_vol(r_bins[1:]) - sphere_vol(r_bins[:-1]))
593
                    # rho_err = err * rho
mid_bins = 10.0**(0.5 * (np.log10(r_bins[1:]) + np.log10(r_bins[:-1])))
594
595
596
                       print 'nbins,=,', len(mid_bins)
597
598
                        # Don't pass NaN's to fitting routine
599
                        rho_err_nonan = np.copy(rho_err)
600
                         nan_check = np.isnan(rho_err_nonan)
                        for i in range(len(rho_err_nonan)):
601
                             #if (nan_check[i] == True):
                           # rho[i] = 1.0e-10
if (mid_bins[i] < res_limit) or (nan_check[i] == True):</pre>
603
604
                                rho_err_nonan[i] = 1.0e10
605
606
607
608 #
                          r, m_enclosed = calc_m_enclosed(mass, pos)
609
                        # Fit an NFW profile to the data
610
611
           #
                          try:
                  nfw_r, nfw_fit, popt, pcov, chisq = fit_profile(mid_bins / r_vir, rho / rho.max(), err = rho_err_nonan / rho.max(), R_vir = 1.0)
612
                        n.max(), k_vii = 1.0)
#nfw_r, nfw_fit, popt, pcov, chisq = fit_mass_profile(r / r_vir, m_enclosed / halo_mass)
nfw_r = nfw_r * r_vir
nfw_fit = nfw_fit * rho.max()
#nfw_fit = nfw_fit * halo_mass
scale_radius = popt[0] * r_vir
613
614
616
617
                        scale_radius_err = pcov[0,0] * r_vir
rho_0 = popt[1] * rho.max()
rho_0_err = pcov[1,1] * rho.max()
618
619
620
621
                        concentration = r_vir / scale_radius
622
                        concentration_err = concentration * scale_radius_err / scale_radius
624
                        # Print parameters
```

```
print 'r vir = '. r vir
                                 print "rho_0_=\%gu+/-\%g" % (rho_0, rho_0_err)
print "scale_uradius_=\%gu+/-\%g" % (scale_radius, scale_radius_err)
print "concentration_=\%gu+/-\%g" % (concentration, concentration_err)
627
628
kin_energy = calc_kinetic_energy(mass, vel)
pot_energy = calc_potential_energy(mass, pos)
633 #
                                    ang_mom = calc_angular_momentum(mass, pos, vel)
635 #
                                   ttow = 2.0 * abs(kin_energy / pot_energy)
                                 lambda_spin = ang_mom * np.sqrt(abs(kin_energy + pot_energy)) / (grav_const * (np.sum(mass))**2.5) kin_energy = 0.0
636 #
638
                                 pot_energy = 0.0
                                  ang_mom = 0.0
639
641
                                 t.t.ow = 0.0
                                 lambda_spin = 0.0
644
646
                        print "inf_covariance_returned,uskipping_this_halo..."
with open(outfile, 'a') as fd:
fd.write("%8d_%16.12guu%14.10guu%14.10guu%14.10guu%14du+-u%14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu%14du-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu&-*14duu
647
649
650
                                       continue
651
                        will be parameters to life
with open(outfile, 'a') as fd:
    #fd.write("%g %g %g %g +- %g %g +- %g %g +- %g %g\n" % (halo_mass, concentration, r_vir,
scale_radius, pcov[0,0], rho_0, pcov[1,1], alpha, pcov[2,2], chisq))
    fd.write("%8d_u/%16.12g_uu/%14.10g_uu/%14.10g_uu/%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_uu-%14.10g_
653
654
655
                          concentration, concentration_err, r_vir, scale_radius, scale_radius_err, rho_0, rho_0_err, chisq, len(r_bins
                        ), len(halo_particles)))
657
658
                                 659
                                 #blah_fit = nfw_fit_rho0(nfw_r, 20.0, 9.0e5)
660
                                  # Plot density profile histogram
661
                                  if (make_plot == True) and (itteration < 10):</pre>
                                      \# Find the maximum of x, y, or z to be limit of projection plots
663
                                       plot_lim = pos.max()
664
665
                                        # Pick only a certain perentage of particles for projection plots
                                      if (draw frac < 1.0):
666
667
                                            np.random.shuffle(pos)
668
                                            pos = pos[:(draw_frac*pos.shape[0])]
669
670
                                       fig = plt.figure()
671
                                               draw_density == True:
                                            fig = draw_density_projection(fig, 0, plot_lim, pos[:,0], pos[:,1])
fig = draw_density_projection(fig, 1, plot_lim, pos[:,0], pos[:,2])
672
674
                                            fig = draw_density_projection(fig, 2, plot_lim, pos[:,1], pos[:,2])
675
                                       else:
676
                                             fig = draw_projection(fig, 0, plot_lim, pos[:,0], pos[:,1])
677
                                            fig = draw_projection(fig, 1, plot_lim, pos[:,0], pos[:,2])
fig = draw_projection(fig, 2, plot_lim, pos[:,1], pos[:,2])
679
                                       fig, ax = draw_density_profile(fig, mid_bins, rho, err=rho_err) #put this back for binning
                                       #fig, ax = draw_density_profile(fig, r, m_enclosed) #
fig = draw_nfw_profile(fig, ax, nfw_r, nfw_fit, R_s=scale_radius)
680
                                                                                                                                                                                                                             #take this out for binning
682
                                       #fig = draw_nfw_profile(fig, ax, nfw_r, blah_fit, R_s=20.0)
                                       fig.tight_layout()
683
                                      plt.savefig(plot_base+str(itteration)+plot_ext)
685
                                       #svs.exit()
686
688
                                itteration += 1
689
691 if __name__ == '__main__':
               main()
```

Appendix E

CROSSMATCH Best Match Code

E.1 Best Match (Python)

```
1 #!/usr/bin/env python
     import svs
  4 import getopt
5 import numpy as np
 8 def main():
9  # read in files
           # read in files
print 'reading_files...'
with open(sys.argv[1]) as f:
    matches1 = f.readlines()
with open(sys.argv[2]) as f:
    matches2 = f.readlines()
print 'done_ureading_ufiles'
10
13
14
16
17
           header = matches1[2:6]
           \label{lem:header.insert(0, '#uBestumatchesuforubi-directionalucrossmatch\n')} \\ header.insert(1, '#\n')
19
20
           matches1 = matches1[7:]
matches2 = matches2[7:]
21
24
25
26
           # convert to numpy arrays
           print 'convertingutounumpyuarrays...'
match_array1 = np.asarray([line.split() for line in matches1], dtype=int)
27
28
            match_array2 = np.asarray([line.split() for line in matches2], dtype=int)
           print 'done converting'
29
30
           # find matches that exist in both lists
31
32
33
           print 'finding_matches...'
mask = np.zeros(len(match_array1), dtype=bool)
           for i, line in enumerate(match_array1):
    id1 = line[id1_col]
    id2 = line[id2_col]
34
35
                  tmp = (match_array2[:,id1_col] == id2)
tmp = (match_array2[tmp,id2_col] == id1)
36
37
38
39
                  mask[i] = tmp.any()
if i % 1000 == 0:
                         print "Finishedulineu", i
41
42
           print 'done_matching'
44
           out_array = match_array1[mask]
45
46
47
           w witte lessts
print 'writing_results...'
with open(sys.argv[3], 'w') as f:
    f.writelines(("%s" % line for line in header))
    np.savetxt(f, out_array, fmt='%10d')
49
50
51
52
53
           print 'Finished.'
54
55 id1_col
                                      = 4
= 5
56 npart1_col
57 id2_col
                                      = 2
58 npart2_col
59 ncommon_col
60 hnum1_col
61 hnum2_col
64 if __name__ == '__main__': 65 main()
```

E.2 PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
2 #PBS -M djsissom@gmail.com
3 #PBS -m bae
4 #PBS -l nodes=27:ppn=1
5 #PBS -l pmem=20000mb
6 #PBS -l mem=54000mb
7 #PBS -l walltime=0:30:00
8 #PBS -o out.log
9 #PBS -j oe
10
11 #nodes=186:ppn=1
```

```
12 #pmem=20000mb
13 #mem=372000mb
 15 minsnap=53
16 maxsnap=61
 18 minbox=1
 19 maxbox=3
20
 21 # Change to working directory
21 # Change to working directory
22 echo %PBS_NODEFILE
23 cd %PBS_O_WORKDIR
24
25 for ((i=$minbox; i<=$maxbox; i++)); do
          for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
            1. [ $snap -lt 10 ]; then
    j=00$snap
elif [ $snap -lt 100 ]; then
    j=0$snap
fi
28
29
30
31
32
33
34
35
             base_dir=^/projects/simulations/rockstar/box${i}
crossmatch_dir=${base_dir}/crossmatch/snap${j}
first_file=${crossmatch_dir}/crossmatch_2lpt_first_000.txt
second_file=${crossmatch_dir}/crossmatch_za_first_000.txt
outfile=${crossmatch_dir}/crossmatch_000.txt
logfile=${crossmatch_dir}/best_crossmatch.log
36
37
38
39
40
41
42
43
44
45
46
              echo "Startingubox\{i\}usnap\{j\}..."
              mpiexec -verbose -n 1 ./best_crossmatch.py ${first_file} ${second_file} ${outfile} > ${logfile} 2>&1
echo "Finished_box${i}_snap${j}"
} &
46
47
48
49
don
50
51
done
52
53 wait
54
          done
 55 # - end of script
```

Appendix F

Database Generation Code

F.1 Halo Match (Python)

```
1 #!/usr/bin/env python
    import svs
 4 import getopt
5 import numpy as np
 8 def main():
      # read and parse command line arguments
      opts, args = get_args(sys.argv[1:])
      output_file, match_file, densprof_files, parents_files, ascii_files = parse_args(opts, args)
      \mbox{\tt\#} read in headers as lists and data as numpy arrays
      match_header, match_data = read_files(match_file, header_line = 3)
densprof_header1, densprof_data1 = read_files(densprof_files[0], header_line = 0)
      densprof_header2, densprof_data2 = read_files(densprof_files[1], header_line = 0)
parents_header1, parents_data1 = read_files(parents_files[0], header_line = 0)
parents_header2, parents_data2 = read_files(parents_files[1], header_line = 0)
      ascii_header1, ascii_data1 = read_files(ascii_files[:(len(ascii_files)/2)], header_line = 0)
ascii_header2, ascii_data2 = read_files(ascii_files[(len(ascii_files)/2):], header_line = 0)
      print 'Finished reading files.'
       # filter matches, remove duplicate halo matches, and reorder match columns
       match data = filter matches(match data)
       if filter_duplicate_matches:
        match_data = filter_dups(match_data, unique_col = match_id1_col)
match_data = filter_dups(match_data, unique_col = match_id2_col)
       if reorder_match_columns:
         match_header, match_data = reorder_match_cols(match_header, match_data)
       # calculate number of subhalos and add column to parents data and headers
      \label{lem:print_print} \begin{split} & print_{} \ 'Finding_{\sqcup} number_{\sqcup} of_{\sqcup} subhalos \dots \\ & parents_{\_} header1.append('N\_subs') \end{split}
       parents_header2.append('N_subs')
       parents_data1 = count_subs(parents_data1)
       parents_data2 = count_subs(parents_data2)
      # create header
       print 'Making_header...'
41
42
      header = make_header(match_header, densprof_header1, densprof_header2, \
parents_header1, parents_header2, ascii_header1, ascii_header2)
      # match halos
print 'Matching halos...'
44
45
      halos = match_halos(match_data, [densprof_data1, densprof_data2, \
parents_data1, parents_data2, ascii_data1, ascii_data2])
      # filter based on given criteria and sort
      print 'Filtering_halo_data...
if filter_halo_properties:
   halos = filter_halos(halos)
50
      if sort_col != None:
    sort_mask = halos[:,sort_col].argsort()
    sort_mask = sort_mask[::-1]
        halos = halos[sort_mask]
      # output matched table
      print 'Writing_resluts...'
write_results(output_file, header, halos)
      print 'Finished.'
65 def get_args(arglist):
         opts, args = getopt.gnu_getopt(arglist, shortopts, longopts)
67
      except getopt.GetoptError:
        print
                  "Invalid_option(s)."
         print help_string
70
          sys.exit(2)
      if opts == []:
   print 'Nouoptionsugiven.'
         print help_string
      sys.exit(2)
return opts, args
79 def parse_args(opts, args):
      densproffiles = None
```

```
parentsfiles = None
        asciifiles = None
use_ascii = False
 83
        for opt in opts:
           if (opt[0] == '-h') or (opt[0] == '--help') or (opts == None):
             print help_string
 86
          print neip_sciin6
   sys.exit(0)
if (opt[0] == '-o') or (opt[0] == '--outfile'):
   outfile = opt[1]
if (opt[0] == '-m') or (opt[0] == '--match'):
   matchfile = opt[1]
'' '--+'\(\cap{n}\) == '-d') or (opt[0] == '--density'):
 88
 89
 91
          matchile = opt[]
if (opt[0] == '--d') or (opt[0] == '--density'):
   densproffiles = create_append(densproffiles, opt[1])
 92
           if (opt[0] == '-p') or (opt[0] == '--parents'):
   parentsfiles = create_append(parentsfiles, opt[1])
if (opt[0] == '-a'):
 94
 95
             use_ascii = True
 97
        if use_ascii:
 99
          if len(args) % 2 != 0:
100
            print 'Must_have_an_even_number_of_ascii_files!'
              sys.exit(3)
       for arg in args:
   asciifiles = create_append(asciifiles, arg)
return outfile, matchfile, densproffiles, parentsfiles, asciifiles
102
103
105
106
107 def create_append(lst, value):
       if lst == None:
lst = [value]
108
109
110
          lst.append(value)
       return 1st
114
115 def read_files(files, header_line = None, comment_char = '#'):
       header = None
data = None
       if type(files) == str:
119
          files = [files]
120
        if header_line != None:
           with open(files[0], 'r') as fd:
for line in range(header_line):
122
123
124
                fd.readline()
          header = fd.readline()
if header[0] != comment_char:
126
            print "Headerumustustartuwithuau'%s'" % comment_char
             sys.exit(4)
128
          header = header[1:]
header = header.split()
129
130
        for file in files:
          print 'Reading_file_%s...' % (file)
134
           if data == None:
135
              data = np.genfromtxt(file, comments='#')
136
             data = np.append(data, np.genfromtxt(file, comments='#'), axis=0)
138
139
        if header_line == None:
140
          return data
        else:
141
142
           return header, data
144
145 def filter matches(halos):
       if filter_bad_matches:
       halos = halos[halos[:,match_id1_col] != -1]
halos = halos[halos[:,match_id2_col] != -1]
if (min_npart != 0) and (min_npart != None):
147
148
          halos = halos[halos[:, match_npart1_col] >= min_npart]
halos = halos[halos[:, match_npart2_col] >= min_npart]
150
151
        if (minperc_ncommon != 0) and (minperc_ncommon != None):
          halos = halos[halos[:, match_ncommon_col] / halos[:, match_npart1_col] >= minperc_ncommon] halos = halos[halos[:, match_ncommon_col] / halos[:, match_npart2_col] >= minperc_ncommon]
154
155
       return halos
156
158 def filter_dups(halos, unique_col = 0):
       ncommon = halos[:, match_ncommon_col]
n1 = halos[:, match_npart1_col]
159
                      = halos[:, match_npart2_col]
= ncommon**2 / (n1 * n2) - np.abs(n1 - n2) / (n1 + n2)
161
        n2
162
        rank
        sort_mask = np.argsort(rank)
halos = halos[sort_mask]
164
       unique, mask = np.unique(halos[:, unique_col], return_index=True)
halos = halos[mask]
167
169
       return halos
170
172 def reorder_match_cols(match_header, match_data):
```

```
global match id1 col
        global match_id2_col
175
         global match_hnum1_col
176
         global match hnum2 col
         global match_npart1_col
178
         global match_npart2_col
179
         global match ncommon col
180
181
        order = [match_id1_col, match_id2_col, \
                      match_hnum1_col, match_hnum2_col, \
183
                       match_npart1_col, match_npart2_col, \
        match_ncommon_col]
match_header = [match_header[index] for index in order]
match_data = match_data[:, order]
184
186
187
189
        match_id2_col
        match_hnum1_col
190
        match_hnum2_col
191
192
        match_npart1_col = 4
        match_npart2_col
194
        match_ncommon_col = 6
195
        return match_header, match_data
197
198
199 def count_subs(halos):
        ef count_subs(naios):
   id = halos[:, id_col]
   parents = halos[:, parents_col]
   parents = parents[parents != -1]
   nsubs = (id[:, np.newaxis] == parents).sum(axis = 1)
   halos = np.column_stack((halos, nsubs))
       id
200
201
203
204
205
206
207
208 def make_header(match, densprof1, densprof2, parents1, parents2, ascii1, ascii2):
        # zeroeth line just lists column number
total_len = len(match + densprof1 + densprof2 + parents1 + parents2 + ascii1 + ascii2)
209
        header_line0 = [str(i) for i in range(total_len)]
header_line0 = 'uu'.join(header_line0)
header_line0 = '#' + header_line0
211
214
        # first line denotes which file columns are from
215
        match_repeat = len(match) - 4
        densprof_repeat = len(densprof1 + densprof2) - 4
        rensproi_repeat = len(qensproi1 + qensproi2) -
parents_repeat = len(parents1 + parents2) - 4
ascii_repeat = len(ascii1 + ascii2) - 4
218
220
        match_part = 'uu'.join(['|---', 'cross', 'match'] + ['----'] * match_repeat + ['---|'])
densprof_part = 'uu'.join(['|---', 'density', 'profile'] + ['----'] * densprof_repeat + ['---|'])
parents_part = 'uu'.join(['|---', 'rockstar', 'parents'] + ['----'] * parents_repeat + ['---|'])
ascii_part = 'uu'.join(['|---', 'rockstar', 'ascii'] + ['----'] * ascii_repeat + ['---|'])
226
        header_line1 = ^{3}_{\ \cup \cup} ^{2}_{\ \cdot} join([match_part, densprof_part, parents_part, ascii_part]) header_line1 = ^{3}#^{3}_{\ \cdot} + header_line1
228
229
        # second line labels 21pt and za columns
        tw second rine labels 21pt and 2a columns
tot_len = len(match + densprof1 + densprof2 + parents1 + parents2 + ascii1 + ascii2)
header_line2 = ['2lpt' if i % 2 == 0 else 'za' if i % 2 == 1 else 'blah' for i in range(tot_len - 1)]
header_line2.insert(len(match) - 1, 'matched')
230
        header_line2 = 'LLL'.join(header_line2)
header_line2 = '#' + header_line2
234
236
        # third line pulls labels from original file headers
        match_part = match
densprof_part = interweave(densprof1, densprof2)
239
        parents_part = interweave(parents1, parents2)
ascii_part = interweave(ascii1, ascii2)
240
        header_line3 = match_part + densprof_part + parents_part + ascii_part
header_line3 = 'uu'.join(header_line3)
header_line3 = '#' + header_line3
242
243
245
246
        header = [header_line0, header_line1, header_line2, header_line3]
        return header
247
248
250 def interweave(list1, list2):
251
       newlist = list1 + list2
        newlist[::2] = list1
newlist[1::2] = list2
253
254
        return newlist
256
257 def interweave_np_2d(array1, array2):
258
       newarray = np.empty((len(array1), len(array1[0]) + len(array2[0])))
        newarray[:,::2] = array1
newarray[:,1::2] = array2
259
260
261
        return newarray
262
264 def match_halos(matches, arrays):
```

```
halos = matches.copv()
       for i, array in enumerate(arrays):
   if array != None:
267
             match_id_col = i % 2
268
             halos = sort_stack(halos, array, match_id_col)
        # interweave columns so that matching 2lpt/za columns are adjacent
        tmp_halos = halos
       halos = np.empty((len(tmp_halos), len(tmp_halos[0])))
halos[:,:len(matches[0])] = matches
startcol = len(matches[0])
273
275
       for i in range(0, len(arrays), 2):
   colrange1 = len(arrays[i][0])
   colrange2 = len(arrays[i+1][0])
276
277
278
279
         endcol = startcol + colrange1 + colrange2
280
281
         cols1 = tmp_halos[:,startcol:startcol+colrange1]
         cols2 = tmp_halos[:,startcol+colrange1:startcol+colrange1+colrange2]
282
283
         halos[:,startcol:endcol] = interweave_np_2d(cols1, cols2)
284
          startcol = endcol
286
287
288
289 def sort_stack(halos, array, match_id_col):
      # add empty columns to halos to later fill with halo data rows = len(halos)
290
       origcols = len(halos[0])
newcols = len(array[0])
292
293
294
       empty = np.empty((rows, newcols))
empty[:] = np.nan
295
296
       halos = np.column_stack((halos, empty))
297
       # remove halos from array with no matches
match_id = halos[:, match_id_col]
array_id = array[:, id_col]
array_mask = np.inid(array_id, match_id)
array = array[array_mask]
298
300
301
303
304
       # create mask so we only add lines for halos in array
305
       array_id = array[:, id_col]
       halo_mask = np.inid(match_id, array_id)
masked_halos = halos[halo_mask]
306
307
308
309
       # create masks to sort by halo id
       match_id_sort_mask = np.argsort(masked_halos[:, match_id_col])
sorted_masked_halos = masked_halos[match_id_sort_mask]
310
311
       # sort array by halo id and copy to empty columns of view of halos
313
       array_id_sort_mask = np.argsort(array[:,id_col])
sorted_masked_halos[:, origcols:] = array[array_id_sort_mask]
314
315
316
       # 'unmask' - put data back in original halos
masked_halos[match_id_sort_mask] = sorted_masked_halos
halos[halo_mask] = masked_halos
317
318
320
       return halos
323
324 def filter_halos(halos):
325
326
       return halos
328
329 def write results(output file, header, halos):
      format = get_format(halos[0])
331
       with open(output_file, 'w') as fd:
        for line in header:
  fd.write(line + '\n')
333
334
          np.savetxt(fd, halos, fmt=format)
335
337 def get_format(line):
338
      format = ['%4' if col in int_cols else '%1.14g' for col in range(len(line))] format = 'u'.join(format)
339
340
       return format
342
343 help_string = '''
344 Available options are:

345 uuuu - h, u - help
346 LULUU-V,U--verbose
347 LULUU-OU<outfile>,U--outfileU<outfile>
348 _____matchlist>,u--match_<matchlist>
349 ____d</br>
__domain_dd</br>
densityprofile_file>,u--densityu</br>
densityprofile_file>
350 UUUUU-pu<parents_file>,u--parents_carents_file>
351 _____ascii_files>,_--ascii_<ascii_files>_-_must_be_last)
353 shortopts = "hvo:m:d:p:a"
354 longopts = ["help", "verbose", "outfile=", "matchfile=", "density=", "parents=", "ascii"]
356 lt_cols = []
```

```
357 lt_vals = []
359 gt_cols = []
360 gt_vals = []
362 eq_cols = []
363 eq_vals = []
364
365 ne_cols = []
366 ne_vals = []
368 #int_cols = [0, 1, 2, 3, 4, 5, 6, 7, 8]
369 int_cols = []
370
371 match id2 col
372 match_npart2_col
373 match_id1_col
374 match_npart1_col
375 match_ncommon_col
376 match_hnum1_col
                                        3
377 match_hnum2_col
                                     = 0
                                                  # col of each input file
# col of final table - use None to turn off sorting
379 id_col
380 sort_col
381 parents_col
383 filter_bad_matches
                                     = True
384 filter_duplicate_matches = False
385 reorder_match_columns
386 filter_halo_properties
                                        True
                                     = False
                                     = 20
                                                 # use 0 or None to use all size halos
# a fraction, use 0 or None to use any match percent
387 min_npart
                                    = 0.05
388 minperc_ncommon
390
391 if __name__ == '__main__':
      main()
```

F.2 PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
 2 #PBS -M djsissom@gmail.com
3 #PBS -m bae
  4 #PBS -1 nodes=1:ppn=1
 5 #PBS -1 pmem=40000mb
6 #PBS -1 mem=4000mb
  7 #PBS -1 walltime=1:00:00
 8 #PBS -o out.log
9 #PBS -j oe
10
11 minsnap=0
12 maxsnap=61
14 \quad minbox=1
15 maxbox=3
13 maxov C

16

17 # Change to working directory

18 echo $PBS_NODEFILE

19 cd $PBS_O_WORKDIR
21 for ((i=$minbox; i<=$maxbox; i++)); do</pre>
      for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
24
25
          if [ $snap -lt 10 ]; then
26
             j=00$snap
27
28
          elif [ $snap -lt 100 ]; then
          j=0$snap
29
30
          base_dir=~/projects/simulations/rockstar/box${i}
crossmatch_dir=${base_dir}/crossmatch/snap${j}
31
32
33
34
35
          snap_dir_21pt=${base_dir}/21pt/snap${j}
          snap_dir_za=${base_dir}/za/snap${j}
logfile=${crossmatch_dir}/match_halos.log
36
37
38
          echo "Startingubox${i}usnap${j}..."
39
             #mpiexec -verbose -n 1 \setminus
41
             ./match.py -o ${crossmatch_dir}/halos.dat \
                             -m ${crossmatch_dir}/crossmatch_000.txt \
-d ${snap_dir_21pt}/halos/density_profile_halos.dat \
                              -d ${snap_dir_za}/halos/density_profile_halos.dat \
-p ${snap_dir_21pt}/halos/out_0.list.parents \
-p ${snap_dir_za}/halos/out_0.list.parents \
                             $\
$\snap_dir_2lpt}/halos/halos_0.*.ascii \
$\snap_dir_za}/halos/halos_0.*.ascii \
50
                              > ${logfile} 2>&1
51
             echo 'Aligning columns...' >> ${logfile} 2>&1
```

Appendix G

Halo Comparison Code

G.1 Particle Comparison (Python)

```
1 #!/usr/bin/env python
        import sys
       import bgc2
 4 import bgc2
5 import numpy as np
6 import matplotlib.pyplot as plt
7 from matplotlib.patches import Circle
8 from matplotlib.ticker import MultipleLocator
9 from scipy.optimize import curve_fit
10 from scipy.stats import chisquare
 12 #id1, id2 = 727, 4420 # 21pt first
13 #id1, id2 = 4416, 727 # za first
 15 #id1, id2 = 4416, 4420 # both za
16 #id1, id2 = 4416, 4416 # both za
  18 #id1, id2 = 653, 4355
10 #1d1, 1d2 = 053, 435b

19 #id1, id2 = 38, 3803

20 #id1, id2 = 155099, 80362

21 #id1, id2 = 98722, 14357

22 id1, id2 = 84289, 143514
24
25 #read_mode = 'ascii2'
26 read_mode = 'bgc2'
28 if read_mode == 'bgc2':
29 use_bgc2 = True
30 use_all = False
            multiple_halos = True
 32
33
             individual_masses = False
            halo_id = 146289
nbins = 50
nfit = 500
ooms = 3.0
 34
35
 37
38
39
             mass_scale = 1.0
            common_mass = 5.33423e5
dist_scale = 1.0e3
#res_limit = 0.488
            #res_limit = 0.488
res_limit = 4.0
#res_limit = 10.0
#draw_frac = 1.0e-2
draw_frac = 1.0
tick_base_major = 10.0
45 tick_base_major = 10.0
46 tick_base_minor = 1.0
47 elif read_mode == 'ascii':
48 use_bgc2 = False
49 use_all = True
50 individual_masses = True
51 halo_id = 0
52 nbins = 100
53 nfit = 500
54 ooms = 5.0
55 mass scale = 1.0e12
individual_masses = True
halo_id = 0
nbins = 100
nfit = 500
ooms = 3.5
66
67
            mass_scale = 1.0e10
dist_scale = 1.0
 70
            dist_scale = 1.0
res_limit = 3.0e-1
draw_frac = 1.0e-2
tick_base_major = 200.0
tick_base_minor = 40.0
 74 tich
75 else:
           sys.exit(98712)
77
78 outfile = 'halo_properties.txt'
79 comfile = 'center_of_mass.txt'
```

```
81 make plot = True
  82 plot_base = 'density_profile.fig.'
83 plot_ext = '.eps'
84 dist_units = 'kpc'
  85 \text{ xlabel\_proj} = [r'X_{\square}Position_{\square}(\%s_{\square}h\$^{-\{-1\}\$})' \% \text{ (dist\_units)}, r'X_{\square}Position_{\square}(\%s_{\square}h\$^{-\{-1\}\$})' \% \text{ (dist\_units)}, r'Y_{\square}Position_{\square}(\%s_{\square}h\$^{-\{-1\}\$})' \% 
 Nature:_proj = [r'Alposition_U(Asunt \tau) / A (dist_units), r'Alposition_U(Asunt \tau) / A (dist_units), r'Yu

Position_U(Asunt \tau -1)\$)' % (dist_units)]

86 ylabel_proj = [r'YuPosition_U(\sunt \tau -1)\$)' % (dist_units), r'ZuPosition_U(\sunt \tau \tau \tau \tau) / A (dist_units), r'ZuPosition_U(\sunt \tau \tau \tau) / A (dist_units)]

87 xlabel_prof = r'Radius_U(\sunt \tau \tau \tau) / A (dist_units)

88 ylabel_prof = r'Density_U(\sunt \tau \tau \tau) / A (\sunt \tau \tau) / A (\sunt \tau \tau) / A (\sunt \tau) / A (\sun
  90 #common_mass = 1.0e-7
91 #common_mass = 1.0e5
  92 \text{ mass col} = 0
  93 pos_cols = (1,2,3)
94 vel_cols = (4,5,6)
  95 \text{ halo_id_col} = 0
  97 grav_const = 4.3e-6 # kpc M_sol^-1 (km/s)^2
   99 profile_type = 0 # 0 -> nfw, fit rho_0
100
                                                                           # 1 -> nfw, calculate rho_0
                                                                          # 2 -> nfw, rho_0 middle of leftmost bin above resolution # 3 -> fit outer slope, fit rho_0
101
103
                                                                          # 4 -> fit outer slope, calculate rho_0
                                                                          # 5 -> fit outer slope, rho_0 middle of leftmost bin above resolution
104
106 def read_files(files):
107
               data = 0
 108
                  for file in files:
                      print 'Reading_file_%s...' % (file)
109
                         if data == 0:
110
                                  data = np.genfromtxt(file, comments='#')
                         else:
                             data = np.append(data, np.genfromtxt(file, comments='#'), axis=0)
114
                  print 'Finished reading files
115
                   return data
118 def calc_density_profile(mass, pos):
119    r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)
                  max_r = r.max()
#min_r = max_r / 10**ooms
120
                   min_r = res_limit
                  log_range = np.log10(max_r) - np.log10(min_r)
124
                  #global nbins
local_nbins = float(nbins + 1)
 125
126
                   #nbins = len(r) / 1000
 128
                    while True:
                        bins = np.arange(local_nbins)
 130
                          bins = max_r * 10.0**(log_range * bins / (local_nbins-1.0) - log_range)
                        bin_mass, r_bins = np. histogram(r, bins, weights=mass)
if (bin_mass == 0.0).any():
                              local_nbins -= 1
134
                                continue
135
                       else:
 136
138
                   #print 'Binning particles using bin edges of \n', r_bins
 139
140
                  rho = bin_mass / (sphere_vol(r_bins[1:]) - sphere_vol(r_bins[:-1]))
142
                   N_bin, blah = np.histogram(r, bins)
                   rho_err = poisson_error(N_bin) * rho
143
145
                  return r_bins, rho, rho_err
146
148 def logbin(pos):
                 r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)
149
                  max_r = r.max()
min_r = max_r / 10**ooms
152
                   log_range = np.log10(max_r) - np.log10(min_r)
154
                   global nbins
                   nbins = float(nbins + 1)
156
                   bins = np.arange(nbins)
                   bins = max_r * 10.0**(log_range * bins / (nbins-1.0) - log_range)
157
159
                  hist, bin_edges = np.histogram(r, bins)
160
                   \label{print Binning particles using bin edges of $$\n'$, bin_edges$}
                   return hist, bin_edges
162
163
 164 def poisson_error(N):
                 err = np.sqrt(N) / N
return err
165
167
168
168
169 def sphere_vol(r):
170 volume = (4.0 / 3.0) * np.pi * r**3
```

```
return volume
174 def get_rho_0(R_s, R_vir):
       H = 70.0e-3 # km s^-1 kpc^-1

G = 4.3e-6 # kpc M_sol^-1 (km/s)^2

rho_crit = 3.0 * H**2 / (8.0 * np.pi * G)
176
179
       v = 178
       c = R_vir / R_s
g = 1.0 / (np.log(1.0+c) - c/(1.0+c))
181
182
       delta_char = v * c**3 * g / 3.0
184
       return rho crit * delta char
185
187 def nfw_fit_rho0(r, R_s, rho_0):
188     return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
190
191 def nfw_fit_rho0_log(r, R_s, rho_0):
    r = 10.0**r
R_s = 10.0**R_s
193
       rho_0 = 10.0**rho_0
195
       profile = rho_0 / ((r / R_s) * (1.0 + r / R_s) **2)
196
       return np.log10(profile)
198
199 def nfw_def_rho0(R_vir):
      def _nfw_def_rho0(r, R_s):
        rho_0 = get_rho_0(R_s, R_vir)
return rho_0 / ((r / R_s) * (1.0 + r / R_s)**2)
201
202
203
       return _nfw_def_rho0
204
206 def nfw_databin_rho0(rho_0):
     def _nfw_databin_rho0(r, R_s):
    return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
207
209
       return _nfw_databin_rho0
210
212 def dm_profile_fit_rho0_log(r, R_s, rho_0, alpha):
213 r = 10.0**r
       r = 10.0**r
R_s = 10.0**R_s
215
       rho 0 = 10.0**rho 0
       alpha = 10.0**alpha
216
       profile = rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**alpha)
218
       return np.log10(profile)
221 def dm_profile_fit_rho0(r, R_s, rho_0, alpha):
222 return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s ) **alpha)
224
225 def dm_profile_def_rho0(R_vir):
226
     def _dm_profile_def_rho0(r, R_s, alpha):
        rho_0 = get_rho_0(R_s, R_vir)
return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s ) **alpha)
229
       return _dm_profile_def_rho0
232 def dm_profile_databin_rho0(rho_0):
     def _dm_profile_databin_rho0(r, R_s, alpha):
    return rho_0 / ((r / R_s) * (1.0 + r / R_s) **alpha)
    return _dm_profile_databin_rho0
234
235
237
238 def fit_profile(r, rho, err=None, R_vir=None):
      for i in range(len(r)):
240
         if r[i] > res_limit:
241
          rho_0_databin = rho[i]
             first_good_bin = i
       break
#------
choose one fitting type ------
#popt, pcov = curve_fit(nfw_fit_rho0, r, rho, sigma=err)
#popt, pcov = curve_fit(nfw_def_rho0(R_vir), r, rho, p0=[10.0], sigma=err)
#popt, pcov = curve_fit(nfw_databin_rho0(rho_0_databin), r, rho, sigma=err)
blah = 2
243
245
246
248
       if blah == 0:
249
         for i in range(100):
           a = 2.0 * np.random.random() * 0.1 * r.max()
b = 2.0 * np.random.random() * 10.0
c = 2.0 * np.random.random() * 2.0
251
252
254
            try:
               popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err)
256
            except RuntimeError:
257
               continue
             if (popt[0] < r.max()) and (popt[2] >= 0.0):
259
             break
elif i >= 99:
260
              print 'nougoodufitufounduforuthisuhalo...'
262 #
                 return None, None, None, None, None
```

```
elif blah == 1:
           #a = r.max() / 100.0
a = 0.001
265
            b = rho[first_good_bin]
266
            #popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, sigma=err)
print '-----'
268
269
270
271
            print 'rho_0_before_=', b
            #try:
            #popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err, maxfev=1, xtol=100.0)
popt, pcov = curve_fit(dm_profile_fit_rho0, r, rho, p0=[a,b,c], sigma=err, xtol=1.0e-1)
273
274
            #except RuntimeError:
# print 'just checking for now...'
276
            print 'rho_0uafteru=', popt[1]
277
            #sys.exit()
           #popt, pcov = curve_fit(dm_profile_fit_rho0_log, np.log10(r), np.log10(rho), sigma=np.log10(err))
popt, pcov = curve_fit(nfw_fit_rho0_log, np.log10(r), np.log10(rho), sigma=np.log10(err))
279
         popt, pcov = curv
popt = 10.0**popt
pcov = 10.0**pcov
elif blah == 3:
281
282
284
           popt, pcov = curve_fit(nfw_fit_rho0, r, rho, sigma=err)
285
         #popt, pcov = curve_fit(dm_profile_def_rho0(R_vir), r, rho, sigma=err)
287
         #popt, pcov = curve_fit(dm_profile_databin_rho0(rho_0_databin), r, rho, sigma=err)
288
        print 'fit_params_=', popt
        print 'covariance_=', pcov

nfw_r = np.linspace(r[0], r[-1], nfit)

#----- choose one fitting type ---
290
291
        nfw_fit = nfw_fit_rho0(nfw_r, popt[0], popt[1])
293
294
        #nfw_fit = nfw_def_rho0(R_vir)(nfw_r, popt[0])
#nfw_fit = nfw_databin_rho0(rho_0_databin)(nfw_r, popt[0])
295
        #nfw_fit = dm_profile_fit_rho0(nfw_r, popt[0], popt[1], popt[2])
#nfw_fit = dm_profile_def_rho0(R_vir)(nfw_r, popt[0], popt[1])
296
298
         #nfw_fit = dm_profile_databin_rho0(rho_0_databin)(nfw_r, popt[0], popt[1])
         #-----
299
                                                           ----#
         #----- choose one fitting type -----
         chi2_fit = nfw_fit_rho0(r, popt[0], popt[1])
#chi2_fit = nfw_def_rho0(R_vir)(r, popt[0])
#chi2_fit = nfw_databin_rho0(rho_0_databin)(r, popt[0])
301
302
        #chi2_fit = dm_profile_fit_rho0(r, popt[0], popt[1], popt[2])
#chi2_fit = dm_profile_def_rho0(R_vir)(r, popt[0], popt[1])
#chi2_fit = dm_profile_databin_rho0(rho_0_databin)(r, popt[0], popt[1])
304
305
306
307
308
        chi2 = chisquare(np.log10(rho[first_good_bin:]), np.log10(chi2_fit[first_good_bin:]))
chi2_nolog = chisquare(rho[first_good_bin:], chi2_fit[first_good_bin:])
print 'chi_square_=', chi2
print 'chi_square_nolog_=', chi2_nolog
309
310
311
312
         return nfw_r, nfw_fit, popt, pcov, chi2[0]
def draw_projection(fig, place, plot_lim, x, y):

316 def draw_projection(fig, place, plot_lim, x, y):

317 ax = plt.subplot(1,3,place+1, aspect='equal')

318 im = ax.plot(x, y, linestyle='', marker='.', markersize=1, markeredgecolor='blue')

319 ax.set_xlabel(xlabel_proj[place])

320 ax.set_ylabel(ylabel_proj[place])
321
        ax.set_xlim(-plot_lim, plot_lim)
ax.set_ylim(-plot_lim, plot_lim)
323 # ax.xaxis.set_major_locator(MultipleLocator(tick_base_major))
324 # ax.xaxis.set_minor_locator(MultipleLocator(tick_base_minor))
325 # ax.yaxis.set_major_locator(MultipleLocator(tick_base_major))
326 # ax.yaxis.set_minor_locator(MultipleLocator(tick_base_minor))
        return fig, ax
329
330 def draw_projection_again(fig, ax, x, y):
331 im = ax.plot(x, y, linestyle='', marker='.', markersize=1, markeredgecolor='red')
        return fig
335 def draw_density_profile(fig, r, rho, err=None):
        ax = plt.subplot(2,1,2)
im = ax.loglog(r, rho, linestyle='steps-mid-')
        line1 = ax.axvline(res_limit, color='black', linestyle=':')
#ax.set_xlim(r_bins[0], r_bins[-1])
ax.set_xlim(r[0] - (r[1]-r[0]), r[-1] + (r[-1]-r[-2]))
338
340
        ax.set_xlabel(xlabel_prof)
341
         ax.set_ylabel(ylabel_prof)
343
        if err != None:
344
           err_bars = ax.errorbar(r, rho, yerr=err,linestyle='None')
        return fig, ax
346
348 def draw_nfw_profile(fig, ax, r, rho, R_s=None):
349 ax.loglog(r, rho, linestyle='-', color='red')
350 if R_s != None:
351
            line = ax.axvline(R_s, color='purple', linestyle='-.')
352
         return fig
354
```

```
355 def calc_kinetic_energy(mass, vel):
      vsq = vel[:,0]**2 + vel[:,1]**2 + vel[:,2]**2
energy = 0.5 * np.sum(mass*vsq)
357
358
        return energy
359
360
361 def calc_potential_energy(mass, pos):
       local_sqrt = np.sqrt
partial_sum = 0.0
363
        for i in range(len(mass)):
365
          for j in range(len(mass)):
       if j != i:
    r_diff = local_sqrt((pos[i,0] - pos[j,0])**2 + (pos[i,1] - pos[j,1])**2 + (pos[i,2] - pos[j,2])**2)
    partial_sum = partial_sum - mass[i]*mass[j]/r_diff
energy = partial_sum * grav_const / 2.0
return energy
366
368
369
370
371
373 def calc_angular_momentum(mass, pos, vel):
       ang_mom_x = np.sum(mass * (pos[:,1] * vel[:,2] - pos[:,2] * vel[:,1]))
ang_mom_y = np.sum(mass * (pos[:,2] * vel[:,0] - pos[:,0] * vel[:,2]))
ang_mom_z = np.sum(mass * (pos[:,1] * vel[:,2] - pos[:,2] * vel[:,1]))
ang_mom = np.sqrt(ang_mom_x**2 + ang_mom_y**2 + ang_mom_z**2)
374
376
        return ang_mom
379
380
381 def main():
382
        #for input_file in sys.argv[1:]:
        #header1, halos1, particles1 = bgc2.read_bgc2(sys.argv[1])
#header2, halos2, particles2 = bgc2.read_bgc2(sys.argv[2])
383
385
        nargs = len(sys.argv) - 1
if (float(nargs) % 2.0) != 0.0:
386
387
          print 'number of arguments must be even'
388
389
           sys.exit()
390
391
        for i in range(nargs / 2):
           temp_header1, temp_halos1, temp_particles1 = bgc2.read_bgc2(sys.argv[i])
temp_header2, temp_halos2, temp_particles2 = bgc2.read_bgc2(sys.argv[(nargs / 2) + i])
if i == 1:
303
394
395
              halos1, particles1 = temp_halos1, temp_particles1 halos2, particles2 = temp_halos2, temp_particles2
396
397
398
399
              halos1 = np.append(halos1, temp_halos1, axis=0)
              halos2 = np.append(halos2, temp_halos2, axis=0)
particles1 = np.append(particles1, temp_particles1, axis=0)
particles2 = np.append(particles2, temp_particles2, axis=0)
400
401
402
403
        halos1 = np.asarray(halos1)
halos2 = np.asarray(halos2)
404
405
        #indices = np.argsort(halos[:,2])
#indices = indices[::-1]
                                                                  # sort by number of particles
407
                                                                    # start with the biggest
408
409
410
        \hbox{\tt\#for index in indices}\,[:1000]:
411
        #for index in indices:
412
        for index in range(halos1.shape[0]):
413
          halo_id = halos1[index,0]
if (halo_id == id1):
414
415
416
              halo_particles1 = np.asarray(particles1[index])
              pos1 = halo_particles1[:,pos_cols[0]:pos_cols[0]+3] * dist_scale
#vel1 = halo_particles1[:,vel_cols[0]:vel_cols[0]+3]
418
419
420
421
               r_vir1 = halos1[index][4] * dist_scale
              halo_mass1 = halos1[index][5]
halo_pos1 = np.array([halos1[index][6] * dist_scale, halos1[index][7] * dist_scale, halos1[index][8] *
422
             dist_scale])
424
              #halo_vel1 = np.array([halos1[index][9], halos1[index][10], halos1[index][11]])
425
              print 'Usingu%duparticlesuinuhalou%d.' % (halo_particles1.shape[0], halo_id)
426
427
428
              # Find center of mass
429
              #pos = pos - halo_pos
#vel = vel - halo_vel
430
431
              \mbox{\tt\#} Pick only a certain perentage of particles for projection plots if (draw_frac < 1.0):
432
434
                 np.random.shuffle(pos1)
435
                 pos1 = pos1[:(draw_frac*pos1.shape[0])]
        for index in range(halos2.shape[0]):
   halo_id = halos2[index,0]
437
438
439
          if (halo_id == id2):
             print '----
440
442
              halo_particles2 = np.asarray(particles2[index])
              mail_particles2 = np.asariay(particles2[index])
pos2 = halo_particles2[:,pos_cols[0]:pos_cols[0]+3] * dist_scale
#vel2 = halo_particles2[:,vel_cols[0]:vel_cols[0]+3]
443
445
```

```
r_vir2 = halos2[index][4] * dist_scale
               halo_mass2 = halos2[index][5]
halo_pos2 = np.array([halos2[index][6] * dist_scale, halos2[index][7] * dist_scale, halos2[index][8] *
448
              dist scale])
449
               #halo_vel2 = np.array([halos2[index][9], halos2[index][10], halos2[index][11]])
450
451
               print 'Using | %duparticles | in | halo | %d. ' % (halo particles 2.shape [0], halo | id)
452
453
               # Find center of mass
454
              #pos = pos - halo_pos
#vel = vel - halo_vel
455
456
457
               # Pick only a certain perentage of particles for projection plots
458
               if (draw frac < 1.0):
                 np.random.shuffle(pos2)
pos2 = pos2[:(draw_frac*pos2.shape[0])]
459
460
461
462
        # Find the maximum of x, y, or z to be limit of projection plots
463
        center = (halo_pos1 + halo_pos2) / 2.0
        pos1 = pos1 - center
pos2 = pos2 - center
464
465
        halo_pos1 = halo_pos1 - center
halo_pos2 = halo_pos2 - center
466
467
        plot_lim = np.append(pos1, pos2).max()
469
        # Plot density profile histogram
if (make_plot == True):
470
472
           fig = plt.figure()
473
474
            fig, ax = draw_projection(fig, 0, plot_lim, pos1[:,0], pos1[:,1])
           fig = draw_projection_again(fig, ax, pos2[:,0], pos2[:,1])
ax.add_patch(Circle((halo_pos1[0], halo_pos1[1]), r_vir1, fc="None", ec="black", lw=1))
ax.add_patch(Circle((halo_pos2[0], halo_pos2[1]), r_vir2, fc="None", ec="black", lw=1))
475
476
478
           fig, ax = draw_projection(fig, 1, plot_lim, pos1[:,0], pos1[:,2])
fig = draw_projection_again(fig, ax, pos2[:,0], pos2[:,2])
ax.add_patch(Circle((halo_pos1[0], halo_pos1[2]), r_vir1, fc="None", ec="black", lw=1))
ax.add_patch(Circle((halo_pos2[0], halo_pos2[2]), r_vir2, fc="None", ec="black", lw=1))
480
481
483
           fig, ax = draw_projection(fig, 2, plot_lim, pos1[:,1], pos1[:,2])
fig = draw_projection_again(fig, ax, pos2[:,1], pos2[:,2])
ax.add_patch(Circle((halo_pos1[1], halo_pos1[2]), r_vir1, fc="None", ec="black", lw=1))
ax.add_patch(Circle((halo_pos2[1], halo_pos2[2]), r_vir2, fc="None", ec="black", lw=1))
484
485
486
487
488
489
            #fig, ax = draw_density_profile(fig, mid_bins, rho, err=rho_err)
490
           #fig = draw_nfw.profile(fig, ax, nfw_r, nfw_fit, R_s=scale_radius)
fig.tight_layout()
491
           #plt.savefig()test.eps')
492
494
495
496 if __name__ == '__main__':
        main()
```

G.2 Density Comparison (Python)

```
1 #!/usr/bin/env python
 3 import sys
 4 import bgc2
 5 import numpy as np
6 import matplotlib as mpl
  mpl.use('Agg')
 8 import matplotlib.pyplot as plt
9 from matplotlib.patches import Circle
10 from matplotlib import patheffects
Il from mpl_toolkits.axes_grid1 import ImageGrid
12 from scipy.stats import ks_2samp
13 from scipy.stats import chisquare
from scipy.optimize import curve_fit from scipy.optimize import curve_fit from scipy.ndimage.filters import gaussian_filter
16 from ipdb import set_trace
19\, #### Note: only run one box pair at a time.
                   ./compare.py /crossmatch_dir/halos.dat /2lpt_dir/halos_0.*.bgc2 /za_dir/halos_0.*.bgc2
20 #### ex:
22 def main():
         crossmatched_halo_file, bgc2_21pt_files, bgc2_za_files = parse_args(sys.argv[1:])
        header, halos = read files(crossmatched halo file, header line = 3)
        bgc2_21pt_header, bgc2_21pt_halos, bgc2_21pt_particles = get_bgc2_data(bgc2_21pt_files)
bgc2_za_header, bgc2_za_halos, bgc2_za_particles = get_bgc2_data(bgc2_za_files)
30
31
        bgc2_21pt_halos, bgc2_za_halos = map(np.asarray, (bgc2_21pt_halos, bgc2_za_halos))
        if sort col != None:
             halos = sort_by_column(halos, sort_col)
         if remove_nonfit_halos:
```

```
halos = remove nans(halos)
         if global_filter_halos:
38
              halos = filter_halos(halos)
         if (nhalos != None) or (nhalos != 0):
 39
              #halos = halos[:nhalos]
halos = halos[[0,70]]
                                                    ########################## hard coded for the moment
41
 42
              #halos = halos[10000:10050]
43
         header, halos = add_c_columns(header, halos)
header = reduce_header(header)
44
 45
46
        47
49
 50
         print 'Finished_all_plots.'
52
 54
    def parse_args(args):
         crossmatched_halo_file = args[0]
if len(args[1:]) % 2 != 0.0:
 55
 56
 57
58
             print 'Mustucalluwithuevenunumberuofubgc2ufiles...exiting.'
               sys.exit(-1)
         bgc2_files = args[1:]
         bgc2_2lpt_files = bgc2_files[:len(bgc2_files)/2]
bgc2_za_files = bgc2_files[len(bgc2_files)/2:]
return crossmatched_halo_file, bgc2_2lpt_files, bgc2_za_files
60
61
63
64
 65 def read_files(files, header_line = None, comment_char = '#'):
         header = None
data = None
66
67
         if type(files) == str:
 68
              files = [files]
69
 70
 71
         if header_line != None:
              with open(files[0], 'r') as fd:
    for line in range(header_line):
 72
73
 74
75
                        fd.readline()
              header = fd.readline()
if header[0] != comment_char:
 77
78
                    print "Header_must_start_with_a_',%s'" % comment_char
                    sys.exit(4)
              header = header[1:]
header = header.split()
 79
80
81
         for file in files:
              print 'Reading_file_%s...' % (file)
if data == None:
83
 85
                    data = np.genfromtxt(file, comments=comment_char)
86
                    data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
88
         print 'Finished_reading_files.'
if header_line == None:
89
 90
91
             return data
92
              return header, data
94
96 def get_bgc2_data(bgc2_files):
97
         header = None
halos = None
         particles = None
00
100
          for bgc2_file in bgc2_files:
              print 'Reading of ile o %s...' % (bgc2_file)
              tmp_header, tmp_halos, tmp_particles = bgc2.read_bgc2(bgc2_file)
if header == None:
    header = tmp_header
    halos = tmp_halos
    particles = tmp_particles
102
105
106
107
108
                    halos = np.append(halos, tmp_halos, axis=0)
         particles = np.append(particles, tmp_particles, axis=0)
print 'Finishedureadingubgc2ufiles.'
109
110
         return header, halos, particles
114 def sort_by_column(halos, col):
         print 'Sorting_halos...'
mask = np.argsort(halos[:, col])
116
         mask = mp.argsort(n
mask = mask[::-1]
halos = halos[mask]
         return halos
119
120
122 def remove_nans(halos):
         print 'Removing NaNs...
124
          halos = halos[halos[:,c_21pt_col] != -9999]
         halos = halos[np.isfinite(halos[:,c_21pt_col])]
halos = halos[np.isfinite(halos[:,c_21pt_col])]
         return halos
```

```
130 def filter_halos(halos):
          print 'Filteringudata...'
for col, val in zip(lt_cols, lt_vals):
               halos = halos[halos[:, col] <= val]
          for col, val in zip(gt_cols, gt_vals):
    halos = halos[halos[:, col] >= val]
134
          for col, val in zip(eq_cols, eq_vals):
    halos = halos[halos[:, col] == val]
136
138
          for col, val in zip(ne_cols, ne_vals):
               halos = halos[halos[:, col] != val]
          return halos
141
142
143 def add_c_columns(header, halos):
          c1_rockstar = halos[:, Rv1_col] / halos[:, Rs1_col]
c2_rockstar = halos[:, Rv2_col] / halos[:, Rs2_col]
144
145
146
          halos = np.column_stack((halos, c1_rockstar, c2_rockstar))
          header = np.append(header, 'c_rockstar')
header = np.append(header, 'c_rockstar')
147
148
149
          return header, halos
150
151
152 def reduce_header(header):
          header_2lpt = header[print_cols_2lpt]
header_za = header[print_cols_za]
153
          if (header_21pt == header_za).all():
156
               header = header_21pt
157
              print 'columnumismatch...uexiting'
158
159
                set_trace()
160
                sys.exit(123)
161
          return header
163
164 def make_plot(itteration, header, halo_pair, bgc2_halos_21pt, bgc2_halos_za, \
165 bgc2_particles_21pt, bgc2_particles_za):
166
          id_21pt = halo_pair[id_col_21pt]
                     = halo_pair[id_col_za]
167
          id_za = halo_pair[id_col_za]
properties_2lpt = halo_pair[print_cols_2lpt]
168
169
          properties_za = halo_pair[print_cols_za]
          # find 21pt and za halo from id
          halo_index_2lpt = np.where(bgc2_halos_2lpt[:, halo_id_col] == id_2lpt)[0][0]
halo_index_za = np.where(bgc2_halos_za[:, halo_id_col] == id_za)[0][0]
174
          bgc2_halos_21pt = bgc2_halos_21pt[halo_index_21pt]
          bgc2_halos_za = bgc2_halos_za[halo_index_za]
176
178
          # convert particles to numpy arrays
179
          bgc2_particles_21pt = np.asarray(bgc2_particles_21pt[halo_index_21pt])
bgc2_particles_za = np.asarray(bgc2_particles_za[halo_index_za])
180
181
          r_2lpt, rho_2lpt, rho_err_2lpt, r_vir_2lpt = density_profile(bgc2_halos_2lpt, bgc2_particles_2lpt)
r_za, rho_za, rho_err_za, r_vir_za = density_profile(bgc2_halos_za, bgc2_particles_za)
183
184
185
186
          # fit density profiles
nfw_r_2lpt, nfw_rho_2lpt, r_s_2lpt = fit_profile( r_2lpt / r_vir_2lpt, rho_2lpt / rho_2lpt.max(), err =
            rho_err_2lpt / rho_2lpt.max() )
188
          nfw_r_za , nfw_rho_za , r_s_za
rho_err_za / rho_za.max() )
                                                           = fit_profile( r_za / r_vir_za, rho_za / rho_za.max(), err =
190
          # de-normalize values
190
          nfw_r_2lpt = nfw_r_2lpt * r_vir_2lpt
          nrw.1_zlpt = nrw.1_zlpt * r_vir_zlpt
nfw_r_za = nfw_r_za * r_vir_za
nfw_rho_2lpt = nfw_rho_2lpt * rho_2lpt.max()
nfw_rho_za = nfw_rho_za * rho_za.max()
r_s_2lpt = r_s_2lpt * r_vir_2lpt
r_s_za = r_s_za * r_vir_za
192
193
194
195
196
197
198
          # find center of halos and plot limit
          halo_pos_21pt = bgc2_halos_21pt[:,halo_pos_cols] * dist_scale
halo_pos_za = bgc2_halos_za[:,halo_pos_cols] * dist_scale
199
200
          particle_pos_21pt = bgc2_particles_21pt[:,particle_pos_cols] * dist_scale
particle_pos_za = bgc2_particles_za[:,particle_pos_cols] * dist_scale
201
202
203
204
          if wrap_box:
                for i in range(3):
206
                     if abs(halo_pos_2lpt[i] - halo_pos_za[i]) > box_size / 2.0:
207
                            if (halo_pos_2lpt[i] > halo_pos_za[i]):
                                 halo_pos_za[i] += box_size
particle_pos_za[:,i] += box_size
209
210
                            if (halo_pos_2lpt[i] < halo_pos_za[i]):
   halo_pos_2lpt[i] += box_size
   particle_pos_2lpt[:,i] += box_size</pre>
211
214
                                 print "error in wrapping"
                                 sys.exit()
```

```
center = (halo_pos_21pt + halo_pos_za) / 2.0
218
         halo_pos_21pt = halo_pos_21pt - center
halo_pos_za = halo_pos_za - center
         halo_pos_za = halo_pos_za - center
particle_pos_21pt = particle_pos_21pt - center
particle_pos_za = particle_pos_za - center
220
224
         if zoom_projections:
             plot_lim = zoom_scale
225
         else:
226
              plot_lim = np.append(particle_pos_21pt, particle_pos_za).max()
228
229
         r_vir_21pt = bgc2_halos_21pt[halo_r_col] * dist_scale
         r_vir_za = bgc2_halos_za[halo_r_col] * dist_scale
              print 'generating_plot...'
fig = plt.figure(figsize = (9.0, 6.0))
234
235
236
              fig = make_projections(fig, 221, halo_pos_21pt, halo_pos_za, particle_pos_21pt, particle_pos_za, \
              r_vir_2lpt, r_vir_za, plot_lim)
ax = fig.add_subplot(223)
              ax = draw_density_profile(ax, r_2lpt, rho_2lpt, err=rho_err_2lpt, color='blue', label='2lpt')
ax = draw_density_profile(ax, r_za, rho_za, err=rho_err_za, color='red', label='za')
239
240
242
243
              ax = fig.add_subplot(122)
ax = draw_parameters(ax, header, properties_21pt, properties_za)
              fig.tight_layout()
245
              plot_name = "%s%0.3d_(%d,%d)%s" % (plot_base, itteration, id_2lpt, id_za, plot_ext) plt.savefig(plot_name, bbox_inches='tight') print 'finished_uplot_u' + plot_name
246
247
248
249
250
         if make_projection:
              print 'generatingudensityuprojectionuplot...'
fig = plt.figure(figsize = (9.0, 6.0))
251
253
254
              if label_projection:
                   ax = fig.add_subplot(111, aspect=2.0/3.2)
ax = hide_axes(ax)
255
256
257
                    ax.set_xlabel(proj_xlabel)
                    ax.set_ylabel(proj_ylabel)
259
              260
261
262
              fig.tight_layout()
              plot_name = "%s%0.3d_(%d,%d)%s%s" % (plot_base, itteration, id_21pt, id_za, proj_name, plot_ext)
263
              plt.savefig(plot_name, blox_inches='tight')
print 'finished_density_projection_plot_' + plot_name
264
265
266
         if make_density_profile:
267
              print 'generating_density_profile_plot...'
fig = plt.figure(figsize = (9.0, 12.0))
268
269
270
271
              if label_projection:
    ax = fig.add_subplot(211, aspect=2.0/3.2)
    ax = hide_axes(ax)
273
274
                    ax.set_xlabel(proj_xlabel)
                    ax.set_ylabel(proj_ylabel)
276
277
              fig = make_projections(fig, 211, halo_pos_21pt, halo_pos_za, particle_pos_21pt, particle_pos_za, \
278
                                            r_vir_2lpt, r_vir_za, plot_lim)
279
280
              ax = fig.add_subplot(212)
281
               ax = hide_axes(ax)
              ax.set_xlabel(prof_xlabel)
282
283
              ax.set_ylabel(prof_ylabel)
284
285
              #grid = ImageGrid(fig. 212. nrows ncols=(2.1), axes pad=0.24)
286
287
              ax1 = fig.add_subplot(413)
              ax1 = draw_density_profile(ax1, r_2lpt, rho_2lpt, err=rho_err_2lpt, color='blue')
ax1 = draw_nfw_profile(ax1, nfw_r_2lpt, nfw_rho_2lpt, R_s=r_s_2lpt, color='red')
288
289
290
291
              ax2 = fig.add_subplot(414)
292
              ax2 = draw_density_profile(ax2, r_za, rho_za, err=rho_err_za, color='blue')
              ax2 = draw_nfw_profile(ax2, nfw_r_za, nfw_rho_za, R_s=r_s_za, color='red')
293
294
295
              if equal_profile_axes:
                    ymin = min(ax1.get_ylim()[0], ax2.get_ylim()[0])
ymax = max(ax1.get_ylim()[1], ax2.get_ylim()[1])
296
298
                    ax1.set_ylim(ymin, ymax)
299
                    ax2.set_ylim(ymin, ymax)
                    xmin = min(ax1.get_xlim()[0], ax2.get_xlim()[0])
xmax = max(ax1.get_xlim()[1], ax2.get_xlim()[1])
301
                    ax1.set_xlim(xmin, xmax)
303
304
                    ax2.set_xlim(xmin, xmax)
305
306
                    ax1.text(0.95, 0.85, '2LPT', color='black', horizontalalignment='right', verticalalignment='center',
           transform=ax1.transAxes)
```

```
ax2.text(0.95, 0.85, 'ZA', color='black', horizontalalignment='right', verticalalignment='center',
308
           transform=ax2.transAxes)
309
310
               #fig.tight_layout()
               plot_name = "%s%0.3d_(%d,%d)%s%s" % (plot_base, itteration, id_2lpt, id_za, dens_name, plot_ext)
               ptt.savefig(plot_name, bbox_inches='tight')
print 'finished_density_profile_plot_' + plot_name
314
315
316
317
320
          halo_pos = halo[halo_pos_cols] * dist_scale
          manupos = nant(manupos_cors) * uns_scale
#mass = np.ones(particles.shape[0]) * common_mass * mass_scale
mass = particles[:,particle_mass_col] * mass_scale
321
          pos = particles[:,particle_pos_cols] * dist_scale
324
          pos = pos - halo_pos
325
          r_bins, rho, rho_err = calc_density_profile(mass, pos)
mid_bins = 10.0**(0.5 * (np.log10(r_bins[1:]) + np.log10(r_bins[:-1])))
326
328
          # Don't pass NaN's to fitting routine
329
330
          rho_err_nonan = np.copy(rho_err)
331
          nan_check = np.isnan(rho_err_nonan)
332
          for i in range(len(rho_err_nonan)):
               if (mid_bins[i] < res_limit) or (nan_check[i] == True):</pre>
                    rho_err_nonan[i] = 1.0e10
334
335
          return mid_bins, rho, rho_err, r_vir
338
339 def calc_density_profile(mass, pos):
         r = np.sqrt(pos[:,0]**2 + pos[:,1]**2 + pos[:,2]**2)
max_r = r.max()
min_r = res_limit
340
342
          log_range = np.log10(max_r) - np.log10(min_r)
local_nbins = float(nbins + 1)
343
344
345
          while True:
               bins = np.arange(local_nbins)
bins = max_r * 10.0**(log_range * bins / (local_nbins-1.0) - log_range)
346
347
               bin_mass, r_bins = np.histogram(r, bins, weights=mass)
if (bin_mass == 0.0).any():
348
349
350
                    local_nbins -= 1
351
                    continue
352
               else:
353
         rho = bin_mass / (sphere_vol(r_bins[1:]) - sphere_vol(r_bins[:-1]))
354
          N_bin, blah = np.histogram(r, bins)
rho_err = poisson_error(N_bin) * rho
355
356
357
          return r_bins, rho, rho_err
350
360 def sphere_vol(r):
361 volume = (4.0 / 3.0) * np.pi * r**3
362
         return volume
363
365 def poisson_error(N):
          err = np.sqrt(N) / N
366
367
          return err
368
369
370 def fit_profile(r, rho, err=None, R_vir=None):
         popt, poov = curve_fit(nfw_profile, r, rho, sigma=err, p0=[0.1, 1.0])
R_s, rho_0 = popt[0], popt[1]
nfw_r = np.linspace(r[0], r[-1], nfit)
nfw_rho = nfw_profile(nfw_r, R_s, rho_0)
return nfw_r, nfw_rho, R_s
372
373
374
375
376
377
378 def nfw_profile(r, R_s, rho_0):
          if R_s >= 1.0:
380
          return (R_s - 1.0) * np.exp(r) + rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
return rho_0 / (( r / R_s ) * ( 1.0 + r / R_s )**2)
381
382
384 def filter_column(x, x_col):
          print 'Filteringudata...'
x = x[x != -9999]
385
         if x_col in lt_cols:
   val = lt_vals[lt_cols.index(x_col)]
387
388
               x = x[x \le val]
         if x_col in gt_cols:
    val = gt_vals[gt_cols.index(x_col)]
390
391
               x = x[x >= val]
         if x_col in eq_cols:
    val = eq_vals[eq_cols.index(x_col)]
    x = x[x == val]
393
395
396
         if x_col in ne_cols:
    val = ne_vals[ne_cols.index(x_col)]
398
               x = x[x != val]
```

```
return x
401
402 def draw hist(fig. ax. x. x min=None, x max=None, use log=False, color=None, label=None):
         if use_log:
    xbins = np.logspace(np.log10(x_min), np.log10(x_max), num=nbins+1)
404
405
               ax.set xscale('log')
406
407
               xbins = np.linspace(x_min, x_max, num=nbins+1)
408
409
          n, bins, patches = ax.hist(x, bins=xbins, histtype='step', log=ylog, color=color, label=label)
410
         412
413 def add_text(fig, ax, textstr):
414 props = dict(boxstyle='round', facecolor='white', alpha=0.7)
415
          ax.text(0.02, 0.08, textstr, transform=ax.transAxes, fontsize=14, \
416
                    verticalalignment='top', bbox=props)
          return fig, ax
417
418
419
420 def make_projections(fig, position, halo_pos1, halo_pos2, pos1, pos2, r_vir1, r_vir2, plot_lim):
         #grid = ImageGrid(fig, position, nrows_ncols=(2,3), axes_pad=0.05, cbar_mode='single')
grid = ImageGrid(fig, position, nrows_ncols=(2,3), axes_pad=0.12, cbar_mode='single')
421
423
          for i, (x, y, hx, hy, r) in enumerate(zip( \
                    424
426
427
429
               ax = grid[i]
430
               draw_projection(ax, x, y, hx, hy, r, plot_lim)
431
               if print_text:
432
                    if i == 0:
                         ax.text(0.05, 0.12, '2LPT', color='white', horizontalalignment='left', verticalalignment='center'
           , transform=ax.transAxes, path_effects=[patheffects.withStroke(linewidth=3, foreground='black
                    if i == 3:
434
                         ax.text(0.05, 0.12, 'ZA', color='white', horizontalalignment='left', verticalalignment='center'
           , transform=ax.transAxes, path_effects=[patheffects.withStroke(linewidth=3, foreground='black
436
            ax.text(0.95, 0.88, 'XY', color='white', horizontalalignment='right', verticalalignment='center', transform=ax.transAxes, path_effects=[patheffects.withStroke(linewidth=3, foreground='black')])
438
440
                        ax.text(0.95, 0.88, 'XZ', color='white', horizontalalignment='right', verticalalignment='center',
             transform=ax.transAxes, path_effects=[patheffects.withStroke(linewidth=3, foreground='black')])
            ax.text(0.95, 0.88, 'YZ', color='white', horizontalalignment='right', verticalalignment='center', transform=ax.transAxes, path_effects=[patheffects.withStroke(linewidth=3, foreground='black')])
442
443
444
445 def draw_projection(ax, x, y, hx, hy, r, plot_lim):
447 limits = [[-plot_lim, plot_lim], [-plot_lim, plot_lim]]
448 z, xedges, yedges = np.histogram2d(x, y, bins=npixels, range=limits)
449 if log_scale_projections:
450
              z[z<1.0] = 0.5
               z = p \cdot \log 10(z)

z = p \cdot \log 10(z)

z = p \cdot \log 10(z)
451
452
453
               \#z[np.isinf(z)] = -0.1
               plot_norm = mpl.colors.LogNorm(vmin = 1, vmax = z.max(), clip=True)
454
               #plot_norm = None
455
456
457
               plot_norm = None
         if extra_smoothing:
458
459
              z = gaussian_filter(z, smoothing_radius)
         im = ax.imshow(z.T, extent=(-plot_lim, plot_lim, -plot_lim, plot_lim), \
    interpolation='gaussian', origin='lower', cmap=colormap, norm=plot_norm)
    #interpolation='gaussian', origin='lower', cmap=colormap)
460
461
462
463
          ax.locator_params(nbins=6)
464
          if draw circle:
465
               ax.add_patch(Circle((hx, hy), r, fc="None", ec="black", lw=1))
         if draw_contours:
    x_midpoints = (xedges[:-1] + xedges[1:]) / 2.0
    y_midpoints = (yedges[:-1] + yedges[1:]) / 2.0
466
467
468
               X, Y = np.meshgrid(x_midpoints, y_midpoints)
ax.contour(X, Y, z.T, 2, colors='black', linewidths=4)
ax.contour(X, Y, z.T, 2, colors='white', linewidths=2)
469
470
471
472
         if label colorbar:
               if log_scale_projections:
474
                    log_format = mpl.ticker.LogFormatterMathtext(10, labelOnlyBase=False)
475
                    ax.cax.colorbar(im, format=log_format)
               else:
                   ax.cax.colorbar(im)
477
478
479
               bar = ax.cax.colorbar(im, ticks=[])
480
               bar.ax.set_yticklabels([])
               #plt.setp(bar.ax.get_yticklabels(), visible=False)
482
483
484 def draw_density_profile(ax, r, rho, err=None, color='black', label=None):
485 im = ax.loglog(r, rho, linestyle='steps-mid-', color=color, label=label)
```

```
line1 = ax.axvline(res_limit, color='black', linestyle=':')
           #ax.set_xlabel(xlabel_prof)
487
488
489
           #ax.set_ylabel(ylabel_prof)
490
           if err != None:
           err_bars = ax.errorbar(r, rho, yerr=err,linestyle='None', color=color)
if label != None:
491
492
103
                 ax.legend(fontsize='x-small')
           return ax
494
495
496
497 def draw_nfw_profile(ax, r, rho, R_s=None, color='black'): 498 ax.loglog(r, rho, linestyle='-', color=color)
499
           if R_s != None:
                line = ax.axvline(R_s, color='purple', linestyle='-.')
500
501
           return ax
502
503
504 def draw_parameters(ax, header, params1, params2):
           strlen = 12
header = [str(item)[:strlen] for item in header]
505
506
           params1 = [str(item)[:strlen] for item in params1
params2 = [str(item)[:strlen] for item in params2]
507
508
509
           header.insert(0, 'simulation')
510
           params1.insert(0, '--u21ptu--')
params2.insert(0, '--uzau---')
511
           header = '\n'.join(header)
params1 = '\n'.join(params1)
513
           params1 = '\n'.join(params1)
params2 = '\n'.join(params2)
ax.text(0.05, 0.5, header, horizontalalignment="left", verticalalignment="center", transform=ax.transAxes)
ax.text(0.40, 0.5, params1, horizontalalignment="left", verticalalignment="center", transform=ax.transAxes)
ax.text(0.75, 0.5, params2, horizontalalignment="left", verticalalignment="center", transform=ax.transAxes)
514
516
517
519
           return ax
520
521
522 def hide aves(av):
           ax.spines['top'].set_color('none')
524
           ax.spines['bottom'].set_color('none')
ax.spines['left'].set_color('none')
526
           ax.spines['right'].set_color('none')
527
           ax.tick_params(labelcolor='w', top='off', bottom='off', left='off', right='off')
528
           return ax
529
530
531
533 nhalos = 1
534 sort_col = 9 # density_profile 21pt halo mass
535 #sort_col = 47 # rockstar 21pt halo mass (M200c)
536
537 nbins = 40
538 nfit = 100
539 npixels = 30
540 #npixels = 100
541 smoothing_radius = 0.9
542 remove_nonfit_halos = True
543 global_filter_halos = True
544 column_filter_halos = True
545 log_scale_projections = True
546 wrap_box = False
547 label_colorbar = False

548 label_projection = True

549 zoom_projections = True
550 zoom_scale = 18.0 # kpc
551 draw_circle = False
552 draw_contours = True
553 extra smoothing = True
554 label_proj = True
555 label_21pt_za = True
556 equal_profile_axes = True
557 print_text = True
558
559 box_size = 10000.0 # kpc
560
561 id_col_2lpt = 0
562 id_col_za
563
564 print_cols_21pt = [43, 57, 6, 9, 17, 23, 31, 47, 51, 59, 61, 63, 65, 67, 69, 71, 73, 75, 77, 91, 93, 97, 99, 101, 103, 105, 107, 111, 163, 201, -2]
565 print_cols_za = [44, 58, 6, 10, 18, 24, 32, 48, 52, 60, 62, 64, 66, 68, 70, 72, 74, 76, 78, 92, 94, 98, 100,
            102, 104, 106, 108, 112, 164, 202, -1]
567 \text{ Rv1\_col} = 53
568 Rv2_col = 54
569 Rs1_col = 55
570 \text{ Rs2\_col} = 56
572 c_21pt_col = 17
573 c_za_col = 18
575 # c_21pt, c_za, chi2_21pt, chi2_za
```

```
576 lt_cols = [17, 18, 37, 38]
577 lt_vals = [100.0, 100.0, 10.0, 10.0]
 579 # c_2lpt, c_za, rho_0_2lpt, rho_0_za, chi2_2lpt, chi2_za

580 gt_cols = [17, 18, 31, 32, 37, 38]

581 gt_vals = [1.0, 1.0, 0.0, 0.0, 0.0, 0.0]
 583 eq_cols = []
 584 eq_vals = []
 586 ne_cols = []
 587 \text{ ne\_vals} = []
 589 # bgc2 halo array columns
 590 halo_id_col = 0
591 halo_r_col = 4
 592 \text{ halo_mass\_col} = 5
 593 halo_pos_cols = [6,7,8]
595 # bgc2 particle array columns
596 particle_mass_col = 0
597 particle_pos_cols = [1,2,3]
598 particle_vel_cols = [4,5,6]
 600 \text{ mass\_scale} = 1.0
mass_state = 1.0
601 common_mass = 5.33423e5
602 dist_scale = 1.0e3
603 res_limit = 0.5 #changed from 4.0 to 0.5 to match density_profile.py <-- maybe check why it was 4.0?
 604 nfit = 500
005
606 dist_units = 'kpc'
607 #xlabel_proj = [r'X Position (%s h$^{-1}$)' % (dist_units), r'X Position (%s h$^{-1}$)' % (dist_units), r'Y
Position (%s h$^{-1}$)' % (dist_units)]
608 #ylabel_proj = [r'Y Position (%s h$^{-1}$)' % (dist_units), r'Z
Position (%s h$^{-1}$)' % (dist_units), r'Z
Position (%s h$^{-1}$)' % (dist_units)]
609 proj_xlabel = r'Position_u(kpc_uh\^(-1)\$)'
610 proj_ylabel = r'Position_u(kpc_uh\^(-1)\$)'
611 prof_xlabel = r'Radius_u(\%s_uh\^(-1)\$)' % (dist_units)
 612 prof_ylabel = r'Density_{\sqcup}(M$_{\odot}$_{\sqcup}%s$^{-3}$_{\sqcup}h$^{2}$)' % (dist_units)
 613
 614 #colormap = 'ocean_r'
614 #colormap = 'ocean_r'
615 colormap = 'rainbow'
616 plot_base = 'plots/halo_pair_'
617 proj_name = '_proj'
618 dens_name = '_dens'
619 plot_ext = '.eps'
 621 make_stats = False
622 make_projection = False
623 make_density_profile = True
 624
 625 plot_dest_type = 'paper'
 626 if plot_dest_type == 'paper':
627 mpl.rcParams['font.family'] = 'serif'
628 mpl.rcParams['font.size'] = 16
                mpl.rcParams['font.size'] = 16
mpl.rcParams['axes.linewidth'] = 3
mpl.rcParams['lines.linewidth'] = 4
mpl.rcParams['patch.linewidth'] = 4
mpl.rcParams['xtick.major.width'] = 3
mpl.rcParams['ytick.major.width'] = 3
mpl.rcParams['ytick.major.size'] = 8
mpl.rcParams['ytick.major.size'] = 8
 629
 630
 632
 633
 634
 635
 637
638 if __name__ == '__main__':
639 main()
```

Appendix H

Concentration Comparison Code (Python)

```
1 #!/usr/bin/env python
  3 import sys
     import numpy as np
   from ipdb import set_trace
                Read in particle files
             header, halos = read_files(sys.argv[1:], header_line = 3)
11
                     print 'Removing_NaNs...'
halos = halos[np.isfinite(halos[:,c_lpt_col])]
                     halos = halos[np.isfinite(halos[:,c_za_col])]
                    print 'Filtering_data...'
for col, val in zip(glob_lt_cols, glob_lt_vals):
                              halos = halos[halos[:, col] <= val]
                   naios = naios[halos[:, col] <= val]
for col, val in zip(glob_gt_cols, glob_gt_vals):
    halos = halos[halos[:, col] >= val]
for col, val in zip(glob_eq_cols, glob_eq_vals):
    halos = halos[halos[:, col] == val]
for col, val in zip(glob_ne_cols, glob_ne_vals):
    halos = halos[halos[:, col] != val]
20
27
28
29
30
            if sort_col != None:
            halos = sort_by_column(halos, sort_col)
if (nhalos != None) or (nhalos != 0):
                     halos = halos[:nhalos]
             #if (nhalos == 'perc25'):
                     halos = halos[:len(halos)/10]
            if bad_halo_pairs != None:
    mask = np.arange(len(halos))
    mask = np.inid(mask, bad_halo_pairs)
                    mask = np.inid(mask, b
mask = np.invert(mask)
halos = halos[mask]
39
40
             c_rockstar_21pt = halos[:, Rv1_col] / halos[:, Rs1_col]
c_rockstar_za = halos[:, Rv2_col] / halos[:, Rs2_col]
41
42
43
             if use_klypin:
                   use_klypin:
    mask = (halos[:,4] < 100)
    print "changed_u, \( \) d_u halos " \( \) (mask.sum())
    print "c_2lpt_ubefore_u", c_rockstar_2lpt[mask][0]
    c_rockstar_2lpt[mask] = halos[mask, Rv1_col] / halos[mask, 79]
    print "c_2lpt_uklypin_u", c_rockstar_2lpt[mask][0]
    mask = (halos[:,5] < 100)
    print "c_nauged_u, \( \) d_uhalos " \( \) (mask.sum())
    print "c_rau_before_u", c_rockstar_za[mask][0]
    c_rockstar_za[mask] = halos[mask, Rv2_col] / halos[mask, 80]
    print "c_rau_klypin_u", c_rockstar_za[mask][0]
    iiff_2lpt = 2.0 * (c_rockstar_ztylet - halos[:, c_lpt_col]) / (c_r.</pre>
45
48
50
51
             c_diff_2lpt = 2.0 * (c_rockstar_2lpt - halos[:, c_lpt_col]) / (c_rockstar_2lpt + halos[:, c_lpt_col]) c_diff_za = 2.0 * (c_rockstar_za - halos[:, c_za_col]) / (c_rockstar_za + halos[:, c_za_col]) #halos = np.column_stack((halos, c_rockstar_2lpt, c_rockstar_za, c_diff_2lpt, c_diff_za))
53
54
             #header.append('c_rockstar')
#header.append('c_rockstar')
             #header.append('c_diff')
59
             #header.append('c_diff')
             c_diff_21pt = c_diff_21pt[np.isfinite(c_diff_21pt)]
62
             c_diff_za = c_diff_za[np.isfinite(c_diff_za)]
c_diff_tot = np.append(c_diff_2lpt, c_diff_za)
64
65
             c_diff_2lpt_frac = (np.abs(c_diff_za) <= cutoff_diff_frac).sum() / float(len(c_diff_2lpt))</pre>
             c_ulif_zipt_liac = (np.abs(c_ulif_za) <= cutoif_ulif_irac).sum() / float(len(c_ulif_za))
c_uliff_za_frac = (np.abs(c_ulif_za) <= cutoiff_ulif_frac).sum() / float(len(c_ulif_za))
c_uliff_tot_frac = (np.abs(c_ulif_tot) <= cutoff_uliff_frac).sum() / float(len(c_ulif_tot))</pre>
68
             70
             print 'Finishedusnapshot.'
     def read_files(files, header_line = None, comment_char = '#'):
             header = None
data = None
76
77
             if type(files) == str:
                    files = [files]
            if header_line != None:
   with open(files[0], 'r') as fd:
```

```
for line in range(header_line):
                               fd.readline()
                  header = fd.readline()
if header[0] != comment_char:
                        print "Header_must_start_with_a_'%s'" % comment_char sys.exit(4)
 88
                  header = header[1:]
header = header.split()
 90
91
            for file in files:
                  print 'Reading file %s...' % (file)
if data == None:
 93
94
                         data = np.genfromtxt(file, comments=comment_char)
                  else:
 96
 97
                         data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
            print 'Finished_reading_files.'
if header_line == None:
 99
100
101
                 return data
            else:
102
                  return header, data
104
105
106 def sort_by_column(halos, col):
         print 'Sorting_Halos...'
mask = np.argsort(halos[:, col])
mask = mask[::-1]
halos = halos[mask]
return halos
107
108
110
113
114
115 remove_nonfit_halos = False
116 global_filter_halos = True
117 use_klypin = False
118
119 \text{ nhalos} = 100
119 hhalos = 100

120 #nhalos = 'perc25'

121 #sort_col = None

122 sort_col = 9
124 cutoff_diff_frac = 0.2
125
126
127 Rv1_col = 53
128 Rv2_col = 54
129 Rs1_col = 55
130 Rs2_col = 56
132 c_lpt_col = 17
133 c_za_col = 18
135
136 lt_cols = [17, 18]
137 lt_vals = [100.0, 100.0]
138
139 gt_cols = [17, 18, 31, 32]
140 gt_vals = [1.0, 1.0, 0.0, 0.0]
141
141
142 eq_cols = []
143 eq_vals = []
144
145 ne_cols = []
146 ne_vals = []
147
149 # global filters
150 glob_lt_cols = []
151 glob_lt_vals = []
153 glob_gt_cols = [4, 5]
154 glob_gt_vals = [100, 100]
156 glob_eq_cols = [109, 110]
157 glob_eq_vals = [-1, -1]
158
159 glob_ne_cols = []
160 glob_ne_vals = []
161
162 bad_halo_pairs = None
163
164 c_diff_file = 'stats/c_diff.dat'
166
167
168 if __name__ == '__main__':
            main()
```

Appendix I

Differential Histogram Code

I.1 Histogram Generation and Fitting (Python)

```
1 #!/usr/bin/env python
    import svs
 4 import numpy as np
5 import matplotlib as mpl
 6 mpl.use('Agg')
7 import matplotlib.pyplot as plt
8 import matplotlib.gridspec as gridspec
9 from scipy import stats
10 from scipy.special import gamma as gamma_func
11 from scipy.optimize import curve_fit
12 import statsmodels.sandbox.distributions.extras as extrastats
13 from ipdb import set_trace
            # Read in particle files
            header, halos = read_files(sys.argv[1:], header_line = 3)
19
            if remove_nonfit_halos:
                   print 'Removing NaNs...
                    halos = halos[np.isfinite(halos[:,c_lpt_col])]
21
                   halos = halos[np.isfinite(halos[:,c_za_col])]
            if global_filter_halos:
                 print 'Filtering_data...'
for col, val in zip(glob_lt_cols, glob_lt_vals):
                  halos = halos[halos[:, col] <= val]

for col, val in zip(glob_gt_cols, glob_gt_vals):
    halos = halos[halos[:, col] >= val]
               halos = naios[naios[:, coi] >= vai]
for col, val in zip(glob_eq_cols, glob_eq_vals):
    halos = halos[halos[:, coi] == val]
for col, val in zip(glob_ne_cols, glob_ne_vals):
    halos = halos[halos[:, coi] != val]
           if sort col != None:
37
38
39
           halos = sort_by_column(halos, sort_col)
if (nhalos != None) or (nhalos != 0):
                  halos = halos[:nhalos]
           if bad_halo_pairs != None:
               mask = np.arange(len(halos))
mask = np.in1d(mask, bad_halo_pairs)
                   mask = np.invert(mask)
44
                  halos = halos[mask]
            c_rockstar_21pt = halos[:, Rv1_col] / halos[:, Rs1_col]
c_rockstar_za = halos[:, Rv2_col] / halos[:, Rs2_col]
46
47
            c_rockstar_za
            if use_klypin:
                  use_klypin:
    mask = (halos[:,4] < 100)
    print "changed_u,d_uhalos" % (mask.sum())
    print "c_2lpt_ubefore_u", c_rockstar_2lpt[mask][0]
    c_rockstar_2lpt[mask] = halos[mask, Rv1_col] / halos[mask, 79]
    print "c_2lpt_uklypin_u", c_rockstar_2lpt[mask][0]
    mask = (halos[:,5] < 100)
    print "changed_u,d_uhalos" % (mask.sum())
    print "c_za_ubefore_u", c_rockstar_za[mask][0]
    c_rockstar_za[mask] = halos[mask, Rv2_col] / halos[mask, 80]
    print "c_za_u,d_vnin_u", c_rockstar_za[mask][0]</pre>
49
50
            print "c_za_uklypin_u", c_rockstar_za[mask][0]
c_diff_2lpt = 2.0 * (c_rockstar_2lpt - halos[:, c_lpt_col]) / (c_rockstar_2lpt + halos[:, c_lpt_col])
c_diff_za = 2.0 * (c_rockstar_za - halos[:, c_za_col]) / (c_rockstar_za + halos[:, c_za_col])
58
59
60
61
62
            halos = np.column_stack((halos, c_rockstar_21pt, c_rockstar_za, c_diff_21pt, c_diff_za))
            header.append('c_rockstar')
header.append('c_rockstar')
63
            header.append('c_diff')
header.append('c_diff')
64
66
67
            if mass quartiles and len(halos) > 50:
                   start_fracs = [0.0, 0.25, 0.50, 0.75, 0.0]
end_fracs = [0.25, 0.50, 0.75, 1.0, 1.0]
69
70
                  start_fracs = [0.0]
end_fracs = [1.0]
            for start_frac, end_frac in zip(start_fracs, end_fracs):
                  if use_alt_frac and (start_frac == 0.0) and (end_frac == 1.0):
                          alt_halos_to_pass = halos[alt_start_frac * len(halos) : alt_end_frac * len(halos)]
                          alt_halos_to_pass = None
```

```
81
              if len(halos_to_pass) > 0:
                  for (lpt_col, za_col, fancy_x_label) in zip(lpt_log_cols, za_log_cols, fancy_log_x_labels):
    make_plot(halos_to_pass, alt_halos_to_pass, lpt_col, za_col, start_frac, end_frac, fancy_x_label,
83
            header, use_log=True)
                  for (lpt_col, za_col, fancy_x_label) in zip(lpt_cols, za_cols, fancy_x_labels):
    make_plot(halos_to_pass, alt_halos_to_pass, lpt_col, za_col, start_frac, end_frac, fancy_x_label,
85
           header, use log=False)
86
         print 'Finishedualluplots.'
87
88
89
90 def read_files(files, header_line = None, comment_char = '#'):
         header = None
data = None
92
93
         if type(files) == str:
    files = [files]
94
95
96
         if header_line != None:
97
             with open(files[0], 'r') as fd:
                  for line in range(header_line):
    fd.readline()
98
             header = fd.readline()
if header[0] != comment_char:
100
101
                   print "Headerumustustartuwithuau'%s'" % comment_char
                   sys.exit(4)
103
104
              header = header[1:]
              header = header.split()
106
        for file in files:
print 'Reading | file | %s...' % (file)
107
108
              if data == None:
109
                   data = np.genfromtxt(file, comments=comment_char)
110
                   data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
113
         print \ 'Finished_{\sqcup} reading_{\sqcup} files.'
114
115
         if header_line == None:
116
             return data
118
              return header, data
119
120
121 def sort_by_column(halos, col):
         print 'Sorting_halos...'
mask = np.argsort(halos[:, col])
124
         mask = mask[::-1]
125
         halos = halos[mask]
126
         return halos
127
129 def make_plot(halos, alt_halos, lpt_col, za_col, start_frac, end_frac, fancy_x_label, header=None, use_log=False)
130
         print 'start_=', start_frac
         print 'end_=', end_frac
x_lpt = halos[:, lpt_col]
         x_za = halos[:, za_col]
         x_lpt, x_za = filter(x_lpt, x_za, lpt_col, za_col)
134
135
136
         if alt_halos != None:
              alt_naios := none.
alt_x_lpt = alt_halos[:, lpt_col]
alt_x_za = alt_halos[:, za_col]
alt_x_lpt, alt_x_za = filter(alt_x_lpt, alt_x_za, lpt_col, za_col)
138
139
140
         if header != None:
141
              header_lpt = header[lpt_col]
header_za = header[za_col]
142
143
144
              if header_lpt == header_za:
145
                  xlabel = header_lpt
xlabel = xlabel.replace('/', '_over_')
147
                   print 'column_mismatch..._exiting'
148
149
                   set_trace()
150
                   sys.exit(123)
151
         if len(x_lpt) == 0 or len(x_za) == 0:
              print "Skippingurangeu%fu-u%fuforu%suplot.uuNouhalosufound." % (start_frac, end_frac, xlabel)
              return
154
155
              #set_trace()
156
         if perc_diff:
158
              print \ 'Finding \_ percent \_ difference \_ stats...'
             159
161
162
             perc_diff_stats(x_perc_diff, perc_diff_file, use_log=use_log)
              print 'done.
163
164
         x = 2.0 * (x_lpt - x_za) / (x_lpt + x_za)
x[np.logical_and(x_lpt == 0, x_za == 0)] = 0
165
166
168
         if alt halos != None:
```

```
alt_x = 2.0 * (alt_x_lpt - alt_x_za) / (alt_x_lpt + alt_x_za)
169
             alt_x[np.logical_and(alt_x_lpt == 0, alt_x_za == 0)] = 0
170
172 #
       set trace()
174
        if x_lim == None:
175
             #x_max = max(abs(x.max()), abs(x.min()))
176
             if lpt_col == 47:
                  x_max = x.mean() + x.std() * 1.5
                 x_min = x.mean() - x.std() * 1.5
178
179
                 x_max = np.std(x) * 3.0
x_min = -x_max
180
182
            x_max = x_lim
x_min = -x_lim
183
185
186
        # get stats
        data_mean = x.mean()
187
        data_stdev = x.std()**2
188
        data_skew = stats.skew(x)
        data_kurt = stats.kurtosis(x)
data_rms = np.sqrt(np.mean(x**2))
data_gt_epsilon = float(len(x[np.abs(x) >= 0.1])) / float(len(x))
190
191
192
193
194
        # Generate plot
        print 'generating', xlabel, 'plot
        fig = plt.figure(figsize=(9.0, 6.0))
196
197
        {\tt if} \ {\tt add\_residuals\_panel:}
198
            grid = gridspec.GridSpec(2, 1, height_ratios=[1,4])
             ax = fig.add_subplot(grid[1])
199
200
        else:
201
             ax = fig.add_subplot(111)
        202
204
        p0 = [1.0, data_mean, data_stdev, 2.0] ax, fit_height, fit_mean, fit_stdev, fit_skew, fit_kurt, fit_height_err, fit_mean_err, fit_stdev_err,
205
         fit_skew_err, fit_kurt_err, chi2, pval = draw_fit(ax, n, bins, p0)
207
208
        if draw_data_fit:
209
             ax = draw_data_gaussian(ax, x, n, bins)
        if alt halos != None:
             ax, n_alt, bins_alt, patches_alt = draw_hist(ax, alt_x, x_min=x_min, x_max=x_max, \
                                                            use_log=use_log, color='green', fill="0.75")
214
            #ax = draw_fit(ax, n, bins)
216
        #ax.grid(color='gray', linestyle='dashed')
        #ax.set_xlabel('(' + xlabel + '_2lpt - ' + xlabel + '_za) / ' + xlabel + '_avg')
217
218
219
        #ax.set_ylabel(ylabel)
220
221
        if label_axes:
            ax.set_xlabel(fancy_x_label, fontsize="xx-large")
ax.set_ylabel(fancy_y_label, fontsize="xx-large")
        #ax.legend()
225
        if add_residuals_panel:
            ax = fig.add_subplot(grid[0])
ax = draw_residuals(ax, n, bins, fit_height, fit_mean, fit_stdev, fit_kurt)
ax.tick_params(axis='x', labelbottom='off')
226
228
229
230
        fig.tight_layout()
        233
234
235
        if save stats:
            statsfile = "%s%s%0.3d%s%0.3d%s%s_(%s-%s)%s" % \
             (stats_base, '(', lpt_col, ',', za_col, ')_', xlabel, start_frac, end_frac, stats_ext) with open(statsfile, 'w') as fd:
238
239
                 if bin_test:
                      for ntestbins in range(nbins_min, nbins_max+1, 5):
    fit_mean, fit_stdev = rebin_stats(ntestbins, x, x_min=x_min, x_max=x_max, use_log=use_log)
    fd.write("%du%gu%gu%gu%gu%g\n" % (ntestbins, data_mean, data_stdev, fit_mean, fit_stdev))
240
241
242
243
                      245
246
           fit_skew_err, fit_kurt, fit_kurt_err, \
247
                                 data_rms, data_gt_epsilon, chi2, pval))
248
249
        print 'finished_plot_' + plot_name
250
        return
253 def perc_diff_stats(x, filename, use_log=False):
254 data_mean = x.mean()
255 data_stdev = x.std()**2
256 data_skew = stats.skew(x)
        data_kurt = stats.kurtosis(x)
258
        data_rms = np.sqrt(np.mean(x**2))
```

```
data_gt_epsilon = float(len(x[np.abs(x) >= 0.1])) / float(len(x))
261
           if x_lim == None:
                 x_max = min((x.mean() + x.std() * 3.0), x.max())
x_min = max((x.mean() - x.std() * 3.0), x.min())
262
264
                x_max = x_lim
x_min = -x_max
265
266
267
268
           global nbins
if nbins <= 0:</pre>
269
                nbins = np.sqrt(len(x))
if nbins % 2 == 0:
270
271
272
273
274
                      nbins = nbins - 1
          if nbins < nbins_min:
nbins = nbins_min
          elif nbins > nbins_max:
    nbins = nbins_max
276
          if use_log:
    xbins = np.logspace(np.log10(x_min), np.log10(x_max), num=nbins+1)
278
280
                 mid_bins = 10.0**(0.5 * (np.log10(xbins[1:]) + np.log10(xbins[:-1])))
281
                 xbins = np.linspace(x_min, x_max, num=nbins+1)
283
                 mid_bins = 0.5 * (xbins[1:] + xbins[:-1])
284
           hist, bin_edges = np.histogram(x, bins=xbins)
           x_peak = mid_bins[hist == hist.max()][0]
286
287
           x_sorted = np.sort(x)
n_halos = len(x_sorted)
288
289
290
291
           x_vals = []
          for frac in fractions:
    x_vals.append(x_sorted[len(x_sorted)*frac])
292
293
294
           x_vals = np.array(x_vals)
295
296
           sum_frac_halos = []
297
           for diff_val in diff_vals:
    n_gt_val = (x_sorted >= diff_val).sum()
298
299
                 sum_frac_halos.append(float(n_gt_val) / float(n_halos))
300
           sum_frac_halos = np.array(sum_frac_halos)
301
302
           doublesum_frac_halos = []
          doublesum_rrac_halos = []
for right_diff_val in diff_vals:
    left_diff_val = (1.0 / (right_diff_val + 1.0)) - 1.0
    n_gt_val = (x_sorted >= right_diff_val).sum() + (x_sorted <= left_diff_val).sum()
    doublesum_frac_halos.append(float(n_gt_val) / float(n_halos))</pre>
303
304
305
306
307
           doublesum_frac_halos = np.array(doublesum_frac_halos)
308
           with open(filename, 'w') as fd:
309
310
                 fd.write("%duuu%guuu%suuu%suuu%suuu%gu%gu%gu%gu%gu%g\n" % \
                              (nbins, x_peak, \
'u'.join("%g" % x for x in x_vals), \
'u'.join("%g" % x for x in sum_frac_halos), \
'u'.join("%g" % x for x in doublesum_frac_halos), \
'u'.join("%g" % x for x in doublesum_frac_halos), \
311
314
                                data_mean, data_stdev, data_skew, data_kurt, \
data_rms, data_gt_epsilon))
317
318
           return
319
320
321 def find_frac_bounds(hist, start_bin, frac):
          n_tot = hist.sum()
n_sum = hist[start_bin]
322
324
325
          left_tot = hist[:start_bin].sum() + hist[start_bin]/2.0
right_tot = hist[start_bin+1:].sum() + hist[start_bin]/2.0
326
327
           if float(left_tot) / float(n_tot) <= frac / 2.0:</pre>
328
           right_only = True

if float(right_tot) / float(n_tot) <= frac / 2.0:
    left_only = True
329
330
333
           left_bound = start_bin
           right_bound = start_bin
while(float(n_sum) / float(n_tot) < frac):</pre>
334
335
336
337
339
           return left_bound, right_bound
340
341
342 def filter(x_lpt, x_za, lpt_col, za_col):
343 mask = np.isfinite(x_lpt)
344
           x_lpt = x_lpt[mask]
           x_za = x_za[mask]
mask = np.isfinite(x_za)
345
347
           x_lpt = x_lpt[mask]
x_za = x_za[mask]
348
350
           if column filter halos:
```

```
x_lpt, x_za = filter_columns(lpt_col, x_lpt, x_za)
351
              x_za, x_lpt = filter_columns(za_col, x_za, x_lpt)
353
354
         return x lpt. x za
355
356
357 def filter_columns(x_col, x1, x2):
358
         print 'Filtering data...
359
360
         mask = np.isfinite(x1)
361
         x1 = x1[mask]

x2 = x2[mask]
362
         mask = (x1 != -9999)
364
         x1 = x1[mask]
x2 = x2[mask]
365
366
367
368
         if x col in lt cols:
369
              val = lt_vals[lt_cols.index(x_col)]
              mask = (x1 <= val)
x1 = x1[mask]
370
371
372
373
              x2 = x2[mask]
         if x_col in gt_cols:
   val = gt_vals[gt_cols.index(x_col)]
374
              mask = (x1 >= val)
x1 = x1[mask]
x2 = x2[mask]
375
376
         if x_col in eq_cols:
   val = eq_vals[eq_cols.index(x_col)]
   mask = (x1 == val)
378
379
380
              x1 = x1[mask]
x2 = x2[mask]
381
382
383
         if x_col in ne_cols:
              val = ne_vals[ne_cols.index(x_col)]
mask = (x1 != val)
384
385
              x1 = x1[mask]

x2 = x2[mask]
386
387
         return x1, x2
389
390
391 def draw_hist(ax, x, x_min=None, x_max=None, use_log=False, color=None, fill=None, label=None):
         global nbins
392
393
         if nbins <= 0:
              nbins = np.sqrt(len(x))
if nbins % 2 == 0:
nbins = nbins - 1
394
395
396
         if nbins < nbins_min:
   nbins = nbins_min</pre>
397
398
         elif nbins > nbins_max:
399
400
              nbins = nbins_max
401
402
         if use_log:
    xbins = np.logspace(np.log10(x_min), np.log10(x_max), num=nbins+1)
403
404
              ax.set_xscale('log')
405
406
              xbins = np.linspace(x_min, x_max, num=nbins+1)
407
408
         if fill == None:
409
         type='step'
else:
410
              type='stepfilled'
411
412
413
         n, bins, patches = ax.hist(x, bins=xbins, histtype=type, facecolor=fill, normed=hist_normed, cumulative=
           hist_cumulative, log=ylog, edgecolor=color, label=label)
414
         return ax, n, bins, patches
415
416
417 def draw_fit(ax, hist, bin_edges, p0):
418 bin_centers = (bin_edges[:-1] + bin_edges[1:]) / 2.0
419
420
         if ignore central bin:
              mask = (np.abs(bin_centers) > 0.000001)
bin_centers = bin_centers[mask]
421
422
423
              hist = hist[mask]
424
         hist[hist==0] = 1 #fix devide by zero error
425
426
427
428
              if poisson_weight:
                   sigma=np.sqrt(hist)/hist
430
                   sigma = sigma / float(hist.max())
431
              else:
                   sigma=None
433
              if fit_in_log:
434
435
                   #if sigma != None:
                   # sigma = np.log10(sigma)
436
437
438
                   coeffs, var_matrix = curve_fit(log_generalized_normal, bin_centers, np.log10(hist/float(hist.max())),
            p0=p0, sigma=sigma)
                   coeffs[0] = coeffs[0]**2
440
```

```
var_matrix[0,0] = var_matrix[0,0]**2
                else:
443
                      coeffs, var_matrix = curve_fit(generalized_normal, bin_centers, hist/float(hist.max()), p0=p0, sigma=
            sigma)
444
               if prevent_small_shape_param and coeffs[3] < 1.0: coeffs[3] = 1.0 / coeffs[3] print 'coeffs_{\sqcup}=', coeffs
445
446
448
          except RuntimeError:
450
                print '******curve_fitufailed!'
451
                return ax, np.nan, np.nan
          height, mean, stdv, skew, kurt = coeffs[0] * hist.max(), coeffs[1], coeffs[2], 0.0, coeffs[3]
453
454
          height_err, mean_err, stdv_err, skew_err, kurt_err = np.sqrt(var_matrix[0,0]*hist.max()), np.sqrt(var_matrix
[1,1]), np.sqrt(var_matrix[2,2]), 0.0, np.sqrt(var_matrix[3,3])
455
456
          fit x = np.linspace(bin edges[0], bin edges[-1], nfitpoints+1)
          hist_fit = generalized_normal(fit_x, height, mean, stdv, kurt)
ax.plot(fit_x, hist_fit, color='red', linestyle='--')
457
458
          chi2_fit = generalized_normal(bin_centers, height, mean, stdv, kurt)
chi2, pval = stats.chisquare(hist / hist.max(), chi2_fit / hist.max())
460
461
463
          return ax, height, mean, stdv, skew, kurt, height_err, mean_err, stdv_err, skew_err, kurt_err, chi2, pval
464
466 def draw_residuals(ax, hist, bin_edges, fit_height, fit_mean, fit_stdev, fit_kurt):
467 bin_centers = (bin_edges[:-1] + bin_edges[1:]) / 2.0
468 fit = generalized_normal(bin_centers, fit_height, fit_mean, fit_stdev, fit_kurt)
          ratio = (hist - fit) / hist.max()
469
          #ax.plot(bin_centers, ratio, linestyle='steps-mid-')
ax.plot(bin_centers, ratio, linestyle='steps-mid-')
470
471
472
          return av
474
475 def draw_data_gaussian(ax, x, hist, bins): 476 bin_centers = (bins[:-1] + bins[1:]) / 2.0
477
          x_min = bins[0]
x_max = bins[-1]
478
479
480
          mean = np.mean(x)
          stdv = np.std(x)**2
skew = stats.skew(x)
481
482
483
          kurt = stats.kurtosis(x)
484
          print \ \ "data_{\sqcup} stats:_{\sqcup \sqcup} mean_{\sqcup} = {}_{\sqcup} {}^{\chi}g_{\sqcup \sqcup} stdv_{\sqcup} = {}_{\sqcup} {}^{\chi}g_{\sqcup \sqcup} skew_{\sqcup} = {}_{\sqcup} {}^{\chi}g_{\sqcup \sqcup} kurt_{\sqcup} = {}_{\sqcup} {}^{\chi}g^{\parallel} \ \ \chi \ \ (mean, \ stdv, \ skew, \ kurt)
485
486
          coeffs, var_matrix = curve_fit(gaussian_height(mean, stdv, skew, kurt), bin_centers, hist, p0=[hist.max()])
488
          height = coeffs[0]
489
490
          \label{eq:fit_x}  \mbox{ = np.linspace(x_min, x_max, nfitpoints+1)} 
491
          hist_fit = gaussian(fit_x, height, mean, stdv, skew, kurt)
ax.plot(fit_x, hist_fit, color='0.25', linestyle='-.')
492
493
494
495
496 #def gaussian(x, A, mu, sigma, skew, kurtosis):
497 # pdf_function = extrastats.pdf_mvsk([mu, sigma, skew, kurtosis])
498 # return A * pdf_function(x)
499
500
501 def double_gaussian(x, A, mu, sigma, skew, kurtosis, A2, mu2, sigma2, skew2, kurtosis2):
502
          return gaussian(x, A, mu, sigma, skew, kurtosis) + gaussian(x, A2, mu2, sigma2, skew2, kurtosis2)
503
505 def gaussian_height(mu, sigma, skew, kurtosis):
506
          def func(x, A):
             pdf_function = extrastats.pdf_mvsk([mu, sigma, skew, kurtosis])
507
508
                 return A * pdf_function(x)
509
          return func
510
511
512 #def log_gaussian(x, A, mu, sigma, skew=0.0, kurtosis=0.0):
513 def log_gaussian(x, A, mu, sigma):
514 A = A**2 # remember to also square fit value for A
515 y = gaussian(x, A, mu, sigma)
516
                 gaussian(x, Å, mu, sigma, skew, kurtosis)
          if (y <= 0.0).any():

#y[y<=0] = -y[y<=0] + 1

y[y<=0] = (y[y<=0] + 0.0001)**2
517
519
          return np.log10(v)
523 #def log_double_gaussian(x, A1, mu1, sigma1, skew1, kurtosis1, A2, sigma2, skew2, kurtosis2):
                                                                                                                                            # for common
            mean
524 #def log_double_gaussian(x, A1, mu1, sigma1, skew1, kurtosis1, A2, mu2, sigma2, skew2, kurtosis2):
525 def log_double_gaussian(x, A1, mu1, sigma1, A2, mu2, sigma2):
526
          #mu2 = mu1 # for common mean
A1 = A1**2 # remember to also square fit value for A
527
          A2 = A2 **2
529
          skew1 = 0.0
```

```
skew2 = 0.0
         kurtosis1 = 0.0
kurtosis2 = 0.0
532
533
         y = double_gaussian(x, A1, mu1, sigma1, skew1, kurtosis1, A2, mu2, sigma2, skew2, kurtosis2)
         if (y <= 0.0).any():
              535
536
537
         return np.log10(y)
538
539
540 def gaussian(x, A, mu, sigma):
         return A * np.exp(-(x - mu)**2 / (2.0 * sigma**2))
541
543
544 def generalized_normal(x, A, mu, alpha, beta):
545 if prevent_small_shape_param and beta < 1.0:
         beta = 1.0 / beta

return A * ( beta / (2.0 * alpha * gamma_func(1.0 / beta)) ) * np.exp(-(np.abs(x - mu)/alpha)**beta)
546
548
549
550 def log_generalized_normal(x, A, mu, alpha, beta):
        A = A**2
y = generalized_normal(x, A, mu, alpha, beta)
551
552
         if (y <= 0.0).any():
              554
555
         return np.log10(y)
557
558
559 def add_text(fig, ax, textstr):
         #props = dict(boxstyle='round', facecolor='white', alpha=0.25)
props = dict(edgecolor='none', facecolor='none')
ax.text(0.02, 0.16, textstr, transform=ax.transAxes, fontsize=14, \
560
561
562
563
                   verticalalignment='top', bbox=props)
         return fig, ax
565
566
    def rebin_stats(ntestbins, x, x_min=None, x_max=None, use_log=False):
568
         if use_log:
    xbins = np.logspace(np.log10(x_min), np.log10(x_max), num=ntestbins+1)
569
570
571
              xbins = np.linspace(x_min, x_max, num=ntestbins+1)
572
573
         hist, bin_edges = np.histogram(x, bins=xbins)
574
575
         bin_centers = (bin_edges[:-1] + bin_edges[1:]) / 2.0
576
         if ignore_central_bin:
              mask = (np.abs(bin_centers) > 0.000001)
577
578
               bin_centers = bin_centers[mask]
579
              hist = hist[mask]
         #p0 = [hist.max(), 0.0, 0.2]
p0 = [hist.max(), hist.mean(), hist.std(), stats.skew(hist), stats.kurtosis(hist)]
hist[hist==0] = 1 #fix devide by zero error
580
581
582
583
         try:
584
               if poisson_weight:
585
                   coeffs, var_matrix = curve_fit(gaussian, bin_centers, hist, p0=p0, sigma=(np.sqrt(hist)/hist))
586
               else:
587
                    coeffs, var_matrix = curve_fit(gaussian, bin_centers, hist, p0=p0)
         except RuntimeError:
    print '******curve_fitufailed!'
588
589
590
               return np.nan, np.nan
591
         mean, stdev = coeffs[1], coeffs[2]
503
         return mean, stdev
594
596 nbins = 35
597 #nbins = 25
598 #nbins = -1
599 \text{ nbins_min} = 15
600 nbins_max = 200
601 #nbins_max = 200
602 nfitpoints = 100
603 remove_nonfit_halos = False
604 global_filter_halos = True
605 column_filter_halos = True
606 use_klypin = False
607 label_axes = True
608 ignore_central_bin = False
609 save_stats = True
610 bin_test = False
611 poisson_weight = True
612 fit_in_log = True
613 draw_data_fit = False
614 mass_quartiles = False
615 prevent_small_shape_param = False
616 add_residuals_panel = False
617 perc_diff = True
619 hist_normed = False
620 hist_cumulative = False
621 ylog = False
```

```
622 ylabel= 'Number_of_Halos'
624 #
0.24 # control = [0.01, 0.05, 0.10, 0.25, 0.50, 0.75, 0.90, 0.95, 0.99] 626 diff_vals = [0.01, 0.05, 0.10, 0.25, 0.50, 0.75, 1.00, 2.00, 4.00]
629 #nhalos = 100
630 nhalos = None
631 sort_col = 9
633 #lpt_log_cols = [ 9, 23, 31, 47, 51, 57]

634 #za_log_cols = [10, 24, 32, 48, 52, 58]

635 #lpt_cols = [17, 77, 91, 93, 97, 99, 107, 111, -4, -2]

636 #za_cols = [18, 78, 92, 94, 98, 100, 108, 112, -3, -1]
638 lpt_log_cols = []
639 za_log_cols = []
                                    = [-4, 47, 91, 107, 111]
= [-3, 48, 92, 108, 112]
= [-4, 31, 47, 91, 107, 111]
640 #lpt_cols
641 #za_cols
642 #lpt_cols
                                    = [-3, 32, 48, 92, 108, 112]
= [-4, 31, 47, 91, 111]
= [-3, 32, 48, 92, 112]
643 #za_cols
644 #1pt_cols
645 #za_cols
646 lpt_cols = [-4, 47, 91, 93, 107]
647 za_cols = [-3, 48, 92, 94, 108]
648 # conentration, mass, x_off, v_off, T/|U|
649
650 fancy_log_x_labels = []
651 #fancy_x_labels = [r"$\mathrm{\frac{c_{2LPT} - c_{ZA}}{c_{avg}}}$",
652 # r"$\mathrm{\frac{\rho_{0, 2LPT} - \rho_{0, ZA}}{\rho_{0, avg}}}$",
653 # r"$\mathrm(\frac{M_{vir, 2LPT} - M_{vir, ZA}}{M_{vir, avg}}}$",
654 # r"$\mathrm{\frac{X_{0ff, 2LPT} - X_{0ff, ZA}}{X_{0ff, avg}}}$",
655 # r"$\mathrm{\frac{N_{subs, 2LPT} - N_{subs, ZA}}{N_{subs, avg}}}$"]
649
657 fancy_x_labels = [r"\mdots mathrm{\frac{c_{2LPT}_{-}c_{ZA}}{c_{avg}}}$"
                                           658
660
661
663 fancy_y_label = r"$\mathbf{N_{halos}}"
664
666 \text{ Rv2\_col} = 54
667 Rs1_col = 55
668 Rs2_col = 56
669
670 c_lpt_col = 17
671 c_za_col = 18
672
073 # c_2lpt, c_za, chi2_2lpt, chi2_za
675 #lt_cols = [17, 18, 37, 38]
676 #lt_vals = [100.0, 100.0, 10.0, 10.0]
677 lt_cols = [17, 18]
678 lt_vals = [100.0, 100.0]
680 # c_2lpt, c_za, rho_0_2lpt, rho_0_za, chi2_2lpt, chi2_za
681 #gt_cols = [17, 18, 31, 32, 37, 38]
682 #gt_vals = [1.0, 1.0, 0.0, 0.0, 0.0]
683 gt_cols = [17, 18, 31, 32]
684 gt_vals = [1.0, 1.0, 0.0, 0.0]
685
686 eq_cols = []
687 eq_vals = []
688
689 ne cols = []
690 ne_vals = []
691
692
693 # global filters
694 glob_lt_cols = [] glob_lt_vals = []
696 glob_gt_cols = [4, 5]
697 glob_gt_vals = [100, 100]
699 glob_eq_cols = [109, 110]
700 glob_eq_vals = [-1, -1]
702 glob_ne_cols = []
703 glob_ne_vals = []
 705
 706
 707 use_alt_frac = True
708 alt_start_frac = 0.75
709 alt_end_frac = 1.0
 710
 711 \text{ #x_lim} = 0.5
712 #x_lim = 0.5
713 x_lim = None
```

I.2 PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
 2 #PBS -M djsissom@gmail.com
3 #PBS -m bae
 4 #PBS -1 nodes=1:ppn=1
5 #PBS -1 pmem=40000mb
6 #PBS -1 mem=4000mb
 7 \#PBS -1 walltime=1:00:00
 8 #PBS -o out.log
 9 #PBS -j oe
10
11 minsnap=0
12 maxsnap=61
14 # Change to working directory
15 echo $PBS_NODEFILE
16 cd $PBS_O_WORKDIR
18 for ((snap=$minsnap; snap<=$maxsnap; snap++)); do
20
        if [ $snap -lt 10 ]; then
        j=00$snap
elif [ $snap -lt 100 ]; then
21
22
23
             j=0$snap
24
25
        new_plot_dir=snap${j}_plots
        if [ ! -e plots_all_snaps/${new_plot_dir} ]; then
29
30
              mkdir plots_all_snaps/${new_plot_dir}
        echo "Startingubox\{i\}_{i:nap}\{j\}..." ./hist.py "/projects/simulations/rockstar/box\{1,2,3\}/crossmatch/snap\{j\}/halos.dat > plots/out.log 2>&1 mv plots/* plots_all_snaps/\{new_plot_dir\}/.
32
33
        echo "Finished⊔snap${j}
41 # - end of script
```

I.3 PBS Submission Script - Individual Boxes (Bash)

```
1 #!/usr/bin/env bash
2 #PBS -M djsissom@gmail.com
3 #PBS -m bae
4 #PBS -l nodes=1:ppn=1
5 #PBS -l pmem=4000mb
6 #PBS -l mem=4000mb
7 #PBS -l walltime=2:00:00
8 #PBS -o out.log
9 #PBS -j oe
10
11 minsnap=0
12 maxsnap=61
13
14 minbox=1
15 maxbox=3
16
17 # Change to working directory
```

```
18 echo $PBS_NODEFILE
19 cd $PBS_O_WORKDIR
22 for ((box=$minbox; box<=$maxbox; box++)); do 23
         new_box_dir=plots_all_snaps_box${box}
25
26
27
         if [! -e ${new_box_dir}]; then
    mkdir ${new_box_dir}
fi
29
30
         for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
              if [ $snap -lt 10 ]; then
31
               j=00$snap
elif [$snap -lt 100]; then
32
33
              j=0$snap
34
35
36
37
38
              new_plot_dir=snap${j}_plots
              if [ ! -e ${new_box_dir}/${new_plot_dir} ]; then
    mkdir ${new_box_dir}/${new_plot_dir}
39
40
42
43
              echo -n "Starting_box${box}_usnap${j}..._u" ./hist.py ~/projects/simulations/rockstar/box${box}/crossmatch/snap${j}/halos.dat > plots/out.log 2>&1 mv plots/* {\text ew_box_dir}/{\text ew_plot_dir}/.
45
               echo "Finished⊔snap${j}"
         done
49 done
51 # - end of script
```

I.4 Statistics Collection Script (Bash)

Appendix J

Redshift Trends Code (Python)

```
1 #!/usr/bin/env python
 3 import sys
 4 import os
   import numpy as np
 6 import matplotlib as mpl
7 mpl.use('Agg')
 8 import matplotlib.pyplot as plt
9 from scipy.special import gamma as Gamma
10 from scipy.special import psi as digamma
11 from ipdb import set_trace
14 def main():
         #for filenum, file in enumerate(sys.argv[1:]):
if (len(sys.argv[1:]) == 4):
               data1 = read_files(sys.argv[1], header_line = None)
data2 = read_files(sys.argv[2], header_line = None)
data3 = read_files(sys.argv[3], header_line = None)
20
               rsnap_data = read_files(sys.argv[4], header_line = None)
21
               print 'need_4_files'
               sys.exit(15)
24
25
26
         if fit_mean_trend:
               with open(statsfile, 'w') as fd:
                     fd.write("#plotuslopeuslope_erruinterceptuintercept_err\n")
28
29
         if skew err boxes:
               skew_err2 = get_skew_err(sys.argv[1])
skew_err2 = get_skew_err(sys.argv[2])
skew_err3 = get_skew_err(sys.argv[3])
31
32
33
34
35
         if minsnap > 0:
               #for data in data1, data2, data3:
               # data = data[data[:,0] >= minsnap]
               data1 = data1[data1[:,0] >= minsnap]
data2 = data2[data2[:,0] >= minsnap]
39
               data3 = data3[data3[:,0] >= minsnap]
40
               if skew err boxes:
                    skew_err1 = skew_err1[-len(data1):]
skew_err2 = skew_err2[-len(data2):]
skew_err3 = skew_err3[-len(data3):]
41
45
         if skew_err_col == -2:
               data1 = np.column_stack((data1, skew_err1))
data2 = np.column_stack((data2, skew_err2))
               data3 = np.column_stack((data3, skew_err3))
48
50
         #if (mean_err_col == -2) or (var_err_col == -2) or (skew_err_col == -2) or (kurt_err_col == -2):
         # fake_err = np.zeros(len(data1))
# data1 = np.column_stack((data1, fake_err))
data2 = np.column_stack((data2, fake_err))
51
53
54
               data3 = np.column_stack((data3, fake_err))
         z = 1.0 / rsnap_data[:,1] - 1.0
if (len(data1) == len(data2)) and (len(data1) == len(data3)):
               z = z[-len(data1):]
          else:
59
               sys.exit(16)
          data1 = np.column_stack((data1, z))
62
          data2 = np.column_stack((data2, z))
64
65
          data3 = np.column_stack((data3, z))
         #data1[:,-1] = data1[:,-1] - 0.12
#data2[:,-1] = data2[:,-1] + 0.12
67
68
70
                if expand_error:
                     eapanu_stirov
mask = (np.abs(data[:,data_mean_col] - data[:,mean_col]) > data[:,mean_err_col])
data[mask,mean_err_col] = np.abs(data[mask,data_mean_col] - data[mask,mean_col])
               if transform variance:
                     data[:,var_col] = data[:,var_col]**2 * Gamma(3.0 / data[:,beta_col]) / Gamma(1.0 / data[:,beta_col]) data[:,var_err_col] = data[:,var_err_col]**2 * Gamma(3.0 / data[:,beta_col]) / Gamma(1.0 / data[:,
           beta coll)
               if transform_kurtosis:
                      #data[:,kurt_col] = ( Gamma(5.0 / data[:,kurt_col]) * Gamma(1.0 / data[:,kurt_col]) / Gamma(3.0 /
           data[:,kurt_col]) ) - 3.0
    beta = data[:,beta_col]
                     beta_err = data[:,beta_err_col]
kurtosis = ( Gamma(5.0 / beta) * Gamma(1.0 / beta) / Gamma(3.0 / beta) ) - 3.0
```

```
kurtosis err = beta err * (1.0 / beta**2) * (kurtosis + 3) * (6.0 * digamma(3.0/beta) - 5.0 * digamma
81
           (5.0/beta) - digamma(1.0/beta))
82
                   data[:.kurt col] = kurtosis[:]
83
                   data[:,kurt_err_col] = kurtosis_err[:]
85
              data[:,var_col] = np.sqrt(data[:,var_col])  # var to stdev
data[:,var_err_col] = np.sqrt(data[:,var_err_col])  # var to stdev
86
87
88
89
90
         if save_transformed_data:
              for data, path in zip([data1, data2, data3], sys.argv[1:4]):
    fname = transform_file_base + os.path.basename(path)
91
93
                   with open(fname, 'w') as fd:
                        fd.write(transformed_data_header)
94
                        np.savetxt(fd, np.column_stack((z, data)), fmt='%g')
96
98
         #~~~~~~~~~~~~~~~~~~
99
100
         101
102
         for (data, ylabel, color, label, name) in zip([data1, data2, data3], ylabels1, colors, labels1, names):
104
              print "Making_%s_plot..." % (name)
fig = plt.figure(figsize=(9.0, 6.0))
105
              ax = fig.add_subplot(111)
107
              ax = make_plot(ax, data[:,z_col], data[:,mean_col], err = data[:,mean_err_col], color = 'blue', marker='o
108
              ax = make_plot(ax, data[:,z_col], data[:,mean_col] + data[:,var_col], color = 'black', linestyle='--')
ax = make_plot(ax, data[:,z_col], data[:,mean_col] - data[:,var_col], color = 'black', linestyle='--')
109
              if add rms line:
                   ax = make_plot(ax, data[:,z_col], data[:,data_rms_col], color = 'green', linestyle=':')
115
              if fit mean trend:
                   ax, slope, slope_err, intercept, intercept_err = add_fit(ax, data[:,z_col], data[:,mean_col], err=
,mean_err_col], color='red')
save_fits(statsfile, name, slope, np.sqrt(slope_err), intercept, np.sqrt(intercept_err))
           data[:,mean_err_col],
117
              #ax.legend(loc='lower right')
ax.set_xlim(z[0] + 1.0, z[-1] - 1.0)
119
              #ax.invert_xaxis()
              ax.set_xlabel(xlabel, fontsize='x-large')
              ax.set_ylabel(ylabel, fontsize='x-large')
126
              fig.tight_layout()
              fig.savefig(plot_base + 'mean_stdev_' + name + plot_ext, bbox_inches='tight')
         #~~~~~~~~~~~~~~~
129
130
         # make skew and kurtosis plots
         #data1[:,-1] = data1[:,-1] + 0.12
#data2[:,-1] = data2[:,-1] - 0.12
134
135
136
         for (data, ylabel_kurt, ylabel_skew, color, name, ylim_low1, ylim_high1, ylim_low2, ylim_high2) in zip([data1
, data2, data3], ylabels2_kurt, ylabels2_skew, colors, names, [-10.0, -10.0, -1.0], [20.0, 20.0, 1.5],
    [-0.2, -1.5, -0.4], [0.5, 3.5, 0.1]):
    print "Making_u%s_uplot..." % (name)
138
              fig = plt.figure(figsize=(9.0, 6.0))
ax = fig.add_subplot(111)
139
140
142
              #ax = make_plot(ax, data[:,z_col] - offset, data[:,kurt_col], err = data[:,kurt_err_col], color = 'red',
           marker='o', linestyle='-', label='Kurtosis')
              #ax = make_plot(ax, data[:,z_col] + offset, data[:,skew_col], err = data[:,skew_err_col], color = 'blue',
143
          marker='0', linestyle='-', label='Skew')
ax = make_plot(ax, data[:,z_col] - offset, data[:,kurt_col], err = data[:,kurt_err_col], color = 'red',
marker='0', linestyle=':', label='Kurtosis')
144
145
              legend_lines1, legend_labels1 = ax.get_legend_handles_labels()
146
147
              ax.set_xlabel(xlabel, fontsize='x-large')
148
             ax.set_ylabel(ylabel_kurt, fontsize='x-large')
ax.set_ylim(ylim_low1, ylim_high1)
150
              if separate_skew_axes:
                        = ax.twinx()
                   ax
          ax = make_plot(ax, data[:,z_col] + offset, data[:,skew_col], err = data[:,skew_err_col], color = 'blue',
marker='o', linestyle=':', label='Skew')
legend_lines2, legend_labels2 = ax.get_legend_handles_labels()
154
156
              ax.set_ylabel(ylabel_skew, fontsize='x-large')
              ax.legend(legend_lines1 + legend_lines2, legend_labels1 + legend_labels2, loc='lower_right')
ax.set_xlim(z[0] + 1.0, z[-1] - 1.0)
ax.set_ylim(ylim_low2, ylim_high2)
158
160
              #ax.invert_xaxis()
161
              fig.tight_layout()
              fig.savefig(plot_base + 'skew_kurtosis_' + name + plot_ext, bbox_inches='tight')
```

```
164
166
167
                 print 'Finishedualluplots.'
169
170 def make_plot(ax, x, y, err=None, color='black', marker='None', linestyle='None', label=None):
                 if err == None:
if label == None:
171
                                   ax.plot(x, y, color=color, marker=marker, linestyle=linestyle)
174
                                   ax.plot(x, y, color=color, marker=marker, linestyle=linestyle, label=label)
176
                          if label == None:
178
                                  ax.errorbar(x, y, yerr=err, color=color, marker=marker, linestyle=linestyle)
180
                                   ax.errorbar(x, y, yerr=err, color=color, marker=marker, linestyle=linestyle, label=label)
181
                return ax
182
183
185 def add_fit(ax, x, y, err=None, color='red'):
                from scipy.optimize import curve_fit
p0 = [0.0, 0.0]
186
188
                 try:
189
                         coeffs, pcov = curve_fit(linear, x, y, sigma=err, p0=p0)
                except RuntimeError:
191
                       print '******** Curve of it of ailed of the state of the 
192
                return np.nan, np.nan
xmin, xmax = ax.get_xlim()
                xmin, xmax = ax.get_xlim()
x_fit = np.linspace(xmin, xmax, 20)
y_fit = linear(x_fit, coeffs[0], coeffs[1])
ax.plot(x_fit, y_fit, color=color, linestyle='--')
return ax, coeffs[0], pcov[0,0], coeffs[1], pcov[1,1]
194
195
196
197
199
200 def linear(x, slope, intercept):
201 return slope * x + intercept
202
203
204 def read_files(files, header_line = None, comment_char = '#'):
                header = None
data = None
205
206
                if type(files) == str:
207
208
                         files = [files]
209
210
                if header_line != None:
                          with open(files[0], 'r') as fd:
                                  for line in range(header_line):
213
                                          fd.readline()
214
                                   header = fd.readline()
215
                          if header[0] != comment_char:
216
                                   print "Header must start with a, %s, % comment char
                                   sys.exit(4)
                         header = header[1:]
header = header.split()
219
220
221
                for file in files:
222
                          print 'Reading_file_%s...' % (file)
if data == None:
                                   data = np.genfromtxt(file, comments=comment_char)
224
226
                                   data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
227
228
                print 'Finished_reading_files.'
                if header_line == None:
230
                          return data
                 else:
                         return header, data
234
       def get_skew_err(filebase):
236
                  z = None
                skew = None
for i in range(3):
238
                         filename = filebase.replace('plots_all_snaps', 'plots_all_snaps_box'+str(i+1))
data = read_files(filename, header_line = None)
239
240
241
242
                          min_length = len(data)
elif len(data) < min_length:
    min_length = len(data)
244
245
246
247
                         if z == None:
                                  z = data[-min_length:,snap_col]
249
250
                                   z = np.column\_stack((z[-min\_length:], data[-min\_length:,snap\_col]))
                          if skew == None:
                                   skew = data[-min_length:,skew_col]
                                   skew = np.column_stack((skew[-min_length:], data[-min_length:,skew_col]))
255
```

```
257
                 if (z[:,0] != z[:,1]).all() or (z[:,0] != z[:,2]).all():
258
                           print \ 'Need_{\sqcup} matching_{\sqcup} snapshots_{\sqcup} for_{\sqcup} skew_{\sqcup} error_{\sqcup} from_{\sqcup} individual_{\sqcup} boxes.'
259
                           print z
260
                           sys.exit(-1)
261
262
                  skew_err = np.std(skew, axis=1) / np.sqrt(3.0)
263
                  return skew_err
264
265
266 def save_fits(file, name, slope, slope_err, intercept, intercept_err):
267
                 with open(file, 'a') as fd:
fd.write("%su%gu%gu%gu%gu%g\n" % (name, slope, slope_err, intercept, intercept_err))
269
270
271 plot_dest_type = 'paper'
        if plot_dest_type == 'paper':
    mpl.rcParams['font.family'] = 'serif'
272
                 mpl.rcParams['font.size'] = 16
mpl.rcParams['axes.linewidth'] = 3
mpl.rcParams['lines.linewidth'] = 4
274
276
277
278
                 mpl.rcParams['patch.linewidth'] = 4
                 mpl.rcParams['xtick.major.width'] = 3
                 mpl.rcParams['ytick.major.width'] = 3
mpl.rcParams['ytick.major.size'] = 8
mpl.rcParams['ytick.major.size'] = 8
280
281
282 #colors = ['red', 'green', 'blue']

284 colors = ['black', 'black', 'black']

285 labelsi = [r'$c$', r'$M_{\mathrm{vir}}$', r'$X_{\mathrm{off}}$']

286 names = ['c_rockstar', 'Mvir', 'Xoff']

287 xlabel = 'Redshift'
ylabels1 = [r'$\mu$\and\u$\sigma$\ufor\u$\Delta\uc$', r'$\mu$\uand\u$\sigma$\ufor\u$\Delta\um_{\mathrm{vir}}$', r'$\mu$\uand\uspace and\uspace\upper and\uspace\upper and\upper and\upper \upper \upper and\upper \upper \upper and\upper \upper \upper \upper and\upper \upper \up
                     {\mathrm{off}}$']
290 ylabels2_skew = [r'Skew_dfor_s\Deltauc$', r'Skew_dfor_s\DeltauM_{\mathrm{vir}}$', r'Skew_dfor_s\DeltauX_{\mathrm{off}}
                   }}$<sup>,</sup>]
291 plot_base = 'plots/'
292 plot_ext = '.eps'
294 statsfile = 'plots/stats.dat'
294 statsfile = 'plots/stats.dat'
295 transform_file_base = 'plots/'
296 transformed_data_header = '#zousnapoudata_meanoudata_stdevoudata_skewoudata_kurtoufit_heightou+/-erroufit_meanou
                   +/-erruufit_stdevuu+/-erruufit_skewuu+/-erruufit_kurtuu+/-erruudata_rmsuudata_gt_epsilonuuchi2uupvaluu
                    skew_err_uz\n'
298 z col
                                   = 0
= 7
299 snap_col
300 mean_col
301 mean_err_col = 8
 302 var_col
303 var_err_col = 10
304 skew col
                                      = 3
305 \text{ skew\_err\_col} = -2
306 #skew_col
307 #skew_err_col = 8
308 #kurt_col
309 #kurt_err_col = -2
310 kurt_col
311 kurt_err_col = 14
312 beta_col
                                    = 13
313 beta_err_col = 14
315 data mean col = 1
316 \text{ data_rms_col} = 15
318 #z col
319 #snap_col
320 #mean_col
                                        = 1
321 #mean_err_col = -2
 322 #var_col
323 \text{ #var_err_col} = -2
324 #skew_col
                                         = 3
325 #skew_err_col = -2
326 #kurt_col
                                        = 4
327 #kurt_err_col = -2
328
329 offset = 0.06
 330 #offset = 0.0
331
332 \text{ minsnap} = 39
 333 #minsnap = None
334
335 transform_variance = True
336 transform_kurtosis = True
                                           = True
337 expand_error
338 fit_mean_trend
                                                    = True
339 separate_skew_axes - ...
340 skew_err_boxes = True
-- line = True
342 save_transformed_data = True
```

```
343
344
345 if __name__ == '__main__':
346 main()
```

Appendix K

Mass Trends Code

K.1 Mass (Python)

```
1 #!/usr/bin/env python
    import svs
 4 import numpy as np
5 import matplotlib as mpl
6 mpl.use('Agg')
 7 import matplotlib.pyplot as plt
8 from matplotlib import cm
9 from scipy import interpolate
10 from scipy.ndimage.filters import gaussian_filter
11 #from ipdb import set_trace
15 def main():
16
           # Read in particle files
           header, halos = read_files(sys.argv[1:], header_line = 3)
          if c_source == 'density_profile':
19
20
                 print 'len(halos) = ', len(halos)
                halos = halos[np.isfinite(halos[:,c_2lpt_col])]

print 'len(halos)_=_', len(halos)
21
          print 'Filteringudata...'
for col, val in zip(lt_cols, lt_vals):
          halos = halos[halos[:, col] <= val]

for col, val in zip(gt_cols, gt_vals):
    halos = halos[halos[:, col] >= val]
          for col, val in zip(eq_cols, eq_vals):
          halos = halos[halos[:, col] == val]

for col, val in zip(ne_cols, ne_vals):
    halos = halos[halos[:, col] != val]
31
32
33
34
35
36
37
38
39
          m_avg = (halos[:,47] + halos[:,48])/2.0
          halos = np.column_stack((halos, m_avg))
          header = np.append(header, 'M_avg')
          if x min lim > 0:
                print 'nhalosu=', len(halos)
mask = (m_avg >= x_min_lim)
halos = halos[mask]
41
42
43
                 print 'nhalos =', len(halos)
44
45
          if c_source == 'rockstar':
                c1 = halos[:, Rv1_col] / halos[:, Rs1_col]
c2 = halos[:, Rv2_col] / halos[:, Rs2_col]
46
47
                 if use_klypin:
                       mask = (halos[:,4] < 100)
c1[mask] = halos[mask, Rv1_col] / halos[mask, 79]
mask = (halos[:,5] < 100)
49
50
         mask = (naios[:,5] < 100)
    c1[mask] = halos[mask, Rv2_col] / halos[mask, 80]
if c_source == 'density_profile':
    c1 = halos[:, c_2lpt_col]
    c2 = halos[:, c_za_col]</pre>
          dc = 2.0 * (c1 - c2) / (c1 + c2)
          \#dc = c1 - c2
          m1 = halos[:,47]
          m2 = halos[:,48]

dm = 2.0 * (m1 - m2) / (m1 + m2)
61
62
63
          for x_col, xlabel in zip(x_cols, xlabels):
   make_plot(dm, x_col, halos, header, xlabel, use_log=False)
for x_col, xlabel in zip(x_log_cols, xlabels_log):
   make_plot(dm, x_col, halos, header, xlabel, use_log=True)
67
69
           print 'Finished_all_plots.'
    def read_files(files, header_line = None, comment_char = '#'):
          header = None
data = None
74
75
76
77
78
          if type(files) == str:
                 files = [files]
          if header_line != None:
                 with open(files[0], 'r') as fd:
                       for line in range(header_line):
```

```
fd.readline()
                       header = fd.readline()
if header[0] != comment_char:
 83
                                print "Header_must_start_with_a_'%s'" % comment_char
 84
                                 sys.exit(4)
 86
                        header = header[1:]
                       header = header.split()
 87
 88
 89
               for file in files:
  90
                       print 'Reading file %s...' % (file)
 91
                         if data == None:
                              data = np.genfromtxt(file, comments=comment_char)
 92
 94
                                data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
 95
 96
               print 'Finished_reading_files.'
               if header_line == None:
return data
 97
 98
 99
100
                        return header, data
101
106
107
                print 'generating plot...
               fig = plt.figure(figsize=(9.0,6.0))
ax = fig.add_subplot(1,1,1)
108
109
110
                ax = draw_hist2d(ax, x, y)
                ax = draw_data_fit(ax, x, y, x.min(), x.max(), use_log=use_log)
               if fit_to_binned_data:
                       ax, mid_bins, mean, stdev = draw_bin_avgs(ax, x, y, use_log=use_log)
ax = draw_bin_fit(ax, mid_bins, mean, stdev, x.min(), x.max(), use_log=use_log)
114
115
116
                ax.set_xlim([x.min(), x.max()])
               #ax.set_yscale("log")
ax.set_xlabel(xlabel, fontsize="xx-large")
118
119
                ax.set_ylabel(ylabel, fontsize="xx-large")
120
               fig.tight_layout()
               rig.Lignt_layout()
col_header = col_header.replace("/", "over")
plot_name = "%s%x%0.3d%s%s%s" % (plot_base, '(', x_col, ')_', col_header, plot_ext)
plt.savefig(plot_name, bbox_inches='tight')
print 'finished_uplot_u' + plot_name
122
123
124
126
128 def draw_hist2d(ax, x, y):
129
              if use_log:
    xbins = np.logspace(np.log10(x.min()), np.log10(x.max()), num=nbins+1)
130
                        xbins = np.linspace(x.min(), x.max(), num=nbins+1)
134
               ybins = np.linspace(y.min(), y.max(), num=nbins+1)
135
136
               if use_log:
                       ax.set_xscale("log")
138
                        im = my_hist2d(ax, x, y, bins=[xbins, ybins])
139
140
                       im = ax.hist2d(x, y, bins=[xbins, ybins], cmap=colormap)
141
142
               if y_lim > 0.0:
143
                        ax.set_ylim([-y_lim, y_lim])
144
               line = ax.plot([x.min(), x.max()], [0.0, 0.0], 'b--')
145
146
                return ax
147
148
149 def my_hist2d(ax, x, y, bins=10, range=None, normed=False, weights=None,
150
                                                         cmin=None, cmax=None, **kwargs):
151
               import matplotlib as mpl
152
               bin_range = range
               range = mpl.axes.__builtins__["range"]
h, xedges, yedges = np.histogram2d(x, y, bins=bins, range=bin_range,
154
156
                                                                                        normed=normed, weights=weights)
157
158
               if cmin is not None:
159
                       h[h < cmin] = None
                if cmax is not None:
161
                       h[h > cmax] = None
162
               if z_log:
                       h[h<1.0] = 0.5
h = np.log10(h)
164
165
166
167
               h = gaussian_filter(h, len(h) / 75.0)
168
169
                pc = ax.imshow(h[:,::-1].T, cmap=colormap, extent=[x.min(), x.max(), y.min(), y.max()], interpolation=', and a substitute of the color of the col
                  gaussian')
                ax.set_xlim(xedges[0], xedges[-1])
                ax.set_ylim(yedges[0], yedges[-1])
```

```
172
         return h, xedges, yedges, pc
174
175 def draw bin avgs(ax, x, v, use log):
              fit_bins = np.logspace(np.log10(x.min()), np.log10(x.max()), num=nfit_bins+1)
178
179
               fit_bins = np.linspace(x.min(), x.max(), num=nfit_bins+1)
180
181
         mid_bins = (fit_bins[:-1] + fit_bins[1:]) / 2.0
182
183
         mean = np.array([])
stdev = np.array([])
185
          for xmin, xmax in zip(fit_bins[:-1], fit_bins[1:]):
              mask = np.logical_and(x > xmin, x <= xmax)
if mask.sum() > 0:
186
                    mean_el = y[mask].mean()
#stdev_el = y[mask].std() / np.sqrt(len(y))
stdev_el = y[mask].std()
188
189
190
191
                    #stdev_el = stdev / np.sqrt(len(y[mask]))
192
               else:
193
                    stdev_el = -1.0
194
195
               mean = np.append(mean, mean_el)
196
               stdev = np.append(stdev, stdev_el)
197
198
         mask = (stdev != -1.0)
         mean = mean[mask]
stdev = stdev[mask]
199
200
201
         mid_bins = mid_bins[mask]
202
203
         ax.errorbar(mid_bins, mean, yerr=stdev, fmt='o')
204
205
         return ax, mid bins, mean, stdev
206
207
208
209 def draw_bin_fit(ax, mid_bins, mean, stdev, x_min, x_max, use_log):
210
          #fit data
          if use_log:
          # coefs = np.polyfit(np.log10(x), y, 1)
               coefs, stats = np.polynomial.polynomial.polyfit(np.log10(mid_bins), mean, 1, w=1.0/stdev, full=True)
214
               coefs, res, rank, singvals, rcond = np.polyfit(np.log10(mid_bins), mean, 1, full=True)
         # coefs = np.polyfit(x, y, 1)
# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, w=1.0/stdev, full=True)
coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, full=True)
216
219
         print 'coefs<sub>□</sub>=<sub>□</sub>', coefs
220
         m = coefs[0]
         b = coefs[1]
224
          if use_log:
              x = np.logspace(np.log10(x_min), np.log10(x_max), 100)
226
               y = m * np.log10(x) +
227
228
              x = np.linspace(x_min, x_max, 100)
         y = m * x + b
#v = x**m + b
229
230
         line = ax.plot(x, y, color='green')
232
         if print_fit_params:
234
               if use_log:
                    textstr = 'y_{\sqcup}=_{\sqcup}m_{\sqcup}\log_{\sqcup}x_{\sqcup}+_{\sqcup}b'n$m_=_\%g$\n$b_=_\%g$' % (m, b)
236
                    textstr = \$y_{\sqcup} = _{\sqcup} m_{\sqcup} x_{\sqcup} + _{\sqcup} b \ n m_{\sqcup} = _{\sqcup} g \ n b_{\sqcup} = _{\sqcup} g  (m, b)
               238
239
240
241
242
         if save fit params:
243
              with open("fits_to_bins.dat", "a") as fd:
fd.write("%gu%g\n" % (m, b))
244
245
246
         return ax
247
248
249 def draw_data_fit(ax, x, y, x_min, x_max, use_log):
250
         if remove_zero_strip:
    mask = (np.abs(y) >= y_epsilon)
    x = x[mask]
252
               y = y[mask]
253
255
         #fit data
256
         if use log:
257
              coefs, residual, rank, singular_values, rcond = np.polyfit(np.log10(x), y, 1, full=True)
              coefs, stats = np.polynomial.polynomial.polyfit(np.log10(mid_bins), mean, 1, w=1.0/stdev, full=True)
coefs, res, rank, singvals, rcond = np.polyfit(np.log10(mid_bins), mean, 1, full=True)
258
260
         else:
         coefs, residual, rank, singular_values, rcond = np.polyfit(x, y, 1, full=True)
# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, w=1.0/stdev, full=True)
# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, full=True)
261
263
```

```
print 'coefsu=', coefs, '+/-', residual
 266
 267
                          m = coefs[0]
                           b = coefs[1]
 269
                          if use_log:
                                 x = np.logspace(np.log10(x_min), np.log10(x_max), 100)
y = m * np.log10(x) + b
 270
271
272
273
                                 x = np.linspace(x_min, x_max, 100)
274
275
276
                          y = m * x + b

#y = x**m + b

line = ax.plot(x, y, color='red')
277
278
279
                          if print_fit_params:
                                        if use_log:
                                                      textstr = \$y_{\square} = \mbox{$\square$} \
 280
 281
 282
                                                      textstr = \$y_{\sqcup}=_{\sqcup}m_{\sqcup}x_{\sqcup}+_{\sqcup}b\$\n\$m_{\sqcup}=_{\sqcup}\%g\$\n\$b_{\sqcup}=_{\sqcup}\%g\$, % (m, b)
                                         283
 285
 286
 287
                         if save_fit_params:
                                    with open "fits_to_data.dat", "a") as fd:
fd.write("%gu%gu%g\n" % (m, b, residual))
 288
 289
 291
                         return ax
 292
294 use_log = True
295 #use_log = False
296 z_log = True
297
298 #fit_bins = True
299 #fit_data = True
 300
 301 print_fit_params = False
302 save_fit_params = True
 303
 304 use_klypin = True
305
 306 remove_zero_strip = True
 307 y_epsilon = 0.01
308
 309 y_lim = 0.5
 310 x_min_lim = 5.33e5 * 100
311
 312 #if use_log:
313 # x_cols = [4, 5, 6, 9, 10, 23, 24, 31, 32, 47, 48, 51, 52, 57, 58] # log10 columns
314 #else:
 315 # x_cols = [17, 18, 77, 78, 91, 92, 93, 94, 97, 98, 99, 100, 107, 108, 111, 112] # nolog columns
316
317 x_cols = []
318 x_log_cols = [-1]
319 \ \text{#x\_log\_cols} = [47, 48, -1]
320
 321 xlabels = []
321 xlabels = []
322 xlabels_log = [r"$\mathrm{M_{avg}_(M_{\oodot})}$"]
323 #xlabels_log = [r"$\mathrm{M_{2LPT} (M_{\oodot})}$",
324 # r"$\mathrm{M_{ZA} (M_{\oodot})}$",
325 # r"$\mathrm{M_{avg} (M_{\oodot})}$"]
 327 ylabel = r"\sum_{\mu_{\mu}} (M_{2LPT}_{\mu_{\mu}} (ZA))_{\mu_{\mu}} (avg)
329 #c_source = 'density_profile'
330 c_source = 'rockstar'
331
332 plot_base = 'plots/diff_M_-_vs_-_'
333 plot_ext = '.eps'
 334
335 #plot_name = 'test.eps'
336 #plot_name = 'c_v_M200c_21pt.eps'
337 fit_to_binned_data = False
 338
339 \text{ Rv1\_col} = 53
 340 \text{ Rv2\_col} = 54
 341 Rs1_col = 55
 342 Rs2_col = 56
344 c_21pt_col = 17
345 c_za_col = 18
347 nbins = 100
348 nfit_bins = 20
 349
350 ## c_21pt, c_za, chi2_21pt, chi2_za
351 #1t_cols = [17, 18, 37, 38]
352 #1t_vals = [100.0, 100.0, 10.0, 10.0]
 353 #
355 #
354 ## c_2lpt, c_za, chi2_2lpt, chi2_za
355 #gt_cols = [17, 18, 37, 38]
```

```
356 #gt_vals = [1.0, 1.0, 0.0, 0.0]
358 lt_cols = []
359 lt_vals = []
361 gt_cols = [4, 5]
362 gt_vals = [100, 100]
364 eq_cols = [109, 110]
365 eq_vals = [-1, -1]
366
367 ne_cols = []
368 ne_vals = []
369
370 #colormap = cm.PuBuGn
371 #colormap = cm.cubehelix_r
372 #colormap = cm.ocean_r
373 #colormap = cm.rainbow
374 #colormap = cm.gnuplot2_r
375 #colormap = cm.CMRmap_r
377 def add_white(orig_map, num):
              add_white(orig_map, num):
    temp_cmap = cm.get_cmap(orig_map, num)
    vals = temp_cmap(np.arange(num))
    nfade = num / 7
    vals[:nfade,0] = np.linspace(1., vals[nfade-1,0], nfade)
    vals[:nfade,1] = np.linspace(1., vals[nfade-1,1], nfade)
    vals[:nfade,2] = np.linspace(1., vals[nfade-1,2], nfade)
    #vals[:nfade,3] = np.linspace(0., vals[nfade-1,2], nfade)
    #vals[0] = [1.0, 1.0, 1.0, 1.0]
    #vals[1] = (vals[1] + [1.0, 1.0, 1.0, 1.0]) / 2.0
    neurman = mpl.colors | UnearSegmentedColorman from list("colors)
378
380
381
383
384
385
386
387
                newcmap = mpl.colors.LinearSegmentedColormap.from_list("custom_1", vals)
                return newcmap
389
390 colormap = add_white('rainbow', 30)
391
mpl.rcParams['axes.linewidth'] = 3
                mpl.rcParams['lines.linewidth'] = 4
mpl.rcParams['patch.linewidth'] = 4
mpl.rcParams['xtick.major.width'] = 3
397
398
399
               mpl.rcrarams['ytick.major.width'] = 3
mpl.rcParams['ytick.major.width'] = 3
mpl.rcParams['ytick.major.size'] = 8
mpl.rcParams['ytick.major.size'] = 8
mpl.rcParams['xtick.minor.width'] = 2
400
401
402
403
                mpl.rcParams['ytick.minor.width'] = 2
mpl.rcParams['ytick.minor.width'] = 2
mpl.rcParams['xtick.minor.size'] = 4
405
                mpl.rcParams['ytick.minor.size'] = 4
406
408
409 if __name__ == '__main__':
410 main()
```

K.2 Concentration (Python)

```
1 #!/usr/bin/env python
3 import sys
4 import numpy as np
 5 import matplotlib as mpl
6 mpl.use('Agg')
7 import matplotlib.pyplot as plt
8 from matplotlib import cm
9 from scipy import interpolate
10 from scipy.ndimage.filters import gaussian_filter
11 #from ipdb import set_trace
15
   def main():
          # Read in particle files
          header, halos = read_files(sys.argv[1:], header_line = 3)
          if c_source == 'density_profile':
                print 'len(halos)u=u', len(halos)
halos = halos[np.isfinite(halos[:,c_2lpt_col])]
20
                halos = halos[np.isfinite(halos[:,c_za_col])]
print 'len(halos)u=u', len(halos)
         print 'Filtering_data...'
for col, val in zip(lt_cols, lt_vals):
   halos = halos[halos[:, col] <= val]</pre>
         for col, val in zip(gt_cols, gt_vals):
    halos = halos[halos[:, col] >= val]
         for col, val in zip(eq_cols, eq_vals):
               halos = halos[halos[:, col] == val]
         for col, val in zip(ne_cols, ne_vals):
    halos = halos[halos[:, col] != val]
```

```
m_avg = (halos[:,47] + halos[:,48])/2.0
halos = np.column_stack((halos, m_avg))
header = np.append(header, 'M_avg')
36
37
 39
          if x_min_lim > 0:
               print 'nhalosu=', len(halos)
mask = (m_avg >= x_min_lim)
 40
41
                halos = halos[mask]
42
43
               print 'nhalosu=', len(halos)
44
45
          if c source == 'rockstar':
               c1 = halos[:, Rv1_col] / halos[:, Rs1_col]
c2 = halos[:, Rv2_col] / halos[:, Rs2_col]
47
48
               if use_klypin:
    mask = (halos[:,4] < 100)</pre>
 49
                     c1[mask] = halos[mask, Rv1_col] / halos[mask, 79]
mask = (halos[:,5] < 100)</pre>
50
                     c1[mask] = halos[mask, Rv2_col] / halos[mask, 80]
         if c_source == 'density_profile':
   c1 = halos[:, c_2lpt_col]
   c2 = halos[:, c_za_col]
53
 55
 56
          dc = 2.0 * (c1 - c2) / (c1 + c2)
 58
59
          \#dc = c1 - c2
          m1 = halos[:,47]
61
          m2 = halos[:,48]
          dm = 2.0 * (m1 - m2) / (m1 + m2)
62
64
          for x_col, xlabel in zip(x_cols, xlabels):
65
          make_plot(dc, x_col, halos, header, xlabel, use_log=False)
for x_col, xlabel in zip(x_log_cols, xlabels_log):
                make_plot(dc, x_col, halos, header, xlabel, use_log=True)
67
69
          print 'Finishedualluplots.'
70
 72
73
    def read_files(files, header_line = None, comment_char = '#'):
          header = None
data = None
 74
          if type(files) == str:
    files = [files]
 75
76
 78
          if header line != None:
               with open(files[0], 'r') as fd:
 79
 80
                     for line in range(header_line):
81
                          fd.readline()
               header = fd.readline()

if header[0] != comment_char:

print "Header_must_start_with_a_'%s'" % comment_char
83
84
                     sys.exit(4)
86
               header = header[1:]
header = header.split()
87
89
         for file in files:
                print 'Reading | file | %s...' % (file)
if data == None:
90
91
92
                     data = np.genfromtxt(file, comments=comment_char)
94
                     data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
95
          print 'Finishedureadingufiles.'
97
          if header_line == None:
98
               return data
99
100
                return header, data
101
103~\mbox{def} make_plot(y, x_col, halos, header, xlabel, use_log):
104
         x = halos[:, x_col]
col_header = header[x_col]
105
106
107
          print 'generating plot ...
          fig = plt.figure(figsize=(9.0,6.0))
ax = fig.add_subplot(1,1,1)
108
109
          ax = draw_hist2d(ax, x, y)
110
          ax = draw_data_fit(ax, x, y, x.min(), x.max(), use_log=use_log)
          if fit_to_binned_data:
               ax, mid_bins, mean, stdev = draw_bin_avgs(ax, x, y, use_log=use_log)
ax = draw_bin_fit(ax, mid_bins, mean, stdev, x.min(), x.max(), use_log=use_log)
114
          ax.set_xlim([x.min(), x.max()])
          #ax.set_yscale("log")
ax.set_xlabel(xlabel, fontsize="xx-large")
118
119
          ax.set_ylabel(ylabel, fontsize="xx-large")
120
121
          fig.tight_layout()
          right_layout();
col_header = col_header.replace("/", "over")
plot_name = "%s%s%0.3d%s%s%s" % (plot_base, '(', x_col, ')_', col_header, plot_ext)
plt.savefig(plot_name, bbox_inches='tight')
print 'finished_uplot_u' + plot_name
```

```
128 def draw_hist2d(ax, x, y):
129
               if use_log:
    xbins = np.logspace(np.log10(x.min()), np.log10(x.max()), num=nbins+1)
                        xbins = np.linspace(x.min(), x.max(), num=nbins+1)
133
               ybins = np.linspace(y.min(), y.max(), num=nbins+1)
134
135
               if use_log:
136
                        ax.set_xscale("log")
                        im = my_hist2d(ax, x, y, bins=[xbins, ybins])
139
                        im = ax.hist2d(x, y, bins=[xbins, ybins], cmap=colormap)
140
141
142
               if y_lim > 0.0:
143
                        ax.set_ylim([-y_lim, y_lim])
144
               line = ax.plot([x.min(), x.max()], [0.0, 0.0], 'b--')
145
147
148
149 def my_hist2d(ax, x, y, bins=10, range=None, normed=False, weights=None,
150
151
                                                         cmin=None, cmax=None, **kwargs):
               import matplotlib as mpl
               bin_range = range
154
               range = mpl.axes.__builtins__["range"]
h, xedges, yedges = np.histogram2d(x, y, bins=bins, range=bin_range,
155
156
                                                                                       normed=normed, weights=weights)
157
158
               if cmin is not None:
               h[h < cmin] = None
if cmax is not None:</pre>
159
160
161
                       h[h > cmax] = None
162
               if z_log:
                        h[h < 1.0] = 0.5
164
                       h = np.log10(h)
165
167
               h = gaussian_filter(h, len(h) / 75.0)
168
               pc = ax.imshow(h[:,::-1].T, cmap=colormap, extent=[x.min(), x.max(), y.min(), y.max()], interpolation=', and a substitute of the color of the colo
169
                  gaussian')
170
               ax.set_xlim(xedges[0], xedges[-1])
171
                ax.set_ylim(yedges[0], yedges[-1])
               return h, xedges, yedges, pc
173
174
175 def draw_bin_avgs(ax, x, y, use_log):
176
               if use_log:
                        fit_bins = np.logspace(np.log10(x.min()), np.log10(x.max()), num=nfit_bins+1)
178
179
                        fit_bins = np.linspace(x.min(), x.max(), num=nfit_bins+1)
180
               mid_bins = (fit_bins[:-1] + fit_bins[1:]) / 2.0
181
183
               mean = np.array([])
stdev = np.array([])
185
                for xmin, xmax in zip(fit_bins[:-1], fit_bins[1:]):
186
                       mask = np.logical_and(x > xmin, x <= xmax)
if mask.sum() > 0:
                                mean_el = y[mask].mean()
#stdev_el = y[mask].std() / np.sqrt(len(y))
stdev_el = y[mask].std()
188
189
191
                                #stdev_el = stdev / np.sqrt(len(y[mask]))
192
                        else:
193
194
                                stdev_el = -1.0
195
                       mean = np.append(mean, mean_el)
196
                       stdev = np.append(stdev, stdev_el)
197
198
               mask = (stdev != -1.0)
               mean = mean[mask]
stdev = stdev[mask]
199
200
               mid_bins = mid_bins[mask]
201
202
203
               ax.errorbar(mid_bins, mean, yerr=stdev, fmt='0')
204
205
               return ax, mid_bins, mean, stdev
206
208
209 def draw_bin_fit(ax, mid_bins, mean, stdev, x_min, x_max, use_log):
210
               #fit data
               if use_log:
               # coefs = np.polyfit(np.log10(x), y, 1)
                       coefs, res, rank, singvals, rcond = np.polyfit(np.log10(mid_bins), mean, 1, w=1.0/stdev, full=True) coefs, res, rank, singvals, rcond = np.polyfit(np.log10(mid_bins), mean, 1, full=True)
213
214
216
                      coefs = np.polyfit(x, y, 1)
```

```
# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, w=1.0/stdev, full=True)
coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, full=True)
219
           print 'coefs<sub>□</sub>=<sub>□</sub>', coefs
220
222
           m = coefs[0]
           b = coefs[1]
224
225
           if use_log:
             x = np.logspace(np.log10(x_min), np.log10(x_max), 100)
y = m * np.log10(x) + b
226
227
228
                x = np.linspace(x_min, x_max, 100)
          y = m * x + b
#y = x**m + b
230
          line = ax.plot(x, y, color='green')
           if print_fit_params:
234
                 if use log:
235
                       textstr = \$y_{\square}=_{\square}m_{\square}\setminus \log_{\square}x_{\square}+_{\square}b\$\setminus n\$m_{\square}=_{\square}\%g\$\setminus n\$b_{\square}=_{\square}\%g\$ '% (m, b)
236
                       textstr = \$y_{\square} = _{\square}m_{\square}x_{\square} + _{\square}b\$ \n\$m_{\square} = _{\square}\%g\$ \n\$b_{\square} = _{\square}\%g\$ \ \% \ (m, b)
                 238
239
240
241
242
          if save_fit_params:
                with open("fits_to_bins.dat", "a") as fd:
fd.write("%gu%g\n" % (m, b))
244
245
246
247
248
249 def draw_data_fit(ax, x, y, x_min, x_max, use_log):
          if remove_zero_strip:
    mask = (np.abs(y) >= y_epsilon)
250
252
                 x = x[mask]
                y = y[mask]
253
255
           #fit data
256
           if use_log:
257
               coefs, residual, rank, singular_values, rcond = np.polyfit(np.log10(x), y, 1, full=True)
                coefs, stats = np.polynomial.polynomial.polyfit(np.log10(mid_bins), mean, 1, w=1.0/stdev, full=True) coefs, res, rank, singvals, rcond = np.polyfit(np.log10(mid_bins), mean, 1, full=True)
258
259
           coefs, residual, rank, singular_values, rcond = np.polyfit(x, y, 1, full=True)

# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, w=1.0/stdev, full=True)

# coefs, stats = np.polynomial.polynomial.polyfit(mid_bins, mean, 1, full=True)
261
262
263
264
          print 'coefs_=', coefs, '+/-', residual
265
266
           m = coefs[0]
267
           b = coefs[1]
269
270
           if use_log:
             x = np.logspace(np.log10(x_min), np.log10(x_max), 100)
y = m * np.log10(x) + b
272
273
                x = np.linspace(x_min, x_max, 100)
          y = m * x + b

#y = x**m + b

line = ax.plot(x, y, color='red')
275
276
278
279
           if print_fit_params:
                 if use_log:
280
                       textstr = 'y_{\sqcup}=_{\sqcup}m_{\sqcup}\log_{\sqcup}x_{\sqcup}+_{\sqcup}b'n$m_=_\%g$\n$b_=_\%g$' % (m, b)
281
282
                      textstr = \$y_{\bot} = _{\bot}m_{\bot}x_{\bot} + _{\bot}b\$ \n\$m_{\bot} = _{\bot}\%g\$ \n\$b_{\bot} = _{\bot}\%g\$ \% (m, b)
                 283
284
285
286
287
          if save_fit_params:
               with open("fits_to_data.dat", "a") as fd:
fd.write("%gu%gu%g\n" % (m, b, residual))
289
290
291
          return ax
292
294 use_log = True
295 #use_log = False
296 z_log = True
297
298 #fit_bins = True
299 #fit_data = True
300
301 print fit params = False
302 save_fit_params = True
303
304 use_klypin = True
305
306 remove_zero_strip = True
307 y_epsilon = 0.01
308
```

```
309 y_1im = 0.5
310 \text{ x_min_lim} = 5.33e5 * 100
312 #if use_log:
313 # x_cols = [4, 5, 6, 9, 10, 23, 24, 31, 32, 47, 48, 51, 52, 57, 58] # log10 columns
314 #else:
315 # x_cols = [17, 18, 77, 78, 91, 92, 93, 94, 97, 98, 99, 100, 107, 108, 111, 112] # nolog columns
317 x_cols = []
318 x_log_cols = [-1]
319 #x_log_cols = [47, 48, -1]
320
327 ylabel = r"\sum_{u=u}^{2} \frac{ZA}{u}_{u} c_{z}
328
329 #c_source = 'density_profile'
330 c_source = 'rockstar'
332 plot_base = 'plots/diff_c_-_vs_-_'
333 plot_ext = '.eps'
334
335 #plot_name = 'test.eps'
336 #plot_name = 'c_v_M200c_21pt.eps'
337 fit_to_binned_data = False
339 \text{ Rv1 col} = 53
340 \text{ Rv2\_col} = 54
341 Rs1_col = 55
342 \text{ Rs2\_col} = 56
344 c_21pt_col = 17
345 c_za_col = 18
347 nbins = 100
348 nfit_bins = 20
350 ## c_21pt, c_za, chi2_21pt, chi2_za
351 #lt_cols = [17, 18, 37, 38]
352 #lt_vals = [100.0, 100.0, 10.0, 10.0]
353 #
354 ## c_21pt, c_za, chi2_21pt, chi2_za
355 #gt_cols = [17, 18, 37, 38]
356 #gt_vals = [1.0, 1.0, 0.0, 0.0]
358 lt_cols = []
359 lt_vals = []
361 gt_cols = [4, 5]
362 gt_vals = [100, 100]
364 eq_cols = [109, 110]
365 eq_vals = [-1, -1]
367 ne_cols = []
368 ne_vals = []
369
370 #colormap = cm.PuBuGn
371 #colormap = cm.cubehelix_r
372 #colormap = cm.ocean_r
373 #colormap = cm.rainbow
375 def add_white(orig_map, num):
           add_wnite(orig_map, num):
temp_cmap = cm.get_cmap(orig_map, num)
vals = temp_cmap(np.arange(num))
nfade = num / 7
vals[:nfade,0] = np.linspace(1., vals[nfade-1,0], nfade)
378
379
            vals[:nfade,1] = np.linspace(1., vals[nfade-1,1], nfade)
vals[:nfade,2] = np.linspace(1., vals[nfade-1,2], nfade)
#vals[:nfade,3] = np.linspace(0., vals[nfade-1,3], nfade)
380
381
            #vals[0] = [1.0, 1.0, 1.0, 1.0]

#vals[1] = (vals[1] + [1.0, 1.0, 1.0, 1.0]) / 2.0
383
            newcmap = mpl.colors.LinearSegmentedColormap.from_list("custom_1", vals)
return newcmap
384
386
387
388 colormap = add_white('rainbow', 30)
389
390 plot_dest_type = 'paper'
391 if plot_dest_type == 'paper':
392 mpl.rcParams['font.family'] = 'serif'
393 mpl.rcParams['font.size'] = 16
             mpl.rcParams['axes.linewidth'] = 3
394
            mpl.rcParams['lines.linewidth'] = 4
mpl.rcParams['patch.linewidth'] = 4
395
396
            mpl.rcParams['xtick.major.width'] = 3
mpl.rcParams['ytick.major.width'] = 3
mpl.rcParams['xtick.major.size'] = 8
mpl.rcParams['ytick.major.size'] = 8
397
398
400
```

```
401 mpl.rcParams['xtick.minor.width'] = 2

402 mpl.rcParams['ytick.minor.width'] = 2

403 mpl.rcParams['xtick.minor.size'] = 4

404 mpl.rcParams['ytick.minor.size'] = 4

405

406

407 if __name__ == '__main__':

408 main()
```

K.3 PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
 2 #PBS -M djsissom@gmail.com
 3 #PBS -m bae
4 #PBS -l nodes=1:ppn=1
 5 #PBS -1 pmem=4000mb
6 #PBS -1 mem=4000mb
7 #PBS -1 walltime=1:00:00
 8 #PBS -o out.log
9 #PBS -j oe
11 minsnap=0
12 maxsnap=61
12 maxsnap=01
13
14 # Change to working directory
15 echo $PBS_NODEFILE
16 cd $PBS_O_WORKDIR
18 rm -v fits_to_bins.dat
19 rm -v fits_to_data.dat
21 for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
22
23
          if [ $snap -lt 10 ]; then
          j=00$snap
elif [$snap -lt 100]; then
25
26
27
28
                j=0$snap
29
30
31
          new_plot_dir=snap${j}_plots
          if [ ! -e plots_all_snaps/${new_plot_dir} ]; then
    mkdir plots_all_snaps/${new_plot_dir}
32
33
34
          fi
35
36
37
                 echo "Starting_lbox{\{i\}_{l}}snap{\{j\}_{...}}" ./residual_hist.py ~/projects/simulations/rockstar/box{\{1,2,3\}/}crossmatch/snap{\{j\}/}halos.dat > plots/out.
38
                mv plots/* plots_all_snaps/${new_plot_dir}/.
echo "Finishedusnap${j}"
39
40
41
42
          #} &
43 done
44
45 wait
47 # - end of script
```

Appendix L

Alternate Differential Distribution Redshift Trends Code (Python)

```
1 #!/usr/bin/env python
 3 import sys
4 import numpy as np
5 import matplotlib as mpl
6 mpl.use('Agg')
 7 import matplotlib.pyplot as plt
from scipy.special import gamma as Gamma
from scipy.special import psi as digamma
in from ipdb import set_trace
13 def main():
        if (len(sys.argv[1:]) == 4):
             data! = read_files(sys.argv[1], header_line = None)
data2 = read_files(sys.argv[2], header_line = None)
             data3 = read_files(sys.argv[3], header_line = None)
            rsnap_data = read_files(sys.argv[4], header_line = None)
             print 'need_4_files'
20
21
             sys.exit(15)
22
23
       if fit mean trend:
            with open(statsfile, 'w') as fd:
24
25
26
27
28
                 fd.write("#plotuslopeuslope_erruinterceptuintercept_err\n")
       if minsnap > 0:
             data1 = data1[data1[:,0] >= minsnap]
data2 = data2[data2[:,0] >= minsnap]
29
             data3 = data3[data3[:,0] >= minsnap]
31
32
33
        z = 1.0 / rsnap_data[:,1] - 1.0
if (len(data1) == len(data2)) and (len(data1) == len(data3)):
    z = z[-len(data1):]
34
35
36
37
38
             sys.exit(16)
        data1 = np.column_stack((data1, z))
        data2 = np.column_stack((data2, z))
data3 = np.column_stack((data3, z))
39
40
        #~~~~
        # make mean and stdv plots
44
45
        for (data, ylabel, label, name) in zip([data1, data2, data3], ylabels1, labels1, names):
    print "Makingu%suplot..." % (name + 'uxvals')
    fig = plt.figure(figsize=(9.0, 6.0))
48
50
             ax = fig.add_subplot(111)
51
             ax = make_plot(ax, data[:,z_col], data[:,peak_col], err = None, color = 'black', marker='o', linestyle='-
         ', label=None)
53
            for (x_val_col, color) in zip(x_val_cols, colors1):
         ax = make_plot(ax, data[:,z_col], data[:,x_val_col], err = None, color = color, marker='o', linestyle ='--', label=None)
55
            #if add_rms_line:
            # ax = make_plot(ax, data[:,z_col], data[:,data_rms_col], color = 'green', linestyle=':')
60
            #if fit_mean_trend:
                ax, slope, slope_err, intercept, intercept_err = add_fit(ax, data[:,z_col], data[:,mean_col], err= :,mean_err_col], color='red')
         data[:,mean_err_col],
62
                 save_fits(statsfile, name, slope, np.sqrt(slope_err), intercept, np.sqrt(intercept_err))
            #ax.legend(loc='lower right')
            ax.set_xlim(z[0] + 1.0, z[-1] - 1.0)
65
            #ax.invert_xaxis()
67
            ax.set_xlabel(xlabel, fontsize='x-large')
ax.set_ylabel(ylabel, fontsize='x-large')
70
71
72
73
74
75
76
77
             fig.tight_layout()
             fig.savefig(plot_base + name + '_xvals' + plot_ext, bbox_inches='tight')
        for (data, ylabel, label, name) in zip([data1, data2, data3], ylabels2, labels1, names):
    print "Makingu%suplot..." % (name + 'usumfrac')
            print "Making "suplot..." % (name + 'usumfrac')
fig = plt.figure(figsize=(9.0, 6.0))
ax = fig.add_subplot(111)
```

```
for (sum_frac_col, color) in zip(sum_frac_cols, colors2):
82
          ax = make_plot(ax, data[:,z_col], data[:,sum_frac_col], err = None, color = color, marker='0',
linestyle='-', label=None)
              for (doublesum_frac_col, color) in zip(doublesum_frac_cols, colors2):
          ax = make_plot(ax, data[:,z_col], data[:,doublesum_frac_col], err = None, color = color, marker='o', linestyle='--', label=None)
84
85
             ax.set_xlabel(xlabel, fontsize='x-large')
ax.set_ylabel(ylabel, fontsize='x-large')
ax.set_xlim(z[0] + 1.0, z[-1] - 1.0)
86
87
88
89
             ax.set_yscale('log')
91
             fig.tight_layout()
             fig.savefig(plot_base + name + '_sumfrac' + plot_ext, bbox_inches='tight')
92
94
         print 'Finishedualluplots.'
96
97
98 def make_plot(ax, x, y, err=None, color='black', marker='None', linestyle='None', label=None):
99
        if err == None:
   if label == None:
100
101
                   ax.plot(x, y, color=color, marker=marker, linestyle=linestyle)
102
103
                   ax.plot(x, y, color=color, marker=marker, linestyle=linestyle, label=label)
105
              if label == None:
                  ax.errorbar(x, y, yerr=err, color=color, marker=marker, linestyle=linestyle)
106
108
                  ax.errorbar(x, y, yerr=err, color=color, marker=marker, linestyle=linestyle, label=label)
109
         return ax
110
113 def add_fit(ax, x, y, err=None, color='red'):
        from scipy.optimize import curve_fit
p0 = [0.0, 0.0]
114
116
         try:
             coeffs, pcov = curve_fit(linear, x, y, sigma=err, p0=p0)
        except RuntimeError:
             print '********Curve_fit_failed_*********
119
              return np.nan, np.nan
        return np.nan, np.nan
xmin, xmax = ax.get_xlim()
x_fit = np.linspace(xmin, xmax, 20)
y_fit = linear(x_fit, coeffs[0], coeffs[1])
ax.plot(x_fit, y_fit, color=color, linestyle='--')
return ax, coeffs[0], pcov[0,0], coeffs[1], pcov[1,1]
124
126
128 def linear(x, slope, intercept):
129 return slope * x + intercept
130
def read_files(files, header_line = None, comment_char = '#'):
       header = None
data = None
134
135
         if type(files) == str:
136
              files = [files]
138
        if header_line != None:
             with open(files[0], 'r') as fd:
139
                 for line in range(header_line):
140
141
                        fd.readline()
                   header = fd.readline()
142
              if header[0] != comment_char:
144
                   print "Header must start with a '%s' % comment_char
                   sys.exit(4)
145
              header = header[1:]
header = header.split()
147
148
149
        for file in files:
              print 'Reading_file_%s...' % (file)
if data == None:
150
151
                   data = np.genfromtxt(file, comments=comment_char)
                   data = np.append(data, np.genfromtxt(file, comments=comment_char), axis=0)
155
         print 'Finishedureadingufiles.'
if header_line == None:
156
158
              return data
159
         else:
160
              return header, data
161
162
163 def save_fits(file, name, slope, slope_err, intercept, intercept_err):
       with open(file, 'a') as fd:
fd.write("%su%gu%gu%gu%g\n" % (name, slope, slope_err, intercept, intercept_err))
164
166
167
168 plot_dest_type = 'paper'
169 if plot_dest_type == 'paper':
```

```
mpl.rcParams['font.family'] = 'serif'
mpl.rcParams['font.size'] = 16
mpl.rcParams['axes.linewidth'] = 3
mpl.rcParams['lines.linewidth'] = 4
172
173
             mpl.rcParams['lines.linewidth'] = 4
mpl.rcParams['yatch.linewidth'] = 4
mpl.rcParams['xtick.major.width'] = 3
mpl.rcParams['ytick.major.width'] = 3
mpl.rcParams['xtick.major.size'] = 8
mpl.rcParams['ytick.major.size'] = 8
174
175
176
178
180 #colors = ['red', 'green', 'blue']

181 colors = ['black', 'black', 'black']

182 labels1 = [r'$c$', r'$M_{\mathrm{vir}}$', r'$X_{\mathrm{off}}$']
183 names = ['c_rockstar', 'Mvir', 'Xoff']
184 xlabel = 'Redshift'
185 ylabels = {\text{keasnit}'}

185 ylabels = {\text{res}bleta'_uc(f_{h},z)}_uand_u$\setminus Delta'_uc_{\mathbf{mathrm}\{peak}}$", r"$\setminus Delta'_uM_{\mathbf{mathrm}\{vir}}(f_{h},z)}_uand_u$\setminus Delta'_uM_{\mathbf{mathrm}\{vir,upeak}}$", r"$\setminus Delta'_uX_{\mathbf{mathrm}\{off}}(f_{h},z)}_uand_u$\setminus Delta'_uX_{\mathbf{mathrm}\{off,upeak}}$"
186 \ \ \textbf{ylabels2} = [r"\$f_{h}(\Delta'_uc,z)\$", r"\$f_{h}(\Delta'_um_{mathrm{vir}},z)\$", r"\$f_{h}(\Delta'_uX_{mathrm{off}},z)
                $"1
187 plot_base = 'plots/'
188 plot_ext = '.eps'
189
190 statsfile = 'plots/stats.dat'
191
192 z_col
                            = -1
                          = 0
= 7
193 snap_col
194 mean_col
195 mean_err_col = 8
196 var_col = 9
197 var_err_col = 10
                               = 3
198 skew_col
199 skew_err_col = -2
200 #skew_col = 7
201 #skew_err_col = 8
202 #kurt_col
                               = 4
203 #kurt_err_col = -2
204 kurt_col = 13
205 kurt_err_col = 14
206 beta_col = 13
207 beta_err_col = 14
208
209 data_mean_col = 1
210 data_rms_col = 15
212
214 peak_col = 1
215 x_val_cols = np.array([4, 6, 8]) + 2
216 sum_frac_cols = np.array([2, 4, 6, 8]) + 2 + 9
217 doublesum_frac_cols = sum_frac_cols + 9
219 colors1 = ['red', 'green', 'blue']
220 colors2 = ['blue', 'green', 'red', 'black']
222 offset = 0.06
223 #offset = 0.0
225 \text{ minsnap} = 39
226 #minsnap = None
228 fit_mean_trend
                                         = False
= False
229 add_rms_line
230
```

Appendix M

Miscellaneous Scripts

M.1 Directory Structure Setup (Bash)

```
1 #!/usr/bin/env bash
      minsnap=0
  4 maxsnap=61
 6 minbox=1
  9 for ((i=$minbox; i<=$maxbox; i++)); do</pre>
10
        if [ ! -e ../box$i ]; then
              mkdir -v ../box$i
           if [ ! -e ../box$i/21pt ]; then
           mkdir -v ../box$i/21pt
fi
           if [ ! -e ../box$i/za ]; then
16
17
              mkdir -v ../box$i/za
           if [ ! -e ../box$i/crossmatch ]; then
  mkdir -v ../box$i/crossmatch
19
20
21
            cp -v run_*.pbs ../box$i/.
            cp -v postprocess.sh ../box$i/.
            for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
27
28
                if [ $snap -lt 10 ]; then
                     j=00$snap
                elif [ $snap -lt 100 ]; then
               j=0$snap
30
31
32
33
                if [ ! -e ../box$i/21pt/snap$j ]; then
                mkdir -v ../box$i/21pt/snap$j
34
35
                if [ ! -e ../box$i/za/snap$j ]; then
36
               mkdir -v ../box$i/za/snap$j
fi
37
38
39
                cp -v -r proto/* ../box$i/21pt/snap$j/.
cp -v -r proto/* ../box$i/za/snap$j/.
41
42
                 ln -v -s ~"/projects/data/2lpt/box\$i/2lpt_512_z300_PM_\$j ~../box\$i/2lpt/snap\$j/particles/2lpt_512_z300_PM_\$j ~../box\$i/2lpt/snap$j/particles/2lpt_512_z300_PM_\$j ~../box\$i/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particles/2lpt/snap$j/particle
                ln -v -s /projects/data/za/box$i/za_512_z300_PM_$j ../box$i/za/snap$j/particles/za_512_z300_PM_$j
44
45
                /21pt/snap$j/particles/snapnames.lst
                echo /home/sissomdj/projects/simulations/rockstar/box$i/za/snap$j/particles/za_512_z300_PM_$j > ../box$i/za/
                   snap$j/particles/snapnames.lst
48
               50
51
52
53
                echo "FILENAME_{\sqcup}=_{\sqcup}\"21pt_512_z300_PM_$j\"" >> ../box$i/21pt/snap$j/onenode.cfg echo "FILENAME_{\sqcup}=_{\sqcup}\"za_512_z300_PM_$j\"" >> ../box$i/za/snap$j/onenode.cfg
54
            done
56 done
```

M.2 CROSSMATCH Setup (Bash)

```
1 #!/usr/bin/env bash
2
3 minsnap=0
4 maxsnap=61
5
6 minbox=1
7 maxbox=3
8
9 for ((i=$minbox; i<=$maxbox; i++)); do
10    if [ ! -e ../box$i/crossmatch ]; then
11    mkdir -v ../box$i/crossmatch
12    i
13
14    cp -v run_crossmatch.pbs ../box$i/.
15
16    for ((snap=$minsnap; snap<=$maxsnap; snap++)); do</pre>
```

```
if [ $snap -lt 10 ]; then
                             j=00$snap
19
                       elif [ $snap -lt 100 ]; then
20
                      j=0$snap
fi
21
22
23
                      if [ ! -e ../box$i/crossmatch/snap$j ]; then
24
25
                            mkdir -v ../box$i/crossmatch/snap$j
26
27
                       cp -v -r crossmatch_proto/* ../box$i/crossmatch/snap$j/.
                       \textbf{echo} \ \texttt{"OUTPUT\_DIR}_{\texttt{UUUUUUUU}} / \texttt{home/sissomdj/projects/simulations/rockstar/box\$i/crossmatch/snap\$j"} >> .../\texttt{box\$i/simulations/rockstar/box\$i/crossmatch/snap\$j"} >> .../\texttt{box\$i/simulations/rockstar/box\$i/crossmatch/snap\$j} >> .../\texttt{box\$i/simulations/rockstar/box} >> .../\texttt{box\$i/simulations/rockstar/box} >> .../\texttt{box\$i/simulations/rockstar/box} >> .../\texttt{box§i/simulations/rockstar/box} >> .../\texttt{box§i/simulations/rockst
                           crossmatch/snap$j/rockstar_21pt.param
                      echo "FIRST_GROUPDIR_uuuu/home/sissomdj/projects/simulations/rockstar/box$i/21pt/snap$j/halos" >> ../box$i/crossmatch/snap$j/rockstar_21pt.param
30
                      echo "SECOND_GROUPDIR_uuu/home/sissomdj/projects/simulations/rockstar/box$i/za/snap$j/halos" >> ../box$i/crossmatch/snap$j/rockstar_2lpt.param
31
33
                                                                                                   /home/sissomdj/projects/simulations/rockstar/box$i/crossmatch/snap$j" >> ../box$i/
                            crossmatch/snap$j/rockstar_za.param
34
                      echo "FIRST_GROUDFDIRUUUU/home/sissomdj/projects/simulations/rockstar/box$i/za/snap$j/halos" >> ../box$i/
                           {\tt crossmatch/snap\$j/rockstar\_za.param}
35
                      echo "SECOND_GROUPDIR_UUU/home/sissomdj/projects/simulations/rockstar/box$i/21pt/snap$j/halos" >> ../box$i/
                           crossmatch/snap$j/rockstar_za.param
38
39 done
```

M.3 Individual Snapshot ROCKSTAR Run Script (Bash)

```
1 #!/bin/bash
2
3 echo "Cleaninguoldufiles..."
4 if [ -e out.log ]; then
5    mv -v out.log out.log.bak
6 fi
7 if [ -e server.out ]; then
8    mv -v server.out server.out.bak
9 fi
10 if [ -e clients.out ]; then
11    mv -v clients.out clients.out.bak
2 fi
13 if [ -e auto-rockstar.cfg ]; then
14    rm -v auto-rockstar.cfg
15 fi
16 if [ $(1s halos/* 2> /dev/null | wc -l) != "0" ]; then
17    rm -rv halos/*
18 fi
19
20 echo "Submittingurunuscript..."
21 echo "qsuburun_rockstar.pbs"
22 qsub run_rockstar.pbs
```

M.4 All Snapshots ROCKSTAR 2LPT PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
 3 #PBS -M djsissom@gmail.com
 4 #PBS -m bae
5 #PBS -l nodes=1:ppn=10
 6 #PBS -1 pmem=3000mb
7 #PBS -1 mem=30000mb
 8 #PBS -1 walltime=6:00:00
 9 #PBS -o out_21pt.log
10 #PBS -j oe
12 echo $PBS NODEFILE
13 cd $PBS_O_WORKDIR
15 for snapdir in 2lpt/*; do
16 # Change to working directory
      echo Working on $snapdir...
18
      cd $PBS_O_WORKDIR/$snapdir
20
      rockstar -c onenode.cfg &> server.out &
      # Wait for auto-rockstar.cfg to be created
perl -e 'sleep 1 while (!(-e "halos/auto-rockstar.cfg"))'
mv halos/auto-rockstar.cfg .
      # Execute the reader processes
28
29
      mpiexec -verbose -n 1 rockstar -c auto-rockstar.cfg >> clients.out 2>&1 &
      sleep 20
      # Execute the analysis processes
      mpiexec -verbose -n 8 rockstar -c auto-rockstar.cfg >> clients.out 2>&1
```

```
34 # - end of script
35 done
```

M.5 All Snapshots ROCKSTAR ZA PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
 3 #PBS -M djsissom@gmail.com
 4 #PBS -m bae
5 #PBS -l nodes=1:ppn=10
 6 #PBS -1 pmem=3000mb
7 #PBS -1 mem=30000mb
 8 #PBS -1 walltime=6:00:00
12 echo $PBS_NODEFILE
13 cd $PBS_O_WORKDIR
13 cd *..._ -
14
15 for snapdir in za/*; do
16 # Change to working directory
17 echo Working on $snapdir...
18 cd $PBS_O_WORKDIR/$snapdir
      # Start the server
      rockstar -c onenode.cfg &> server.out &
      \mbox{\tt\#} Wait for auto-rockstar.cfg to be created
      mv halos/auto-rockstar.cfg .
      # Execute the reader processes
      mpiexec -verbose -n 1 rockstar -c auto-rockstar.cfg >> clients.out 2>&1 & sleep 20
      \# Execute the analysis processes mpiexec -verbose -n 8 rockstar -c auto-rockstar.cfg >> clients.out 2>&1
     # - end of script
35 done
```

M.6 All Snapshots ROCKSTAR Post-Process Script (Bash)

```
1 #!/usr/bin/env bash
2
3 startdir='pwd'
4
5 for snapdir in {21pt,za}/*; do
6 echo Working on $snapdir...
7 cd $startdir/$snapdir
8
9 ./postprocess
10
11 done
12
13 # - end of script
```

M.7 All Snapshots CROSSMATCH PBS Submission Script (Bash)

```
1 #!/usr/bin/env bash
  3 #PBS -M djsissom@gmail.com
 4 #PBS -m bae

5 #PBS -l nodes=62:ppn=1

6 #PBS -l pmem=3000mb

7 #PBS -l mem=186000mb

8 #PBS -l walltime=1:00:00
9 #PBS -o out_crossmatch.log
10 #PBS -j oe
12 echo $PBS_NODEFILE
13 cd $PBS_O_WORKDIR
15 for snapdir in crossmatch/*; do
16  # Change to working directory
       echo Working on $snapdir...
cd $PBS_O_WORKDIR/$snapdir
18
19
20
             mpiexec -verbose -n 1 crossmatch rockstar_2lpt.param > out_2lpt_first.log 2>&1
             mpiexec -verbose -n 1 crossmatch rockstar_za.param > out.za_first.log 2>&1
23
24
             echo "Finished<sub>□</sub>$snapdir"
26 done
29 # - end of script
```

M.8 All Snapshots Density Profile PBS Submission Script (Bash)

```
#!/usr/bin/env bash

2
3 #PBS -M djsissom@gmail.com
4 #PBS -m bae
5 #PBS -l nodes=124:ppn=1
6 #PBS -l pmem=4000mb
7 #PBS -l mem=49600mb
8 #PBS -l walltime=1:00:00
9 #PBS -o out_density_profile.log
10 #PBS -j oe
11
12 echo $PBS_NODEFILE
13 cd $PBS_O_WORKDIR
14
15 for snapdir in {2lpt,za}/snap*/halos; do
16 # Change to working directory
17 echo Working on $snapdir...
18 cd $PBS_O_WORKDIR/$snapdir
19
20 {
21 mpiexec -verbose -n 1 density_profile halos_0.*.bgc2 > density_profile_out.log 2>&1
22 echo "Finished_u$snapdir"
23 } &
24
25 done
26
27 wait
28 # - end of script
```