

# Micro-economic models of fertility (1): "the cost of time"

Economic Demography

Econ/Demog c175

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UC Berkeley

Week 8, Lecture A

Spring 2017

# The big questions

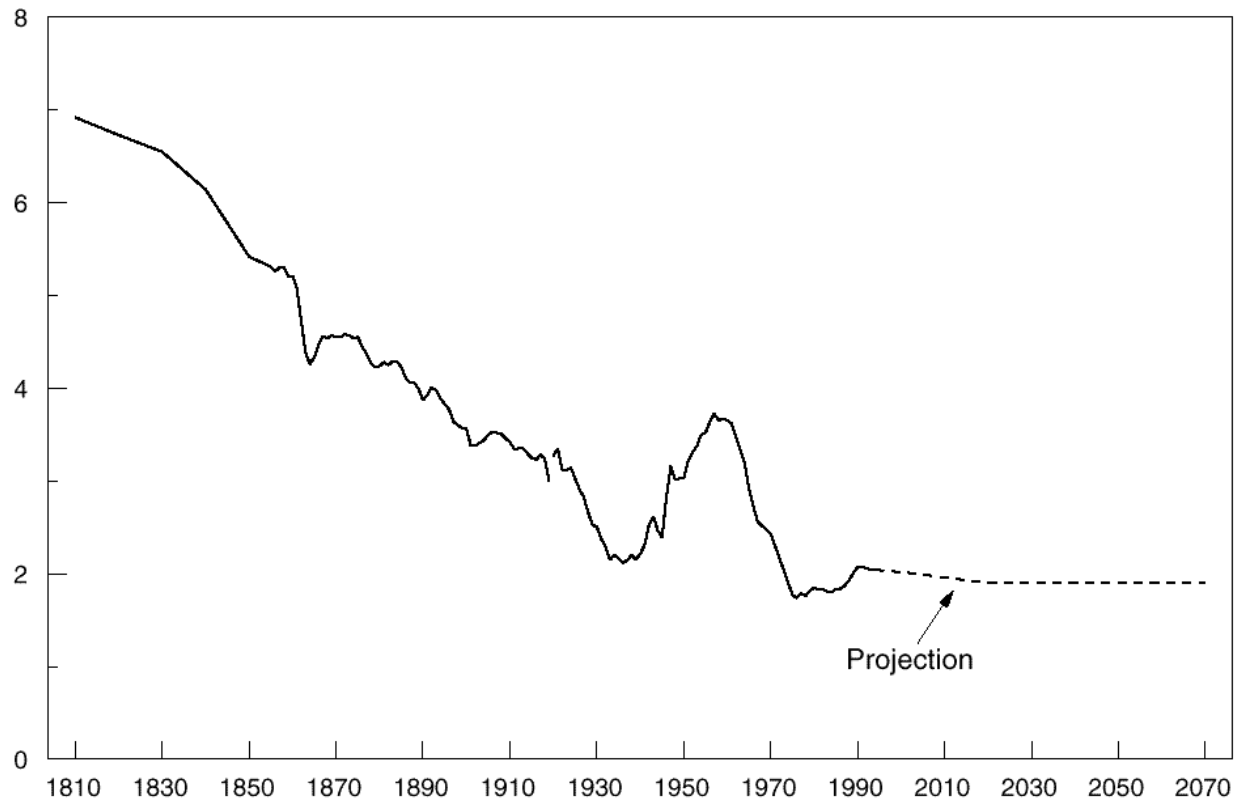
- Big Puzzle: If kids are “normal” goods, why has fertility fallen as incomes have climbed?
- A big problem in socio-biology: why doesn't social/economic success produce more offspring?
- Two kinds of questions:
  - Temporal
  - Cross-sectional (within a society & between societies)
- Additional motivation: what will happen in the future?

# Example of temporal decline

Chart 3-1 **Total Fertility Rate**

The total fertility rate has been falling steadily over time, with the exception of the post-World War II baby boom.

Births per woman

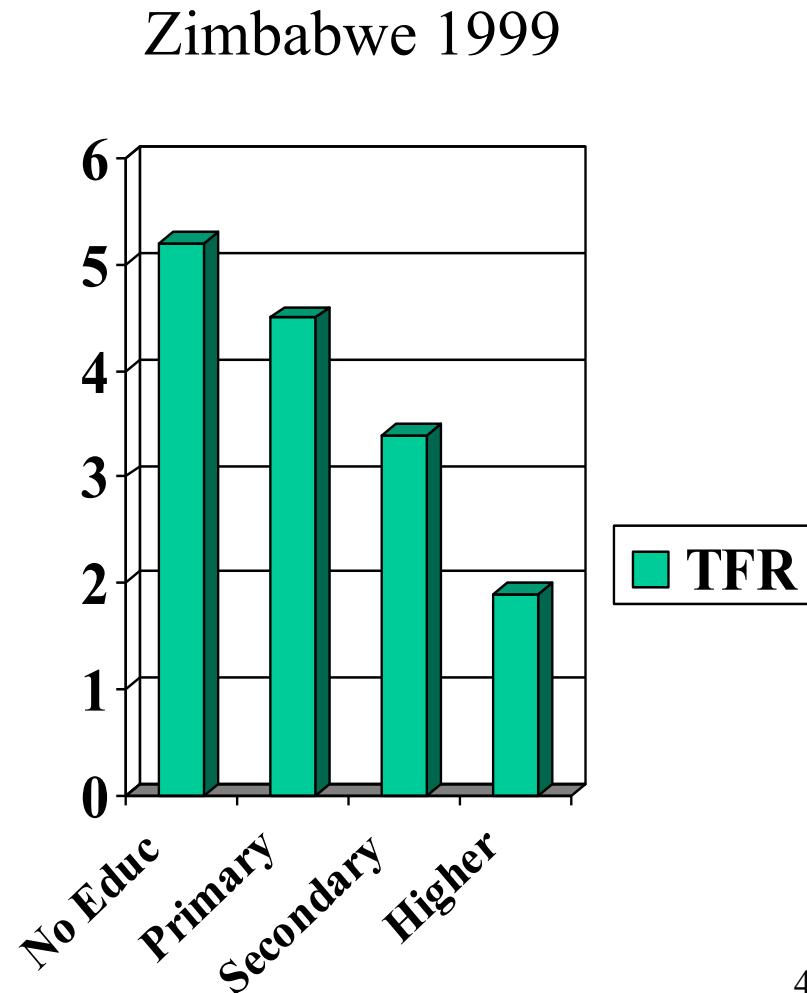


Note: The total fertility rate is the average number of births per woman during childbearing years. Data prior to 1920 are for whites only.

Sources: Data prior to 1920: Coale, A. and M. Zelnick (1963), "New Estimates of Fertility and Population in the U.S.;" 1920-1969: Department of Health and Human Services; 1970-2070: Social Security Administration.

# Example of differential fertility

- Total Fertility Rate for everyone is 4.0
- A very strong educational gradient
- (Note: TFR is a period measure and has some caveats.)



# Fertility differences between populations

In 2000, TFRs

- Austria (1.3)
- France (1.8)
- Italy (1.2)
- Greece (1.3)
- Spain (1.2)
- UK (1.7)
- US (2.0)

# Micro-economic models

- Today, opportunity cost of childbearing
- Thursday, Becker's quantity-quality tradeoff model

# Set up of our model

1. Utility is a function of goods and kids  
$$U(\text{X} = \text{goods}, \text{N} = \# \text{ of kids})$$
2. Budget constraint: can only spend what you earn
3. Earnings a function of wages, hours worked, and “other income”
4. Time spent only working or taking care of children (leisure is left out of simple model)
  - Model will take into account opportunity costs of time
  - (For convenience, fix costs of  $\text{X} = 1$ )

# Time constraint

$$T = L + cN$$

The diagram illustrates the time constraint equation  $T = L + cN$ . It features three arrows pointing from descriptive text to the variables in the equation: 

- An arrow from "total available hours" points to  $T$ .
- An arrow from "hours in labor force" points to  $L$ .
- An arrow from "hours caring for kids" points to  $c$ .

 Additionally, the text "number of kids" is positioned above the equation, with an arrow pointing down to the variable  $N$ , which is highlighted in red.

total available hours

hours in labor force

hours caring for kids

number of kids



# Budget constraint (1)

\$ expenses = \$ income

$$\begin{array}{ccccccc} & \nearrow & \text{X} & + & p & \text{N} & = \text{earnings} + \text{I} \nwarrow \\ \text{goods} & & & & \nearrow & & \text{other income} \\ & & & & \text{money} & & \\ & & & & \text{cost per} & & \\ & & & & \text{kid} & & \end{array}$$

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$$wL = w(T - cN)$$

hours worked =  $T$  – hours caring for kids

Can rewrite earnings

$$\text{X} + p\text{N} = (wT - wcN) + I$$

# Budget constraint (2)

We have

$$X + pN = wT - wcN + I$$

Reconceptualize in terms of “full income” and all expenses (including opportunity costs).

A decision-making framework incorporating full cost of kids.

$$X + (p+wc)N = wT + I$$

money cost

per kid (food, ...)

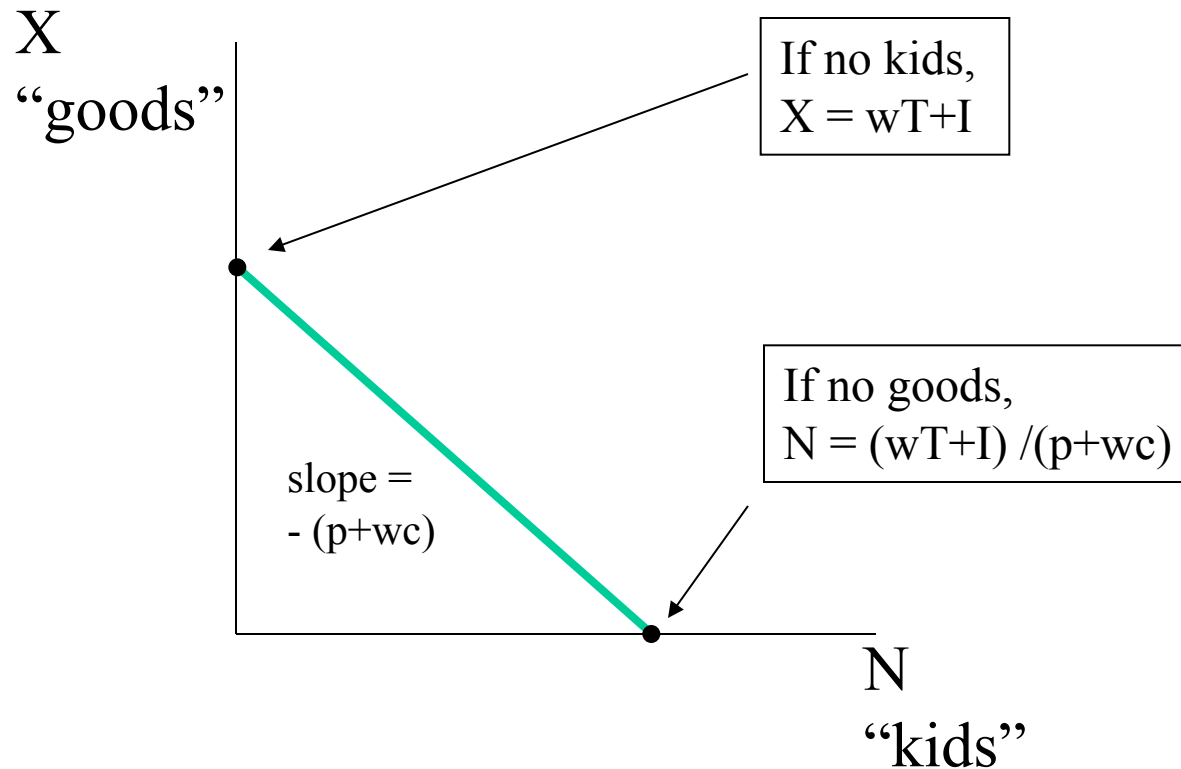
opportunity cost

per kid

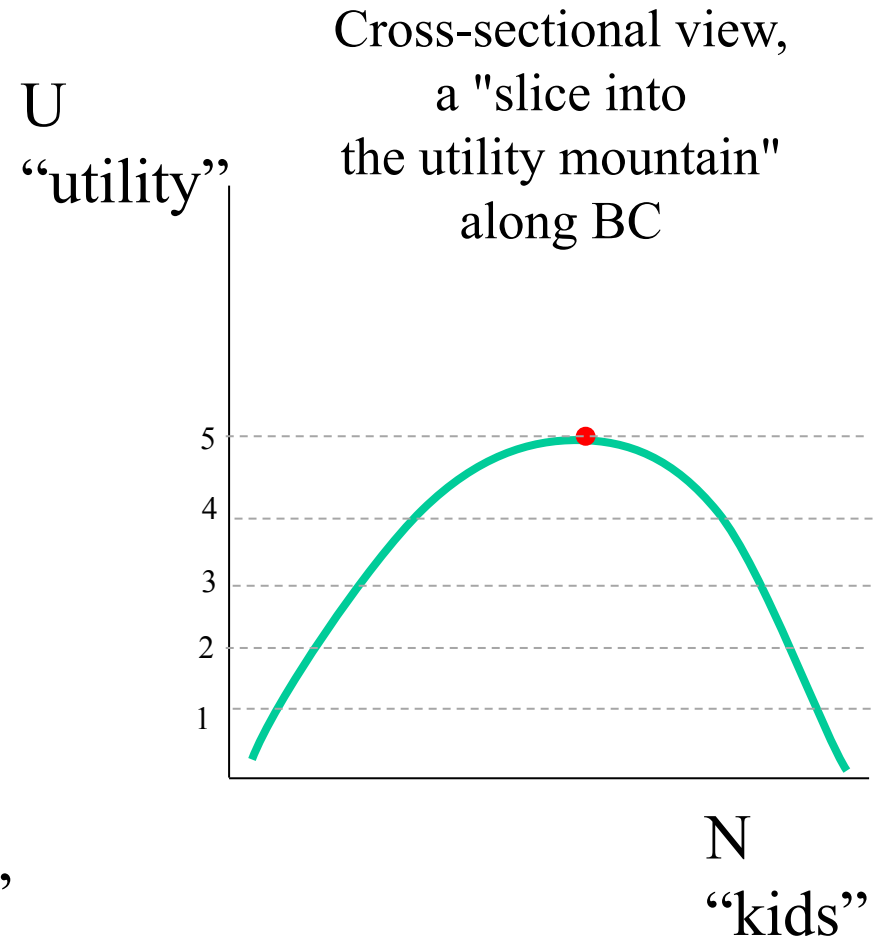
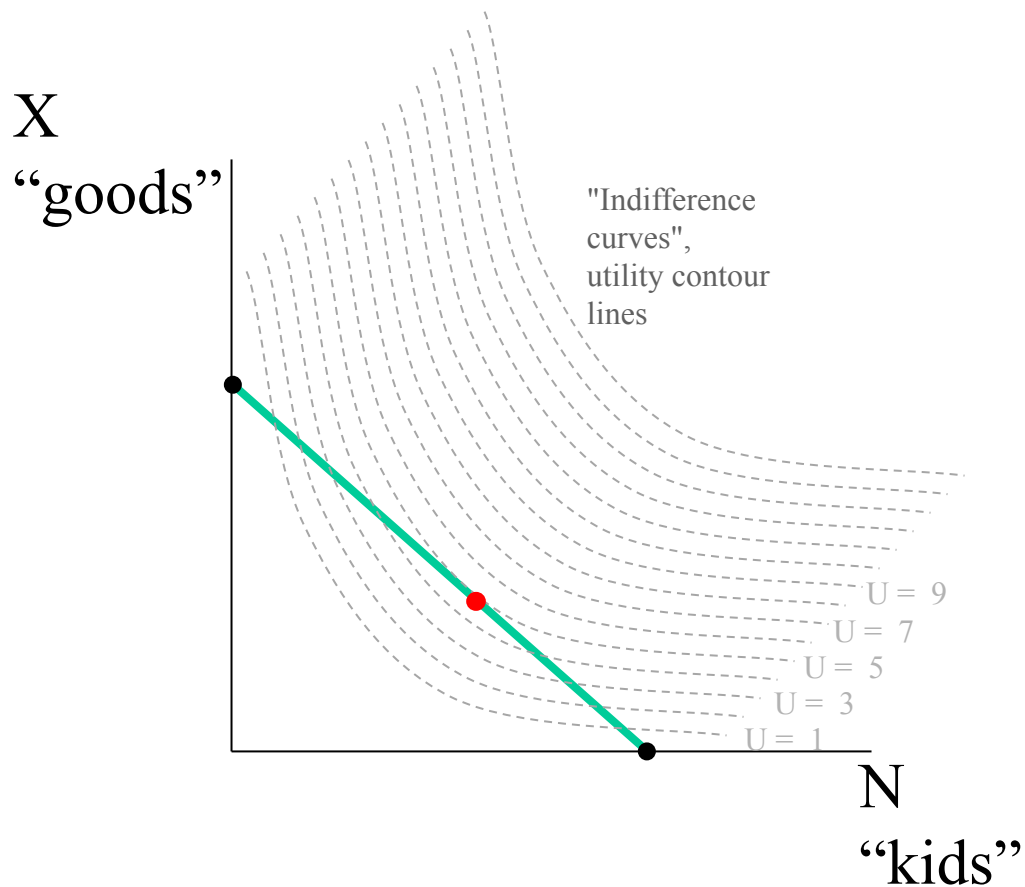
“full income”

# Graph of budget constraint

$$X + (p+wc)N = wT + I$$



# Maximizing utility along the budget constraint



$$X = wT + I - (p + wc) N$$

Assume

$w = \$20$  per hour

$T = 40$  hours per week

$I = \$1,000$  per week

$p = \$200$  per kid per week

$c = 5$  hours per kid per week

Let's calculate for  $N = 5$

# $(N, X)$ bundles along BC

N	X	U?
0	1800	
1	1500	
2	1200	
3	900	
4	600	
5	300	

Let's assume Cobb-Douglas utility

$$U(N, X) = X^{0.7}N^{0.3}$$

N	X	U(N,X)
0	1800	0
1	1500	167
2	1200	176
3	900	?
4	600	?
5	300	?



# A picture

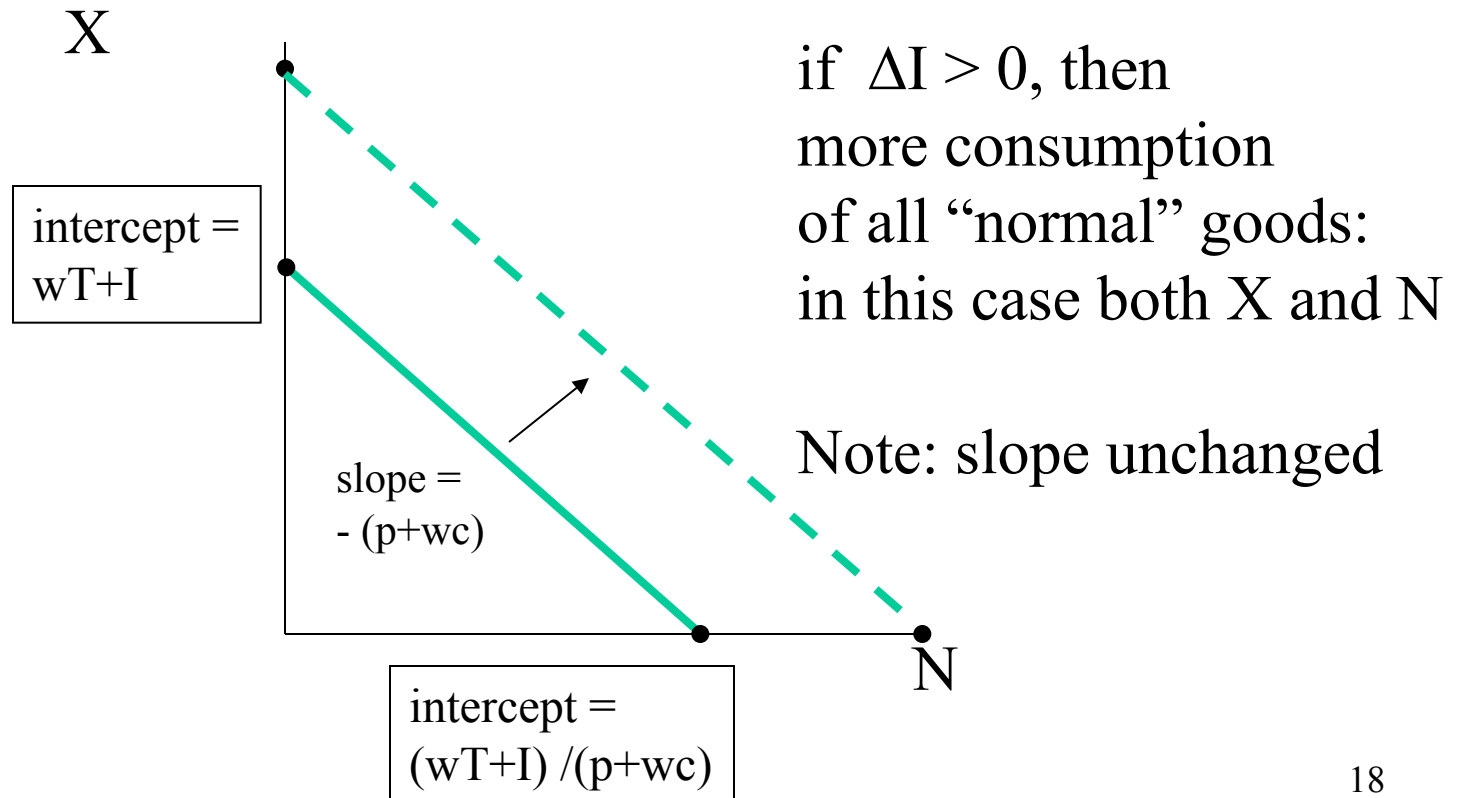
```
## some parameter values
p = 200; c = 5; w = 20; I = 1000; T = 40

## X = f(N) along BC
N.vec = seq(0, 5, .1)
X.vec = w*T + I - (p + w*c)*N.vec

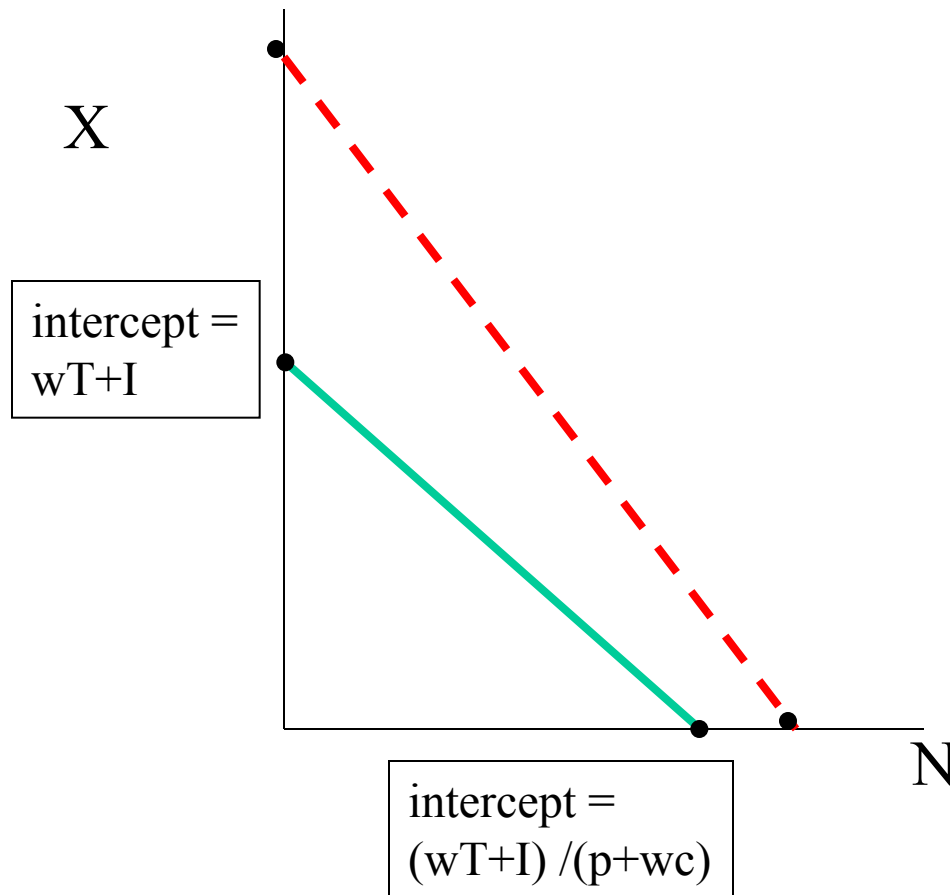
## Utility for each "bundle"
a = .7 ; U.vec = X.vec^a * N.vec^(1-a)

## Maximization
plot(N.vec, U.vec)
N.opt = N.vec[which.max(U.vec)]
abline(v = N.opt, col = 2)
title(paste("Utility maximized when N =",
            N.opt))
```

# What happens if non-wage income increases by $\Delta I$ ?



# What happens if wages increase?

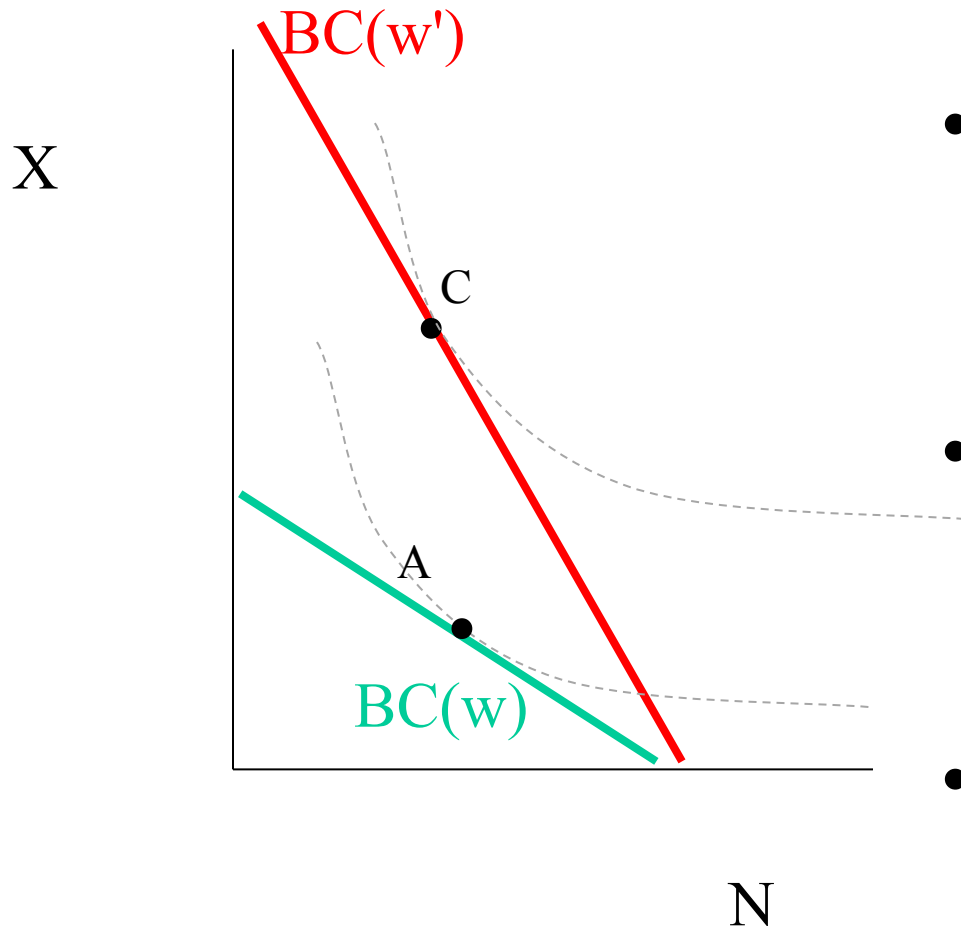


slope will change:  
effect on number of  
kids is *ambiguous*

*could increase fertility  
because more income to  
spend on fixed costs of  
childbearing (income effect)*

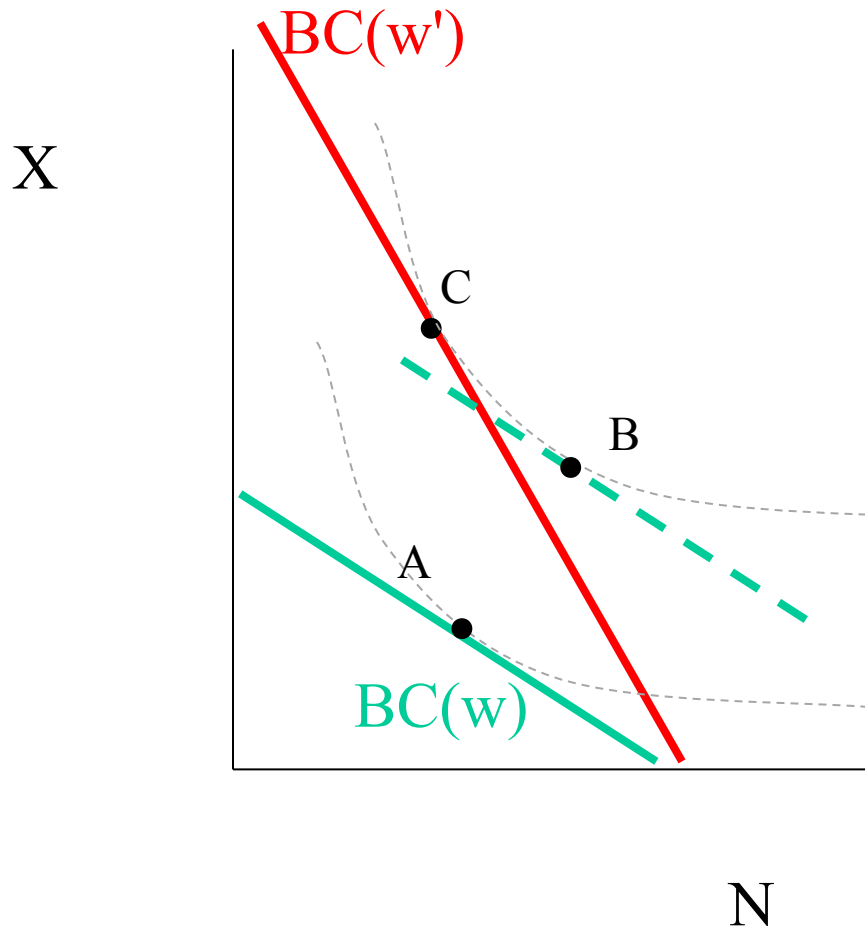
*OR, could decrease fertility  
because opportunity cost  
of childbearing increases  
(substitution effect  $\rightarrow$  goods)*

# What happens if wages increase?



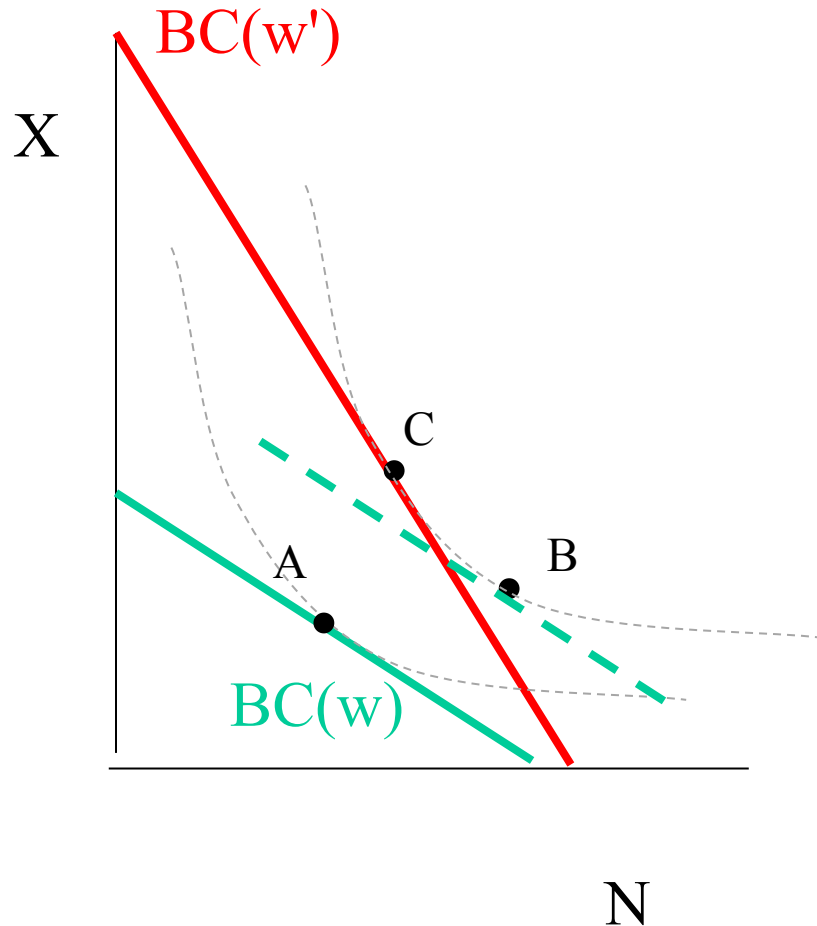
- When we change wages, we go from bundle  $A \rightarrow C$
- Here, we choose fewer children (!) and more goods
- "Substitution effect dominates income effect"

# Income and substitution effects



- $A \rightarrow B = \textit{income effect}$   
We hold prices (slope) constant and move to new  $U$
- $B \rightarrow C = \textit{substitution}$   
(or "*price*") effect  
We change price, moving along new  $U$

# A different picture (when income effect dominates)



- $A \rightarrow B = \text{income effect}$   
Always positive
- $B \rightarrow C = \text{substitution effect}$   
Always negative
- But now net effect of wage increase is to increase consumption of both kids and goods

# Is our model great, or terrible?

- Effect of wage increase goes either way
  - bad for prediction
  - good for after-the-fact
- Stronger predictions for other changes

# Other changes

- $dN / dp?$  (lower price of schools?)
- $dN / dI?$  (increase "male" income?)
- $dN / dc?$  (clothes washing machine?)
- $dN / df(U)?$  (changing preferences?)

We'll look at these more on Thursday

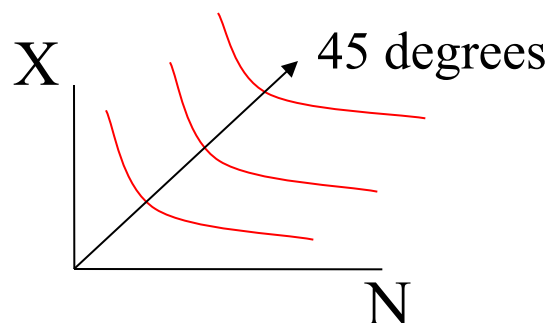


# Tastes and the utility function

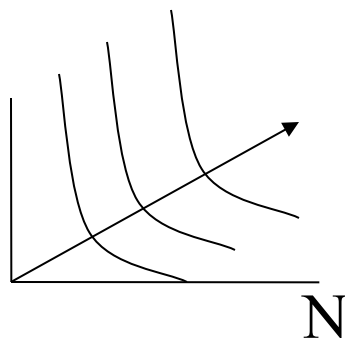
Let  $U(X, N)$  be the standard Cobb-Douglas utility function  
 $= X^a N^{(1-a)}$  for  $0 < a < 1$

$a$  is an index of marginal rate of substitution between goods  
and children: big  $a$  means lot of  $N$  for little  $X$   
small  $a$  = little  $N$  for lot of  $X$

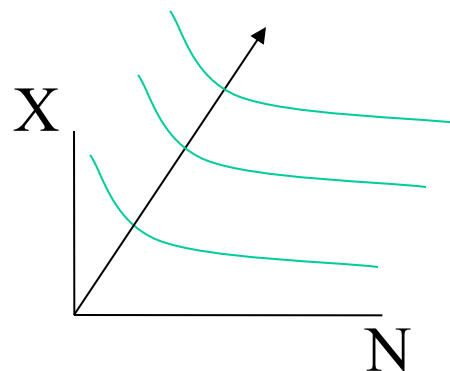
$a = 1/2$



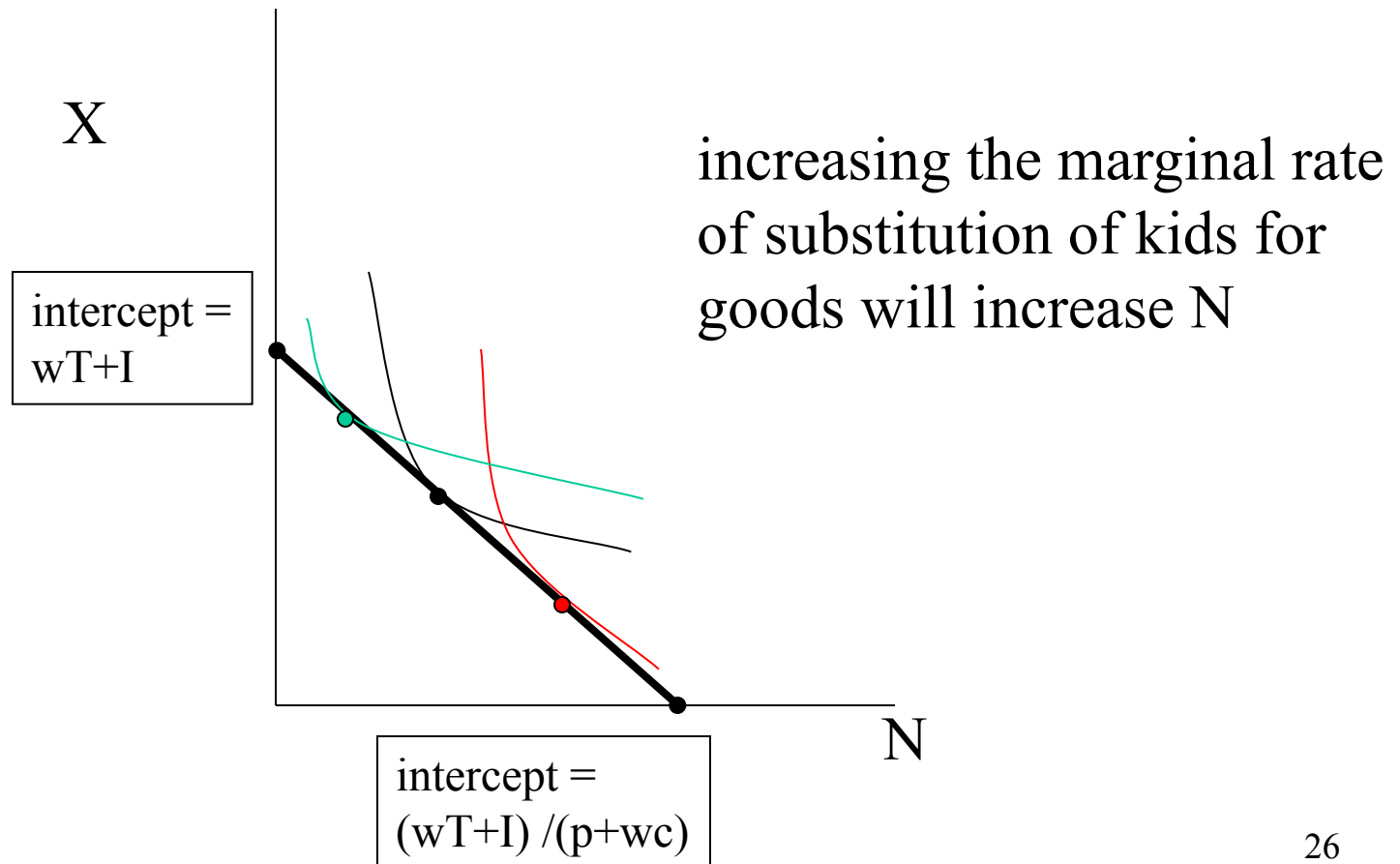
$a < 1/2$



$a > 1/2$



# Effect of changing tastes



# Conclusions from model

(If kids are “normal” goods)

- increasing price of kids ( $p$ ), decreases fertility
- increasing non-wage income ( $I$ ), increases fertility
- increasing preferences for kids ( $1-a$ ), increases fertility; increasing preferences for goods ( $a$ ) decreases fertility
- but: increasing wages ( $w$ ), is ambiguous
- *So the idea that increasing **wages** reduces fertility is based on empirical research, not theoretical necessity*

# Explanations?

- Kuwait vs. Switzerland.
- Why as an increasing share of income comes from women, fertility declines
- Why increasing female education decreases fertility
- Next time, endogenizing costs per child (what happens if costs per child depends on number of children?)