

Forces - More Practice

Section 1 - \vec{F}_g

- 1.) Calculate the force of gravity on a 25 kg mass at the surface of the earth.

$$\vec{F}_g = m \times \vec{g} \quad \text{SAME AS } F = m\vec{a}$$

$$\vec{F}_g = (25)(-9.81) \quad \boxed{\vec{F}_g = -245 \text{ N}}$$

- 2.) A 75 kg mass is on the surface of Mars when an astronaut lifts it with a spring scale. The scale has a reading of 259 N. What is the gravitational field strength on Mars?

$$\vec{F}_g = m \times \vec{g} \quad \frac{-259}{75} = \cancel{75}(\vec{g}) \quad \vec{g} = -3.45 \text{ m/s}^2 \Rightarrow \boxed{(-3.45 \text{ N/kg})}$$

- 3.) How much force must a horizontal surface exert to hold up a 2.0 kg book and what is the name of that force? \vec{F}_n

$$\vec{w} = m \vec{g} \quad \vec{w} = (2.0)(-9.81)$$

$$\vec{w} = -19.6 \text{ N} \quad \therefore \vec{F}_n = +19.6 \text{ N}$$

Section 2 - \vec{F}_{net}

- 1.) A cat is dragged at a constant velocity of $+3.0 \frac{\text{m}}{\text{s}}$ across sandpaper. What is the total force on the cat?

ON $\begin{array}{l} \text{-- NEWTON'S FIRST LAW} \\ \text{-- ALL FORCES IN BALANCE} \end{array}$

- 2.) A 1200 kg car is pushed by three students from rest to $+5.0 \frac{\text{m}}{\text{s}}$, 30 m along a level surface. What was the unbalanced force used on the car? $\textcircled{2} \quad \vec{F}_{net} = m\vec{a}$

$$\textcircled{1} \quad \vec{v}_f^2 = \vec{v}_0^2 + 2\vec{a}d$$

$$(+5.0)^2 = 0^2 + 2(\vec{a})(+30)$$

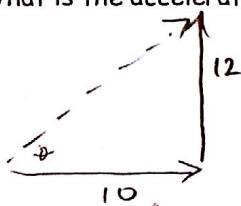
$$\vec{a} = +0.4166 \text{ m/s}^2$$

$$\vec{F}_{net} = (1200)(0.4166) \quad \boxed{\vec{F}_{net} = +500 \text{ N}}$$

- 3.) Assuming the force of friction on the car in problem 2 was 100 N how much combined force did the students have to exert?



- 4.) What is the acceleration of a 5.0 kg mass when pulled with 10 N [E] and 12 N [N]?



$$10^2 + 12^2 = h^2$$

$$\theta \Rightarrow \tan \theta = \frac{12}{10}$$

$$\theta = 50.1944^\circ$$

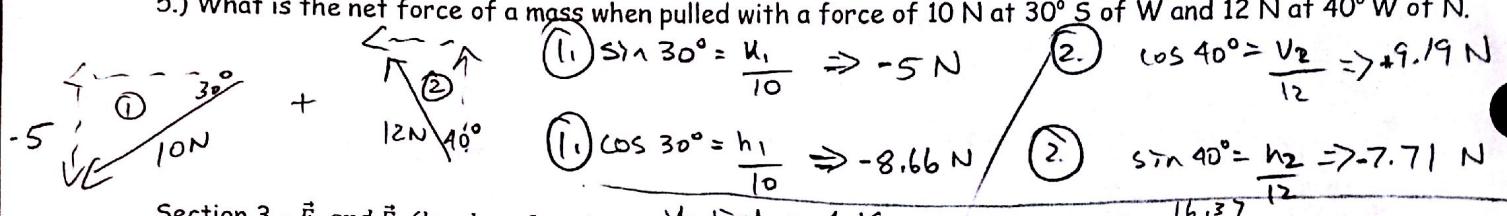
$$\vec{F}_{net} = m\vec{a}$$

$$+15.6 = (5.0)(\vec{a})$$

$$\vec{a} = 3.12 \text{ m/s}^2$$

$$\boxed{3.12 \text{ m/s}^2 \text{ at } 50.2^\circ \text{ N of E}}$$

5.) What is the net force of a mass when pulled with a force of 10 N at 30° S of W and 12 N at 40° W of N.



Section 3 - \vec{F}_f and \vec{F}_n (level surfaces)

1.) A 10 kg mass is pulled along a level surface using a force of 25 N. What is the coefficient of friction?

$$\vec{F}_f = \mu \vec{F}_n$$

$$-25 = \mu (98.1)$$

$$\boxed{\mu = 0.255}$$

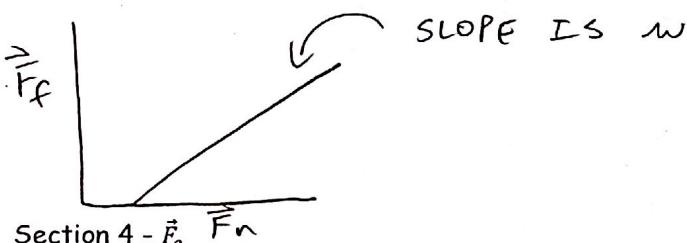
2.) A force of 7.5 N is used to pull a rubber friction block across a table at constant speed. If the coefficient of friction is 0.35 what is the mass of the block?

$$\textcircled{1} \quad \vec{F}_f = \mu \vec{F}_n \quad (-7.5) = (0.35)(\vec{F}_n) \quad \vec{F}_n = +21.42875 \text{ N}$$

$$\textcircled{2} \quad \vec{W} = m \vec{g} \quad -21.42875 = m(-9.81)$$

$$\boxed{m = 2.18 \text{ kg}}$$

3.) What shape is a graph of \vec{F}_f vs. \vec{F}_n and what is the slope?



Section 4 - \vec{F}_e

1.) Calculate the extension of a spring whose spring constant is $20 \frac{N}{m}$ when a 0.50 kg mass is hung on it.

$$\textcircled{1} \quad \vec{F}_e = \vec{W} \quad \vec{W} = m \vec{g} \quad \vec{W} = (0.50)(-9.81) \quad \vec{W} = -4.905$$

$$\textcircled{2} \quad \vec{F}_e = kx \quad 4.905 = (20)(x)$$

$$\boxed{x = 0.245 \text{ m}}$$

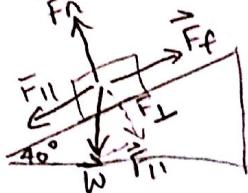
2.) What is the spring constant of a desk if a force of 784 N compresses it from height 1.00 m to 0.92 m?

$$\vec{F}_e = kx \quad 784 = k(0.08)$$

$$\boxed{k = 9800 \frac{N}{m}}$$

Section 5: Forces on Ramps

1.) What is the normal force and force down the ramp on a 5.0 kg mass resting on a 40° slope?



$$\textcircled{2.} \quad \vec{F}_n = \vec{F}_{\perp} \quad / \quad F_{\perp} \Rightarrow \cos 40^\circ = \frac{F_{\perp}}{\vec{W}}$$

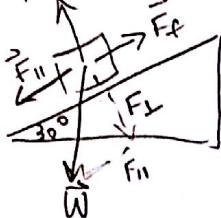
$$\textcircled{1.} \quad \vec{W} = m \vec{g}$$

$$\vec{W} = (5.0)(-9.8)$$

$$\cos 40^\circ = \frac{F_{\perp}}{49.05} \quad \boxed{\vec{F}_{\perp} = +37.6 \text{ N}}$$

$$\textcircled{3.} \quad \vec{F}_{11} \Rightarrow \sin 40^\circ = \frac{\vec{F}_{11}}{49.05} \quad \boxed{\vec{F}_{11} = -31.5 \text{ N}}$$

2.) What is the acceleration of a 3.0 kg mass on a 30° frictionless slope?



$$\textcircled{2.} \quad \vec{F}_{11} \Rightarrow \sin 30^\circ = \frac{\vec{F}_{11}}{-29.43}$$

$$\vec{F}_{11} = -14.715 \text{ N}$$

$$\textcircled{1.} \quad \vec{W} = m \vec{g}$$

$$\vec{W} = (3.0)(-9.8)$$

$$\vec{W} = -29.43 \text{ N}$$

$$\textcircled{3.} \quad \vec{F}_{\text{net}} = m \vec{a} \quad -14.71 = (3.0)(\vec{a}) \quad \boxed{\vec{a} = -4.9 \text{ m/s}^2}$$

3.) What is the normal force on the mass in #2 above?

$$\vec{F}_n = \vec{F}_{\perp}$$

$$\vec{F}_{\perp} \Rightarrow \cos 30^\circ = \frac{\vec{F}_{\perp}}{W}$$

$$\vec{F}_{\perp} \Rightarrow \cos 30^\circ = \frac{\vec{F}_{\perp}}{-29.43}$$

$$\boxed{\vec{F}_{\perp} = +25.5 \text{ N}}$$

4.) What is the force of friction on the mass in #3 above if $\mu = 0.2$?

$$\vec{F}_f = \mu \vec{F}_n \quad \vec{F}_f = (0.2)(25.5)$$

$$\boxed{\vec{F}_f = -5.1 \text{ N}}$$

5.) What would be the acceleration of the mass in #4 above given $\mu = 0.2$??

$$\textcircled{1.} \quad \vec{F}_{\text{net}} = \vec{F}_{11} + \vec{F}_f \quad \vec{F}_{\text{net}} = -14.715 + (-5.1) \quad \vec{F}_{\text{net}} = -19.615 \text{ N}$$

$$\textcircled{2.} \quad \vec{F}_{\text{net}} = m \vec{a} \quad -19.61 = (3.0)(\vec{a})$$

$$\boxed{\vec{a} = -3.21 \text{ m/s}^2}$$

Answers

- | | | | | | | | |
|-----------------------------------|---|--|-----------------------|---------------------------------------|--|--|---------------------------------|
| 1.) -245 N | 2.) $-3.45 \frac{\text{m}}{\text{s}^2}$ | 3.) $+19.6 \text{ N}$, \vec{F}_n | 1.) 0 N | 2.) $+500 \text{ N}$ | 3.) $+600 \text{ N}$ | 4.) $+3.12 \frac{\text{m}}{\text{s}^2}$ at 50° N of E | 5.) 16.9 N at 14° N of W |
| 1.) 0.26 | 2.) 2.19 kg | 3.) linear, μ | 1.) 0.245 m | 2.) $+9800 \frac{\text{N}}{\text{m}}$ | | | |
| 1.) $\vec{F}_n = +37.5 \text{ N}$ | 2.) -31.5 N | 2.) $+4.9 \frac{\text{m}}{\text{s}^2}$ | 3.) $+25.5 \text{ N}$ | 4.) -5.09 N | 5.) $+3.20 \frac{\text{m}}{\text{s}^2}$ at 50° N of E | | |