```
In [ ]:
In [1]: %matplotlib widget
         import pandas as pd
         import networkx as nx
         import numpy as np
         import matplotlib.pyplot as plt
         import analysis as analysis
         from analysis import read pickle, asnp
         from mpl toolkits.mplot3d import Axes3D
         from matplotlib import cm
         import statsmodels.api as sm
         import statsmodels.formula.api as smf
         from statsmodels.stats.anova import anova lm
 In [2]: filename = 'base' #'mod'
         #df = analysis.read pickle('df sayama change all')
         #df = read pickle('df group size10-40 changeall')
         df_full = analysis.read_pickle('df_' + filename)
         print(df full.shape)
         df_full.columns
         df = analysis.data cleanup(df full)
         (21600, 18)
 In [3]: #load SPL on undirected conversion of graph
         filename = 'base' + 'mod'
         dfmod = analysis.read pickle('df ' + filename)
         dfmod.columns
         #load SPL on scc analysis of graph
         filename = 'base' + 'modsc'
         dfsc = analysis.read pickle('df ' + filename)
In [9]: df = df.loc[df['giantComponent'] >= 0.99]
         dfsc = dfsc.loc[df full['giantComponent'] >= 0.99]
In [10]: #mplot3d doesnt handle sympy floats
         stdd = np.asarray(df['std d'].values, dtype = "float")
         stdrs = np.asarray(df['std_rs'].values, dtype = "float")
         stdrw = np.asarray(df['std rw'].values, dtype = "float")
         spl = np.asarray(df['SPL'].values, dtype = "float")
         cd = np.asarray(df['CD'].values, dtype = "float")
         cc = np.asarray(df['giantComponent'].values, dtype = "float")
         sc = np.asarray(dfsc['sc'].values, dtype = "float")
In [11]: analysis.plotfig(stdd, sc, spl, '$d$', 'stdd-sc-spl', fsize=(7,7) )
         #analysis.plotfig(stdrs, cd, spl, '$r s$', 'base-rs')
         #analysis.plotfig(stdrw, cd, spl, '$r w$', 'base-rw')
```

discrepancy in SPL

```
In [119]: fig = plt.figure()
          fig.set size inches (11,13)
          ax = fig.gca(projection='3d')
          alp = 0.2
          #ax.scatter(asnp(dfsc['std_d']), asnp(dfsc['CD']), asnp(dfsc['SPL']),
                    #label='Largest directed strongly connected component', c='g', marker=
          '.', alpha=alp)
          ax.scatter(stdd, cd, spl, label = 'Sayama and Yamanoi', c='r', marker='.',alpha=al
          ax.scatter(asnp(dfmod['std d']), asnp(dfmod['CD']), asnp(dfmod['SPL']),
                    #label='Largest undirected weakly connected component', c='b', marker='x
           ', alpha=alp)
          ax.legend()
          ax.set xlabel("s.d. of $d$")
          ax.set_ylabel("<CD>")
          ax.set zlabel("<SPL>")
          ax.view init(elev=3, azim=305)
          plt.draw()
```

analysis of strongly/weakly connected components

```
In [107]: def ddgroupby(df, labels):
               sdf = pd.DataFrame(df.groupby(labels)[['sc', 'giantComponent']].mean())
               sdf.reset index(inplace=True)
              return sdf
          def plt surf(label, df, sdf):
              plt.close('all')
              fig = plt.figure()
              fig.set size inches(9, 9)
               ax = fig.gca(projection='3d')
               #ax.scatter(asnp(df[label1[0]]), asnp(df[label1[1]]), asnp(df['sc']), marker=
           1.1)
              ax.plot\_trisurf(asnp(sdf[label[0]]), asnp(sdf[label[1]]), asnp(sdf['sc']), label{eq:continuous})
          el='Strongly Connected',
                                cmap=cm.coolwarm, linewidth=0, edgecolor='none')
               ax.plot_trisurf(asnp(sdf[label[0]]), asnp(sdf[label[1]]), asnp(sdf['giantCompo
          nent']),
                               cmap=cm.viridis, linewidth=0, edgecolor='none')
               ax.set xlabel('s.d. of $r w$')
               ax.set ylabel('s.d. of $r s$')
               ax.set zlabel('Component Size')
              plt.draw()
```

```
In [45]: def cum_components(dfsc):
             x = []
             sc = []
             gc_ = []
             for i in np.linspace(0, 1.0, 21):
                 cum = 1 - i
                 con = dfsc['sc'] >= cum
                 con2 = dfsc['giantComponent'] >= cum
                 x.append(cum)
                 sc .append(dfsc.loc[con].shape[0])
                 gc .append(dfsc.loc[con2].shape[0])
             for i in np.linspace(0,0.15,15):
                 cum = 1 - i
                 con = dfsc['sc'] >= cum
                 con2 = dfsc['giantComponent'] >= cum
                 x.append(cum)
                 sc .append(dfsc.loc[con].shape[0])
                 gc .append(dfsc.loc[con2].shape[0])
             return x, sc_, gc_
In [12]: dfca = read pickle('df sayama change allmodsc')
         \#x, sc_{,} gc_{,} = cum_{,} components (dfca)
In [48]: plt.close('all')
         fig = plt.figure()
         ax = fig.add subplot(111)
         ax.scatter(x,sc_, label = 'Strongly Connected',color='g')
         ax.scatter(x,gc_, label='Weakly Connected', color='b', marker ='x')
         ax.legend()
         ax.set ylabel('Number of Experiments')
         ax.set xlabel('Relative size of Largest Component')
         plt.draw()
In [ ]:
```

Start with 0.8 as minimum gc size. Filter df:

```
In [108]: #df's are df, dfmod (undir SPL), dfsc, dfca(changeall)
    label1 = ['std_rw', 'std_rs']
    label2 = ['std_d', 'std_rw']
    label3 = ['std_d', 'std_rs']
    labels = label1

sdf = ddgroupby(dfca, labels)
    plt_surf(labels, df, sdf)
```

linreg

```
In [112]: res = smf.ols(formula='sc ~ (std_d + std_rs + std_rw)**2', data=dfsc).fit()
           print(str(res.summary()))
                                  OLS Regression Results
          ______
                                               sc R-squared:
          Dep. Variable:
                                                                                        0.700
                                              OLS Adj. R-squared:
                                                                                        0.700
                             Least Squares F-statistic:
          Method:
                                                                                        8388.
                               Mon, 20 Jul 2020 Prob (F-statistic):
                                                                                        0.00
                                                                                   37033.
          Date:
                                                                                 37033.
-7.405e+04
                                       21:53:39 Log-Likelihood:
                                           21600 AIC:
          No. Observations:
          Df Residuals:
                                           21593 BIC:
                                                                                   -7.400e+04
          Df Model:
                                             6
          Covariance Type: nonrobust
          ______
                              coef std err t P>|t| [0.025 0.97
          Intercept 1.0365 0.001 759.174 0.000 1.034 1.03
          std d -0.3997 0.004 -100.137 0.000 -0.408 -0.39
                          -0.0061 0.004 -1.530 0.126 -0.014
          std rs
                                                                                           0.00
                           -0.0172 0.004 -4.298 0.000
                                                                             -0.025
                                                                                          -0.00
          std_d:std_rs -0.1080 0.010 -10.623 0.000
                                                                            -0.128
                                                                                          -0.08
          std_d:std_rw 0.1630 0.010 16.038 0.000
                                                                              0.143
                                                                                          0.18
          std_rs:std_rw 0.0068 0.010 0.670 0.503 -0.013
          ______
                                         5927.231 Durbin-Watson:
                                         0.000 Jarque-Bera (JB):
                                                                                   38082.159
          Prob(Omnibus):
          Skew:
                                           -1.163 Prob(JB):
                                                                                     0.00
          Kurtosis:
                                            9.075 Cond. No.
                                                                                         42.4
          _____
          [1] Standard Errors assume that the covariance matrix of the errors is correctly
          specified.
In [110]: print(str(anova lm(res)))

        df
        sum_sq
        mean_sq
        F
        PR(>F)

        std_d
        1.0
        93.831200
        93.831200
        49415.864717
        0.000000e+00

        std_rs
        1.0
        0.621218
        0.621218
        327.162022
        1.370843e-72

        std_rw
        1.0
        0.403358
        0.403358
        212.426995
        6.853623e-48

        std_d:std_rs
        1.0
        0.214294
        0.214294
        112.856957
        2.693272e-26

        std_d:std_rw
        1.0
        0.488377
        0.488377
        257.201753
        1.503337e-57

        std_rs:std_rw
        1.0
        0.000852
        0.000852
        0.448904
        5.028630e-01

        Residual
        21593.0
        41.000944
        0.001899
        NaN
```

how much does sc explain SPL?

Residual 21593.0 41.000944 0.001899

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NaN

NaN

```
In [113]: df['sc'] = dfsc['sc']
                  df.columns
Out[113]: Index(['degrees', 'clusterCoeff', 'reciprocity', 'center_1', 'center_2',
                                'mean_centers', 'overall_mean_culture', 'giantComponent', 'diam', 'SPL',
                                'CD', 'c1_init', 'c2_init', 'c_avg_init', 'std_d', 'std_rs', 'std_rw',
                                'tags', 'comps', 'sc'],
                              dtype='object')
In [122]: res = smf.ols(formula='SPL ~ (sc + CD) ** 2', data=dfsc).fit()
                   print(str(res.summary()))
                                                      OLS Regression Results
                  ______
                  Dep. Variable: SPL R-squared:
                                                                                                                                                        0.388
                 Model:

Model:

Date:

Mon, 20 Jul 2020

Time:

Mondel:

                                                                                                                                                         0.388
                                                                                                                                                        4561.
                                                                                                                                            0.00
16000.
-3.199e+04
                                                       22:09:41 Log-Likelihood:
                 Time:
                 No. Observations:
                                                                          21600 AIC:
                                                                        21596 BIC:
3
                 Df Residuals:
                                                                                                                                                -3.196e+04
                 Df Model:
                  Di Model: 3
Covariance Type: nonrobust
                  ______
                                                coef std err t P>|t| [0.025 0.975]
                 Intercept 2.1451 0.117 18.387 0.000 1.916 2.374 sc 0.0675 0.118 0.574 0.566 -0.163 0.298 CD 0.3514 0.040 8.776 0.000 0.273 0.430 sc:CD -0.2545 0.040 -6.290 0.000 -0.334 -0.175
                  ______
                  Omnibus:
                                                                     3506.301 Durbin-Watson:
                                                                                                                                                       1.899
                                                                         0.000 Jarque-Bera (JB):
                                                                                                                                               19684.744
                  Prob(Omnibus):
                  Skew:
                                                                            0.666 Prob(JB):
                                                                                                                                                     0.00
                                                                                                                                                           881.
                  Kurtosis:
                                                                            7.483 Cond. No.
                  ______
                  [1] Standard Errors assume that the covariance matrix of the errors is correctly
                  specified.
 In [71]: plt.close('all')
                  fig = plt.figure()
                  fig.set size inches(9, 9)
                  ax = fig.gca(projection='3d')
                  ax.scatter(asnp(dfsc['SPL']), asnp(dfsc['std d']), asnp(dfsc['sc']), marker='.')
                  ax.scatter(asnp(dfsc['SPL']), asnp(dfsc['std d']), asnp(dfsc['giantComponent']), ma
                  rker='.', color='r')
                  ax.set ylabel('s.d. of d')
                  ax.set xlabel('<SPL>')
                  ax.set zlabel('Size of largest Strongly Connected Component')
                  plt.draw()
   In [ ]: #
```

linear relation between splsc and splgc?

```
In [94]: | dtemp = dfmod['SPL']
         dtemp.name = "SPLweak"
         dtemp2 = dfsc['SPL']
         dtemp2.name = "SPLstrong"
         dfspl = pd.concat([dtemp, dtemp2], axis=1)
         dfspl.head()
```

Out[94]:

	SPLweak	SPLstrong
0	1.974694	2.463265
1	1.951837	2.430204
2	2.040000	2.560816
3	1.937143	2.337143
4	1.932245	2.351429

```
In [95]: res = smf.ols(formula='SPLstrong ~ SPLweak', data=dfspl).fit()
         print(str(res.summary()))
```

OLS Regression Results

Dep. Variable:	SPLstrong	R-squared:	0.798
Model:	OLS	Adj. R-squared:	0.798
Method:	Least Squares	F-statistic:	8.514e+04
Date:	Mon, 20 Jul 2020	<pre>Prob (F-statistic):</pre>	0.00
Time:	21:32:56	Log-Likelihood:	27956.
No. Observations:	21600	AIC:	-5.591e+04
Df Residuals:	21598	BIC:	-5.589e+04
Df Model:	1		
a ' ==			

Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]		
Intercept SPLweak	-0.2541 1.3652	0.009	-26.756 291.795	0.000	-0.273 1.356	-0.235 1.374		
Omnibus: Prob(Omnibus) Skew: Kurtosis:	· :	C - C	0.000 Jaro 0.393 Prok	pin-Watson: que-Bera (JB) p(JB):	:	1.887 255132.610 0.00 53.1		

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

analysis with 0.8 of graph as scc

```
In [128]: | dfred = dfsc.loc[dfsc['sc'] >= 0.8]
          dfred.shape
Out[128]: (20259, 20)
In [134]: analysis.plotfig(asnp(dfred['std rw']), asnp(dfred['CD']), asnp(dfred['SPL']), '$r
          _w$')
```

```
In [130]: import linReg
linReg.fit_model(dfred, 'reduced-base-linreg')
In [131]: linReg.fit_model(df, 'sayama-base')
```

analyze experiment where we change all parameters.

• 0.8 cutoff for scc

```
In [137]: res = smf.ols(formula='sc ~ (std_d + std_rs + std_rw)**2', data=dfcaR).fit()
      print(str(res.summary()))
                   OLS Regression Results
      ______
      Dep. Variable:
                          sc R-squared:
                OLS Adj. R-squared:
Least Squares F-statistic:
      Model:
                                                  0.622
     Method:
                                                  4305.
     Date:
                 Mon, 20 Jul 2020 Prob (F-statistic):
                                                  0.00
                                               29496.
                                              0.00
29496.
-5.898e+04
                      22:29:17 Log-Likelihood:
     No. Observations:
                        15687 AIC:
      Df Residuals:
                        15680 BIC:
                                               -5.892e+04
      Df Model:
                          6
      Covariance Type: nonrobust
      ______
                 coef std err t P>|t| [0.025 0.97
      Intercept 1.0237 0.001 805.053 0.000 1.021 1.02
      std d -0.3050 0.005 -63.511 0.000 -0.314 -0.29
               -0.0087 0.004 -2.299 0.022 -0.016
                                                  -0.00
      std rs
               -0.0046 0.004 -1.207 0.227
                                           -0.012
                                                   0.00
      std_d:std_rs -0.1346 0.013 -10.762 0.000
                                           -0.159
                                                   -0.11
      std_d:std_rw 0.0034 0.012 0.277 0.782
                                           -0.021
                                                   0.02
      std_rs:std_rw -0.0314 0.010 -3.086 0.002 -0.051 -0.01
      ______
                       829.822 Durbin-Watson:
                       0.000 Jarque-Bera (JB):
                                               1020.324
      Prob(Omnibus):
      Skew:
                        -0.544 Prob(JB):
                                               2.75e-222
      Kurtosis:
                         3.613 Cond. No.
                                                49.4
      _____
```

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

how much does spl weak correlate with spl strong?

```
In [141]: dtemp = camodR['SPL']
        dtemp.name = "SPLweak"
         dtemp2 = dfcaR['SPL']
         dtemp2.name = "SPLstrong"
         dfspl = pd.concat([dtemp, dtemp2], axis=1)
         dfspl.head()
Out[141]:
           SPLweak SPLstrong
         0 1.951020
                  2.432653
         1 1.906122
                  2.347755
         2 1.906939
                  2.315918
         3 1.931429
                  2.431837
         4 1.989388
                  2.409796
In [142]: | res = smf.ols(formula='SPLstrong ~ SPLweak', data=dfspl).fit()
        print(str(res.summary()))
                                OLS Regression Results
        ______
        Dep. Variable:
                               SPLstrong R-squared:
                                    OLS Adj. R-squared:
        Model:
                                                                       0.848
        Method:
Date:
                            Least Squares F-statistic:
                                                                   8.733e+04
                         Mon, 20 Jul 2020 Prob (F-statistic):
                                                                        0.00
                                22:34:29 Log-Likelihood:
        Time:
                                                                      13139.
        No. Observations:
                                    15687 AIC:
                                                                   -2.627e+04
        Df Residuals:
                                    15685 BIC:
                                                                   -2.626e+04
        Df Model:
                                       1
        Covariance Type: nonrobust
```

	coef	std err	t	P> t	[0.025	0.975]
	-0.6226 1.5513	0.011 0.005	-56.629 295.524	0.000	-0.644 1.541	-0.601 1.562
Omnibus: Prob(Omnibus): Skew: Kurtosis:		1.	000 Jarq 720 Prob	in-Watson: ue-Bera (JB): (JB): . No.		1.960 163281.140 0.00 33.8

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In []:
```

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