

# Math 170 Sections 5.1-5.2 Study Guide

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## 1 Section 5.1

**Problem 1)** Graph the following system of linear inequalities. Then, determine all the corner points.

$$3x + 2y \geq 6$$

$$3x - 2y \leq 6$$

$$x \geq 0$$

**Problem 2)** Graph the following system of linear inequalities. Then, determine all the corner points.

$$2x + 4y \geq 12$$

$$x \leq 5$$

$$y \leq 3$$

$$x \geq 0$$

$$y \geq 0$$

**Problem 3)** Graph the following system of linear inequalities. Then, determine all the corner points.

$$30x + 20y \leq 600$$

$$10x + 40y \leq 400$$

$$20x + 30y \leq 450$$

$$x \geq 0$$

$$y \geq 0$$

**Problem 4)** A college's math department offers two courses: Finite Math and Applied Calculus. Each section of Finite Math has 60 students, and each section of Applied Calculus has 50 students. The department is allowed to offer a total of up to 110 sections between the two classes. Furthermore, no more than 6000 students may take a math course. Set up the system of inequalities and draw the feasible region (solution set). Then identify the corner points.

## 2 Section 5.2

**Problem 5)** Consider the following linear program:

$$\begin{aligned} \max \quad & x + y \text{ s.t.} \\ & x + 2y \leq 9 \\ & 2x + y \leq 9 \\ & x \geq 0 \\ & y \geq 0 \end{aligned}$$

In order to solve the linear program, you need to do the following.

- (a) Graph the inequalities and identify the feasible region.
- (b) Determine the corner points.
- (c) Plug the corner points into the objective function (the function you are trying to maximize/minimize; here, that is  $x + y$ ).
- (d) Which of the corner points maximizes  $x + y$ ? What is the maximum value  $x + y$  obtains in the feasible region?

**Problem 6)** Solve the following linear program. That is, go through steps (a)-(d) outlined in Problem 5.

$$\begin{aligned} \max \quad & x + 2y \text{ s.t.} \\ & x + 3y \leq 24 \\ & 2x + y \leq 18 \\ & x \geq 0 \\ & y \geq 0 \end{aligned}$$

**Problem 7)** Solve the following linear program. That is, go through steps (a)-(d) outlined in Problem 5.

$$\begin{aligned} \min \quad & 3x + y \text{ s.t.} \\ & 10x + 20y \geq 100 \\ & 0.3x + 0.1y \geq 1 \\ & x \geq 0 \\ & y \geq 0 \end{aligned}$$

**Problem 8)** You manage an ice cream factory that produces two flavors: Creamy Vanilla and Continental Mocha. Into each quart of Creamy Vanilla goes 2 eggs and 3 cups of cream. Into each quart of Continental Mocha goes 1 egg and 3 cups of cream. You have in stock 500 eggs and 900 cups of cream. You make a profit of 3 on each quart of Creamy Vanilla and 2 on each quart of Continental Mocha. How many quarts of each flavor should you make in order to maximize profit?