### Homework #6

Dongkyu Kim(20162050)

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# Benchmark with results for the general Poisson equation

Analytic results:  $\vec{E_s}|_x = \sqrt{\frac{2K_bTN_a^-}{\epsilon_{\text{silicon}}}} \left\{ \left( e^{-\frac{q_0\phi_d}{K_bT}} + \frac{q_0\phi_d}{K_bT} - 1 \right) + \left( \frac{n_i}{N_a^-} \right)^2 \left( e^{\frac{q_0\phi_d}{K_bT}} - \frac{q_0\phi_d}{K_bT} - 1 \right) \right\}^{\frac{1}{2}}$  where  $\phi_d = \phi_s - \phi_N$ ,  $\phi_s$  is the external potential at the oxide surface and  $\phi_N$  is the potential at the silicon juction with satisfying the charge neutrality condition.

Numerical results:  $-\nabla \phi|_x \simeq -\frac{\phi_2 - \phi_1}{x_2 - x_1}$ , where  $\phi_1 = \phi_s$ .

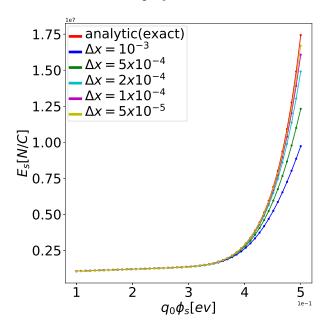


Figure 1: Comparison between the analytic results and numerical results for the general Poisson equation in the metal oxide silicon(MOS) structure

## Results for the Eigensolver embedded with the potential $\phi(x)$

#### case1.

 $T_{\rm si} = 1 \mu m, \, \phi_s = 10^{-2} {\rm ev}, \, \phi_N = -0.287 {\rm ev}, \, N_a^- = 10^{15} {\rm cm}^{-3}, \, \Delta x = 10^{-3} \mu m$ 

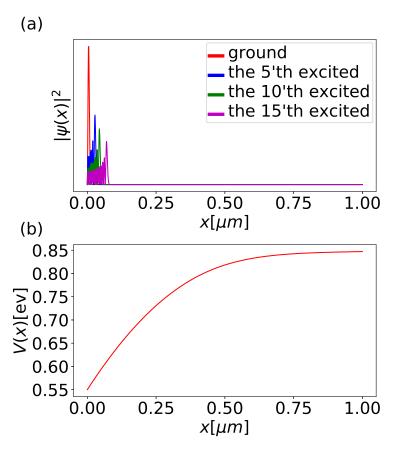


Figure 2: The wave funtions and the given potential V(x) where  $V(x) = -q\phi(x) + E_c - E_i$ 

#### case 2.

 $T_{\rm si} = 1 \mu m, \, \phi_s = -0.28 {\rm ev}, \, \phi_N = -0.287 {\rm ev}, \, N_a^- = 10^{15} {\rm cm}^{-3}, \, \Delta x = 10^{-3} \mu m$ 

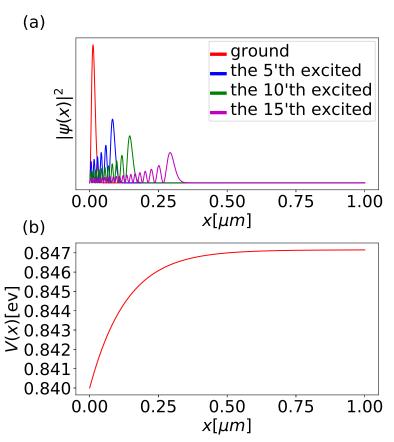


Figure 3: The wave funtions and the given potential V(x) where  $V(x)=-q\phi(x)+E_c-E_i$