

DEPT. _____ CLASS _____ DIV _____ ROLL NO. _____ DATE _____
SUBJECT _____

Questions	1	2	3	4	5	6	7	8	Total
Marks obtained									

Examiner

Unit - III

Content Free Grammar

List of Problems for Practice

Q. ①

Defⁿ

- ① CFG
- ② Ambiguous Grammar
- ③ Unambiguous Grammar

eg. 1

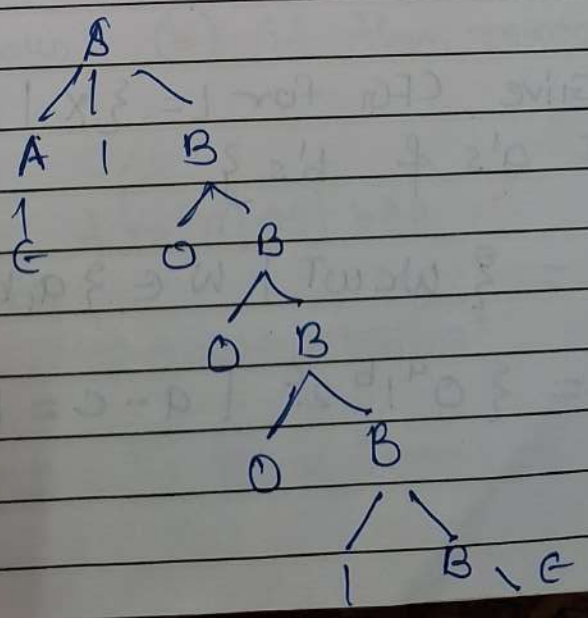
Give Left Most Derivation, Rightmost Derivation and parse tree for following grammars.

④ $S \rightarrow A1B$, $A \rightarrow 0A \mid \epsilon$ $B \rightarrow 0B \mid 1B \mid \epsilon$
LMD RMD "1001"

⑤

$S \rightarrow A1B$	$S \rightarrow A1B$
$\Rightarrow \epsilon 1 B$	$\Rightarrow A10B$
$\Rightarrow \epsilon 10B$	$\Rightarrow A100B$
$\Rightarrow \epsilon 100B$	$\Rightarrow A1001B$
$\Rightarrow \epsilon 1001B$	$\Rightarrow A1001\epsilon$
$\Rightarrow 1001\epsilon$	$\Rightarrow \epsilon 1001$
$\Rightarrow 1001$	$\Rightarrow 1001$

Parse Tree



② $S \rightarrow XY, Y \rightarrow XY | b \quad X \rightarrow YY | a$
 "aabb²b"

③ $E \rightarrow E+T | T$
 $T \rightarrow T \times F | F$
 $F \rightarrow (E) | a | b$ " (a+b) * a+b "

Q.2 Give CFG for following lang.

① $L = \{ a^i b^j, i \leq j \leq 2i, i \geq 1 \}$

② $0(0+1)^*01(0+1)^*1$

③ $(0+1)^* (1+(0+1)^*)$

④ $L = \{ a^i b^j c^q; i+j=q, i, j \geq 1 \}$

⑤ $L = \{ a^i b^j c^k \mid i \neq j+k \}$

⑥ $L = \{ a^i b^j c^k \mid i=j \text{ or } j \leq k \}$

⑦ $L = \{ 0^i 1^j 0^k \mid j > i+k \}$

⑧ Give CFG for matching parenthesis

⑨ CFG for $L = \{ a^n b^m c^n \mid m, n \geq 1 \}$

⑩ Give CFG for $L = \{ x \mid x \text{ contains equal no. of } a's \text{ \& } b's \}$

⑪ $L = \{ w c w^T \mid w \in \{ a, b \}^* \}$

⑫ $L = \{ 0^a 1^b 2^c \mid a-c=b \}$

3* Show grammar is ambiguous

$$\textcircled{1} \quad E \rightarrow E+E \mid E * E \mid (E) \mid \epsilon \\ I \rightarrow a \mid b$$

(a) Show Grammar is ambiguous

(b) Remove Ambiguity

② Give ambiguous grammar for "if-then-else" statement & rewrite unambiguous grammar for it.

$$\textcircled{3} \quad S \rightarrow SS \mid (S) \mid \epsilon$$

(a) Show ambiguous (b) Remove Ambiguity

④ Is it ambiguous?

$$S \rightarrow aB \mid ab \quad A \rightarrow aAB \mid a, \quad B \rightarrow ABb \mid b$$

$$\textcircled{5} \quad \left. \begin{array}{l} S \rightarrow aAS \mid a \\ A \rightarrow SbA \mid SS \mid ba \end{array} \right\} \text{Is ambiguous?}$$

$$\textcircled{6} \quad S \rightarrow as \mid \epsilon \quad S \rightarrow asbs$$

(a) is ambiguous (b) if then remove ambiguity

$$\textcircled{7} \quad \begin{array}{l} S \rightarrow aB \mid bA \quad A \rightarrow a \mid as \mid bAA \\ B \rightarrow b \mid bS \mid aBB \end{array}$$

For string "aaabbabbba" find

(a) LMD (b) RMD (c) Parse Tree (d) is it ambiguous.

$$(8) \quad S \rightarrow SS \mid a \mid b$$

$$(9) \quad S \rightarrow ABA \mid A \rightarrow aA \mid \epsilon \quad B \rightarrow bB \mid \epsilon$$

$$(10) \quad S \rightarrow aSb \mid aaSb \mid \epsilon$$

$$(11) \quad G = (V = \{E, F\}, T = \{a, b, -\}, E, P)$$

$$P \text{ is } E \rightarrow F, E \rightarrow F-E, F \rightarrow a, E \rightarrow E-F, F \rightarrow b$$

(a) is it Ambiguous

(b) Remove Ambiguity

Q.4 Simplify the grammar

(1) Find Non-generating symbols in the grammar

$$S \rightarrow AB \mid CA$$

$$A \rightarrow a$$

$$B \rightarrow BC \mid AB$$

$$C \rightarrow AB \mid b$$

(2) Find Non-reachable Symbols

$$S \rightarrow aBa \mid BC$$

$$A \rightarrow aC \mid BCC$$

$$C \rightarrow a$$

$$B \rightarrow bCC, D \rightarrow E, E \rightarrow d$$

(3) Simplify the following grammar

$$S \rightarrow ASB \mid \epsilon$$

$$A \rightarrow aAS \mid \epsilon$$

$$B \rightarrow SbS \mid A \mid bb$$

②

$$S \rightarrow 0A0 \mid 1B1 \mid BB$$

$$A \rightarrow C$$

$$B \rightarrow S \mid A$$

$$C \rightarrow S \mid e$$

⑧

$$S \rightarrow Ab, A \rightarrow a, B \rightarrow C \mid b, C \rightarrow D, D \rightarrow E, E \rightarrow a$$

2.5

convert to chomsky Normal Form (CNF)

①

$$S \rightarrow aAbB \quad A \rightarrow aA \mid b \quad B \rightarrow bB \mid b$$

②

$$S \rightarrow PQQ \quad P \rightarrow OP \mid e \quad Q \rightarrow IQ \mid e$$

③

$$S \rightarrow bA \mid ab \quad A \rightarrow bAA \mid as \mid a \quad B \rightarrow aBB \mid bs \mid b$$

④

$$S \rightarrow Aba, S \rightarrow aab, B \rightarrow \cancel{A}Ac$$

.6.

convert to Greibach Normal Form (GNF)

①

$$S \rightarrow AA \mid a \quad A \rightarrow SS \mid b$$

②

$$E \rightarrow E+T \mid T$$

$$T \rightarrow T \times F \mid F$$

$$F \rightarrow a$$

③

$$S \rightarrow AB, A \rightarrow Bs \mid b \quad B \rightarrow SA \mid b$$

④

$$A_1 \rightarrow A_2A_3, A_2 \rightarrow A_3A_1 \mid b, A_3 \rightarrow A_1A_2 \mid a$$

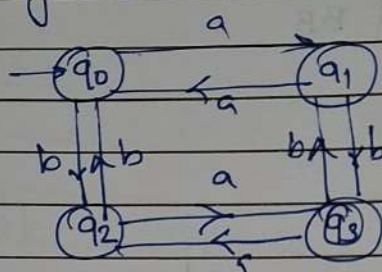
Q.7

Write short note on
Chomsky classification or Hierarchy.

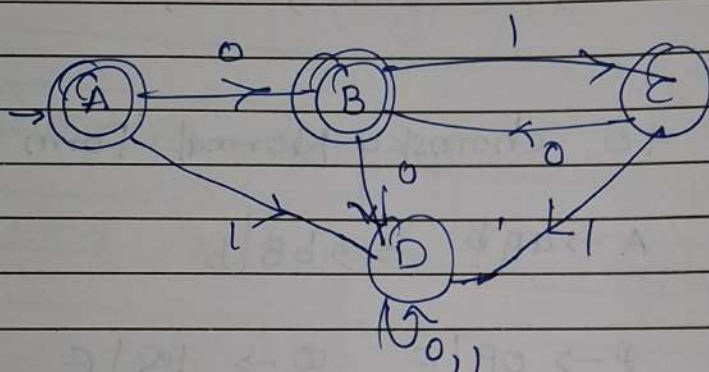
Q.8

Convert following

① Give Right Linear Grammar (RLG) for DFA



②



Q.9

convert RLG to DFA

③

$S \rightarrow bB$ $B \rightarrow bC$ $B \rightarrow aB$ $C \rightarrow a$ $B \rightarrow b$

④

$S \rightarrow 0A \mid 1B$

$A \rightarrow 0C \mid 1A \mid 0$

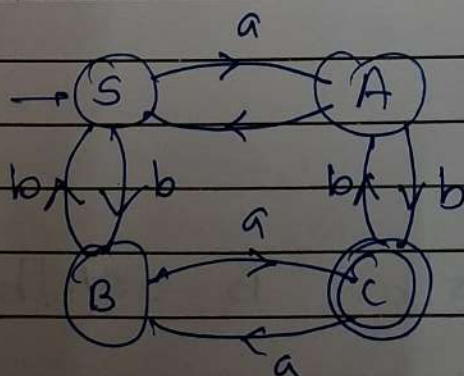
$B \rightarrow 1B \mid 1A \mid 1$

$C \rightarrow 0 \mid 0A$

Q.10

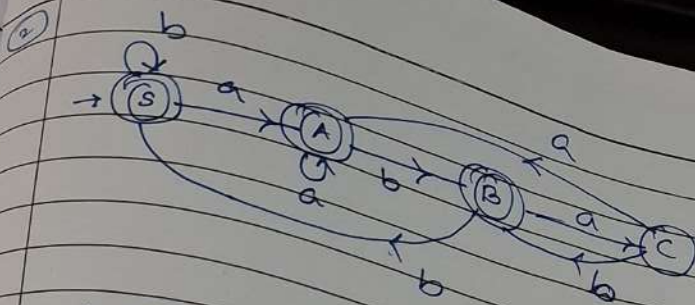
Convert DFA to LLG

①



Hierarchy

RLG) for DFA



LLG to DFA

① $S \rightarrow \epsilon \mid A \mid Bb$, $C \rightarrow Bb$, $B \rightarrow Ba \mid b$

② $S \rightarrow B \mid A \mid C$, $C \rightarrow A$, $B \rightarrow \epsilon \mid B \mid 1$, $A \rightarrow A \mid B \mid C \mid 0$

Q.12 RLG to LLG

① $S \rightarrow bB \mid b$, $B \rightarrow bC \mid aB \mid b$, $C \rightarrow a$

② $S \rightarrow 0A \mid 1B$, $A \rightarrow 0C \mid 1A \mid 0$, $B \rightarrow 1B \mid 1A \mid 1$, $C \rightarrow 0 \mid 0A$

$B \rightarrow b$

Q.13 LLG to RLG

$S \rightarrow C \mid A \mid B$

$A \rightarrow A \mid C \mid B \mid 0$

$B \rightarrow B \mid 1$, $C \rightarrow A$

Q.14

Write short not on.

CFL closed under ① Union ②

③ concatenation ④ Kleene star