$$S = (a_x + b_x)(a_y + b_y) - (a_x a_y + b_x b_y + a_y b_x + a_y b_x)$$

$$S = a_x a_y + a_x b_y + a_y b_x + b_x b_y - a_x a_y - b_x b_y - 2a_y b_x$$

$$S = a_x b_y - a_y b_x$$

$$a_y b_x$$

$$\frac{1}{2} a_x a_y$$

$$S = det \begin{bmatrix} a_x & b_x \\ a_y & b_y \end{bmatrix}$$

$$A = \begin{bmatrix} a & b \end{bmatrix}$$

$$S = det \begin{bmatrix} a_x & b_x \\ a_y & b_y \end{bmatrix}$$

$$S = det \begin{bmatrix} a_x & b_x \\ a_y & b_y \end{bmatrix}$$

$$a_x + b_x$$