# 카메라Camera와 투영Projection

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# 간단한 OpenGL 코드를 만들어 보자

```
from OpenGL.GL import *
from OpenGL.GLU import *
from PyQt6.QtWidgets import QApplication, QWidget
from PyQt6.QtOpenGLWidgets import QOpenGLWidget
import sys
def drawAxes():
    glBegin(GL_LINES)
    # x축 (0,0,0) - (1,0,0)
    glColor(1, 0, 0) # 빨간색
    glVertex3f(0,0,0)
    glVertex3f(1,0,0)
    # v축
    glColor(0, 1, 0) # 녹색
    glVertex3f(0,0,0)
    glVertex3f(0,1,0)
    # z축
    glColor(0, 0, 1) # 파란색
    glVertex3f(0,0,0)
    glVertex3f(0,0,1)
```

glEnd()



OpenGL 프리미티브를 이용하여 x, y, z 축을 그리는 함수

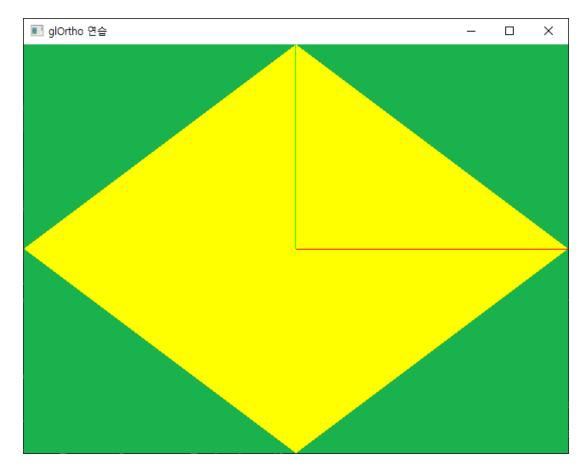
# OpenGL 윈도우 클래스의 구현

```
class MyGLWindow(QOpenGLWidget) : # QOpenGLWidget 상속
    def __init__(self):
        super().__init__() # 슈퍼클래스 QMainWindow 생성자 실행
        self.setWindowTitle('glOrtho 연습')
    def initializeGL(self) :
        glClearColor(0.1, 0.7, 0.3, 1.0)
    def resizeGL(self, w: int, h: int) :
        glMatrixMode(GL PROJECTION)
       glLoadIdentity()
    def paintGL(self):
        glClear(GL COLOR BUFFER BIT | GL DEPTH BUFFER BIT)
        glBegin(GL POLYGON)
        glColor3f(1, 1, 0)
        glVertex3f(1, 0, 0)
       glVertex3f(0, 1, 0)
        glVertex3f(-1, 0, 0)
       glVertex3f( 0, -1, 0)
        glEnd()
       drawAxes()
```

# 윈도우 생성 및 OpenGL 위짓 포함

```
def main(argv = sys.argv) :
## 윈도우 생성하기
app = QApplication(argv)
window = MyGLWindow()
window.show()
app.exec()

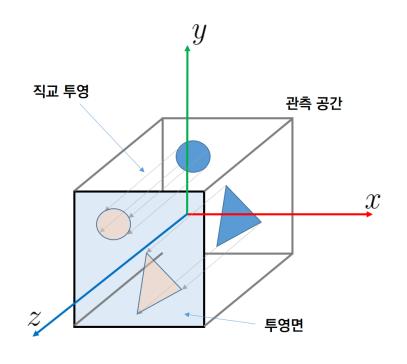
if __name__ == '__main__':
main(sys.argv)
```

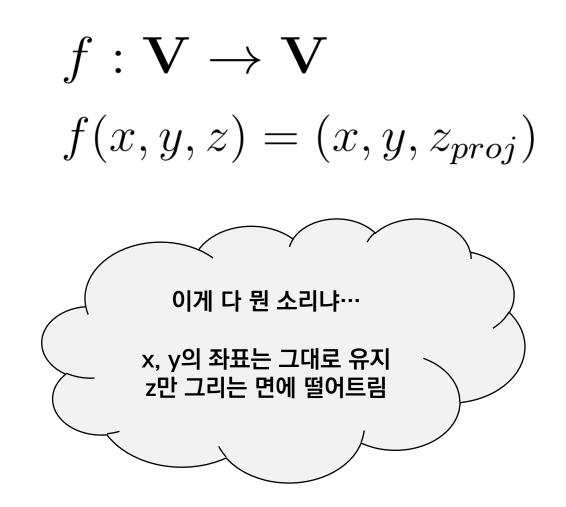


왜 이런 장면을 보게 된 것일까?

### 카메라 모델

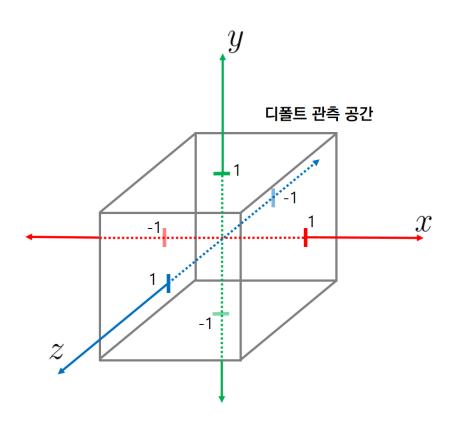
• 직교 투영 공간



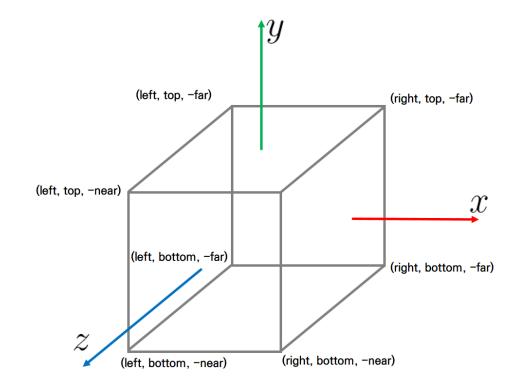


# 카메라 모델

• 디폴트 직교 투영 공간과 변경



glOrtho(left, right, bottom, top, near, far)



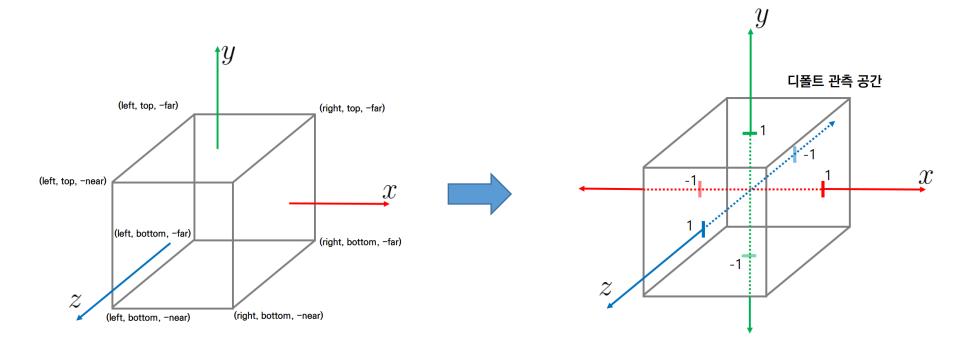
### 화면에 그리기 위해 좌표는 어떻게 바뀌나

- 정규 관측 공간으로 옮기기
  - 정규 관측 공간
    - x, y, z 축 방향으로 [-1, 1] 사이의 공간
  - 좌표를 정규 관측 공간으로 옮긴다는 것 →

 $x : [left, right] \Rightarrow x' : [-1, 1]$ 

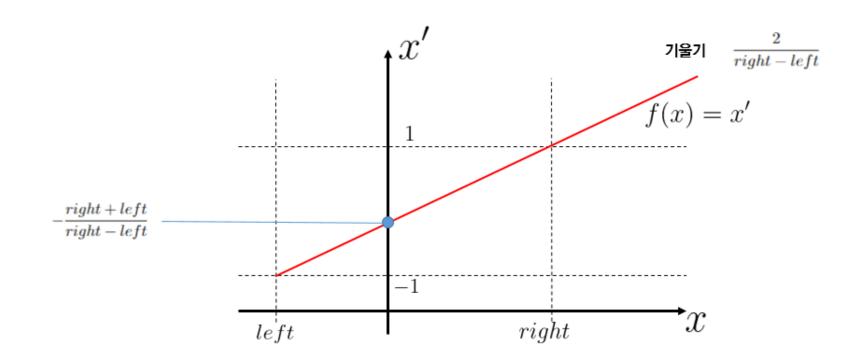
y: [bottom, top]  $\Rightarrow y'$ : [-1, 1]

z: [near, far]  $\Rightarrow z'$ : [-1, 1]



#### X 좌표를 바꾸어 보자

- left에 해당하는 값은 -1, right에 해당하는 값은 1
- right-left의 간격은 길이 2의 간격으로 변환



#### X 좌표를 바꾸어 보자

- left에 해당하는 값은 -1, right에 해당하는 값은 1
- right-left의 간격은 길이 2의 간격으로 변환

$$x' = f(x) = \left(\frac{2}{right - left}\right)x - \frac{right + left}{right - left}$$

# x,y,z 좌표를 바꾸어 보자

$$x' = f(x) = \left(\frac{2}{right - left}\right)x - \frac{right + left}{right - left}$$

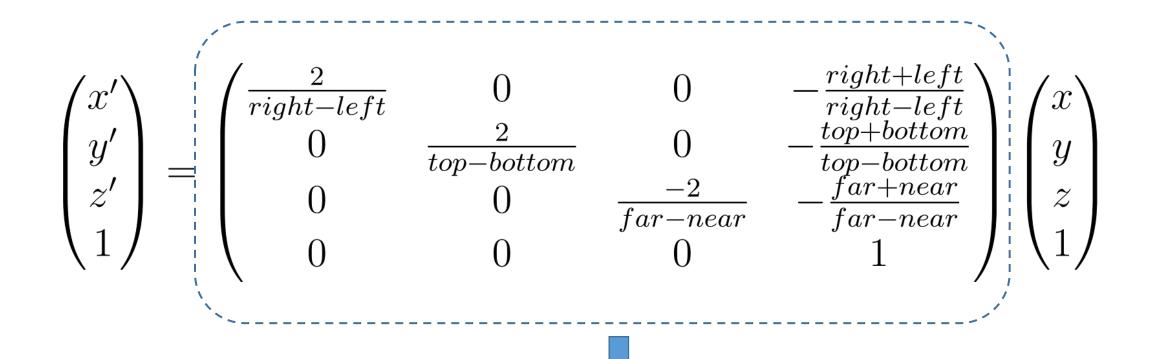
$$y' = \left(\frac{2}{top - bottom}\right)y - \frac{top + bottom}{top - bottom}$$

$$z' = -\left(\frac{2}{far - near}\right)z - \frac{far + near}{far - near}$$



부호 바뀜 주의

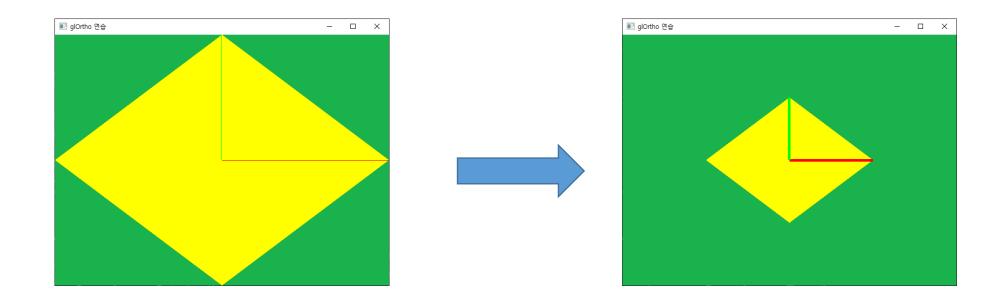
# 직교 투영 = 선형 변환 행렬을 적용하는 것



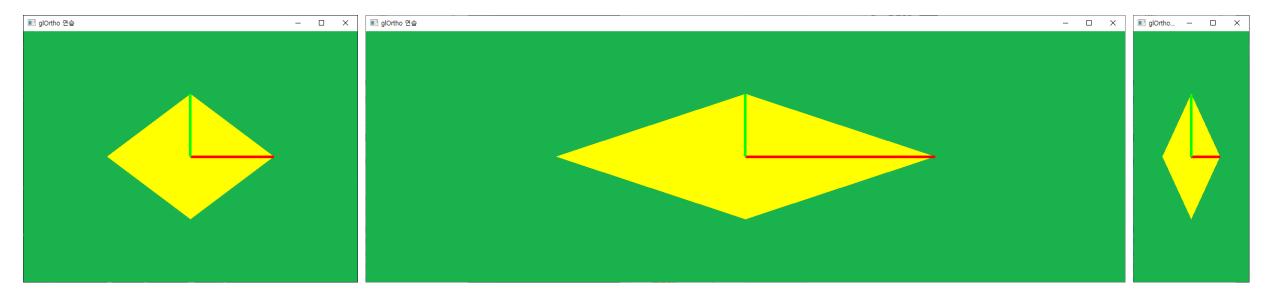
투영행렬: 모든 점들은 이 행렬이 곱해져서 최종 좌표가 결정된다

# glOrtho 사용하기

```
def resizeGL(self, w: int, h: int) :
    glMatrixMode(GL_PROJECTION)
    glLoadIdentity()
    glOrtho(-2, 2, -2, 2, -1, 1)
```



# 문제점



#### 왜곡이 없는 투영

• 화면의 크기에 맞춰 투영행렬 설정

```
def resizeGL(self, w: int, h: int) :

aspRatio = w / h # 종횡비를 계산한다.
range = 2
glMatrixMode(GL_PROJECTION)
glLoadIdentity()
glOrtho(-range*aspRatio, range*aspRatio, -range, range, range)
```



# 투영의 관찰을 위한 두 개의 OpenGL 위짓

• OpenGL 위짓 클래스 정의

```
from OpenGL.GL import *
from OpenGL.GLU import *
import sys
from PyQt6.QtWidgets import *
from PyQt6.QtOpenGLWidgets import QOpenGLWidget
class MyGLWidget(QOpenGLWidget):
    def __init__(self, parent=None, observation = False):
        super(). init_(parent)
        self.observation = observation
    def initializeGL(self):
        pass
    def resizeGL(self, w, h):
        pass
    def paintGL(self):
        pass
```

#### 메인 윈도우 생성 - 두 개의 OpenGL 위짓 배치

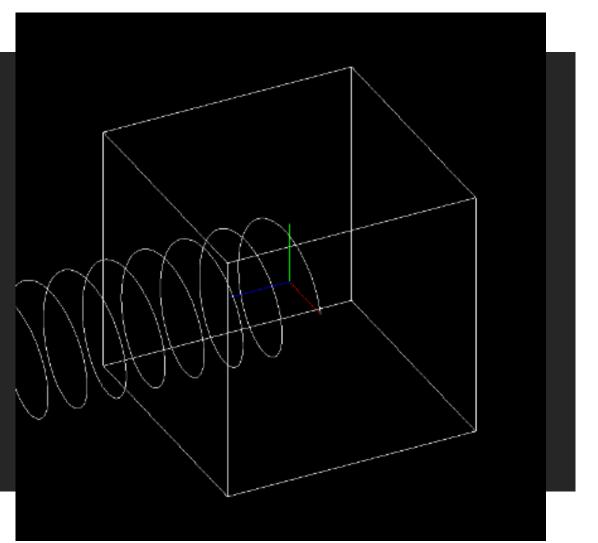
```
class MyWindow(QMainWindow):
                                                      MyWindow
                                                                   central_widget
   def init (self, title=''):
       super(). init ()
       self.setWindowTitle(title)
       ## GUI 설정
       central widget = QWidget()
                                                          HBoxLayout
       self.setCentralWidget(central widget)
       gui_layout = QHBoxLayout()
       central_widget.setLayout(gui_layout)
       self.glWidget1 = MyGLWidget()
                                                          MyGLWidget
                                                                               MyGLWidget
       self.glWidget2 = MyGLWidget()
       gui_layout.addWidget(self.glWidget1)
       gui_layout.addWidget(self.glWidget2)
```

## 윈도 띄우기

```
def main(argv = sys.argv):
    app = QApplication(argv)
    window = MyWindow('glOrtho 관측')
    window.setFixedSize(1200, 600)
    window.show()
    app.exec()
                                            🔳 glOrtho 관측
if __name__ == '__main__':
    main(sys.argv)
```

## 두 창에 나선 그리기

```
def drawAxes():
    glBegin(GL_LINES)
   glColor3f(1,0,0) # red x axis
   glVertex3f(0,0,0); glVertex3f(1,0,0)
   glColor3f(0,1,0) # green y axis
    glVertex3f(0,0,0); glVertex3f(0,1,0)
   glColor3f(0,0,1) # blue z axis
   glVertex3f(0,0,0); glVertex3f(0,0,1)
   glEnd()
def drawHelix():
   glColor3f(1,1,1)
   glBegin(GL_LINE_STRIP)
   for i in range(1000):
       angle = i/10
       x, y = math.cos(angle), math.sin(angle)
       glVertex3f(x, y, angle/10)
    glEnd()
```



# OpenGL 위짓에 나선 그리기 추가

```
class MyGLWidget(QOpenGLWidget):
   def __init__(self, parent=None, observation = False):
        super().__init__(parent)
        self.observation = observation
   def initializeGL(self):
        pass
                                                   ■ glOrtho 관측
   def resizeGL(self, w, h):
        glMatrixMode(GL PROJECTION)
        glLoadIdentity()
   def paintGL(self):
        glClear(GL COLOR BUFFER BIT)
        glMatrixMode(GL_MODELVIEW)
        glLoadIdentity()
        drawAxes()
        drawHelix()
```

# glOrtho 영역 확인하기

```
def drawBox(l, r, b, t, n, f): # glOrtho가 만드는 공간(육면체)을 가시화
   glColor3f(1, 1, 1)
   glBegin(GL LINE LOOP)
   # 앆면
   glVertex3f(1,t,n)
   glVertex3f(1,b,n)
   glVertex3f(r,b,n)
   glVertex3f(r,t,n)
   glEnd()
   glBegin(GL_LINE_LOOP)
   # 뒷면
   glVertex3f(1,t,f)
   glVertex3f(1,b,f)
   glVertex3f(r,b,f)
   glVertex3f(r,t,f)
   glEnd()
```

# OpenGL 위짓에 observation 속성 추가

```
class MyGLWidget(QOpenGLWidget):
   left = bottom = near = -2
   right = top = far = 2
    def __init__(self, parent=None, observation = False):
       super().__init__(parent)
       self.observation = observation
    def initializeGL(self):
        pass
    def resizeGL(self, w, h):
       glMatrixMode(GL_PROJECTION)
       glLoadIdentity()
       if self.observation:
            glortho(-4, 4, -4, 4, -100, 100)
        else:
            glOrtho(self.left, self.right, self.bottom, self.top, self.near, self.far)
```

#### 관찰용 위짓은 눈의 위치를 변경

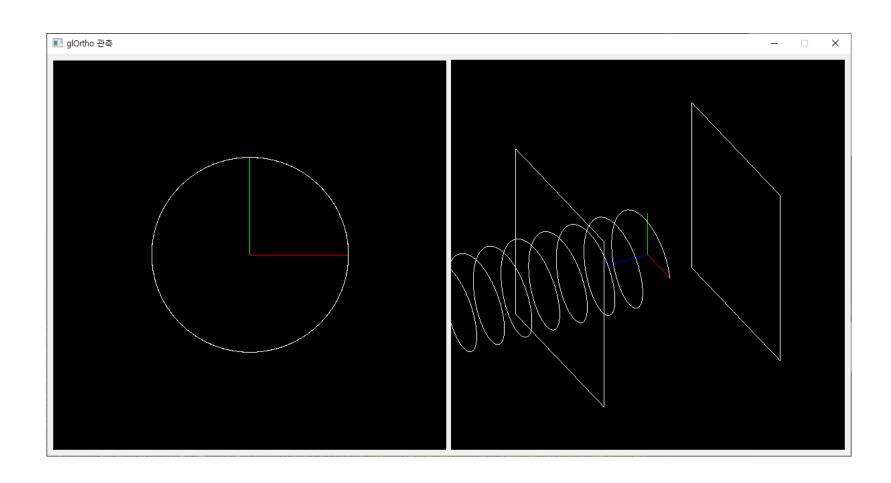
```
def paintGL(self):
    glClear(GL_COLOR_BUFFER_BIT)
    glMatrixMode(GL_MODELVIEW)
    glLoadIdentity()
    if self.observation:
        gluLookAt(1, 0.7, 0.5, 0, 0, 0, 1, 0)
    drawAxes()
    drawHelix()
    drawBox(self.left, self.right, self.bottom, self.top, self.near, self.far)
```

#### MyWindow에서 오픈지엘 위짓 생성시에 관찰용인지 여부를 지정

```
class MyWindow(QMainWindow):
    def __init__(self, title=''):
        . . .

self.glWidget1 = MyGLWidget()
    self.glWidget2 = MyGLWidget(observation = True) # 관측용 OpenGL 위짓
```

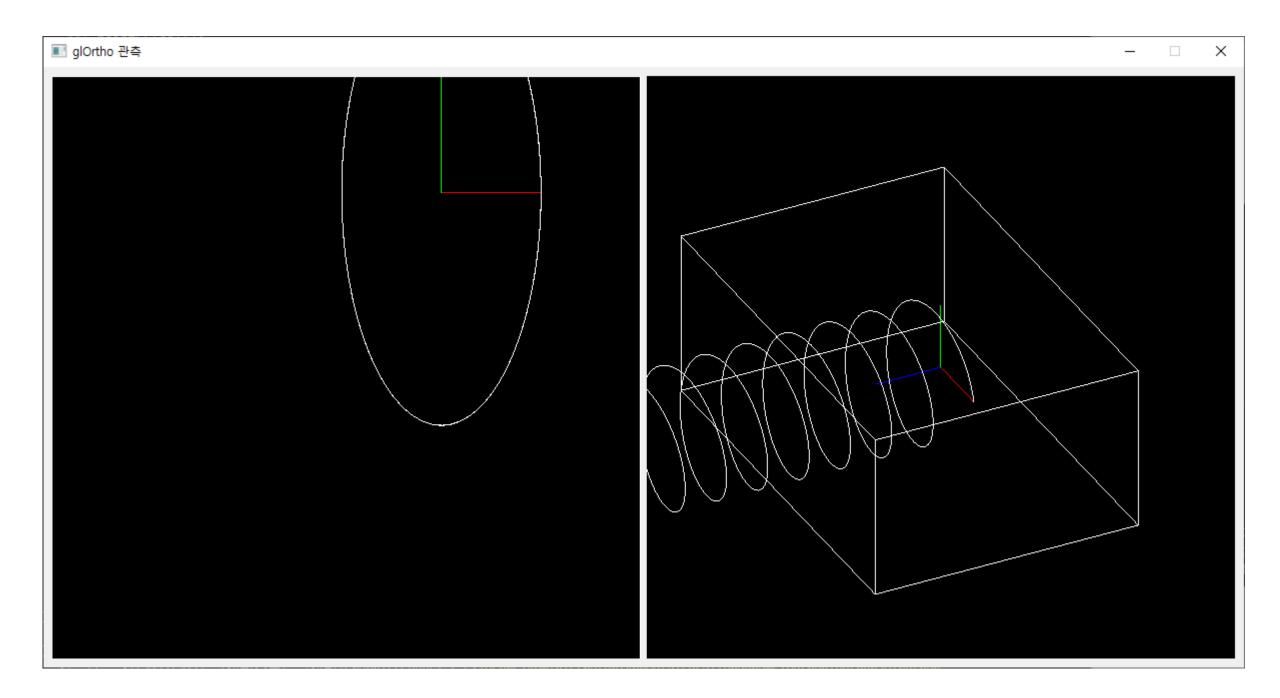
# 결과



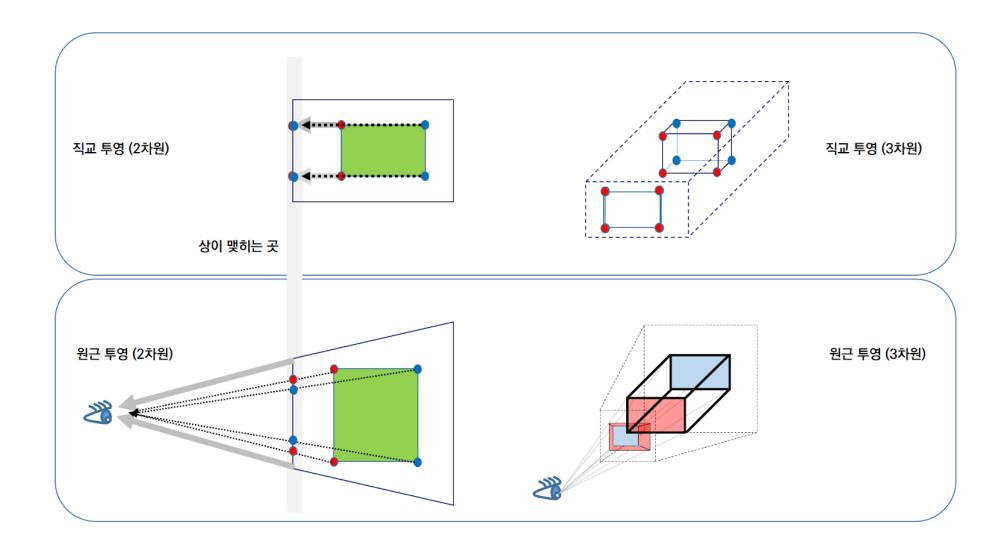
### 키보드를 통한 관측 공간 제어

```
class MyWindow(QMainWindow):
   def keyPressEvent(self, e):
       if e.key() == Qt.Key.Key A:
           MyGLWidget.left -= 0.1
       elif e.key() == Qt.Key.Key S:
           MyGLWidget.left += 0.1
       elif e.key() == Qt.Key.Key D:
           MyGLWidget.right -= 0.1
       elif e.key() == Qt.Key.Key F:
           MvGLWidget.right += 0.1
       elif e.key() == Qt.Key.Key Q:
           MyGLWidget.top += 0.1
       elif e.key() == Qt.Key.Key W:
           MyGLWidget.top -= 0.1
       elif e.key() == Qt.Key.Key Z:
           MyGLWidget.near += 0.1
       elif e.key() == Qt.Key.Key X:
           MyGLWidget.near -= 0.1
       elif e.key() == Qt.Key.Key V:
           MyGLWidget.far += 0.1
       elif e.key() == Ot.Key.Key C:
           MyGLWidget.far -= 0.1
       self.glWidget1.update()
       self.glWidget2.update()
```

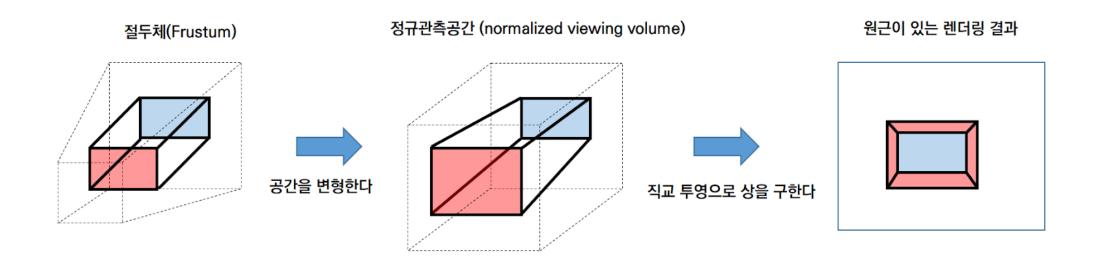
```
class MyGLWidget(QOpenGLWidget):
    def paintGL(self):
        self.projection update()
        glClear(GL COLOR BUFFER BIT)
    def projection update(self):
        glMatrixMode(GL PROJECTION)
        glLoadIdentity()
        if self.observation:
            glortho(-4, 4, -4, 4, -100, 100)
        else:
            glOrtho(self.left, self.right,
                    self.bottom, self.top,
                    self.near, self.far)
```



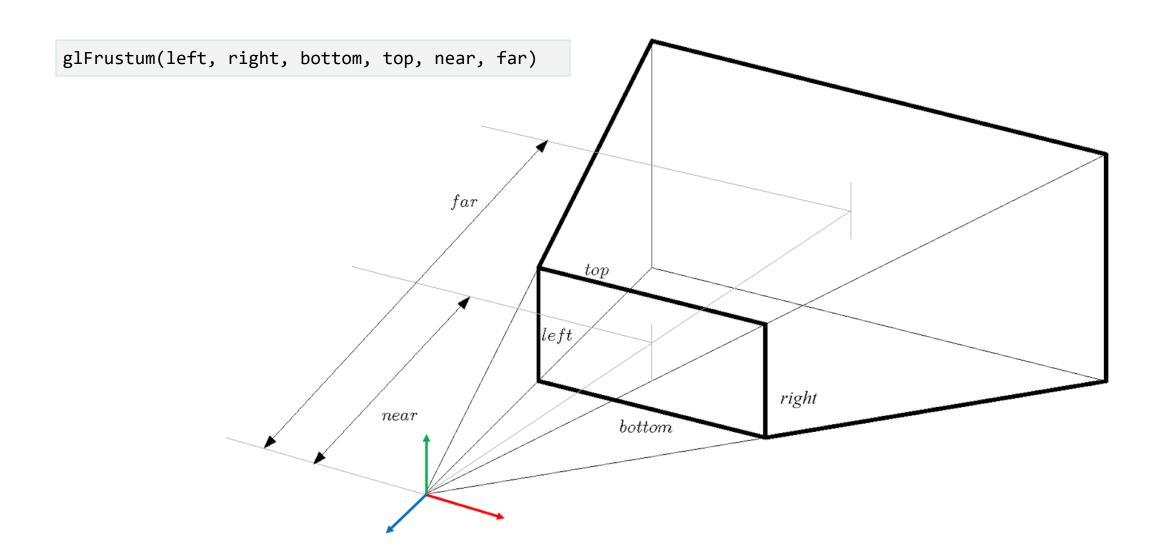
# 원근이 파악되는 투영 - glFrustum



# 원근이 파악되는 투영 – glFrustum



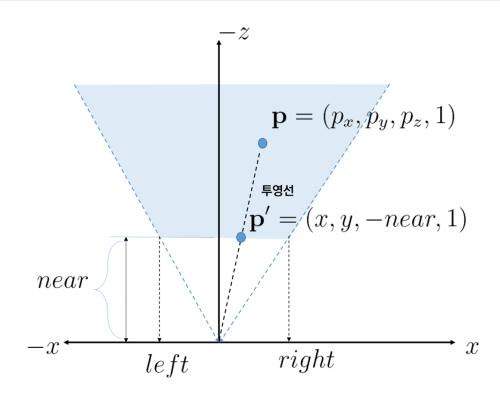
# 원근이 파악되는 투영 – glFrustum



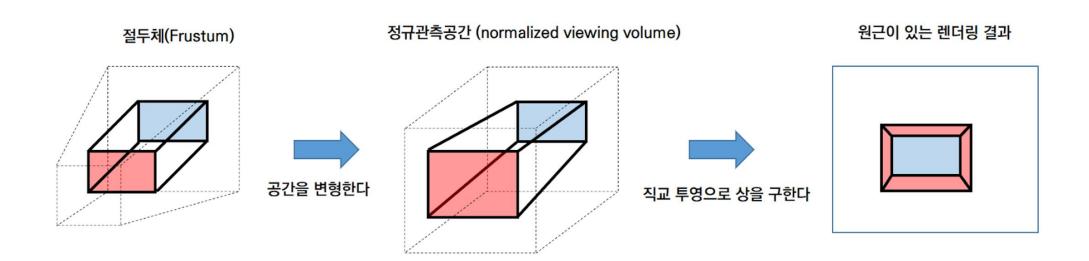
#### 사용 방법

```
glMatrixMode(GL_PROJECTION) # 투영 행렬 수정 모드로 지정
glLoadIdentity(); # 투영 행렬을 항등행렬 I로 지정
glFrustum(l, r, b, t, n, f) # 현재 투영 행렬에 새로운 행렬을 곱한다.
```





## 정규 좌표계로 이동



$$x = -near \frac{p_x}{p_z}$$



$$x' = \left(-\frac{2near}{right - left}\right) \frac{p_x}{p_z} - \frac{right + left}{right - left}$$

# 투영행렬

$$x' = \left(-\frac{2near}{right - left}\right) \frac{p_x}{p_z} - \frac{right + left}{right - left}$$

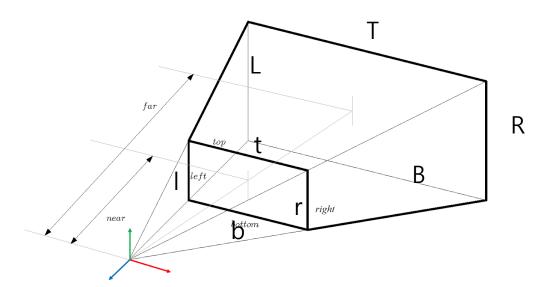
$$y' = \left(-\frac{2near}{top - bottom}\right) \frac{p_y}{p_z} - \frac{top + bottom}{top - bottom}$$

$$\mathbf{M} = \begin{pmatrix} \frac{2near}{right-left} & 0 & \frac{right+left}{right-left} & 0\\ 0 & \frac{2near}{top-bottom} & \frac{top+bottom}{top-bottom} & 0\\ 0 & 0 & -\frac{far+near}{far-near} & \frac{-2near\cdot far}{far-near}\\ 0 & 0 & -1 & 0 \end{pmatrix}$$

\* 상세한 유도 방법은 교재 문서 참고

glFrustum(l, r, b, t, n, f)

$$L = \frac{l}{n}f$$
,  $R = \frac{r}{n}f$ ,  $B = \frac{b}{n}f$ ,  $T = \frac{t}{n}f$ 



```
def drawFrustum(1, r, b, t, n, f):
    L = 1 * (f/n)
    R = r * (f/n)
    B = b * (f/n)
   T = t * (f/n)
    glColor3f(1,1,1)
    glBegin(GL LINE LOOP)
    glVertex3f(1,t,-n)
    glVertex3f(1,b,-n)
    glVertex3f(r,b,-n)
    glVertex3f(r,t,-n)
    glEnd()
    glBegin(GL LINE LOOP)
    glVertex3f(L,T,-f)
    glVertex3f(L,B,-f)
    glVertex3f(R,B,-f)
    glVertex3f(R,T,-f)
    glEnd()
    glBegin(GL_LINES)
    glVertex3f(1,t,-n)
    glVertex3f(L,T,-f)
    glVertex3f(1,b,-n)
    glVertex3f(L,B,-f)
    glVertex3f(r,b,-n)
    glVertex3f(R,B,-f)
    glVertex3f(r,t,-n)
    glVertex3f(R,T,-f)
    glEnd()
```

```
def drawHelix():
   glBegin(GL LINE STRIP)
   for i in range(1000):
       z = i/10
       x, y = 0.5*math.cos(z), 0.5*math.sin(z)
       glVertex3f(x, y, -1.5-z/100)
   glEnd()
   def resizeGL(self, width, height):
       # 카메라의 투영 특성을 여기서 설정
       glMatrixMode(GL_PROJECTION)
       glLoadIdentity()
       if not self.observation:
           glFrustum(
               self.left, self.right,
               self.bottom, self.top,
               self.near, self.far)
        else :
            glOrtho(
                -4, 4, -4, 4, -100, 100)
```

```
def paintGL(self):
   glClear(GL COLOR BUFFER BIT | GL DEPTH BUFFER BIT)
    glMatrixMode(GL_MODELVIEW)
   glLoadIdentity()
    if self.observation:
       gluLookAt(1.5,1.0,0.2, 0,0,-self.near, 0,1,0)
    drawHelix()
    drawAxes()
    drawFrustum(
        self.left, self.right,
        self.bottom, self.top,
        self.near, self.far)
   # 그려진 프레임버퍼를 화면으로 송출
   glFlush()
```

```
from OpenGL.GL import *
from OpenGL.GLU import *
import sys
from PyQt6.QtWidgets import QApplication, QMainWindow
from PyQt6.QtWidgets import QWidget, QHBoxLayout
from PyQt6.QtOpenGLWidgets import QOpenGLWidget
from PyQt6.QtCore import *
import math
def drawAxes() :
    glBegin(GL_LINES)
    glColor3f(1,0,0)
    glVertex3f(0,0,0)
    glVertex3f(1,0,0)
    glColor3f(0,1,0)
    glVertex3f(0,0,0)
    glVertex3f(0,1,0)
    glColor3f(0,0,1)
    glVertex3f(0,0,0)
    glVertex3f(0,0,1)
    glEnd()
```

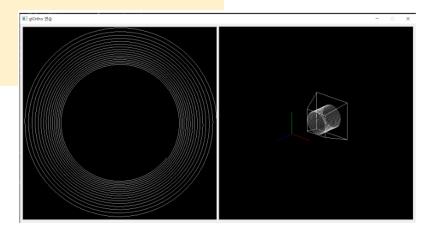
```
def drawFrustum(1, r, b, t, n, f):
    L = 1 * (f/n)
    R = r * (f/n)
   B = b * (f/n)
   T = t * (f/n)
   glColor3f(1,1,1)
   glBegin(GL_LINE_LOOP)
    glVertex3f(1,t,-n)
    glVertex3f(1,b,-n)
    glVertex3f(r,b,-n)
    glVertex3f(r,t,-n)
    glEnd()
    glBegin(GL_LINE_LOOP)
    glVertex3f(L,T,-f)
    glVertex3f(L,B,-f)
    glVertex3f(R,B,-f)
    glVertex3f(R,T,-f)
    glEnd()
    glBegin(GL LINES)
    glVertex3f(1,t,-n)
    glVertex3f(L,T,-f)
    glVertex3f(1,b,-n)
   glVertex3f(L,B,-f)
   glVertex3f(r,b,-n)
   glVertex3f(R,B,-f)
   glVertex3f(r,t,-n)
    glVertex3f(R,T,-f)
    glEnd()
```

```
class MyGLWidget(QOpenGLWidget):
   def init (self, parent=None, observation=False):
       super(). init (parent)
       self.observation = observation
       self.left = self.bottom = -0.5
       self.right = self.top = 0.5
       self.near = 1.5
       self.far = 2.5
   def initializeGL(self):
       # OpenGL 그리기를 수행하기 전에 각종 상태값을 초기화
       glClearColor(0.0, 0.0, 0.0, 1.0)
   def resizeGL(self, width, height):
       # 카메라의 투영 특성을 여기서 설정
       glMatrixMode(GL_PROJECTION)
       glLoadIdentity()
       if not self.observation:
           glFrustum(
               self.left, self.right,
               self.bottom, self.top,
               self.near, self.far)
       else :
           glOrtho(
               -4, 4, -4, 4, -100, 100)
```

```
def paintGL(self):
    self.projection update()
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT)
    glMatrixMode(GL_MODELVIEW)
    glLoadIdentity()
    if self.observation:
        gluLookAt(1.5,1.0,0.2, 0,0,-self.near, 0,1,0)
    drawHelix()
    drawAxes()
    drawFrustum(
       self.left, self.right,
        self.bottom, self.top,
        self.near, self.far)
    # 그려진 프레임버퍼를 화면으로 송출
    glFlush()
def projection update(self):
    glMatrixMode(GL_PROJECTION)
    glLoadIdentity()
    if not self.observation:
        glFrustum(
            self.left, self.right,
            self.bottom, self.top,
            self.near, self.far)
    else :
        glOrtho(
            -4, 4, -4, 4, -100, 100)
```

```
class MyWindow(QMainWindow):
   def init (self, title=''):
       QMainWindow. init (self) # QMainWindow 슈퍼 클래스의 초기화
       self.setWindowTitle(title)
       ### GUI 설정
       central_widget = QWidget()
       self.setCentralWidget(central_widget)
       gui layout = QHBoxLayout() # CentralWidget의 수평 나열 레이아웃
       # 배치될 것들 - 정점 입력을 받기 위한 위짓
       central_widget.setLayout(gui_layout)
       ############### OpenGL Widget 추가
       self.glWidget1 = MyGLWidget(observation=False) # OpenGL Widget
       self.glWidget2 = MyGLWidget(observation=True)
       gui_layout.addWidget(self.glWidget1)
       gui_layout.addWidget(self.glWidget2)
   def keyPressEvent(self, e):
       if e.key() == Qt.Key.Key_A:
           self.glWidget1.left -= 0.1
           self.glWidget2.left -= 0.1
       elif e.key() == Qt.Key.Key_S:
           self.glWidget1.left += 0.1
           self.glWidget2.left += 0.1
       elif e.key() == Qt.Key.Key_D:
           self.glWidget1.right -= 0.1
           self.glWidget2.right -= 0.1
       elif e.key() == Qt.Key.Key_F:
           self.glWidget1.right += 0.1
           self.glWidget2.right += 0.1
       elif e.key() == Qt.Key.Key_Q:
           self.glWidget1.top += 0.1
           self.glWidget2.top += 0.1
       elif e.key() == Qt.Key.Key_W:
```

```
elif e.key() == Qt.Key.Key_W:
            self.glWidget1.top -= 0.1
            self.glWidget2.top -= 0.1
       elif e.key() == Qt.Key.Key Z:
            self.glWidget1.near += 0.1
           self.glWidget2.near += 0.1
        elif e.key() == Qt.Key.Key X:
           self.glWidget1.near -= 0.1
           self.glWidget2.near -= 0.1
       elif e.key() == Qt.Key.Key_V:
           self.glWidget1.far += 0.1
           self.glWidget2.far += 0.1
        elif e.key() == Qt.Key.Key C:
           self.glWidget1.far -= 0.1
           self.glWidget2.far -= 0.1
        self.glWidget1.update()
        self.glWidget2.update()
def main(argv = []):
    app = QApplication(argv)
   window = MyWindow('glOrtho 연습')
   window.setFixedSize(1200, 600)
   window.show()
   app.exec()
if name == ' main ':
   main(sys.argv)
```



# gluPerspective

