$$\frac{\partial}{\partial x} \frac{\partial}{\partial x} \phi(\vec{x}) + \dots = q(\vec{x})$$

$$\downarrow \text{ discretization}$$

$$\frac{\frac{\phi_{i+1} - \phi_i}{h} - \frac{\phi_i - \phi_{i-1}}{h}}{h} + \dots = q_{i,j}$$

$$\downarrow \text{ canonical form}$$

$$\frac{1}{h^2} \phi_{i+1} - \frac{2}{h^2} \phi_i + \frac{1}{h^2} \phi_{i-1} + \dots = q_{i,j}$$

$$\downarrow \text{ code generation}$$

$$01 \text{ function applyStencil(A, b, i, j)}$$

$$02 \quad \text{row = index(i, j)}$$

$$03 \quad \text{A[row, index(i+1, j)] = 1/(h^*h)}$$

$$04 \quad \text{A[row, index(i, j)] = -2/(h^*h)}$$

$$05 \quad \text{A[row, index(i-1, j)] = 1/(h^*h)}$$

$$06 \quad \dots$$

$$07 \quad \text{b[row] = q[i, j]}$$