## HMDelimit: A pipeline for heuristic species delimitation under the multispecies coalescent model using multilocus sequence data

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The multispecies coalescent (MSC) model accommodates genealogical variations across the genome and provides a natural framework for comparative analysis of genomic sequence data to infer the history of species divergence and gene flow. Given a set of populations, hypotheses of species delimitation (and species phylogeny) may be formulated as instances of MSC models (e.g., MSC for one species versus MSC for two species) and compared using Bayesian model selection. This approach, implemented in the Bayesian program BPP, has been found to be prone to over-splitting. Alternatively heuristic criteria based on population parameters under the MSC model (such as population/species divergence times, population sizes, and migration rates) estimated from genomic sequence data may be used to delimit species. Here we extend the approaches of Jackson *et al.* (2017) and Leaché *et al.* (2019) based on the genealogical divergence index (*gdi*) and develop hierarchical merge and split algorithms for species delimitation, and implemented them as a python pipeline. Applied to data simulated under a model of isolation by distance, the approach was able to recover the correct species delimitation, whereas model comparison by BPP failed. Analyses of empirical datasets suggested that the procedure may avoid the problem of over-splitting. We discuss possible strategies for accommodating gene flow in the procedure, as well as the challenges of species delimitation based on heuristic criteria.

BPP | genealogical divergence index | multispecies coalescent | species delimitation

#### Introduction

Accurate delimitation of species boundaries is important to characterizing patterns of biological diversity, especially during the current global changes in climate and environment. Traditionally, species have been identified and distinguished using morphological characteristics. Molecular genetic data can provide additional information about many processes related to species delimitation and identification, including population identities, interspecific hybridization and gene flow, and phylogenetic relationships among the populations and their divergence times (Jiao *et al.*, 2021).

Given a set of populations, different species delimitations correspond to different ways of merging populations into the same species. Each species delimitation, combined with the phylogeny for the delimited species, can be formulated as an instance of the multispecies coalescent (MSC) model (Rannala and Yang, 2003) and fitted to genomic sequence data sampled from the modern species or populations. Competing models can then be compared via Bayesian model selection (i.e., using posterior model probabilities or Bayes factors) to find the best supported delimitation. In the Bayesian program BPP,

this is accomplished by using a Markov chain Monte Carlo (MCMC) algorithm to estimate the posterior probabilities for different MSC models (Yang and Rannala, 2010; Yang, 2014, 2015; Flouri *et al.*, 2018). In simulations, BPP showed lower rates of species overestimation and underestimation than the generalized mixed Yule-coalescent or Poisson tree processes (Luo *et al.*, 2018). In empirical datasets, BPP was effective in identifying cryptic species in many ancient lineages that were not recognised by other molecular or morphological approaches. For example, Ramirez-Reyes *et al.* (2020) identified 13 new species of leaf-toed geckoes in a lineage that diverged 30 Ma.

However, BPP has been noted to often over-split, identifying more lineages as distinct species than many other methods (Sukumaran and Knowles, 2017). For example, Campillo *et al.* (2020) analyzed 99 population pairs in the genus *Drosophila* and found that BPP identified 80 pairs as distinct species, whereas reproductive isolation was identified in only 69 pairs. Similarly, Bamberger *et al.* (2022) examined 48 *Albinaria cretensis* land snail populations, and found that morphological delimitation ?? suggested 3–9 species, ADMIXTURE ?? suggested 15, while BPP suggested 45-48. Barley *et al.* (2018) simulated multiple populations from a single species that exhibits isolation by distance, and found that BPP delimits geographically

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separated populations as distinct species. Those results suggest that the lineages identified by BPP sometimes correspond to populations rather than species (Chambers and Hillis, 2020). Multiple studies using BPP have suggested significant taxonomic reassignments not supported using other methods (e.g., Wu *et al.*, 2018 in Yunnan Bananas). A number of authors have expressed concerns about the apparent over-splitting of BPP (MacGuigan *et al.*, 2021).

Rather than treating species delimitation as a model-selection problem, an alternative approach is to estimate population parameters, such as population split time  $(\tau)$ , population sizes  $(\theta)$ , and migration rates (M), and define species status using empirical criteria based on those parameters. For example, the '10× rule' specifies the interspecific divergence to be at least 10 times as large as the intraspecific diversity (Hebert *et al.*, 2004).

Jackson *et al.* (2017) suggested a criterion called the *genealogical divergence index* (gdi), defined using population parameters. Consider two sequences ( $a_1$  and  $a_2$ ) sampled population A and one sequence (b) from B (see fig. 1). Let the probability that the two sequences from population A coalesce first, so that the gene tree is  $G_1 = ((a_1, a_2), b)$ , be  $P_1 = \mathbb{P}(G_1)$ . In the case of no gene flow, this is given as

$$P_1 = 1 - \frac{2}{3} e^{-2\tau_{AB}/\theta_A},\tag{1}$$

This is a simple function of  $2\tau_{AB}/\theta_A = T_{AB}/(2N_A)$ , the population divergence time in coalescent units (with one coalescent time unit to be  $2N_A$  generations in population A). Jackson *et al.* (2017) rescaled  $P_1$  so that the *gdi* ranges from 0 to 1.

$$gdi = 1 - e^{-2\tau_{AB}/\theta_A} = 1 - e^{-T_{AB}/(2N_A)}$$
. (2)

Thus the gdi is the probability that the two A sequences coalesce before reaching species divergence ( $\tau_{AB}$ ) when we trace the genealogy of the sample backwards in time. A gdi close to 1 indicates a high level of population divergence. Based on a meta-analysis of data from Pinho and Hey (2010), Jackson  $et\ al.$  (2017) suggest that populations are likely to be a single species if gdi < 0.2, and separate species if gdi > 0.7. Intermediate values (0.2 < gdi < 0.7) indicate ambiguous species status.

When there is migration between the two populations, the probability for the gene tree  $G_1$  depends on the parameters of the MSC-M model:

$$P_1 = \mathbb{P}(G_1 | \tau_{AB}, \theta_A, \theta_B, \theta_{AB}, M_{AB}, M_{BA}). \tag{3}$$

Thus the minimum and maximum of  $P_1$  used by Jackson *et al.* (2017) for rescaling  $P_1$  depend on the model parameters. Instead, here we redefine *gdi* as the probability that the first coalescence is between the two A sequences and it occurs before reaching species divergence when we trace the genealogy backwards in time. This definition applies whether or not there is gene flow in the model (fig. 1), with  $0 \le gdi \le 1$ .

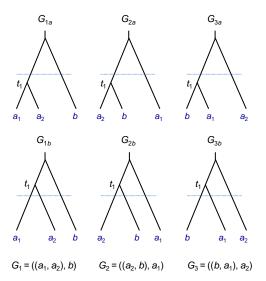


Figure 1: For a locus with two sequences  $a_1$ ,  $a_2$  from species A and one sequence b from B, there are three possible gene trees:  $G_1 = ((a_1, a_2), b)$ ;  $G_2 = ((a_2, b), a_1)$ ; and  $G_3 = ((b, a_2), a_1)$ . If the first coalescence time is more recent than the species divergence time (indicated by the dashed line), we label the gene tree as  $G_{1a}$ ,  $G_{2a}$ ,  $G_{3a}$ ; otherwise they are labeled  $G_{1b}$ ,  $G_{2b}$ ,  $G_{3b}$ . We have  $gdi = \mathbb{P}(G_{1a})$ . The gdi is the probability that two A sequences coalesce first and before the population split. Note that if there is no gene flow between species A and B, gene trees  $G_{2b}$  and  $G_{3b}$  are impossible.

Leaché et al. (2019) described a hierarchical merge algorithm for species delimitation based on gdi. Given a set of populations and a guide tree for them, the procedure attempts to merge two populations into one species, judged by gdi. Here we develop a python pipeline to automate the procedure. We include a hierarchical split algorithm as well. We first describe the computation of gdi when there is gene flow in the model, following Leaché et al. (2019). Then we discuss our new pipeline. We apply the pipeline to four empirical datasets, for giraffes, snails, milksnakes, and sunfish.

#### COMPUTATION OF GDI UNDER THE MSC-M MODEL

Under the MSC-M model, the gdi can be computed analytically, using the Markov chain characterization of the backward-in-time process of coalescent and migration (Leaché et al., 2019). For two populations (A and B) with gene flow and three sequences ( $a_1$ ,  $a_2$ , and b), the genealogical process of coalescent and migration when one traces the history of the sample backwards in time can be described by a Markov chain. The state of the chain is specified by the number of sequences remaining in the sample and the population IDs (A and B) and the sequence IDs ( $a_1$ ,  $a_2$ , b, etc.). For example, The initial state is  $A_{a_1}A_{a_2}B_b$ , in which three sequences  $a_1$ ,  $a_2$ , b are in populations A, A, and

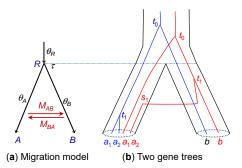


Figure 2: (a) An MSC-with-migration (MSC-M) model for two species or populations (A, B) showing the parameters. The two species diverged time  $\tau \equiv \tau_{AB}$ ago and have since been exchanging migrants at the rate of  $M_{AB} = m_{AB}N_B$  migrants per generation from A to B and at the rate  $M_{BA}$  from B to A. (b) Two gene trees at two loci, each with two sequences  $(a_1, a_2)$  from population A and one sequence (b) from B. In the blue tree, sequences  $a_1$  and  $a_2$  coalesce first, in population A, resulting in the gene tree  $G_1 = ((a_1, a_2), b)$ . In the red tree, sequence  $a_2$  migrates into population B and coalesce with sequence b in population B, resulting in the gene tree  $G_2 = ((a_2, b), a_1)$ . The gdi index is defined as the probability that the first coalescence occurs between the two A sequences and before reaching species divergence when we trace the genealogy backwards in time.

B, respectively. This is also written as 'AAB'. State  $A_{a_1a_2}B_b$ , abbreviated ' $AB_b$ ', means that two sequences remain in the sample, with the ancestor of sequences  $a_1$  and  $a_2$  in population A and sequence b in population B. There are 21 states in the Markov chain.

The transition rate matrix of the Markov chain  $Q = \{q_{ij}\}$  is given in table S1. The transition probability matrix over time t is then  $P(t) = \{p_{ij}(t)\} = e^{Qt}$ , where  $p_{ij}(t)$  is the probability that the Markov chain is in state j at time t in the past given that it is in state i at time 0 (the present time). Suppose Q has the spectral decomposition

$$q_{ij} = \sum_{k=1}^{21} u_{ik} v_{kj} \lambda_k, \tag{4}$$

where  $0 = \lambda_1 > \lambda_2 \ge \cdots \ge \lambda_{21}$  are the eigenvalues of Q, and columns in  $U = \{u_{ij}\}$  are the corresponding right eigenvectors, with  $V = \{v_{ij}\} = U^{-1}$ . Then

$$p_{ij}(t) = \sum_{k=1}^{21} u_{ik} v_{kj} e^{\lambda_k t} . {5}$$

Consider the coalescent time t between sequences  $a_1$  and  $a_2$  given that they are to coalesce first and before  $\tau$  (as in the blue gene tree of fig. 2b). This has density

$$f(t) = \left[ p_{AAB,AAA}(t) + p_{AAB,AAB}(t) \right] \frac{2}{\theta_A}$$

$$+ \left[ p_{AAB,BBA}(t) + p_{AAB,BBB}(t) \right] \frac{2}{\theta_B}, \ t < \tau.$$
(6)

The two terms in the sum correspond to coalescence between  $a_1$  and  $a_2$  occurring in populations A and B, respectively. The first term is the probability,  $p_{AAB,AAA}(t) + p_{AAB,AAB}(t)$ , that sequences  $a_1$  and  $a_2$  are in A right before time t, times the rate for them to coalesce  $\left(\frac{2}{\theta_A}\right)$ . Similarly the second term is the probability density that  $a_1$  and  $a_2$  coalesce at time t in B.

By averaging over the distribution of t, we have

$$gdi = \int_0^{\tau} f(t) \, \mathrm{d}t,\tag{7}$$

where f(t) is given in eq. 6. To calculate the integral in eq. 7, note that from eq. 5,

$$\int_0^{\tau} p_{ij}(t) dt = u_{i1} v_{1j} \tau + \sum_{k=2}^{21} u_{ik} v_{kj} \frac{e^{\lambda_k \tau} - 1}{\lambda_k}.$$
 (8)

We have implemented this calculation of the *gdi* in the python pipeline for the case where the two populations are sister lineages exchanging migrants between themselves but not with other populations.

When populations A and B are involved in gene flow with other populations, analytical calculation of the gdi becomes complicated. It is simpler to simulate gene trees for sequences  $a_1, a_2, b$  under the extended migration model involving more than two populations to calculate the gdi. Specifically, given the fully specified MSC-M model for all species/populations (including the species tree topology and parameters such as  $\tau$ ,  $\theta$ , M), simulate the gene trees with branch lengths (coalescent times) for a large number of loci  $(R=10^6, \mathrm{say})$ , at which three sequences  $(a_1, a_2, b)$  are sampled. The gdi is simply the proportion of loci at which the gene tree is  $G_{1a}$ , that is,  $G_1$  with  $t_1 < \tau_{AB}$  (fig. 1).

## THE HIERARCHICAL MERGE AND SPLIT ALGORITHMS

We implement both the hierarchical merge and hierarchical split algorithms in a python pipeline (fig. 3). Both algorithms require a guide tree for populations, possibly with migration events. In the merge algorithm, we progressively merge the populations into the same species, starting from the tips of the tree and moving towards the root. The merge is accepted if and only if the gdi < 0.2 for the population pair. The algorithm stops when no population/species pair can be merged (fig. 3a).

In the hierarchical split algorithm, we start from the MSC model of one species and progressively split each species into distinct species, starting from the root and moving towards the tips of the tree (fig. 3b). The split is accepted if and only if the gdi > 0.7 for the species

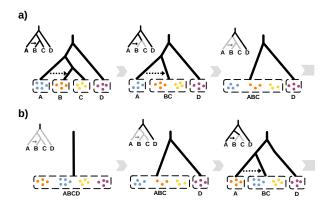


Figure 3: (a) Hierarchical merge and (b) hierarchical split algorithms applied to the same guide tree for four populations.

pair. The algorithm stops when no species can be split (fig. 3b).

If there are K populations on the guide tree, the merge algorithm arrives at a high number of species while the split algorithm arrives at a low number, with  $1 \le K_l \le K_u \le K$ .

#### Example with simulated data (ABCDX)

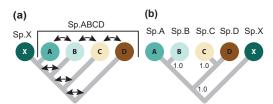


Figure 4: (a) An isolation-by-distance model used to simulate multilocus sequence data. A, B, C, D represent populations of a widely distributed species while X is a new species that split off from population A. (b) Incorrect species delimitation and phylogeny in Bayesian model selection using BPP under the MSC model assuming no gene flow. Use of the guide tree and the *gdi* criterion leads to delimitation of two species. Redrawn after Leaché *et al.* (2019, fig. 5).

Leaché *et al.* (2019) simulated sequence data under the MSC-with-migration model for five populations (fig. 4). Populations A, B, C, D represent a single large paraphyletic species distributed across a wide geographic range. Migration between any two neighbouring populations occurs at the rate of M = Nm = 2 migrants per generation. X represents a new species that split off from population A, and there is no gene flow to or from X. The data consisted of L = 100 simulated loci, with two sequences sampled per species per locus, and 500 sites in the sequence. We use the dataset to illustrate our pipeline.

The complete master control file for the program can be found in S1. During the analysis, the pipeline provides written feedback to the user about the current state of the delimitation and the decisions made during each iteration (S2). This is accompanied by visualisations of the species delimitation and the decision process (Fig. 5).

During the first iteration of the iterative refinement, the pipeline proposes to merge the two current leaf node pairs (A-B, C-D). As the gdi values for the population pairs were below the 0.2 threshold, the A-B and C-D population pairs are merged. During the second iteration, the pipeline proposes to merge the AB-CD population pair. During the third iteration, the pipeline proposes that the ABCD-X population pair could be merged. However, after calculating the gdi values, the proposal is rejected and the final delimitation is reached. The final species delimitation (ABCD, X), is the known correct solution.

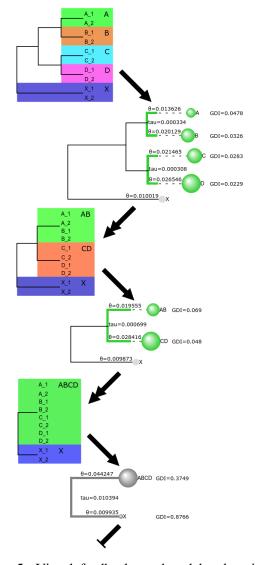
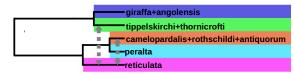


Figure 5: Visual feedback produced by the pipeline during the three iterations. Visualisations of the currently accepted species delimitation are in the left column. Visualisation of the changes to the phylogenetic tree are in the left column



## a) Starting delimitation



## b) Merge result



## c) Split result

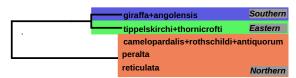


Figure 6: (a) The geographical distributions of nine subspecies of giraffa, modified from Petzold and Hassanin (2020), figure. (b) The hierarchical split algorithm supports 3 species, while (c) The hierarchical merge algorithm supports 5 species.

#### EMPIRICAL EXAMPLES

#### Species delimitation in the genus Giraffa

Species delimitation in the genetically isolated, but phenotypically convergent Giraffes has generated sizeable controversy (Fišer et al., 2018). Based on morphological characters and molecular data, various hypotheses have classified the nine giraffe subspecies ( camelopardalis, angolensis, antiquorum, giraffa, peralta, reticulata, rothschildi, thornicrofti and tippelskirchi. ) into anywhere from one to six species.

Petzold and Hassanin (2020) compiled a multilocus dataset of 21 introns (average sequence length 808 bp), sampled from 66 individuals from the nine subspecies. They found that population genetic approaches, such as the program STRUCTURE and the phylogenetic

approaches implemented in MrBayes, PhyML, and SuperTRI all supported three species. However, the MSC based methods in \*BEAST, STACEY, and BPP strongly supported five species.

Based on the observations of mitochondrial haplotypes and hybridized individuals (Fennessy *et al.*, 2016; Petzold and Hassanin, 2020), bidirectional migration was specified between the *tippelskirchi* and *reticulata*, as well as the *reticulata* and *rothschildi* subspecies. The migration rate was assigned the prior ( $\Gamma(1,100)$ ) with mean 0.01 migrant individuals per generation. Merge and split analyses were conducted with the animal specific *gdi* thresholds of 0.3 and 0.7, as recommended by Jackson *et al.* (2017) (master control files available in S3 and S4).

The split algorithm suggested three species while the merge algorithm suggested five (fig. 6). Both grouped the Eastern populations *thornicrofti* and *tippelskirchi* into one species, and the Southern populations *angolensis* and *giraffa* into another species. The split algorithm lumped the remaining five subspecies into a single Northern species, while the merge algorithm recognized four species.

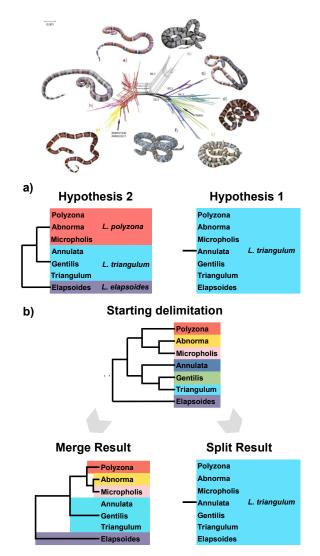


Figure 7: **Top:** Species delimitation hypotheses in *Lampropeltis triangulum*. **a)** Three-species, and one-species delimitation hypotheses suggested by Chambers and Hillis (2020). **b)** Starting delimitation, and results from merge and split analysis.

# Species delimitation in milksnakes (Lampropeltis triangulum)

The American milksnake *Lampropeltis triangulum* is a New World snake with one of the widest known geographic distributions within the squamates, with seven subspecies known: *abnorma*, *polyzona*, *micropholis*, *triangulum*, *gentilis*, *annulata*, *elapsoides* (fig. 7a). Ruane *et al.* (2014) analyzed 11 nuclear loci (average length 537 bp) for 164 individuals from the seven subspecies using BPP and found evidence for seven independent species.

Chambers and Hillis (2020) criticised these results, suggesting that several of the hypothesized species of milksnakes appear to represent arbitrary slices of continuous geographic clines. Based on a combination



Figure 8: East-West splits. Coloured dots represent the sampling location and original classification of individuals (blue: *triangulum*, green: *gentilis*).

of phylogeographic and genetic evidence, they suggested two alternative hypotheses: a one-species hypothesis merging all subspecies into a single species, or a three-species hypothesis separating the *polyzona*, *triangulum*, and *elapsoides* lineages as species.

Chambers and Hillis (2020) also demonstrated that five different arbitrary east-west splits of the the *gentilis* and *triangulum* populations are all supported by BPP as being two separate species (Fig. 7). This result is highly concerning, as these five alternative species delimitations are not mutually compatible. These results also echo the simulations of Barley *et al.* (2018), who demonstrated that BPP will delimit geographically separated clusters of individuals from a single species as distinct species entities.

We analyzed the data using our pipeline, using the guide tree of Chambers and Hillis (2020), with no migration rates assumed (fig. 7). Merge and split algorithms were run using gdi thresholds of 0.3 and 0.7 (master control files available in S5 and S6).

The merge algorithm established an upper bound of five species. When compared with the three-species hypothesis that was the suggested upper bound by Chambers and Hillis (2020), two of the species (*elapsoides* and *triangulum*) were identical, but HMDelimit identified additional diversity in the *polyzona* branch, marking each population as a distinct species. The split analysis only supported a single species.

We conducted a second analysis using only the 38 individuals from the *gentilis*, *triangulum*, and *alterna* populations (which acted as an outgroup in all analyses). The assignment of individuals to the *gentilis* and *triangulum* populations was varied in each analysis, according to the five arbitrary East-West splits of Chambers and Hillis (2020) (fig. 7). Merge and split analyses were ran using the settings as above (master control files available in S7 and S8).

For all five of the East-West geographic splits tested, our merge and split analyses converged on an identical result, merging the *gentilis* and *triangulum* populations into a single species, congruent with the suggestions of Chambers and Hillis (2020).

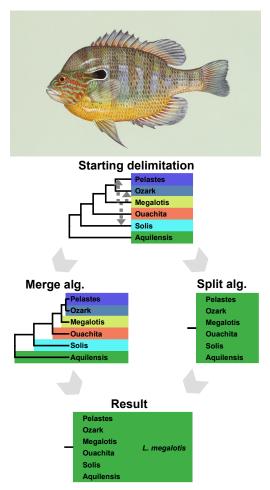


Figure 9: Species delimitation in the Longear Sunfish *Lepomis megalotis*. Both the merge and split algorithms support a single species.

Introgression and species delimitation in the longear sunfish (Lepomis megalotis).

The longear sunfish (*Lepomis megalotis*) is a freshwater fish in the sunfish family, Centrarchidae, of order Perciformes. It is native to eastern North America from the Great Lakes down to northeastern Mexico. Due to widespread geographic distributions and frequent hybridizations, species delimitation in the longear sunfish poses considerable challenges.

Kim et al. (2022) analyzed a dataset of 163 ddRAD loci (average sequence length 89 bp) sampled from 50 individuals from the six subspecies: aquilensis, solis, ouachita, megalotis, ozark, pelastes. After determining a species tree using IQ-tree, they used BPP A00 without migration to calculate  $\tau$  and  $\theta$  parameters for each of the subspecies, and used these values to calculate gdi scores, and delimit species in the group. They found that none of the populations have gdi values supporting distinct species status. Kim et al. (2022) also utilized Fastsimcoal2 to identify patterns of gene flow, and find evidence for multiple instances of significant historical or ongoing genetic exchange. This may be problematic,

as their genetic delimitation procedure did not account for the patterns of gene flow observed.

We reanalyzed the data, taking into account migration between the subspecies. Based on the hybridization patterns observed by Kim *et al.* (2022), migration from the *megalotis* population to the *pelastes*, *solis*, and *ozark* populations was specified. The migration rate was assigned the prior ( $\Gamma(1,100)$ ) with mean 0.01 migrant individuals per generation. Merge and split algorithms were run using *gdi* thresholds of 0.3 and 0.7 (master control files available in S9 and S10).

Both merge and split analyses supported a single species. This is congruent with the *gdi* based delimitation of Kim *et al.* (2022), who found that all populations have *gdi* values below the threshold for distinct species status.

#### Discussion

## Challenges of heuristic species delimitation

Several issues with the *gdi* criterion have been noted before (Leaché *et al.*, 2019). First, given populations *A* and *B*, two *gdi* values may be calculated:

$$gdi_A = 1 - e^{-2\tau_{AB}/\theta_A}$$
  

$$gdi_B = 1 - e^{-2\tau_{AB}/\theta_B}$$
(9)

These may not be consistent concerning the species status of populations A and B (Leaché et al., 2019).

Second, the gdi may be large because the population is very small. Rannala and Yang (2020) recommended the use of absolute divergence time, such that two populations are considered distinct species only if their gdi > 0.7.

Assignment of individuals to populations and construction of the guide tree. Our pipeline requires the user to supply a guide tree. This may be inferred using a species tree estimation method under the MSC model with no gene flow (Yang, 2014; Rannala and Yang, 2017). Alternatives include maximum likelihood tree inference using concatenated data, or use of the mitochondrial genes.

The arbitrariness of the criterion. However, for mammals, a 10% CO1 (or cytb) divergence is a sure thing for distinct species.

Any empirical thresholds for particular criteria or properties will be imprecise, as it is recognized by multiple authors that such an attempt is futile Wells *et al.* (2022). While there can be no set of universal criteria or properties applicable to species delimitation, a heuristic approach does provide useful guide.

Molecular phylogenetic or population genetic analysis should always be integrated with an assessment of congruence with morphological and ecological data. Using genetic data, one should not exclude species generated by processes that do not automatically or immediately result in monophyly, such as hybrid speciation, polyploidy, or paraphyly in the case of recent ancestor-descendant speciation. Where molecular phylogenetic analysis is impractical due to inadequate samples or easily sequenced material, or where it fails to resolve well-supported relationships, species delimitation remains possible, but should be based on a strong hypothesis of phylogenetic relatedness resulting from multiple and unambiguous phenotypic and ecological traits.

The effects of sampling. Many empirical biologists emphasized the importance of sampling: Chambers and Hillis (2020); Wells *et al.* (2022). Yang and Rannala (2017) has pointed out that rarity and singletons should not be a major problem. Migration rates can also be estimated when some species are missing or unsampled. Zhang *et al.* (2011) through simulation illustrated that failure to sample the intermediate populations in a stepping-stones design does not cause false positives

for species delimitation by BPP.

## Gene flow and non-monophyletic species

Analyses of genomic data in the past two decades have demonstrated the prevalence of interspecific gene flow. Several studies suggested evidence for speciation despite ongoing gene flow, as in *Heliconius* butterflies (Martin *et al.*, 2013), Mangrove trees (He *et al.*, 2019), and Western Pacific abalones (Hirase *et al.*, 2021). Issues arise when we want to delimit species when there is gene flow between the species or populations.

Bayesian model selection. First consider Bayesian model selection. There are three models for two populations (A, B): M1: one species, M2-0 two species with no migration, and M2-m two species with migration. Leaché et al. (2019) compare M1 and M2-0 to decide whether there are one or two species, even though the data were simulated with gene flow, and M2-m was not considered. Alternatively one may insist species status only if there is no significant amount of gene flow (i.e., only if M2-0 wins over M2-m), and consider M2-m as representing one species. This approach may suffer from over-lumping.

It is not so clear how to incorporate gene flow in the hierarchical merge and split algorithms. In Leaché et al. (2019), we used MSC with no gene flow (M2-0) to construct the guide tree, and then the merge or split algorithms rely on the MSC model with no gene flow. The migration model is used to simulate data but not used in analysis of the data. This way the guide tree of figure 3b (Leaché et al., 2019) was incorrect, but we arrived at the correct answer of two species: ABCD and X. If we use the MSC-M model and use the correct guide tree with migration of figure 4a, there are two problems. First we will never recover the correct answer of two species by merging or splitting species and populations, keeping the migration events in the model. Second, when we merge populations according to the guide tree it may not be clear whether we want to keep the migration rate. For example if we merge X and A, it is unclear whether we want migration between XAand B since according to the guide tree there is gene flow between A and B but none between X and B. Another approach may be to populations that have high migration rates between them (with, M > 1, say), even if they are not sister lineages on the guide tree. For example, in the case of figure 4a, we will attempt to merge AB, BC, and CD, besides XA. Again there may be ambiguities in the specification of migration events in the new model with merged populations.

## PROGRAM AVAILABILITY

The pipeline is written in python, which drives parameter estimation under the MSC or MSC-M models using BPP. The source code, documentation, and empirical datasets analyzed in the paper are available

at https://github.com/abacus-gene/xxx.

#### ACKNOWLEDGEMENTS

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#### HEURISTIC SPECIES DELIMITATION

#### SUPPLEMENTAL MATERIALS

## Extended Methods and Materials

## Implementation details

We use the example of the simulated data of figure 4 to illustrate the details of implementation.

A control file is used to specify the analysis procedure.

```
# output
output_directory = res_sim_merge

# input files
Imapfile = Leache_2019_starting_populations.txt
seqfile = Leache_2019_sequences.txt

# guide tree
guide_tree = ((A, B), (C, D)), X);

# hierarchical algo. parameters
mode = merge
GDI threshold = <0.2

# computational parameters
threads = 16
burnin = 50000
nsample = 1000000</pre>
```

Figure S1: Control file for the ABCDX merge analysis, presented in fig. 6.

output directory specifies the location where results will be written. seqfile is the sequence alignment file in PHYLIP formatt. Imapfile specifies the mapping of individuals to populations. guide tree is a Newick representation of the guide tree topology. mode specifies the direction of the algorithm. GDI threshold specifies the *gdi* value below which two populations are merged into a candidate species. threads specifies the number of cpu threads used in the calculations. burnin and nsample specify the settings for the MCMC run.

**Output.** The program output is self-explanatory (fig. ??).

```
((A, B), (C, D)), X);
*** Tteration 1 ***
Inferred tau and theta parameters:
        theta
        0.0098
X
Α
        0.0138
В
        0.0202
C
        0.0212
D
        0.0263
        0.0368
ABCDX
                0.0101
ABCD
        0.0432 0.0006
        0.0128 0.0003
AB
CD
        0.0204 0.0002
Proposal results:
                 gdi 1
Node pair
                         gdi 2
                                 merge_accepted
'A', 'B'
'C', 'D'
                 0.05
                         0.03
                                 True
                 0.03
                         0.02
                                 True
Accepted species (3) after iteration 1:
((AB, CD), X);
*** Iteration 2 ***
Inferred tau and theta parameters:
        theta
               tau
X
        0.0098
        0.0194
AB
CD
        0.0286
ABCDX
        0.0367 0.0101
ABCD
        0.0428 0.0006
Proposal results:
Node pair
                 gdi 1
                         gdi 2
                                 merge_accepted
'AB', 'CD'
                 0.07
                         0.05
Accepted species (2) after iteration 2:
(ABCD, X);
*** Iteration 3 ***
Inferred tau and theta parameters:
        theta
               tau
Х
        0.0098
ABCD
        0.0441
ABCDX
        0.0365 0.0102
Proposal results:
                 gdi 1
                         gdi 2
Node pair
                                 merge accepted
'ABCD', 'X'
                 0.39
                         0.87
                                 False
Accepted species (2) after iteration 3:
(ABCD. X):
All modifications rejected. Final delimitation reached.
```

Accepted species (5) in starting delimitation:

Figure S2: Screen output from running the pipeline to analyze the simulated dataset of figure 4.

#### KORNAI ET AL.

## Giraffe control files

```
# Notes: species are renamed such that
# gir_ang = giraffa+angolensis
# tip_tho = tippelskirchi+thornicrofti
# cam_rot_ant = camelopardalis+rothschildi+antiquorum
# per = peralta
# ret = reticulata
# output
output_directory = res_giraffe_merge
# input files
Imapfile = Imap_Giraffe.txt
seqfile = MSA_Giraffe.txt
# quide tree
guide_tree = ((gir_ang,tip_tho),((cam_rot_ant,per),ret));
# migration events and priors
migration = {
   ret -> tip_tho,
    tip_tho -> ret,
    ret -> cam_rot_ant,
    cam_rot_ant -> ret,
migprior = 0.1 10
# hierarchical algo. parameters
mode = merge
gdi_threshold = <0.3</pre>
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S3: Control file for the merge analysis in Giraffes, presented in fig. 6.

```
# output
output_directory = res_giraffe_split
# input files
Imapfile = Imap_Giraffe.txt
seqfile = MSA_Giraffe.txt
# guide tree
guide_tree = ((gir_ang,tip_tho),((cam_rot_ant,per),ret));
# migration events and priors
migration = {
   ret -> tip_tho,
   tip_tho -> ret,
   ret -> cam_rot_ant,
    cam_rot_ant -> ret,
migprior = 0.1 10
# hierarchical algo. parameters
mode = split
gdi_threshold = >0.7
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S4: Control file for the split analysis in Giraffes, presented in fig. 6.

#### HEURISTIC SPECIES DELIMITATION

#### Milksnake control files

```
# Notes: species are renamed such that
# Po = polyzona
# Ab = abnorma
# Mi = micropholis
# An = annulata
# Ge = gentilis
# Tr = triangulum
# El = elapsoides
# output
output_directory = output_directory = res_milksnake_merge
# input files
Imapfile = Imap_Lampropeltis.txt
seqfile = MSA_Lampropeltis.txt
# quide tree
guide_tree = (((Po, (Ab, Mi)), (An, (Ge, Tr))), El);
# hierarchical algo. parameters
mode = merge
gdi_threshold = <0.3
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S5: Control file for the merge analysis in Milksnakes, presented in fig. 7.

```
# output
output_directory = output_directory = res_milksnake_split
# input files
Imapfile = Imap_Lampropeltis.txt
seqfile = MSA_Lampropeltis.txt
# guide tree
guide_tree = (((Po, (Ab, Mi)), (An, (Ge, Tr))), El);
# hierarchical algo. parameters
mode = split
gdi_threshold = >0.7
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S6: Control file for the split analysis in Milksnakes, presented in fig. 7.

```
# output
output_directory = # will be set from the command line
# input files
Imapfile = # will be set from the command line
seqfile = trigentalt.txt
guide_tree = ((Ge,Tr),Al);
mode = merge
gdi_threshold = <0.3
threads = 16
burnin = 50000
nsample = 1000000</pre>
```

Figure S7: Control file for the East-West splits, presented in fig. 7. The Imapfile and output directory parameters are left empty, as they will be provided via the command line. This ensures that the same basic control file can be used for each of the five alternative East-West delimitations.

```
HMDelimit --mcfile mcf_milksnake_EW.txt --mcfpor \
Imapfile = trigent1alt.Imap.txt, output_directory = res_EW_1
HMDelimit --mcfile mcf_milksnake_EW.txt --mcfpor \
Imapfile = trigent2alt.Imap.txt, output_directory = res_EW_2
HMDelimit --mcfile mcf_milksnake_EW.txt --mcfpor \
Imapfile = trigent3alt.Imap.txt, output_directory = res_EW_3
HMDelimit --mcfile mcf_milksnake_EW.txt --mcfpor \
Imapfile = trigent4alt.Imap.txt, output_directory = res_EW_4
HMDelimit --mcfile mcf_milksnake_EW.txt --mcfpor \
Imapfile = trigent5alt.Imap.txt, output_directory = res_EW_5
```

Figure S8: Shell script used to iterate through alternative East-West delimitation hypotheses in Milksnakes, presented in fig. 7. The -mcfpor (master control file parameter override) flag is used to override parameters of the mcf via the command line interface, setting the Imap file to one of the alternative East-West delimitations, and specifying the individual output directories for each analysis.

#### KORNAI ET AL.

## Sunfish control files

```
# Notes: species are renamed such that
# PEL = pelastes
# OZK = ozark
# MEG = megalotis
# LIT = ouachita
\# SOL = solis
# AQU = aquilensis
# output
output_directory = res_sunfish_merge
# input files
Imapfile = Imap_Sunfish.txt
seqfile = MSA_Sunfish.txt
# guide tree
guide_tree = (((((PEL,OZK),MEG),LIT),SOL),AQU);
# migration events and priors
migration = {
    MEG -> PEL,
    MEG -> SOL,
    MEG \rightarrow OZK
}
migprior = 0.1 10
# hierarchical algo. parameters
mode = merge
gdi_threshold = <0.3</pre>
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S9: Control file for the merge analysis in Sunfish, presented in fig. 9.

```
# output
output_directory = res_sunfish_split
# input files
Imapfile = Imap_Sunfish.txt
seqfile = MSA_Sunfish.txt
# guide tree
guide_tree = (((((PEL,OZK),MEG),LIT),SOL),AQU);
# migration events and priors
migration = {
   MEG -> PEL,
   MEG -> SOL,
   MEG -> OZK
migprior = 0.1 10
# hierarchical algo. parameters
mode = split
gdi_threshold = >0.7
# computational parameters
threads = 16
burnin = 50000
nsample = 200000
```

Figure S10: Control file for the split analysis in Sunfish, presented in fig. 9.

Table S1: Rate matrix for Markov chain describing transitions between states in multispecies coalescent with migration model with two populations (A and B) and three sequences  $(a_1, a_2, and b)$ .

AAA         Wab         WBA         WBA <th>,</th> <th>AAA</th> <th>AAB</th> <th>ABA</th> <th>AAA AAB ABA ABB</th> <th>BAA</th> <th>BAB</th> <th>BBA</th> <th>BBB</th> <th><math display="block">BBB  A_{a_1}A  A_{a_2}A  A_bA  C_{a_1}B  B_{a_2}B</math></th> <th><math>A_{\alpha_2}A</math></th> <th><math>A_bA</math></th> <th><math>C_{a_1}B</math></th> <th><math>B_{a_2}B</math></th> <th><math>B_b B</math></th> <th><math>A_{a_1}B</math></th> <th><math>A_{a_2}B</math></th> <th><math>A_bB</math></th> <th><math>A_{a_1}B</math> <math>A_{a_2}B</math> <math>A_bB</math> <math>AB_{a_1}</math></th> <th><math>AB_{a_2}</math></th> <th><math>AB_b</math></th> <th>A B</th>	,	AAA	AAB	ABA	AAA AAB ABA ABB	BAA	BAB	BBA	BBB	$BBB  A_{a_1}A  A_{a_2}A  A_bA  C_{a_1}B  B_{a_2}B$	$A_{\alpha_2}A$	$A_bA$	$C_{a_1}B$	$B_{a_2}B$	$B_b B$	$A_{a_1}B$	$A_{a_2}B$	$A_bB$	$A_{a_1}B$ $A_{a_2}B$ $A_bB$ $AB_{a_1}$	$AB_{a_2}$	$AB_b$	A B
VAB         WBA         WBA <td></td> <td></td> <td>WBA</td> <td>ı</td> <td></td> <td>WBA</td> <td></td> <td></td> <td></td> <td><math>c_A</math></td> <td><math>c_A</math></td> <td><math>c_A</math></td> <td></td>			WBA	ı		WBA				$c_A$	$c_A$	$c_A$										
WAB         WAB         WBA         WBA <td></td> <td>WAB</td> <td></td> <td></td> <td>WBA</td> <td></td> <td>WBA</td> <td></td> <td><math>_{CA}</math></td> <td></td>		WAB			WBA		WBA														$_{CA}$	
WAB         WAB         WBA         WBA         WBA         WBA         WBA         CB		WAB			WBA			WBA												$c_A$		
WAB         WAB         WBA         WBA         CA         CB         CB <th< td=""><td></td><td></td><td>WAB</td><td></td><td></td><td></td><td></td><td></td><td>WBA</td><td></td><td></td><td></td><td></td><td></td><td></td><td><math>c_B</math></td><td></td><td></td><td></td><td></td><td></td><td></td></th<>			WAB						WBA							$c_B$						
WAB         WAB         WAB         WBA         CB         WBA         W		WAB					WBA	WBA											CA			
WAB         WAB         WAB         WBA         WAB         WAB         WAB         WAB         WAB         WAB         WBA         WBA <td>В</td> <td></td> <td>WAB</td> <td></td> <td></td> <td>WAB</td> <td>•</td> <td></td> <td>WBA</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td><math>c_B</math></td> <td></td> <td></td> <td></td> <td></td> <td></td>	В		WAB			WAB	•		WBA								$c_B$					
WAB         WAB         WAB         CB         CB         CB         WBA         WBA         WBA         WBA         WBA         WBA         WBA         WBA         WBA         WAB         WAB         WAB         WAB         WAB         WAB         WAB         WAB         WBA	Ą					WAB			WBA									$c_B$				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	В				WAB		WAB	WAB					CB	CB	CB							
WAB       WBA       WBA       WBA       WBB       WAB       W	A															WBA			WBA			$c_A$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Α																WBA			WBA		$c_A$
WAB         WAB <td>₹'</td> <td></td> <td>WBA</td> <td></td> <td></td> <td>WBA</td> <td><math>_{CA}</math></td>	₹'																	WBA			WBA	$_{CA}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	В															WAB			WAB			$c_B$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	В																WAB			WAB		$c_B$
$WAB \qquad WBA $	~																	WAB			WAB	$c_B$
$WAB \qquad WBA \\ WAB \qquad WBA \\ WAB \qquad WBA \\ WBA \qquad WBA \\ WBA \qquad WBA \\ WBA \qquad WBA \qquad WBA \\ WAB \qquad WBA \qquad WBA \\ WBA WBA $	В									WAB			WBA									
WAB $WAB$ $WBA$ $WBA$ $WBA$	В										WAB			WBA								
$WAB \qquad WBA \\ WAB \qquad WBA \\ WAB \qquad WBA$	22											WAB			WBA							
WAB $WBA$ $WAB$	$a_1$									WAB			WBA									
WAB	$a_2$										WAB			WBA								
	q											$w_{AB}$			WBA							

 $A_{a_1a_2}B_b$  means that two sequences remain in the sample, with the ancestor of sequences  $a_1$  and  $a_2$  is in population A while sequence b is in population B. This is abbreviated ' $AB_b$ ', with the Note.—  $w_{AB} = 4M_{AB}/\theta_B = m_{AB}/\mu$  and  $w_{BA} = 4M_{BA}/\theta_A = m_{BA}/\mu$  are mutation-scaled migration rates, and  $c_A = 2/\theta_A$  and  $c_B = 2/\theta_B$  are the coalescent rates. The state of the chain is given by the population IDs (A or B) and sequence IDs (such as  $a_1$ ,  $a_2$ ,  $a_1a_2$ ). For example the initial state  $A_{a_1}A_{a_2}B_b$  means that the three sequences  $a_1$ ,  $a_2$ , and b are from populations A, A, and B, respectively. States with three sequences are abbreviated, with the three sequences assumed to be in the order  $a_1, a_2, b$  so that the sequence IDs are suppressed. Thus  $A_{a_1}A_{a_2}B_b$  is 'AAB'. State sequence ID 'a<sub>1</sub>a<sub>2</sub>' suppressed. 'A|B' is an absorbing state in which only one sequence remains in the sample, in either A or B, after two coalescent events have occurred. From Leaché et al.