

A pipeline for heuristic species delimitation under the multispecies coalescent model using multilocus sequence data

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The multispecies coalescent (MSC) model accommodates genealogical variations across the genome and provides a natural framework for comparative analysis of genomic sequence data to infer the history of species divergence and gene flow. Given a set of populations, hypotheses of species delimitation (and species phylogeny) may be formulated as instances of MSC models (e.g., MSC for one species versus MSC for two species) and compared using Bayesian model selection. This approach, implemented in the Bayesian program BPP, has been found to be prone to over-splitting. Alternatively heuristic criteria based on population parameters under the MSC model (such as population/species divergence times, population sizes, and migration rates) estimated from genomic sequence data may be used to delimit species. Here we extend the approaches of Jackson *et al.* (2017) and Leaché *et al.* (2019) based on the genealogical divergence index (*gdi*) and develop hierarchical merge and split algorithms for species delimitation, and implemented them as a python pipeline. Applied to data simulated under a model of isolation by distance, the approach was able to recover the correct species delimitation, whereas model comparison by BPP failed. Analyses of empirical datasets suggested that the procedure may avoid the problem of over-splitting. We discuss possible strategies for accommodating gene flow in the procedure, as well as the challenges of species delimitation based on heuristic criteria.

BPP | genealogical divergence index | multispecies coalescent | species delimitation

Notes

- collect estimates of τ and θ into tables.
- Move all descriptions of MCMC setting etc. into SI. Provide data files in SI.

INTRODUCTION

Accurate delimitation of species boundaries is important to characterizing patterns of biological diversity, especially during the current global changes in climate and environment. Traditionally, species have been identified and distinguished using morphological characteristics. Molecular genetic data can provide additional information about many processes related to species delimitation and identification, including population identities, interspecific hybridization and gene flow, and phylogenetic relationships among the populations and their divergence times (Jiao *et al.*, 2021).

Given a set of populations, different species delimitations correspond to different ways of merging populations into the same species. Each species delimitation, combined with the phylogeny for the delimited species, can be formulated as an instance of the multispecies coalescent (MSC) model

(Rannala and Yang, 2003) and fitted to genomic sequence data sampled from the modern species or populations. Competing models can then be compared via Bayesian model selection (i.e., using posterior model probabilities or Bayes factors) to find the best supported delimitation. In the Bayesian program BPP, this is accomplished by using a Markov chain Monte Carlo (MCMC) algorithm to estimate the posterior probabilities for different MSC models (Yang and Rannala, 2010; Yang, 2014, 2015; Flouri *et al.*, 2018). In simulations, BPP showed lower rates of species overestimation and underestimation than the generalized mixed Yule-coalescent or Poisson tree processes (Luo *et al.*, 2018). In empirical datasets, BPP was effective in identifying cryptic species in many ancient lineages that were not recognised by other molecular or morphological approaches. For example, Ramirez-Reyes *et al.* (2020) identified 13 new species of leaf-toed geckoes in a lineage that diverged 30 Ma.

However, BPP has been noted to often over-split, identifying more lineages as distinct species than many other methods (Sukumaran and Knowles, 2017). For example, Campillo *et al.* (2020) analyzed 99 population pairs in the genus *Drosophila* and found that BPP identified 80 pairs as distinct species, whereas reproductive isolation was identified in only 69 pairs. Similarly, Bamberger *et al.* (2022) examined 48

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Albinaria cretensis land snail populations, and found that morphological delimitation ?? suggested 3–9 species, ADMIXTURE ?? suggested 15, while BPP suggested 45–48. Barley *et al.* (2018) simulated multiple populations from a single species that exhibits isolation by distance, and found that BPP delimits geographically separated populations as distinct species. Those results suggest that the lineages identified by BPP sometimes correspond to populations rather than species (Chambers and Hillis, 2020). Multiple studies using BPP have suggested significant taxonomic reassignments not supported using other methods (e.g., Wu *et al.*, 2018 in Yunnan Bananas). A number of authors have expressed concerns about the apparent over-splitting of BPP (MacGuigan *et al.*, 2021).

Rather than treating species delimitation as a model-selection problem, an alternative approach is to estimate population parameters, such as population split time (τ), population sizes (θ), and migration rates (M), and define species status using empirical criteria based on those parameters. For example, the ‘10 \times rule’ specifies the interspecific divergence to be at least 10 times as large as the intraspecific diversity (Hebert *et al.*, 2004).

Jackson *et al.* (2017) suggested a criterion called the *genealogical divergence index* (*gdi*), defined using population parameters. Consider two sequences (a_1 and a_2) sampled population A and one sequence (b) from B (see fig. 1). Let the probability that the two sequences from population A coalesce first, so that the gene tree is $G_1 = ((a_1, a_2), b)$, be $P_1 = \mathbb{P}(G_1)$. In the case of no gene flow, this is given as

$$P_1 = 1 - \frac{2}{3} e^{-2\tau_{AB}/\theta_A}, \quad (1)$$

This is a simple function of $2\tau_{AB}/\theta_A = T_{AB}/(2N_A)$, the population divergence time in coalescent units (with one coalescent time unit to be $2N_A$ generations in population A). Jackson *et al.* (2017) rescaled P_1 so that the *gdi* ranges from 0 to 1.

$$gdi = 1 - e^{-2\tau_{AB}/\theta_A} = 1 - e^{-T_{AB}/(2N_A)}. \quad (2)$$

Thus the *gdi* is the probability that the two A sequences coalesce before reaching species divergence (τ_{AB}) when we trace the genealogy of the sample backwards in time. A *gdi* close to 1 indicates a high level of population divergence. Based on a meta-analysis of data from Pinho and Hey (2010), Jackson *et al.* (2017) suggest that populations are likely to be a single species if *gdi* < 0.2, and separate species if *gdi* > 0.7. Intermediate values (0.2 < *gdi* < 0.7) indicate ambiguous species status.

When there is migration between the two populations, the probability for the gene tree G_1 depends on the parameters of the MSC-M model:

$$P_1 = \mathbb{P}(G_1 | \tau_{AB}, \theta_A, \theta_B, \theta_{AB}, M_{AB}, M_{BA}). \quad (3)$$

Thus the minimum and maximum of P_1 used by Jackson *et al.* (2017) for rescaling P_1 depend on the

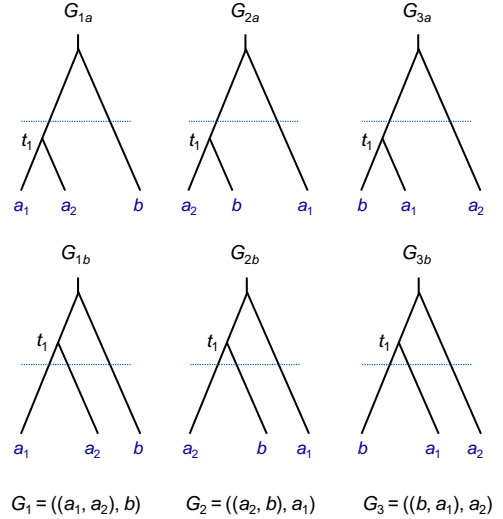


Figure 1: For a locus with two sequences a_1, a_2 from species A and one sequence b from B, there are three possible gene trees: $G_1 = ((a_1, a_2), b)$; $G_2 = ((a_2, b), a_1)$; and $G_3 = ((b, a_1), a_2)$. If the first coalescence time is more recent than the species divergence time (indicated by the dashed line), we label the gene tree as G_{1a}, G_{2a}, G_{3a} ; otherwise they are labeled G_{1b}, G_{2b}, G_{3b} . We have $gdi = \mathbb{P}(G_{1a})$. The *gdi* is the probability that two A sequences coalesce first and before the population split. Note that if there is no gene flow between species A and B, gene trees G_{2b} and G_{3b} are impossible.

model parameters. Instead, here we redefine *gdi* as the probability that the first coalescence is between the two A sequences and it occurs before reaching species divergence when we trace the genealogy backwards in time. This definition applies whether or not there is gene flow in the model (fig. 1), with $0 \leq gdi \leq 1$.

Leaché *et al.* (2019) described a hierarchical merge algorithm for species delimitation based on *gdi*. Given a set of populations and a guide tree for them, the procedure attempts to merge two populations into one species, judged by *gdi*. Here we develop a python pipeline to automate the procedure. We include a hierarchical split algorithm as well. We first describe the computation of *gdi* when there is gene flow in the model, following Leaché *et al.* (2019). Then we discuss our new pipeline. We apply the pipeline to four empirical datasets, for giraffes, snails, milksnakes, and sunfish.

COMPUTATION OF GDI UNDER THE MSC-M MODEL

Under the MSC-M model, the *gdi* can be computed analytically, using the Markov chain characterization of the backward-in-time process of coalescent and migration (Leaché *et al.*, 2019). For two populations (A and B) with gene flow and three sequences (a_1, a_2 , and b), the genealogical process of coalescent and migration when one traces the history of the sample

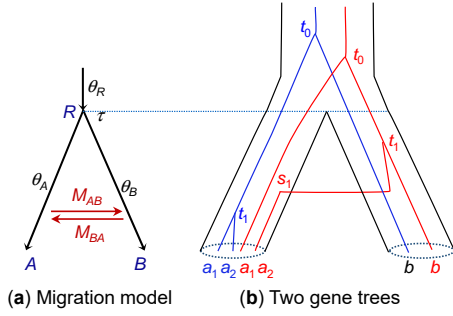


Figure 2: **(a)** An MSC-with-migration (MSC-M) model for two species or populations (A, B) showing the parameters. The two species diverged time $\tau \equiv \tau_{AB}$ ago and have since been exchanging migrants at the rate of $M_{AB} = m_{AB}N_B$ migrants per generation from A to B and at the rate M_{BA} from B to A . **(b)** Two gene trees at two loci, each with two sequences (a_1, a_2) from population A and one sequence (b) from B . In the blue tree, sequences a_1 and a_2 coalesce first, in population A , resulting in the gene tree $G_1 = ((a_1, a_2), b)$. In the red tree, sequence a_2 migrates into population B and coalesce with sequence b in population B , resulting in the gene tree $G_2 = ((a_2, b), a_1)$. The gdi index is defined as the probability that the first coalescence occurs between the two A sequences and before reaching species divergence when we trace the genealogy backwards in time.

backwards in time can be described by a Markov chain. The state of the chain is specified by the number of sequences remaining in the sample and the population IDs (A and B) and the sequence IDs (a_1, a_2, b , etc.). For example, The initial state is $A_{a_1}A_{a_2}B_b$, in which three sequences a_1, a_2, b are in populations A, A , and B , respectively. This is also written as ‘ AAB ’. State $A_{a_1a_2}B_b$, abbreviated ‘ AB_b ’, means that two sequences remain in the sample, with the ancestor of sequences a_1 and a_2 in population A and sequence b in population B . There are 21 states in the Markov chain.

The transition rate matrix of the Markov chain $Q = \{q_{ij}\}$ is given in table S1. The transition probability matrix over time t is then $P(t) = \{p_{ij}(t)\} = e^{Qt}$, where $p_{ij}(t)$ is the probability that the Markov chain is in state j at time t in the past given that it is in state i at time 0 (the present time). Suppose Q has the spectral decomposition

$$q_{ij} = \sum_{k=1}^{21} u_{ik} v_{kj} \lambda_k, \quad (4)$$

where $0 = \lambda_1 > \lambda_2 \geq \dots \geq \lambda_{21}$ are the eigenvalues of Q , and columns in $U = \{u_{ij}\}$ are the corresponding right eigenvectors, with $V = \{v_{ij}\} = U^{-1}$. Then

$$p_{ij}(t) = \sum_{k=1}^{21} u_{ik} v_{kj} e^{\lambda_k t}. \quad (5)$$

Consider the coalescent time t between sequences a_1 and a_2 given that they are to coalesce first and before τ (as in the blue gene tree of fig. 2b). This has density

$$f(t) = [p_{AAB,AAA}(t) + p_{AAB,AAB}(t)] \frac{2}{\theta_A} + [p_{AAB,BBA}(t) + p_{AAB,BBB}(t)] \frac{2}{\theta_B}, \quad t < \tau. \quad (6)$$

The two terms in the sum correspond to coalescence between a_1 and a_2 occurring in populations A and B , respectively. The first term is the probability, $p_{AAB,AAA}(t) + p_{AAB,AAB}(t)$, that sequences a_1 and a_2 are in A right before time t , times the rate for them to coalesce ($\frac{2}{\theta_A}$). Similarly the second term is the probability density that a_1 and a_2 coalesce at time t in B .

By averaging over the distribution of t , we have

$$gdi = \int_0^\tau f(t) dt, \quad (7)$$

where $f(t)$ is given in eq. 6. To calculate the integral in eq. 7, note that from eq. 5,

$$\int_0^\tau p_{ij}(t) dt = u_{i1} v_{1j} \tau + \sum_{k=2}^{21} u_{ik} v_{kj} \frac{e^{\lambda_k \tau} - 1}{\lambda_k}. \quad (8)$$

We have implemented this calculation of the gdi in the python pipeline for the case where the two populations are sister lineages exchanging migrants between themselves but not with other populations.

When populations A and B are involved in gene flow with other populations, analytical calculation of the gdi becomes complicated. It is simpler to simulate gene trees for sequences a_1, a_2, b under the extended migration model involving more than two populations to calculate the gdi . Specifically, given the fully specified MSC-M model for all species/populations (including the species tree topology and parameters such as τ, θ, M), simulate the gene trees with branch lengths (coalescent times) for a large number of loci ($R = 10^6$, say), at which three sequences (a_1, a_2, b) are sampled. The gdi is simply the proportion of loci at which the gene tree is G_{1a} , that is, G_1 with $t_1 < \tau_{AB}$ (fig. 1).

HIERARCHICAL MERGE AND SPLIT (HMS?)

ALGORITHMS

We implement both the hierarchical merge and hierarchical split algorithms in a python pipeline (fig. 3). Both algorithms require a guide tree for populations, possibly with migration events. In the merge algorithm, we progressively merge the populations into the same species, starting from the tips of the tree and moving towards the root. The merge is accepted if and only if the $gdi < 0.2$ for the population pair. The algorithm stops when no population/species pair can be merged (fig. 3a).

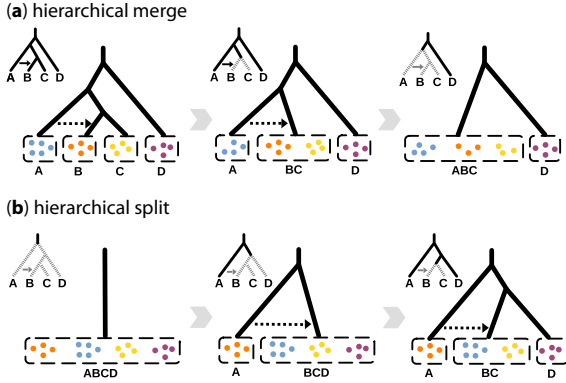


Figure 3: **(a)** Hierarchical merge and **(b)** hierarchical split algorithms applied to the same guide tree for four populations.

[Prepare a version of the figure without gene flow using the same guide tree for merge and split.

Edit this version (with migration) to have the same guide tree for merge and split. I suppose with migration it's not obvious how merge should work, but we can discuss options in relation to the issue of non-monophyletic species.]

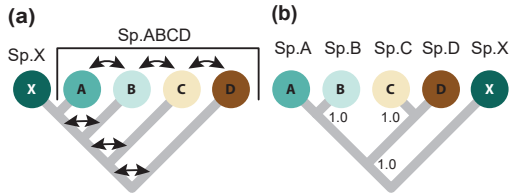


Figure 4: **(a)** An isolation-by-distance model used to simulate multilocus sequence data. *A*, *B*, *C*, *D* represent populations of a widely distributed species while *X* is a new species that split off from population *A*. **(b)** Incorrect species delimitation and phylogeny in Bayesian model selection using BPP under the MSC model assuming no gene flow. Use of the guide tree and the *gdi* criterion leads to delimitation of two species. Redrawn after Leaché *et al.* (2019, fig. 5).

In the hierarchical split algorithm, we start from the MSC model of one species and progressively split each species into distinct species, starting from the root and moving towards the tips of the tree (fig. 3b). The split is accepted if and only if the *gdi* > 0.7 for the species pair. The algorithm stops when no species can be split (fig. 3b).

If there are K populations on the guide tree, the merge algorithm arrives at a high number of species while the split algorithm arrives at a low number, with $1 \leq K_l \leq K_u \leq K$.

EXAMPLE WITH SIMULATED DATA (*ABCDX*)

Leaché *et al.* (2019) simulated sequence data under the MSC-with-migration model for five populations of figure 4. Populations *A*, *B*, *C*, *D* represent a

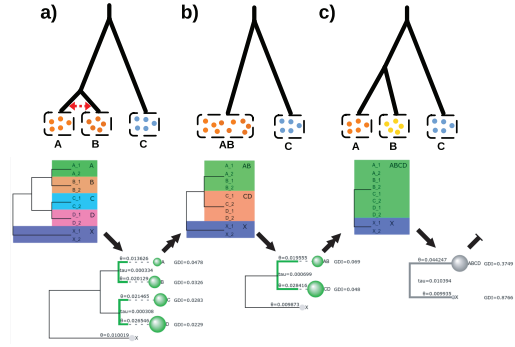


Figure 5: **[Delete this. We are using the ABCDX example.]** Simulated model with three populations and two species used for the tutorial. **a)** Simulated speciation scenario. **b)** Correct species delimitation. **c)** Incorrect species delimitation inferred by BPP A11. Output produced by the pipeline recording the iterations, using the model of figure 5.

single large paraphyletic species distributed across a wide geographic range. Migration between any two neighbouring populations occurs at the rate of $M = Nm = 2$ migrants per generation. *X* represents a new species that split off from population *A*, and there is no gene flow to or from *X* (fig. 4). The data consisted of $L = 100$ simulated loci, with two sequences sampled per species per locus, and 500 sites in the sequence. We use the dataset to illustrate our pipeline. The control file and the program output for the BPP analyses are shown in figures .

TUTORIAL WITH SIMULATED DATA (*ABC*)

[delete this ABC simulation example and replace with the ABCDX example]

Simulation scenario. Sequence data was simulated using a model tree for three populations, $((A, B), C)$, with parameter $\tau_{ABC} = 0.02$, $\tau_{AB} = 0.001$, $\theta_A = \theta_B = \theta_C = 0.02$, with migration rates $M_{AB} = M_{BA} = 2$ (fig. ??). *A* and *B* represent two geographic populations of a single species, which diverged recently and have been exchanging migrants. Five diploid individuals were sampled from each population per locus.

When BPP A11 mode is used to delimit species in this dataset, it incorrectly recovers three species with posterior probability > 0.999 (fig. ??c).

The analyses is specified using a control file, as follows.

```
output_directory = Results
Imapfile = Sim_imap.txt
seqfile = Sim_MSA.txt

guide_tree = ((A,B),C);
migration = {A -> B, B -> A}
migprior = 1 10

mode = merge
```


gdi_threshold = <0.2

burnin = 200000

nsample = 500000

The variable `output_directory` specifies the folder where the results of the analysis will be written. `seqfile` points to phylip formatted multiple sequence alignment. `imapfile` specifies the text file which describes the mapping of individuals to populations in the starting delimitation. `guide_tree` is a Newick representation of the guide tree topology. `migration` is used to specify the source and destination of migration events. `migprior` defines the gamma prior on migration rate. In this case, the value of 1 10 specifies a prior mean $M = 0.1$. `mode` specifies that the direction of iterative refinement. `gdi_threshold` specifies the gdi value below which two populations are merged into a candidate species. `burnin` specifies number of discarded iterations in the burn-in period of the MCMC analysis. `nsample` specifies the number of samples used in the estimation of τ, θ and M parameters. A detailed overview of all possible control file parameters is provided in the documentation for the program.

The program can be launched from a terminal, as follows

```
python HMDelimit.py --mcfile tutorial_sim_merge.txt
```

During the analysis, the pipeline provides written feedback to the user about the current state of the delimitation and the decisions and modifications made during each iteration:

```
Analysis started
Starting state of merge mode
Accepted species (3) in starting delimitation:
((A,B),C);
```

```
*** Iteration 1 ***
Inferred tau and theta parameters:
theta      tau
C    0.019639
A    0.018053
B    0.020506
AB   0.020471  0.000964
ABC  0.019852  0.020066
```

```
Migration rates:
source destination      M
A          B 2.138254
B          A 2.090163
```

```
Proposal results:
node 1 node 2 gdi 1 gdi 2 merge accepted
A      B    0.07  0.06             True
```

```
Accepted species (2) after iteration 1:
(AB,C);
```

```
*** Iteration 2 ***
Inferred tau and theta parameters:
theta      tau
```

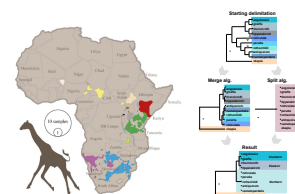


Figure 6: [For each of the empirical examples, perhaps include a picture of the animal, a map showing geographical distribution, the guide tree, and the merge and split results.] (a) The geographical distributions of nine subspecies of giraffa, modified from Petzold and Hassanin (2020), figure. (b) The hierarchical split algorithm supports 3 species, while (c) the hierarchical merge algorithm supports 6 species. [colours on the map and on the tree do not seem to match.]

Merge and Split analyses in the Giraffe and Okapia dataset. Top shows starting delimitation with migration patterns. Merge and split analyses converge to three giraffe species, which correspond to the geographically separated Southern, Eastern, and Northern metapopulations.

```
C    0.019649
AB   0.025840
ABC  0.019670  0.020204
```

Proposed results:

```
node 1 node 2 gdi 1 gdi 2 merge accepted
AB      C    0.79  0.87             False
```

```
Accepted species (2) after iteration 2:
(AB,C);
```

All modifications rejected. Final delimitation reached.

During the first iteration of the merge analysis, the *gdi* score of the *A* and *B* populations was inferred to be below the threshold for distinct species, causing them to be merged into the new species *AB*. The merge proposal between the *AB* and *C* species in the second iteration is rejected, leaving two species, the known correct delimitation (fig. 5b).

The control files and data files are all provided in the supplementary materials.

EMPIRICAL EXAMPLES

Species delimitation in the genus *Giraffa*

Data. Nine giraffe subspecies have been recognised: *camelopardalis*, *angolensis*, *antiquorum*, *giraffa*, *peralta*, *reticulata*, *rothschildi*, *thornicrofti* and *tippelskirchi*. Genetically isolated populations exhibit phenotypic convergence, which complicates the recognition of distinct species (Fiser *et al.*, 2018). Based on morphological and molecular data, several hypotheses of delimitation have been presented, ranging from one species to as many as six.

Petzold and Hassanin (2020) compiled a multilocus dataset of 21 introns (average sequence length 808 bp), sampled from 66 individuals from the nine subspecies. They found that population genetic approaches, such as the program STRUCTURE and the phylogenetic approaches implemented in MrBayes, PhyML, and SuperTRI all supported three species. However, the MSC based methods in *BEAST, STACEY, and BPP strongly supported five species, which was the maximum that was tested. [How are structure and stacey used to delimit species? Phylogenetic programs MrBayes, PhyML, and SuperTRI are not for delimiting species? Why are the BPP results different in the two analyses?]

[Here, the original authors tested if bpp supports 2, 3, 4, or 5 species. They found that 5 were supported. I retested the dataset (which contained 9 populations) without specifying the possible number of species (in A11 mode) and found that BPP supported 6 species. The original authors never tested a 6 species hypothesis.]

We analyzed the data using our pipeline. We augmented the data with further (?) sequences from the outgroup species, *Okapia johnstoni*. [The use of outgroup is unnecessary and complicates comparison with previous results. Shall we remove the outgroup and use the same data as Petzold and Hassanin (2020).] We used the guide tree for the nine subspecies of Petzold and Hassanin (2020). The mutation rate was set at $\mu = 2.12 \times 10^{-8}$ per site per generation (Chen *et al.*, 2019). BPP supported six species.

Hierarchical merge and split analyses were conducted with the default *gdi* thresholds of 0.2 and 0.7, and default generation thresholds of 1000 and 10000 for each method respectively. The split algorithm suggested three species while the merge algorithm suggested six (fig. 6). Both grouped the Eastern populations *thornicrofti* and *tippelskirchi* into one species, and the Southern populations *angolensis* and *giraffe* into another species. The split algorithm lumped the remaining five subspecies into a single Northern species, while the merge algorithm recognized four species. Mitochondrial introgression has been detected between the *rotschildi* and *reticulata* subspecies (Fennessy *et al.*, 2016).

2023.3.29-giraffe. Based on the observations of mitochondrial haplotypes and hybridized individuals (Fennessy *et al.*, 2016; Petzold and Hassanin, 2020), bidirectional migration was specified between the *tippelskirchi* and *reticulata*, as well as the *reticulata* and *rotschildi* subspecies. The migration rate was assigned the prior $G(1, 100)$ with mean 0.01 migrant individuals per generation. Merge and split analyses were conducted with the animal specific *gdi* thresholds of 0.3 and 0.7, as recommended by Jackson *et al.* (2017). Both algorithms suggested three species, separating the northern, eastern, and southern populations into distinct species. The result is consistent with Petzold

and Hassanin (2020).

Species delimitation of *Albinaria* snails in Crete

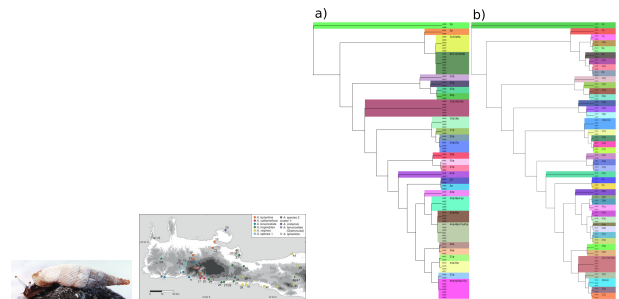


Figure 7: Analyses of the *Albinaria* snail data suggested (a) 29 species by the split algorithm and (b) 44 species by the merge algorithm. Inset *Albinaria* snail image from (Schilthuizen, 2018, fig. 3A).

Data. The genus *Albinaria* is one of the largest radiations of land snails, with up to 140 species found in their native habitats of Greece and south-western Turkey (Schilthuizen 2018). Delimiting species in such ongoing radiations is challenging due to the small differences between the incipient species and possible gene flow between lineages. Bamberger *et al.* (2022) applied three molecular delimitation methods to data of 393 nuclear loci (with an average length of 209bp), sampled from 93 individuals across the 48 populations in the *Albinaria cretensis* complex from Western Crete. While traditional morphological delimitation ?? supported 3-9 species, Gaussian clustering ?? supported 6 species, ADMIXTURE (Alexander and Lange, 2011) supported 11-17 species, while BPP supported 45-48 species.

We used the phylogenetic tree for the 48 populations produced by Bamberger *et al.* (2022) as the guide tree. [delete? As no nuclear mutation rate was available for snails, we estimated it by taking a known mtDNA μ derived in the snail *Radix balthica* ($\mu = 7.95 \times 10^{-7}$) (Bolotov *et al.*, 2017), and multiplying it by the mitochondrial to nuclear gene mutation rate ratio (0.24) recently estimated for gastropods (Duda, 2021), which yielded $\mu = 1.92 \times 10^{-7}$.]

We used the merge and split algorithms, with the default *gdi* thresholds of 0.2 and 0.7, and default generation thresholds of 1000 and 10000. [??]

Output and interpretation. The progressive split and merge algorithms suggested 29 and 44 species, respectively (fig. 7). [delete?] The large range may be due to the fact that some speciation processes are ongoing, so that the species status may be ambiguous (Stankowski and Ravinet, 2021).

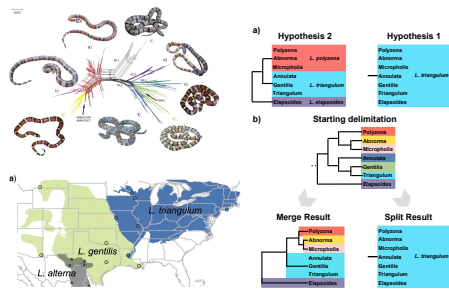


Figure 8: Species delimitation hypotheses in *Lampropeltis triangulum*. **a)** Three-species, and one-species delimitation hypotheses suggested by Chambers and Hillis (2020). **b)** Starting delimitation, and results from merge and split analysis.

Coloured dots represent the sampling location and original classification of individuals (blue: *triangulum*, green: *gentilis*).

Species delimitation in milksnakes (*Lampropeltis triangulum*)

The American milksnake *Lampropeltis triangulum* is a New World snake with one of the widest known geographic distributions within the squamates, with seven subspecies known: *abnorma*, *polyzona*, *micropholis*, *triangulum*, *gentilis*, *annulata*, *elapsoides* (fig. 8a). Ruane *et al.* (2014) analyzed 11 nuclear loci (average length 537 bp) for 164 individuals from the seven subspecies using BPP and found evidence for seven independent species. Chambers and Hillis (2020) criticised these results, suggesting that several of the hypothesized species of milksnakes appear to represent arbitrary slices of continuous geographic clines. Based on a combination of phylogeographic and genetic evidence, they suggested two alternative hypotheses: a one-species hypothesis merging all subspecies into a single species, or a three-species hypothesis separating the *polyzona*, *triangulum*, and *elapsoides* lineages as species.

We analyzed the data using our pipeline, using the guide tree of ???, with no migration rates assumed (fig. 8). Merge and split algorithms were run using *gdi* thresholds of 0.3 and 0.7.

The merge algorithm established an upper bound of five species. When compared with the three-species hypothesis that was the suggested upper bound by Chambers and Hillis (2020), two of the species (*elapsoides* and *triangulum*) were identical, but HMDelimit identified additional diversity in the *polyzona* branch, marking each population as a distinct species. The split analysis only supported a single species.

[I'll probably delete this later. I seem to remember there were many problems with the Chambers&Hillis paper, but i need to read it to refresh my memory.] We conducted a second analysis using only the 38 individuals from the *gentilis*, *triangulum*, and

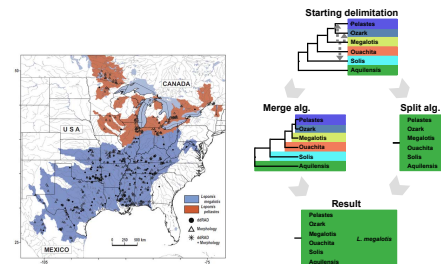


Figure 9: Species delimitation in the Longear Sunfish *Lepomis megalotis*. Both the merge and split algorithms support a single species.

alterna populations (which acted as an outgroup in all analyses). The assignment of individuals to the *gentilis* and *triangulum* populations was **varied?** in each analysis (fig. 8). Merge and split analyses were ran using the settings as above. For all five of the East-West geographic splits tested, our merge and split analyses converged on an identical result, merging the *gentilis* and *triangulum* populations into a single species.

Introgression and species delimitation in the longear sunfish (*Lepomis megalotis*).

The longear sunfish (*Lepomis megalotis*) is a freshwater fish in the sunfish family, Centrarchidae, of order Perciformes. It is native to eastern North America from the Great Lakes down to northeastern Mexico. Due to widespread geographic distributions and frequent hybridizations, species delimitation in the longear sunfish poses considerable challenges. Kim *et al.* (2022) analyzed a dataset of 163 ddRAD loci (average sequence length 89 bp) sampled from 50 individuals from the six subspecies: *aquilensis*, *solis*, *ouachita*, *megalotis*, *ozark*, *pelastes*. After determining a species tree using IQ-TREE, they used BPP A00 without migration to calculate τ and θ parameters for each of the subspecies, and used these values to calculate *gdi* scores, and delimit species in the group.

They found that none of the populations have *gdi* values supporting distinct species status. Kim *et al.* (2022) also utilized FASTSIMCOAL2 to identify patterns of gene flow, and find evidence for multiple instances of significant historical or ongoing genetic exchange. However, their delimitation analysis assumed no gene flow.

We reanalyzed the data, taking into account migration between the subspecies. Based on presence of hybridized individuals, migration from the *megalotis* population to the *pelastes*, *solis*, and *ozark* populations was specified. Merge and split analyses were conducted with *gdi* thresholds of 0.3 and 0.7. The MCMC parameters *burnin* and *nsample* were set at 200000 and 500000 respectively. The migration rate prior was $G(1,100)$ with the prior mean 0.01 migrant individuals per generation (fig. 9). [Move details to

SL.]

Both merge and split analyses supported a single species. This is congruent with the *gdi* based delimitation of Kim *et al.* (2022), who found that all populations have *gdi* values below the threshold for distinct species status.

DISCUSSION

Challenges of heuristic species delimitation

Several issues with the *gdi* criterion have been noted before (Leaché *et al.*, 2019). First, given populations *A* and *B*, two *gdi* values may be calculated:

$$\begin{aligned} gdi_A &= 1 - e^{-2\tau_{AB}/\theta_A} \\ gdi_B &= 1 - e^{-2\tau_{AB}/\theta_B} \end{aligned} \quad (9)$$

These may not be consistent concerning the species status of populations *A* and *B* (Leaché *et al.*, 2019).

Second, the *gdi* may be large because the population is very small. Rannala and Yang (2020) recommended the use of absolute divergence time, such that two populations are considered distinct species only if their *gdi* > 0.7.

Assignment of individuals to populations and construction of the guide tree. Our pipeline requires the user to supply a guide tree. This may be inferred using a species tree estimation method under the MSC model with no gene flow (Yang, 2014; Rannala and Yang, 2017). Alternatives include maximum likelihood tree inference using concatenated data, or use of the mitochondrial genes.

The arbitrariness of the criterion. However, for mammals, a 10% CO1 (or cytb) divergence is a sure thing for distinct species.

Any empirical thresholds for particular criteria or properties will be imprecise, as it is recognized by multiple authors that such an attempt is futile Wells *et al.* (2022). While there can be no set of universal criteria or properties applicable to species delimitation, a heuristic approach does provide useful guide.

Molecular phylogenetic or population genetic analysis should always be integrated with an assessment of congruence with morphological and ecological data. Using genetic data, one should not exclude species generated by processes that do not automatically or immediately result in monophyly, such as hybrid speciation, polyploidy, or paraphyly in the case of recent ancestor-descendant speciation. Where molecular phylogenetic analysis is impractical due to inadequate samples or easily sequenced material, or where it fails to resolve well-supported relationships, species delimitation remains possible, but should be based on a strong hypothesis of phylogenetic relatedness resulting from multiple and unambiguous phenotypic and ecological traits.

The effects of sampling. Many empirical biologists

emphasized the importance of sampling: Chambers and Hillis (2020); Wells *et al.* (2022). Yang and Rannala (2017) has pointed out that rarity and singletons should not be a major problem. Migration rates can also be estimated when some species are missing or unsampled. Zhang *et al.* (2011) through simulation illustrated that failure to sample the intermediate populations in a stepping-stones design does not cause false positives for species delimitation by BPP.

Gene flow and non-monophyletic species

Analyses of genomic data in the past two decades have demonstrated the prevalence of interspecific gene flow. Several studies suggested evidence for speciation despite ongoing gene flow, as in *Heliconius* butterflies (Martin *et al.*, 2013), Mangrove trees (He *et al.*, 2019), and Western Pacific abalones (Hirase *et al.*, 2021). Issues arise when we want to delimit species when there is gene flow between the species or populations.

Bayesian model selection. First consider Bayesian model selection. There are three models for two populations (*A*, *B*): M1: one species, M2-0 two species with no migration, and M2-m two species with migration. Leaché *et al.* (2019) compare M1 and M2-0 to decide whether there are one or two species, even though the data were simulated with gene flow, and M2-m was not considered. Alternatively one may insist species status only if there is no significant amount of gene flow (i.e., only if M2-0 wins over M2-m), and consider M2-m as representing one species. This approach may suffer from over-lumping. **[Generate an example. What about the ABCDX dataset?]**

It is not so clear how to incorporate gene flow in the hierarchical merge and split algorithms. In Leaché *et al.* (2019), we used MSC with no gene flow (M2-0) to construct the guide tree, and then the merge or split algorithms rely on the MSC model with no gene flow. The migration model is used to simulate data but not used in analysis of the data. This way the guide tree of figure 3b (Leaché *et al.*, 2019) was incorrect, but we arrived at the correct answer of two species: *ABCD* and *X*. If we use the MSC-M model and use the correct guide tree with migration of figure 4a, there are two problems. First we will never recover the correct answer of two species by merging or splitting species and populations, keeping the migration events in the model. Second, when we merge populations according to the guide tree it may not be clear whether we want to keep the migration rate. For example if we merge *X* and *A*, it is unclear whether we want migration between *XA* and *B* since according to the guide tree there is gene flow between *A* and *B* but none between *X* and *B*. Another approach may be to populations that have high migration rates between them (with, $M > 1$, say), even if they are not sister lineages on the guide tree. For example, in the case of figure 4a, we will attempt to merge *AB*, *BC*, and *CD*, besides *XA*. Again there may

be ambiguities in the specification of migration events in the new model with merged populations.

PROGRAM AVAILABILITY

The pipeline is written in python, which drives parameter estimation under the MSC or MSC-M models using BPP. The source code, documentation, and empirical datasets analyzed in the paper are available at <https://github.com/abacus-gene/xxx>.

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SUPPLEMENTAL MATERIALS

*Extended Methods and Materials**Implementation details*

We use the example of the simulated data of figure 4 to illustrate the details of implementation.

A control file is used to specify the analysis procedure.

Output. The program output is self-explanatory (fig. S1).

```
seqfile = Leache_2019_sequences.txt
Imapfile = Leache_2019_starting_populations.txt
guide tree = ((A, B), (C, D)), X);

mode = merge
GDI threshold = 0.2
decision criteria = all

burnin = 50000
nsample = 100000
```

`seqfile` is the sequence alignment file in PHYLIP format. `Imapfile` specifies the mapping of individuals to populations. `guide tree` is a Newick representation of the guide tree topology. `mode` specifies the algorithm, with `split` for hierarchical split and `merge` for hierarchical merge. `GDI threshold` specifies the *gdi* value below which two populations are merged into a candidate species. `decision criteria` specifies how the *gdi* values should be interpreted. As a mutation rate is not specified, the number of generations cannot be inferred. Accordingly, the decision criteria of all currently indicates that both *gdi* values need to be less than the threshold (0.2) for two populations to be merged. `burnin` and `nsample` specify the settings for the MCMC run.

ACCEPTED SPECIES IN STARTING DELIMITATION:
A, B, C, D, X

ITERATION 1:

PROPOSED MERGE	GDI 1	GDI 2	MERGE ACCEPTED
'A', 'B'	0.0478	0.0326	True
'C', 'D'	0.0283	0.0229	True

THE FOLLOWING PROPOSALS TO MERGE WERE ACCEPTED:

- 1) 'A', 'B' -> 'AB'
- 2) 'C', 'D' -> 'CD'

ACCEPTED SPECIES AFTER ITERATION 1:
AB, CD, X

ITERATION 2:

PROPOSED MERGE	GDI 1	GDI 2	MERGE ACCEPTED
'AB', 'CD'	0.0689	0.0475	True

THE FOLLOWING PROPOSALS TO MERGE WERE ACCEPTED:

- 1) 'AB', 'CD' -> 'ABCD'

ACCEPTED SPECIES AFTER ITERATION 2:
ABCD, X

ITERATION 3:

PROPOSED MERGE	GDI 1	GDI 2	MERGE ACCEPTED
'ABCD', 'X'	0.3749	0.8766	False

ACCEPTED SPECIES AFTER ITERATION 3:
ABCD, X

ALL PROPOSALS REJECTED, FINAL DELIMITATION REACHED

Figure S1: Screen output from running the pipeline to analyze the simulated dataset of figure 4.

Table S1: Rate matrix for Markov chain describing transitions between states in multispecies coalescent with migration model with two populations (A and B) and three sequences (a_1, a_2 , and b).

	AAA	AAB	ABA	ABB	BAA	BAB	BBA	BBB	$A_{a_1}A$	$A_{a_2}A$	A_bA	$C_{a_1}B$	$B_{a_2}B$	B_bB	$A_{a_1}B$	$A_{a_2}B$	A_bB	AB_{a_1}	AB_{a_2}	AB_b	$A B$
AAA	.	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_A	C_A	C_A										
AAB	w_{AB}	.	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}												C_A	
ABA	w_{AB}	w_{AB}	.	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}												C_A	
ABB	w_{AB}	w_{AB}	w_{AB}	.	w_{BA}	w_{BA}	w_{BA}	w_{BA}							C_B						
BAA	w_{AB}	w_{AB}	w_{AB}	w_{AB}	.	w_{BA}	w_{BA}	w_{BA}								C_B				C_A	
BAB	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	.	w_{BA}	w_{BA}									C_B				
BBB	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	.	w_{BA}				C_B	C_B	C_B	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_A
$A_{a_1}A$.												C_A
$A_{a_2}A$.											C_A
A_bA											.										C_A
$B_{a_1}B$															w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	C_B
$B_{a_2}B$															w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	C_B
B_bB															w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	w_{AB}	C_B
$A_{a_1}B$									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
$A_{a_2}B$									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
A_bB									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
AB_{a_1}									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
AB_{a_2}									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
AB_b									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B
$A B$									w_{AB}	w_{AB}	w_{AB}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	w_{BA}	C_B

Note.— $w_{AB} = 4M_{AB}/\theta_B = m_{AB}/\mu$ and $w_{BA} = 4M_{BA}/\theta_A = m_{BA}/\mu$ are mutation-scaled migration rates, and $c_A = 2/\theta_A$ and $c_B = 2/\theta_B$ are the coalescent rates. The state of the chain is given by the population IDs (A or B) and sequence IDs (such as a_1, a_2, a_1a_2). For example the initial state $A_{a_1}A_{a_2}B_b$ means that the three sequences a_1, a_2 , and b are from populations A, A , and B , respectively. States with three sequences are abbreviated, with the three sequences assumed to be in the order a_1, a_2, b so that the sequence IDs are suppressed. Thus $A_{a_1}A_{a_2}B_b$ is ' AAB '. State $A_{a_1}a_2B_b$ means that two sequences remain in the sample, with the ancestor of sequences a_1 and a_2 is in population A while sequence b is in population B . This is abbreviated ' AB_b ', with the sequence ID ' a_1a_2 ' suppressed. ' $A|B$ ' is an absorbing state in which only one sequence remains in the sample, in either A or B , after two coalescent events have occurred. From Leaché *et al.* (2019).