

1. Marks of set of students for a certain subject are approximately normally distributed with mean 62 and variance 9. If 4 students are randomly selected what is probability that 3 of them have less than 60 marks.

Let X represent the marks obtained
 $\mu = 62$ $\sigma^2 = 9 \Rightarrow \sigma = 3$

$$X \sim N(\mu, \sigma^2)$$

$$Z \sim N(0, 1)$$

$$Z = \frac{X - \mu}{\sigma} = \frac{X - 62}{3}$$

~~For~~

$$Z_1 = \frac{60 - 62}{3} = -\frac{2}{3}$$

$$P(X < 60) = P(Z < -\frac{2}{3})$$

$$= P(Z < -0.67)$$

$$= 0.5 - P(0 < Z < 0.67)$$

$$= 0.5 - 0.2486$$

$$P = 0.2514 \quad \text{--- (1)}$$

\therefore For 3 students out of 4 have < 60 is of binomial distribution.
 $n = 4$ $x = 3$ $p = 0.2514$ $q = 1 - p$

$${}^4C_3 p^3 q^1 = 0.0475 \text{ is required ans}$$

2. The amount of time a postal clerk spends with his customers is known an exponential distribution with an average amount of time equal to 4 minutes. Find the probability that clerk spends 4 to 5 minutes with randomly selected customer.

Let X be the time spend
 $X \sim E(\beta)$

$$\frac{1}{\beta} = \frac{1}{\text{Mean}} = \frac{1}{4} \Rightarrow \beta = 4$$

$$P(4 < X < 5)$$

$$f(x) = \begin{cases} \frac{1}{\beta} e^{-x/\beta} & x \geq 0 \\ 0 & x < 0 \end{cases}$$

$$\therefore P(4 < X < 5) = \int_4^5 0.25 e^{-x/4} dx$$

$$= 0.25 \left[e^{-x/4} \right]_4^5 = 0.25 \left[e^{-5/4} - e^{-1} \right]$$

$$= 0.0625 \left[e^{-1.25} - e^{-1} \right]$$

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$$= 0.25 \cdot 4 \left[e^{-5/4} - e^{-1} \right] = 0.08137$$

3. On the average a certain computer part last ten year. The length of time the computer part last is exponentially distributed. What is the probability that a computer part lasts more than 7

Let X be the years lasts by computer

$$\text{Mean} = 10 \text{ yrs} = \beta$$

$$X \sim E(\beta)$$

$$f(x) = \begin{cases} \frac{1}{\beta} e^{-x/\beta} & x \geq 0 \\ 0 & x < 0 \end{cases}$$

$$P(X > 7)$$

$$P(X > 7) = \int_7^{\infty} \frac{1}{\beta} e^{-x/\beta} dx$$

$$= \frac{1}{\beta} \int_7^{\infty} e^{-x/\beta} dx$$

$$= \frac{1}{10} \cdot 10 \cdot \left[e^{-x/10} \right]_7^{\infty}$$

$$= e^{-7/10} = 0.4966$$