texti 1.1,1.2, little 1.3

try to say things

that make sonse.

If we want to understand rate of change at a point"

slape = rise = Dy - dy how much is x actually

changing? its not.

Lamits

We say that the limit of f(x) as x approaches a is L
to mean that: f(x) gets close to L whenever x
gets close to (but not equal to)
a.

ex: $f(x) = \frac{x}{2}$ as x approaches 4, f(x) approaches limit of 1/2 as xappronches 4 is 2. f 1x-4/(2 => -2 < x-4 < 2 $-1 < \frac{x}{2} - 2 < 1$ (x/2-2) < 1 can ne ensure | f(x) -2/24? Sur. |x-4| < = $-\frac{1}{4} \times \frac{x}{2} - 2 < \frac{1}{4}$ - 2 6 x - 4 < = 7. It does't mather what number you ask: we can always loit! if you pick ξ , can make $|\frac{x}{2}-2| 2\xi$ where 1x-4/ <28 - 22 CX-4 CZE= S -2 < \frac{\frac{1}{2}-2\frac{2}{2}}{2}

how clase can ue make it? as close as me want.

Definition lim f(x) = L (limit of f(x) as x gets clar to a
is L)
ineans, for any 200, there is a number 800.

so that If(x)-L/ < wherever oclx-al < &

exi lim = 2 = 2 should this by noticing that fr any x > 4 E70, if we let S = 2 & floor ifo<|x-4| < S = 2 \ + len | \frac{x}{2} - 2 | < \frac{6}{2} = \frac{2}{2}

Compute limits

Limit Facts

1. lim C = C

Constant

 $\lim_{x \to a} x = a$

Limit Laws

Suppose f(x), g(x) are functions and

lim f(x)=L, lim g(x)=M

xaa

xaa

tlen'
1. ((1)+c(x)) = L+M

4)
$$\lim_{x \to 0} \frac{x}{x} = 1$$
 (can't ox role 4)
 $\lim_{x \to 0} \frac{x}{x} = 1$ (can't ox role 4)

(can't ux role 4)

lim
$$\left(\frac{1}{x} + \left(-\frac{1}{x}\right)\right)$$
 $x \to 0$
 $x \to 0$
 $x \to 0$

exi
$$\lim_{x\to 2} 3x^2 - 1 = \lim_{x\to 2} 3x^2 + (-1)$$

 $= \lim_{x\to 2} 3x^2 + \lim_{x\to 2} (-1)$
 $= \lim_{x\to 2} 3x^2 + (-1)$
 $= 3\lim_{x\to 2} x^2 + (-1)$
 $= 3\lim_{x\to 2} (\lim_{x\to 2} x) (\lim_{x\to 2} x) + (-1)$

$$\frac{2}{3}(2)(2) - 1 = 3(2)^{2} - 1$$

$$\lim_{x \to 3} \frac{(x^{2} - 9) 2x}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3) 2x}{x - 3} \times \frac{43}{x - 3}$$

$$\lim_{x \to 3} \frac{(x^{2} - 9) 2x}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3) 2x}{x - 3}$$

$$\lim_{x \to 3} \frac{(x + 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x + 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_{x \to 3} \frac{(x - 3)(x - 3)(x - 3)(x - 3)}{x - 3} = \lim_$$