

Softmax exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission.

In this exercise, you will:

- implement a fully-vectorized **loss function** for the Softmax classifier
- implement the fully-vectorized expression for its **analytic gradient**
- **check your implementation** with numerical gradient
- use a validation set to **tune the learning rate and regularization** strength
- **optimize** the loss function with **SGD**
- **visualize** the final learned weights

Acknowledgement: This exercise is adapted from [Stanford CS231n](#).

```
import random
import numpy as np
from data_utils import load_CIFAR10
import matplotlib.pyplot as plt

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of
plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-
modules-in-ipython
%load_ext autoreload
%autoreload 2

def rel_error(out, correct_out):
    return np.sum(abs(out - correct_out) / (abs(out) +
abs(correct_out)))

def get_CIFAR10_data(num_training=49000, num_validation=1000,
num_test=1000, num_dev=500):
    """
    Load the CIFAR-10 dataset from disk and perform preprocessing to
    prepare
    it for the linear classifier. These are the same steps as we used
    for the
    Softmax, but condensed to a single function.
    """
    # Load the raw CIFAR-10 data
    cifar10_dir = 'datasets/cifar-10-batches-py'
```

```

X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# subsample the data
mask = range(num_training, num_training + num_validation)
X_val = X_train[mask]
y_val = y_train[mask]
mask = range(num_training)
X_train = X_train[mask]
y_train = y_train[mask]
mask = range(num_test)
X_test = X_test[mask]
y_test = y_test[mask]

# We will also make a development set, which is a small subset
of
the training set.
mask = np.random.choice(num_training, num_dev, replace=False)
X_dev = X_train[mask]
y_dev = y_train[mask]

# Preprocessing: reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_val = np.reshape(X_val, (X_val.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# Normalize the data: subtract the mean image
mean_image = np.mean(X_train, axis = 0)
X_train -= mean_image
X_val -= mean_image
X_test -= mean_image
X_dev -= mean_image

# add bias dimension and transform into columns
X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])

    return X_train, y_train, X_val, y_val, X_test, y_test, X_dev,
y_dev

# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev =
get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)

```

```

print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
print('dev data shape: ', X_dev.shape)
print('dev labels shape: ', y_dev.shape)

Train data shape: (49000, 3073)
Train labels shape: (49000,)
Validation data shape: (1000, 3073)
Validation labels shape: (1000,)
Test data shape: (1000, 3073)
Test labels shape: (1000,)
dev data shape: (500, 3073)
dev labels shape: (500,)

# Create one-hot vectors for label
num_class = 10
y_train_oh = np.zeros((y_train.shape[0], 10))
y_train_oh[np.arange(y_train.shape[0]), y_train] = 1
y_val_oh = np.zeros((y_val.shape[0], 10))
y_val_oh[np.arange(y_val.shape[0]), y_val] = 1
y_test_oh = np.zeros((y_test.shape[0], 10))
y_test_oh[np.arange(y_test.shape[0]), y_test] = 1

y_dev_oh = np.zeros((y_dev.shape[0], 10))
y_dev_oh[np.arange(y_dev.shape[0]), y_dev] = 1

```

Regression as classifier

The most simple and straightforward approach to learn a classifier is to map the input data (raw image values) to class label (one-hot vector). The loss function is defined as following:

$$L = \frac{1}{n} \| XW - y \|_F^2 \quad (1)$$

Where:

- $W \in R^{(d+1) \times C}$: Classifier weight
- $X \in R^{n \times (d+1)}$: Dataset
- $y \in R^{n \times C}$: Class label (one-hot vector)

Optimization

Given the loss function (1), the next problem is how to solve the weight W . We now discuss 2 approaches:

- Random search
- Closed-form solution

Random search

```
bestloss = float('inf')
for num in range(100):
    W = np.random.randn(3073, 10) * 0.0001
    loss = np.linalg.norm(X_dev.dot(W) - y_dev_oh)
    if (loss < bestloss):
        bestloss = loss
        bestW = W
    print('in attempt %d the loss was %f, best %f' % (num, loss,
bestloss))
```

```
in attempt 0 the loss was 31.646948, best 31.646948
in attempt 1 the loss was 34.008923, best 31.646948
in attempt 2 the loss was 37.093963, best 31.646948
in attempt 3 the loss was 36.530236, best 31.646948
in attempt 4 the loss was 34.392341, best 31.646948
in attempt 5 the loss was 35.102759, best 31.646948
in attempt 6 the loss was 32.668202, best 31.646948
in attempt 7 the loss was 32.214424, best 31.646948
in attempt 8 the loss was 34.549410, best 31.646948
in attempt 9 the loss was 31.578647, best 31.578647
in attempt 10 the loss was 33.946023, best 31.578647
in attempt 11 the loss was 35.252005, best 31.578647
in attempt 12 the loss was 34.363430, best 31.578647
in attempt 13 the loss was 31.739588, best 31.578647
in attempt 14 the loss was 34.230789, best 31.578647
in attempt 15 the loss was 32.226306, best 31.578647
in attempt 16 the loss was 32.191760, best 31.578647
in attempt 17 the loss was 35.079365, best 31.578647
in attempt 18 the loss was 35.081925, best 31.578647
in attempt 19 the loss was 32.988724, best 31.578647
in attempt 20 the loss was 32.818960, best 31.578647
in attempt 21 the loss was 33.670704, best 31.578647
in attempt 22 the loss was 33.811987, best 31.578647
in attempt 23 the loss was 35.268279, best 31.578647
in attempt 24 the loss was 32.524998, best 31.578647
in attempt 25 the loss was 34.745619, best 31.578647
in attempt 26 the loss was 30.797645, best 30.797645
in attempt 27 the loss was 31.929377, best 30.797645
in attempt 28 the loss was 32.808447, best 30.797645
in attempt 29 the loss was 31.873468, best 30.797645
in attempt 30 the loss was 34.827538, best 30.797645
in attempt 31 the loss was 33.564244, best 30.797645
in attempt 32 the loss was 33.020578, best 30.797645
in attempt 33 the loss was 33.478551, best 30.797645
in attempt 34 the loss was 35.949671, best 30.797645
in attempt 35 the loss was 31.421600, best 30.797645
in attempt 36 the loss was 32.676920, best 30.797645
in attempt 37 the loss was 34.012656, best 30.797645
in attempt 38 the loss was 32.388713, best 30.797645
```

in attempt 39 the loss was 31.007192, best 30.797645
in attempt 40 the loss was 34.393742, best 30.797645
in attempt 41 the loss was 33.334930, best 30.797645
in attempt 42 the loss was 33.225607, best 30.797645
in attempt 43 the loss was 33.512755, best 30.797645
in attempt 44 the loss was 34.074827, best 30.797645
in attempt 45 the loss was 32.564844, best 30.797645
in attempt 46 the loss was 34.448253, best 30.797645
in attempt 47 the loss was 34.395739, best 30.797645
in attempt 48 the loss was 36.757437, best 30.797645
in attempt 49 the loss was 32.045727, best 30.797645
in attempt 50 the loss was 38.332217, best 30.797645
in attempt 51 the loss was 31.324367, best 30.797645
in attempt 52 the loss was 32.303588, best 30.797645
in attempt 53 the loss was 34.367892, best 30.797645
in attempt 54 the loss was 35.144431, best 30.797645
in attempt 55 the loss was 34.130066, best 30.797645
in attempt 56 the loss was 34.230622, best 30.797645
in attempt 57 the loss was 31.953963, best 30.797645
in attempt 58 the loss was 34.968321, best 30.797645
in attempt 59 the loss was 35.372038, best 30.797645
in attempt 60 the loss was 34.026372, best 30.797645
in attempt 61 the loss was 32.280270, best 30.797645
in attempt 62 the loss was 36.925841, best 30.797645
in attempt 63 the loss was 31.603271, best 30.797645
in attempt 64 the loss was 31.871215, best 30.797645
in attempt 65 the loss was 34.586772, best 30.797645
in attempt 66 the loss was 36.134483, best 30.797645
in attempt 67 the loss was 33.077824, best 30.797645
in attempt 68 the loss was 34.574326, best 30.797645
in attempt 69 the loss was 31.052882, best 30.797645
in attempt 70 the loss was 36.139611, best 30.797645
in attempt 71 the loss was 32.894288, best 30.797645
in attempt 72 the loss was 30.797714, best 30.797645
in attempt 73 the loss was 34.740489, best 30.797645
in attempt 74 the loss was 33.651901, best 30.797645
in attempt 75 the loss was 33.284834, best 30.797645
in attempt 76 the loss was 34.038722, best 30.797645
in attempt 77 the loss was 31.285261, best 30.797645
in attempt 78 the loss was 34.206383, best 30.797645
in attempt 79 the loss was 32.988481, best 30.797645
in attempt 80 the loss was 34.219089, best 30.797645
in attempt 81 the loss was 33.479736, best 30.797645
in attempt 82 the loss was 31.059631, best 30.797645
in attempt 83 the loss was 33.109615, best 30.797645
in attempt 84 the loss was 35.419799, best 30.797645
in attempt 85 the loss was 33.375349, best 30.797645
in attempt 86 the loss was 34.854809, best 30.797645
in attempt 87 the loss was 36.083109, best 30.797645
in attempt 88 the loss was 34.652516, best 30.797645

```

in attempt 89 the loss was 34.575511, best 30.797645
in attempt 90 the loss was 33.407179, best 30.797645
in attempt 91 the loss was 29.729416, best 29.729416
in attempt 92 the loss was 34.818540, best 29.729416
in attempt 93 the loss was 33.306617, best 29.729416
in attempt 94 the loss was 32.641330, best 29.729416
in attempt 95 the loss was 34.379827, best 29.729416
in attempt 96 the loss was 37.666729, best 29.729416
in attempt 97 the loss was 33.581988, best 29.729416
in attempt 98 the loss was 33.696833, best 29.729416
in attempt 99 the loss was 34.947318, best 29.729416

```

How bestW perform:

```

print('Accuracy on train set: ', np.sum(np.argmax(np.abs(1 -
X_dev.dot(W)), axis=1) ==
y_dev).astype(np.float32)/y_dev.shape[0]*100)
print('Accuracy on test set: ', np.sum(np.argmax(np.abs(1 -
X_test.dot(W)), axis=1) ==
y_test).astype(np.float32)/y_test.shape[0]*100)

```

Accuracy on train set: 8.4

Accuracy on test set: 9.0

You can clearly see that the performance is very low, almost at the random level.

Closed-form solution

The closed-form solution is achieved by:

$$\frac{\partial L}{\partial W} = \frac{2}{n} X^T (XW - y) = 0$$

$$\Leftrightarrow W^i = (X^T X)^{-1} X^T y$$

```

#####
#####
# TODO:
#
# Implement the closed-form solution of the weight W.
#
#####
#####
W =
np.linalg.inv(X_train.T.dot(X_train)).dot(X_train.T.dot(y_train_oh))
#####
#####
#
#
#
#####
#####

```

END OF YOUR CODE

```
Train set accuracy: 51.163265306122454
Test set accuracy: 36.199999999999996
```

Regularization

$$L = \frac{1}{n} \|XW - y\|_F^2 + \lambda \|W\|_F^2 \quad (2)$$
$$\Leftrightarrow W^i = (X^T X + \lambda n I)^{-1} X^T y$$

#####

```
#####
    train_acc[i] = np.sum(np.argmax(np.abs(1 - X_train.dot(W)),
axis=1) == y_train).astype(np.float32)/y_train.shape[0]*100
    test_acc[i] = np.sum(np.argmax(np.abs(1 - X_test.dot(W)), axis=1)
== y_test).astype(np.float32)/y_test.shape[0]*100

plt.semilogx(lambdas, train_acc, 'r', label="Training accuracy")
plt.semilogx(lambdas, test_acc, 'g', label="Testing accuracy")

plt.legend()
plt.grid(True)
plt.show()
```



Question: Try to explain why the performances on the training and test set have such behaviors as we change the value of λ .

Your answer: The regularization parameter λ compensates for overfitting in the training examples by introducing a penalty in the loss function. Therefore as λ increases there is an decrease in its training accuracy while as we move towards an optimal λ , the test accuracy increases to a certain point. However after that point, the penalty is too high when updating the weights causing a fall in accuracy in the test examples as well.

Softmax Classifier

The predicted probability for the j -th class given a sample vector x and a weight W is:

$$P(y=j \mid x) = \frac{e^{-xw_j}}{\sum_{c=1}^C e^{-xw_c}}$$

softmax

Your code for this section will all be written inside **classifiers/softmax.py**.

```
# First implement the naive softmax loss function with nested loops.  
# Open the file classifiers/softmax.py and implement the  
# softmax_loss_naive function.
```

```
from classifiers.softmax import softmax_loss_naive  
import time
```

```
# Generate a random softmax weight matrix and use it to compute the  
loss.
```

```
W = np.random.randn(3073, 10) * 0.0001  
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)
```

```
# As a rough sanity check, our loss should be something close to -  
log(0.1).
```

```
print('loss: %f' % loss)  
print('sanity check: %f' % (-np.log(0.1)))
```

```
loss: 2.350621
```

```
sanity check: 2.302585
```

Question: Why do we expect our loss to be close to $-\log(0.1)$? Explain briefly.**

Your answer: There are 10 classes and the probability for a class to be the ground-truth class would be 0.1. Hence, the loss for random searching should be close to $-\log(0.1)$

Optimization

Random search

```
bestloss = float('inf')  
for num in range(100):  
    W = np.random.randn(3073, 10) * 0.0001  
    loss, _ = softmax_loss_naive(W, X_dev, y_dev, 0.0)  
    if (loss < bestloss):  
        bestloss = loss  
        bestW = W  
    print('in attempt %d the loss was %f, best %f' % (num, loss,  
bestloss))
```

in attempt 0 the loss was 2.346179, best 2.346179
in attempt 1 the loss was 2.351812, best 2.346179
in attempt 2 the loss was 2.304880, best 2.304880
in attempt 3 the loss was 2.262815, best 2.262815
in attempt 4 the loss was 2.417005, best 2.262815
in attempt 5 the loss was 2.331234, best 2.262815
in attempt 6 the loss was 2.311196, best 2.262815
in attempt 7 the loss was 2.318043, best 2.262815
in attempt 8 the loss was 2.274020, best 2.262815
in attempt 9 the loss was 2.382983, best 2.262815
in attempt 10 the loss was 2.405071, best 2.262815
in attempt 11 the loss was 2.378609, best 2.262815
in attempt 12 the loss was 2.345328, best 2.262815
in attempt 13 the loss was 2.395356, best 2.262815
in attempt 14 the loss was 2.387060, best 2.262815
in attempt 15 the loss was 2.403402, best 2.262815
in attempt 16 the loss was 2.401419, best 2.262815
in attempt 17 the loss was 2.295298, best 2.262815
in attempt 18 the loss was 2.297233, best 2.262815
in attempt 19 the loss was 2.305519, best 2.262815
in attempt 20 the loss was 2.338854, best 2.262815
in attempt 21 the loss was 2.356137, best 2.262815
in attempt 22 the loss was 2.372829, best 2.262815
in attempt 23 the loss was 2.343593, best 2.262815
in attempt 24 the loss was 2.392668, best 2.262815
in attempt 25 the loss was 2.383637, best 2.262815
in attempt 26 the loss was 2.337435, best 2.262815
in attempt 27 the loss was 2.338166, best 2.262815
in attempt 28 the loss was 2.352747, best 2.262815
in attempt 29 the loss was 2.438777, best 2.262815
in attempt 30 the loss was 2.328003, best 2.262815
in attempt 31 the loss was 2.364642, best 2.262815
in attempt 32 the loss was 2.336120, best 2.262815
in attempt 33 the loss was 2.350209, best 2.262815
in attempt 34 the loss was 2.313322, best 2.262815
in attempt 35 the loss was 2.374541, best 2.262815
in attempt 36 the loss was 2.344926, best 2.262815
in attempt 37 the loss was 2.312077, best 2.262815
in attempt 38 the loss was 2.395869, best 2.262815
in attempt 39 the loss was 2.403531, best 2.262815
in attempt 40 the loss was 2.323386, best 2.262815
in attempt 41 the loss was 2.428796, best 2.262815
in attempt 42 the loss was 2.379578, best 2.262815
in attempt 43 the loss was 2.412333, best 2.262815
in attempt 44 the loss was 2.351020, best 2.262815
in attempt 45 the loss was 2.391164, best 2.262815
in attempt 46 the loss was 2.396949, best 2.262815
in attempt 47 the loss was 2.333226, best 2.262815
in attempt 48 the loss was 2.375310, best 2.262815
in attempt 49 the loss was 2.362124, best 2.262815

in attempt 50 the loss was 2.352665, best 2.262815
in attempt 51 the loss was 2.348217, best 2.262815
in attempt 52 the loss was 2.328266, best 2.262815
in attempt 53 the loss was 2.346669, best 2.262815
in attempt 54 the loss was 2.342626, best 2.262815
in attempt 55 the loss was 2.300102, best 2.262815
in attempt 56 the loss was 2.358637, best 2.262815
in attempt 57 the loss was 2.337587, best 2.262815
in attempt 58 the loss was 2.359386, best 2.262815
in attempt 59 the loss was 2.397125, best 2.262815
in attempt 60 the loss was 2.277193, best 2.262815
in attempt 61 the loss was 2.393318, best 2.262815
in attempt 62 the loss was 2.384012, best 2.262815
in attempt 63 the loss was 2.342260, best 2.262815
in attempt 64 the loss was 2.353040, best 2.262815
in attempt 65 the loss was 2.367611, best 2.262815
in attempt 66 the loss was 2.320883, best 2.262815
in attempt 67 the loss was 2.339536, best 2.262815
in attempt 68 the loss was 2.359385, best 2.262815
in attempt 69 the loss was 2.417828, best 2.262815
in attempt 70 the loss was 2.372812, best 2.262815
in attempt 71 the loss was 2.400610, best 2.262815
in attempt 72 the loss was 2.383270, best 2.262815
in attempt 73 the loss was 2.428583, best 2.262815
in attempt 74 the loss was 2.287747, best 2.262815
in attempt 75 the loss was 2.374516, best 2.262815
in attempt 76 the loss was 2.339635, best 2.262815
in attempt 77 the loss was 2.318416, best 2.262815
in attempt 78 the loss was 2.385256, best 2.262815
in attempt 79 the loss was 2.377160, best 2.262815
in attempt 80 the loss was 2.317216, best 2.262815
in attempt 81 the loss was 2.421459, best 2.262815
in attempt 82 the loss was 2.287018, best 2.262815
in attempt 83 the loss was 2.362835, best 2.262815
in attempt 84 the loss was 2.345498, best 2.262815
in attempt 85 the loss was 2.329448, best 2.262815
in attempt 86 the loss was 2.386530, best 2.262815
in attempt 87 the loss was 2.344345, best 2.262815
in attempt 88 the loss was 2.366561, best 2.262815
in attempt 89 the loss was 2.327520, best 2.262815
in attempt 90 the loss was 2.352506, best 2.262815
in attempt 91 the loss was 2.381681, best 2.262815
in attempt 92 the loss was 2.343357, best 2.262815
in attempt 93 the loss was 2.373196, best 2.262815
in attempt 94 the loss was 2.344916, best 2.262815
in attempt 95 the loss was 2.379197, best 2.262815
in attempt 96 the loss was 2.301495, best 2.262815
in attempt 97 the loss was 2.368075, best 2.262815
in attempt 98 the loss was 2.377312, best 2.262815
in attempt 99 the loss was 2.379633, best 2.262815

```
# How bestW perform on trainset
scores = X_train.dot(bestW)
y_pred = np.argmax(scores, axis=1)
print('Accuracy on train set %f' % np.mean(y_pred == y_train))
```

```
# evaluate performance of test set
scores = X_test.dot(bestW)
y_pred = np.argmax(scores, axis=1)
print('Accuracy on test set %f' % np.mean(y_pred == y_test))
```

Accuracy on train set 0.159245

Accuracy on test set 0.171000

Compare the performance when using random search with *regression classifier* and *softmax classifier*. You can see how much useful the softmax classifier is.

Stochastic Gradient descent

Even though it is possible to achieve closed-form solution with softmax classifier, it would be more complicated. In fact, we could achieve very good results with gradient descent approach. Additionally, in case of very large dataset, it is impossible to load the whole dataset into the memory. Gradient descent can help to optimize the loss function in batch.

$$W^{t+1} = W^t - \alpha \frac{\partial L(x; W^t)}{\partial W^t}$$

Where α is the learning rate, L is a loss function, and x is a batch of training dataset.

```
# Complete the implementation of softmax_loss_naive and implement a
(naive)
```

```
# version of the gradient that uses nested loops.
```

```
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)
```

```
# Use numeric gradient checking as a debugging tool.
```

```
# The numeric gradient should be close to the analytic gradient.
```

```
from gradient_check import grad_check_sparse
```

```
f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 0.0)[0]
```

```
grad_numerical = grad_check_sparse(f, W, grad, 10)
```

```
# gradient check with regularization
```

```
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 1e2)
```

```
f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 1e2)[0]
```

```
grad_numerical = grad_check_sparse(f, W, grad, 10)
```

```
numerical: 0.037678 analytic: 0.037678, relative error: 1.396159e-06
```

```
numerical: -0.674141 analytic: -0.674141, relative error: 9.114512e-09
```

```
numerical: -1.477780 analytic: -1.477780, relative error: 3.556684e-09
```

```
numerical: 6.554071 analytic: 6.554071, relative error: 1.446550e-08
```

```
numerical: -1.233332 analytic: -1.233332, relative error: 7.925469e-09
```

```
numerical: 1.485715 analytic: 1.485715, relative error: 6.347583e-08
```

```
numerical: 3.297879 analytic: 3.297879, relative error: 3.526046e-08
numerical: 2.983203 analytic: 2.983203, relative error: 2.706680e-09
numerical: -0.215564 analytic: -0.215564, relative error: 6.702050e-09
numerical: 0.498396 analytic: 0.498396, relative error: 5.755922e-08
numerical: 1.351679 analytic: 1.351679, relative error: 7.027422e-09
numerical: 0.386922 analytic: 0.386922, relative error: 1.622620e-07
numerical: 4.262728 analytic: 4.262728, relative error: 7.455098e-09
numerical: 0.545613 analytic: 0.545613, relative error: 5.196671e-08
numerical: 1.189124 analytic: 1.189124, relative error: 2.962051e-08
numerical: 1.898937 analytic: 1.898937, relative error: 2.723462e-08
numerical: 0.513493 analytic: 0.513493, relative error: 5.892753e-08
numerical: -1.432516 analytic: -1.432516, relative error: 2.518735e-09
numerical: -2.212356 analytic: -2.212356, relative error: 2.626736e-09
numerical: 1.329182 analytic: 1.329182, relative error: 1.526368e-08
```

```
# Now that we have a naive implementation of the softmax loss function
and its gradient,
# implement a vectorized version in softmax_loss_vectorized.
# The two versions should compute the same results, but the vectorized
version should be
# much faster.
```

```
tic = time.time()
loss_naive, grad_naive = softmax_loss_naive(W, X_dev, y_dev, 0.00001)
toc = time.time()
print('naive loss: %e computed in %fs' % (loss_naive, toc - tic))
```

```
from classifiers.softmax import softmax_loss_vectorized
tic = time.time()
loss_vectorized, grad_vectorized = softmax_loss_vectorized(W, X_dev,
y_dev, 0.00001)
toc = time.time()
print('vectorized loss: %e computed in %fs' % (loss_vectorized, toc -
tic))
```

```
# We use the Frobenius norm to compare the two versions
# of the gradient.
```

```
grad_difference = np.linalg.norm(grad_naive - grad_vectorized,
ord='fro')
print('Loss difference: %f' % np.abs(loss_naive - loss_vectorized))
print('Gradient difference: %f' % grad_difference)
```

```
naive loss: 2.379633e+00 computed in 0.759134s
vectorized loss: 2.379633e+00 computed in 0.002994s
Loss difference: 0.000000
Gradient difference: 0.000000
```

```
from classifiers.linear_classifier import *
```

```
classifier = Softmax()
tic = time.time()
```

```
loss_hist = classifier.train(X_train, y_train, learning_rate=1e-7,  
reg=5e4,
```

```
num_iters=1500, verbose=True)
```

```
toc = time.time()
```

```
print('That took %fs' % (toc - tic))
```

```
iteration 0 / 1500: loss 1561.750528  
iteration 100 / 1500: loss 210.226041  
iteration 200 / 1500: loss 29.963198  
iteration 300 / 1500: loss 5.845058  
iteration 400 / 1500: loss 2.589247  
iteration 500 / 1500: loss 2.272963  
iteration 600 / 1500: loss 2.148371  
iteration 700 / 1500: loss 2.160891  
iteration 800 / 1500: loss 2.134328  
iteration 900 / 1500: loss 2.194744  
iteration 1000 / 1500: loss 2.124950  
iteration 1100 / 1500: loss 2.132936  
iteration 1200 / 1500: loss 2.208860  
iteration 1300 / 1500: loss 2.103605  
iteration 1400 / 1500: loss 2.089449  
That took 5.934543s
```

```
# Write the Softmax.predict function and evaluate the performance on  
both the
```

```
# training and validation set
```

```
y_train_pred = classifier.predict(X_train)
```

```
print('training accuracy: %f' % (np.mean(y_train == y_train_pred), ))
```

```
y_val_pred = classifier.predict(X_val)
```

```
print('validation accuracy: %f' % (np.mean(y_val == y_val_pred), ))
```

```
training accuracy: 0.306143
```

```
validation accuracy: 0.329000
```

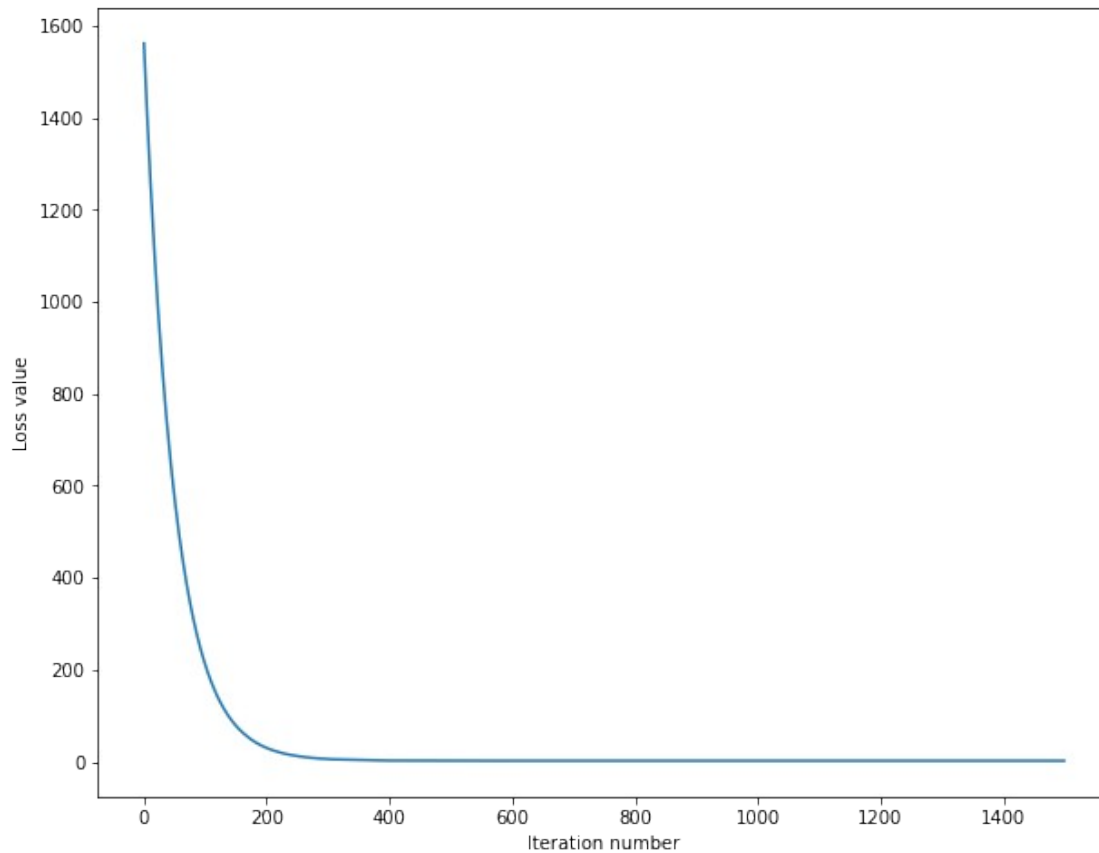
```
# A useful debugging strategy is to plot the loss as a function of  
# iteration number:
```

```
plt.plot(loss_hist)
```

```
plt.xlabel('Iteration number')
```

```
plt.ylabel('Loss value')
```

```
plt.show()
```



```
# evaluate on test set  
# Evaluate the best softmax on test set  
y_test_pred = classifier.predict(X_test)  
test_accuracy = np.mean(y_test == y_test_pred)  
print('softmax on raw pixels final test set accuracy: %.2f' %  
(100*test_accuracy, ))
```

softmax on raw pixels final test set accuracy: 32.00