

## Exercise Round 1 Daniel Kusnetsoff

### Task 1

a) Convert the four points below (cartesian x,y-coordinates) into their corresponding homogeneous coordinate form.

$$x_1 = [2; 1]$$

$$x_1 = \begin{matrix} 2 \times 1 \\ 2 \\ 1 \end{matrix}$$

$$x_1 = [2; 1; 1]$$

$$x_1 = \begin{matrix} 3 \times 1 \\ 2 \\ 1 \\ 1 \end{matrix}$$

$$x_2 = [1; -2]$$

$$x_2 = \begin{matrix} 2 \times 1 \\ 1 \\ -2 \end{matrix}$$

$$x_2 = [1; -2; 1]$$

$$x_2 = \begin{matrix} 3 \times 1 \\ 1 \\ -2 \\ 1 \end{matrix}$$

$$x_3 = [1; 1]$$

$$x_3 = \begin{matrix} 2 \times 1 \\ 1 \\ 1 \end{matrix}$$

$$x_3 = [1; 1; 1]$$

$$x_3 = \begin{matrix} 3 \times 1 \\ 1 \\ 1 \\ 1 \end{matrix}$$

$$x_4 = [-1; 0]$$

$$x_4 = \begin{matrix} 2 \times 1 \\ -1 \\ 0 \end{matrix}$$

$$x_4 = [-1; 0; 1]$$

$$\mathbf{x4} = \begin{pmatrix} 3 \times 1 \\ -1 \\ 0 \\ 1 \end{pmatrix}$$

b) The line  $\mathbf{l}$  through two points  $\mathbf{x}$  and  $\mathbf{x}'$  is  $\mathbf{l} = \mathbf{x} \times \mathbf{x}'$ . Use this to form two lines, line  $\mathbf{l1}$  through homogeneous points  $\mathbf{x1}$  and  $\mathbf{x2}$ , and  $\mathbf{l2}$  through  $\mathbf{x3}$  and  $\mathbf{x4}$ .

As  $\mathbf{l} = \mathbf{x} \times \mathbf{x}'$ ,

$$\mathbf{x}(\text{transpose}) * \mathbf{l} = \mathbf{x}(\text{transpose}) * \mathbf{x} \text{ cross}(\mathbf{x}') = 0$$

$$\mathbf{A} = \text{cross}(\mathbf{x1}, \mathbf{x2})$$

$$\mathbf{A} = \begin{pmatrix} 3 \times 1 \\ 3 \\ -1 \\ -5 \end{pmatrix}$$

$$\mathbf{B} = \text{cross}(\mathbf{x3}, \mathbf{x4})$$

$$\mathbf{B} = \begin{pmatrix} 3 \times 1 \\ 1 \\ -2 \\ 1 \end{pmatrix}$$

c. The intersection of two lines  $\mathbf{l}$  and  $\mathbf{l}'$  is the point  $\mathbf{x} = \mathbf{l} \times \mathbf{l}'$ . Use lines  $\mathbf{l1}$  and  $\mathbf{l2}$  to calculate their point of intersection and convert this back into cartesian coordinates.

$$\mathbf{C} = \text{cross}(\mathbf{A}, \mathbf{B})$$

$$\mathbf{C} = \begin{pmatrix} 3 \times 1 \\ -11 \\ -8 \\ -5 \end{pmatrix}$$

$$-11/5$$

$$\text{ans} = -2.2000$$

$$-8/5$$

$$\text{ans} = -1.6000$$

Point of intersection  $[-2.2; -1.6]$