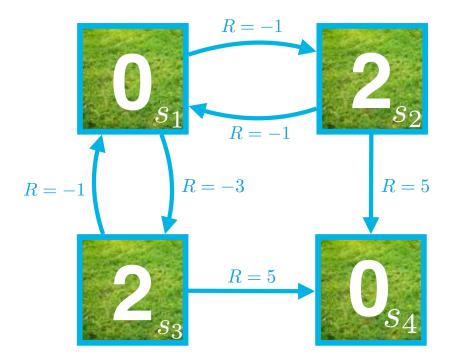


Action Values

Action Values

In a previous concept, you wrote your own implementation of iterative policy evaluation to estimate the state-value function v_π for a policy π . In this concept, you will use the simple gridworld from the videos to practice converting a state-value function v_π to an action-value function q_π .

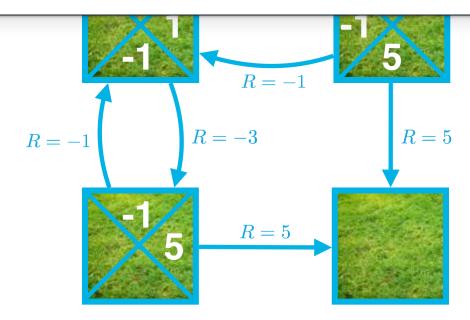
Consider the small gridworld that we used to illustrate iterative policy evaluation. The **state-value function** for the equiprobable random policy is visualized below.



Take the time now to verify that the below image corresponds to the **action-value function** for the same policy.



Action Values



As an example, consider $q_{\pi}(s_1, \text{right})$. This action value can be calculated as

$$q_{\pi}(s_1, \text{right}) = -1 + v_{\pi}(s_2) = -1 + 2 = 1$$
,

where we just use the fact that we can express the value of the state-action pair s_1 , \mathbf{right} as the sum of two quantities: (1) the immediate reward after moving right and landing on state s_2 , and (2) the cumulative reward obtained if the agent begins in state s_2 and follows the policy.

Please now use the state-value function v_{π} to calculate $q_{\pi}(s_1, \text{down})$, $q_{\pi}(s_2, \text{left})$, $q_{\pi}(s_2, \text{down})$, $q_{\pi}(s_3, \text{up})$, and $q_{\pi}(s_3, \text{right})$.

For More Complex Environments

In this simple gridworld example, the environment is **deterministic**. In other words, after the agent selects an action, the next state and reward are 100% guaranteed and non-random. For deterministic environments, $p(s',r|s,a) \in \{0,1\}$ for all s',r,s,a.

In this case, when the agent is in state s and takes action a, the next state s' and reward r can be predicted with certainty, and we must have $q_\pi(s,a)=r+\gamma v_\pi(s')$

.



Action Values

case, once the agent selects an action, the next state and reward cannot be predicted with certainty and instead are random draws from a (conditional) probability distribution p(s', r|s, a).

In this case, when the agent is in state s and takes action a, the probability of each possible next state s' and reward r is given by p(s',r|s,a). In this case, we must have $q_\pi(s,a) = \sum_{s' \in \mathcal{S}^+, r \in \mathcal{R}} p(s',r|s,a)(r+\gamma v_\pi(s'))$, where we take the expected value of the sum $r+\gamma v_\pi(s')$.

Over the next couple concepts, you'll use this equation to write a function that yields an action-value function q_{π} corresponding to a policy π for the FrozenLake environment.

NEXT