# Convolution and Pooling

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# Gliederung

- Convolutional Neural Networks
  - Convolution with one filter
  - Convolution with N filters
  - What does convolution do?
- 2 Pooling
- Application to NLP
- 4 Comparison: RNN vs. CNN

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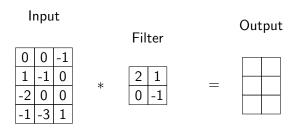
# Convolutional Neural Networks (CNNs)

- Technique from Computer Vision (e.g., object recognition in images)
- Alternative to RNNs for many (not all) NLP tasks
- General idea: Filter bank with N learnable filters

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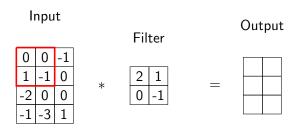
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- Move filter over input with step size (stride) s (here: 1)
- At every position, multiply filter and input entries together (elementwise), and sum the results into a single value



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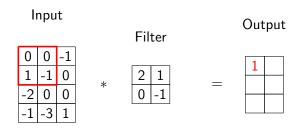
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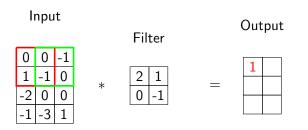


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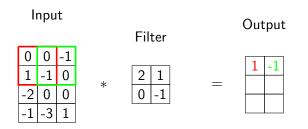


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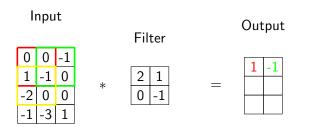
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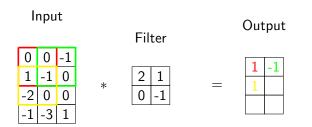
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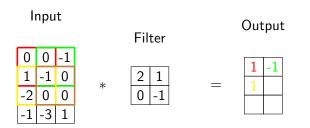
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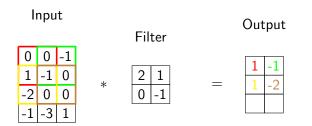
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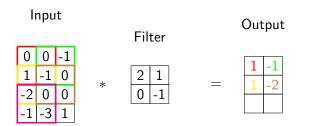
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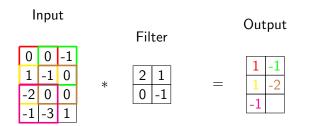
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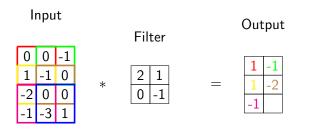


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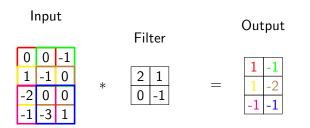
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## Building an edge detector filter

- Assume that -1 means black and +1 means white
- We want to build a filter that can detect diagonal edges where the upper left side is dark and the lower right side is bright
- = a filter that calculates a high positive number on windows that look like this:





 In CNNs, the filters are not manually chosen, but learned with gradient descent



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-3	-3	-3	-3	-3
-3	-3	-3	-3	3
-3	-3	-3	3	3
-3	-3	3	3	3
-3	3	3	3	3

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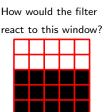


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#### Convolution with one filter: Tensor sizes

- Most images are not 2D but 3D
  - ▶ 3rd dimension is # channels, e.g., RGB values
  - ▶ image height × image width × # channels
- As a consequence, each filter is also 3D
  - ► filter height × filter width × # channels
- The operation stays the same, with an additional summation over the channel dimension

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- ullet Stack the N matrices on top of each other o 3D tensor, where the last dimension is N
- Also known as a feature map
- Feature map is slightly smaller than input (why?)

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- Also known as a feature map
- Feature map is slightly smaller than input (why?)
- Because a filter of size k fits into an input of size h only h k + 1 times
- ... unless we pad the input with zeros

### Convolution with N filters: Tensor sizes

- Tensor sizes:
  - ▶ **Input 3D**: input height  $\times$  input width  $\times$  # channels (if this is the first layer, otherwise # filters of previous layer)
  - Parameter tensor 4D: filter height × filter width × # channels × #filters
  - ▶ Output 3D: input height\* × input width\* × #filters
  - \*height and width are slightly reduced by convolution unless we do padding

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• Contextualization: Feature vector computed for position (i,j) contains info from (i-k,j-k) to (i+k,j+k) (where k is filter size).

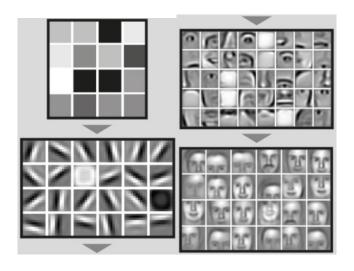
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- Locality-preserving: In one convolution layer, info can travel no further than k positions
- Computer Vision: Many convolutional layers applied one after another
- Typical nonlinearity between convolution layers: ReLU
- With every layer, feature maps become more complex
- $\bullet \ \mathsf{Pixels} \to \mathsf{edges} \to \mathsf{shapes} \to \mathsf{small} \ \mathsf{objects} \to \mathsf{bigger}, \ \mathsf{compositional}$

## Convolution



Source: Computer science: The learning machines. Nature (2014).

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- Often applied between convolution steps
- Divide feature map into "grid"
- Combine vectors inside the same grid cell with some operator
- Most popular: Average pooling, Max pooling
- Max pooling: only select maximum value for each dimension
- "Feature detector", "Cat neuron fires"

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0	2	0

2	1	2	0
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0	4	2	3
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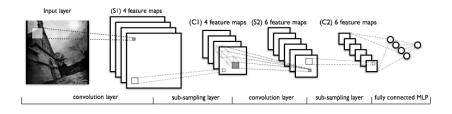


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## Convolution and Pooling: LeNet



LeCun et al. (1998). Gradient-based learning applied to document recognition.

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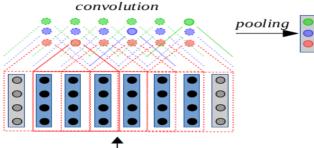
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#### Convolution for NLP

- Images have width and height, but text only has "width" (length)
- ullet o We can discard the "height" dimension from our filters
- Tensor sizes (in NLP):
  - ▶ Input 2D: sentence length × # channels (word embedding size, or # filters of previous convolution)
  - **Parameter tensor 3D**: filter length  $\times$  # channels  $\times$  #filters
  - ▶ Output 2D: sentence length\* × #filters
  - \*length slightly reduced unless we do padding
- Computer vision: 2D convolution (over height and width)
- NLP: 1D convolution (over length)
- Typically fewer convolutional layers than Computer Vision

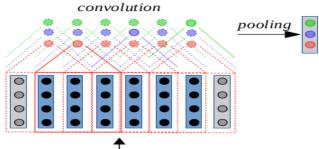
### Pooling for NLP

- Pooling between convolutional layers less frequently used than in Computer Vision
- After last convolutional layer: "global" pooling step
- Calculate max/average over the entire sequence ("pooling over time")

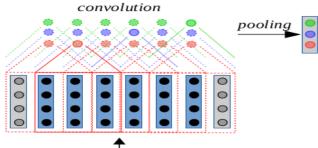


the sopranos was the best show

▶ What is the unpadded input size (=length)?

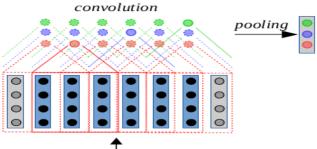


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- ▶ What is the unpadded input size (=length)? 6
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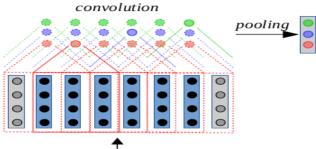
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- ▶ What is the unpadded input size (=length)? 6
- ▶ What is the padded input size? 8
- How many filters?



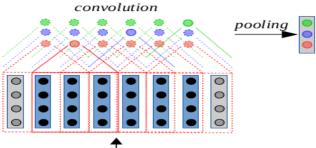
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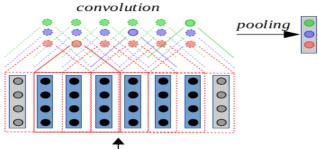
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- What is the filter size (=filter width)?



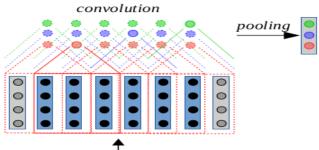
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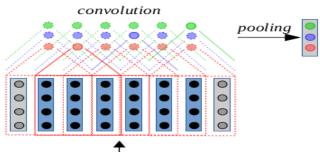
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- What is the output size of the convolution operation?



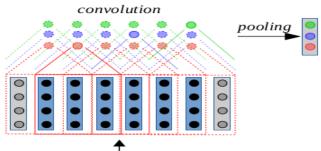
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- ▶ What is the output size of the convolution operation?  $6 \times 3$
- What is the output size of the pooling operation?



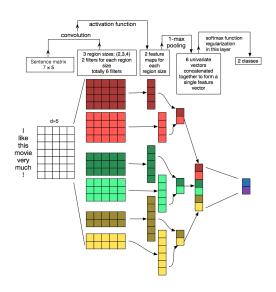
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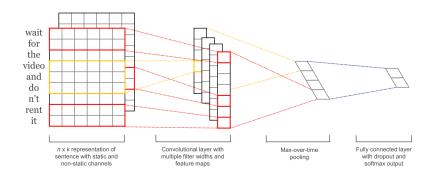


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- ► How many parameters have to be learned?  $3 \times 3 \times 4 = 36$



Source: Zhang, Y., & Wallace, B. (2015). A Sensitivity Analysis of ConvNets for Sentence Classification. , 4 🚊 👂 💂 🥒 🖅 😞



Source: Kim, Y. (2014). Convolutional Neural Networks for Sentence Classification.

```
# binary classifier, e.g., sentiment polarity
from keras.layers import Embedding, Conv1D, GlobalMaxPooling1D, Dense
from keras.models import Sequential
embedding = Embedding(input_dim = VOCAB_SIZE, output_dim = EMB_DIM)
conv layer = Conv1D(filters = NUM FILTERS, kernel size = FILTER WIDTH,
        activation = "relu")
pool_layer = GlobalMaxPooling1D()
dense laver = Dense(units = 1. activation = "sigmoid")
model = Sequential(layers = [emb_layer, conv_layer, pool_layer, dense_layer])
model.compile(loss = "binary crossentropy", optimizer = "sgd")
X, Y = \# load_data()
model.fit(X, Y)
```

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#### RNN vs. CNN

#### Range

- ▶ CNN: Cannot capture dependencies with range above  $k \times L$  (where k is filter width and L is the number of layers
- ► RNN: Can capture long-range dependencies
- Information transport
  - RNN: Must learn to "transport" salient information across many time steps.
  - ► CNN: No information transport across time, salient information "fast-tracked" by global max pooling
- Efficiency
  - lacktriangleright RNN: Sequential data processing ightarrow not parallelizable over time
  - ightharpoonup CNN: Input windows are independent from one another ightarrow highly parallelizable over time

- Given a task description, choose appropriate architecture!
  - ► Task: predict the number of the main verb (sleep or sleeps)
    - ★ The cats, who were sitting on the map inside the house, [sleep/sleeps?]
  - ▶ Which architecture should we use?

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    - \* [... many useless sentences ...] best book ever [... many useless sentences ...]
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  - ► Attention gives CNNs the ability to capture long-range dependencies, while maintaining parallel processing (Gehring et al.)
  - ▶ More about attention: Next week

#### Next week?

- Attention
- Keras advanced features
- Adversarial training
- Generative pre-training (a.k.a. Elmo & Bert)