



Figure 1: Wire displacement about the undisplaced center (dashed) line. Undisplaced wires are separated by a distance,  $s$ .

This is all worked out in Fabio Sauli's CERN report, Principles of Operation of Multiwire Proportional and Drift Chambers. [http://lhcb-muon.web.cern.ch/lhcb-muon/documents/Sauli\\_77-09.pdf](http://lhcb-muon.web.cern.ch/lhcb-muon/documents/Sauli_77-09.pdf).

## 0.1 Problem 1

$$F = qE = (CV_0)E \quad (1)$$

$$= (CV_0) \frac{q}{2\pi\epsilon_0} \frac{1}{r} \quad (2)$$

$$= \frac{(CV_0)^2}{2\pi\epsilon_0} \frac{1}{r} \quad (3)$$

## 0.2 Problem 2

$$\sum_n F_{\perp n} \simeq 2 \sum_n \frac{(CV_0)^2}{2\pi\epsilon_0} \frac{2\delta}{n^2 s^2} = \frac{(CV_0)^2 \pi}{4\epsilon_0} \frac{\delta}{s^2} \quad (4)$$

## 0.3 Problem 3

The wire's displacement  $\delta$  is really a function of the position along the length of the wire,  $\delta(x)$ .  $\delta(0) = \delta(L) = 0$  because the wires are fixed at the end.

The restoring force should be equal and opposite of the tension in Equation 4.

$$R = T \frac{d^2 \delta(x)}{dx^2} = -\frac{(CV_0)^2 \pi}{4\varepsilon_0} \frac{\delta(x)}{s^2} \quad (5)$$

$$\delta(x) = \delta_0 \sin \left( \frac{CV_0}{2s} \sqrt{\frac{\pi}{\varepsilon_0 T}} x \right) \quad (6)$$

$$\frac{CV_0}{2s} \sqrt{\frac{\pi}{\varepsilon_0 T}} L = \pi \rightarrow T = \frac{1}{4\pi\varepsilon_0} \left( \frac{CV_0 L}{s} \right)^2 \quad (7)$$