

(1) 1요인 변량효과 분산분석 모형

$$E(MSTR) = \sigma^2 + n' \sigma_{\mu}^2, \quad n' = (N - \sum n_i^2 / N) / (p - 1)$$

(2) 반복이 없는 2요인 모형

변인	EMS		
	Fixed	Random	Mixed(A:고정, B:변량)
A	$\sigma^2 + \frac{b}{a-1} \sum_i \alpha_i^2$	$\sigma^2 + b\sigma_{\alpha}^2$	$\sigma^2 + \frac{b}{a-1} \sum_i \alpha_i^2$
B	$\sigma^2 + \frac{a}{b-1} \sum_j \beta_j^2$	$\sigma^2 + a\sigma_{\beta}^2$	$\sigma^2 + a\sigma_{\beta}^2$

(3) 반복이 있는 2요인 모형

변인	EMS		
	Fixed	Random	Mixed(A:고정, B:변량)
A	$\sigma^2 + \frac{nb}{a-1} \sum_i \alpha_i^2$	$\sigma^2 + n\sigma_{(\alpha\beta)}^2 + nb\sigma_{\alpha}^2$	$\sigma^2 + n\sigma_{(\alpha\beta)}^2 + \frac{nb}{a-1} \sum_i \alpha_i^2$
B	$\sigma^2 + \frac{na}{b-1} \sum_j \beta_j^2$	$\sigma^2 + n\sigma_{(\alpha\beta)}^2 + na\sigma_{\beta}^2$	$\sigma^2 + na\sigma_{\beta}^2$
(AB)	$\sigma^2 + \frac{n}{(a-1)(b-1)} \sum_{ij} (\alpha\beta)_{ij}^2$	$\sigma^2 + n\sigma_{(\alpha\beta)}^2$	$\sigma^2 + n\sigma_{(\alpha\beta)}^2$

(4) 반복 측정 분산 분석

1) 단일 요인 반복 측정 분산 분석

- $E(MSB) = \sigma^2 + p\sigma_s^2$
- $E(MSTR) = \sigma^2 + n \sum \tau_j^2 / (p - 1)$

2) 다요인 반복 측정 분산 분석

- $E(MSA) = \sigma^2 + b\sigma_s^2 + bs \sum \alpha_j^2 / (a - 1)$
- $E(MSB) = \sigma^2 + as \sum \beta_k^2 / (b - 1)$
- $E(MS(AB)) = \sigma^2 + s \sum \sum (\alpha\beta)_{jk}^2 / ((a - 1)(b - 1))$
- $E(MSS(A)) = \sigma^2 + b\sigma_s^2$