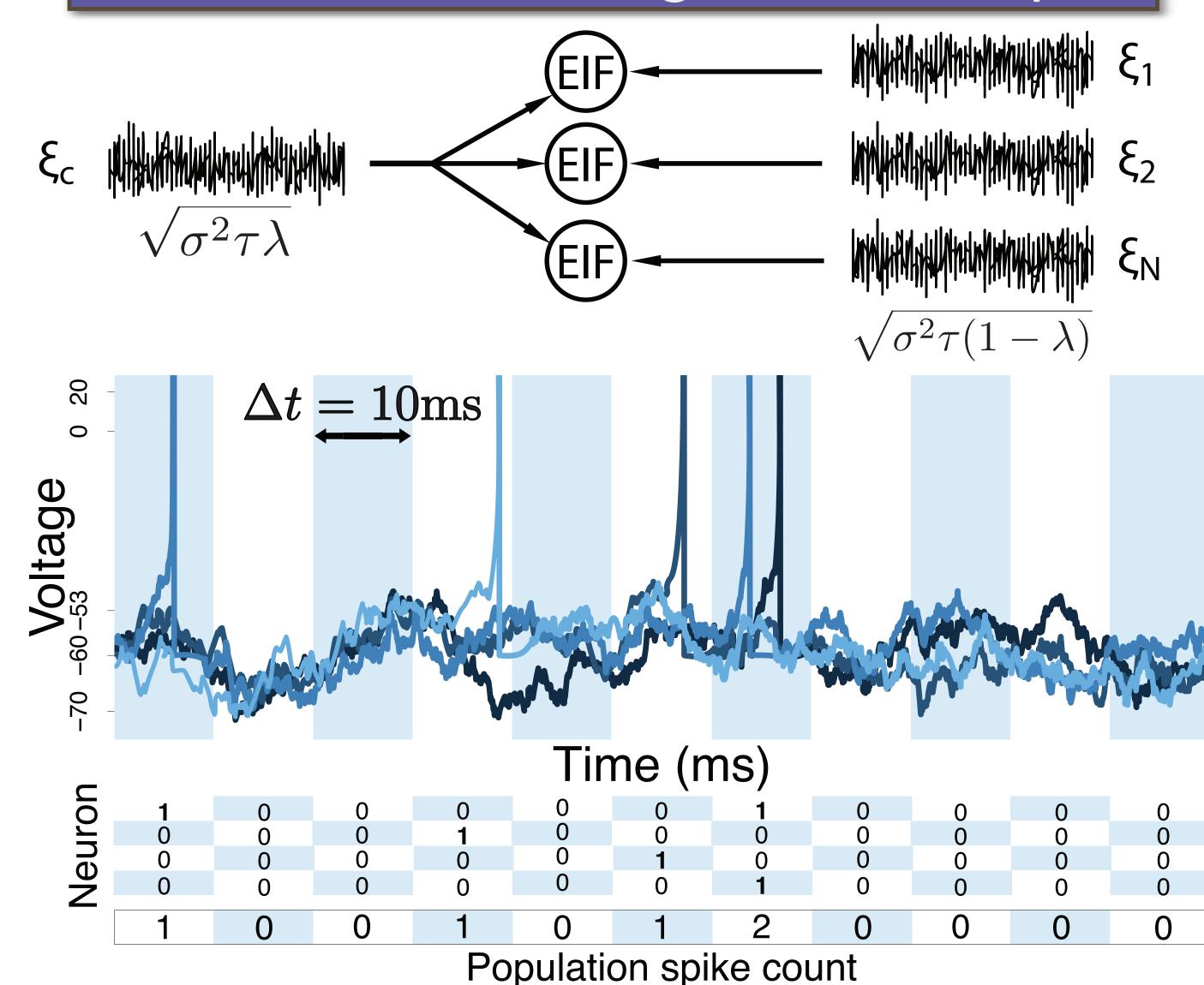
Introduction

- This study asks whether common input to integrate-and-fire neurons gives rise to higher-order correlations.
- A tractable reduction of the EIF model the linear-nonlinear cascade is used to provide an analytic description of our results.
- The Dichotomized Gaussian model provides an excellent description of the EIF setup.
- Finally we compare the LNL cascade to the Dichotomized Gaussian model.

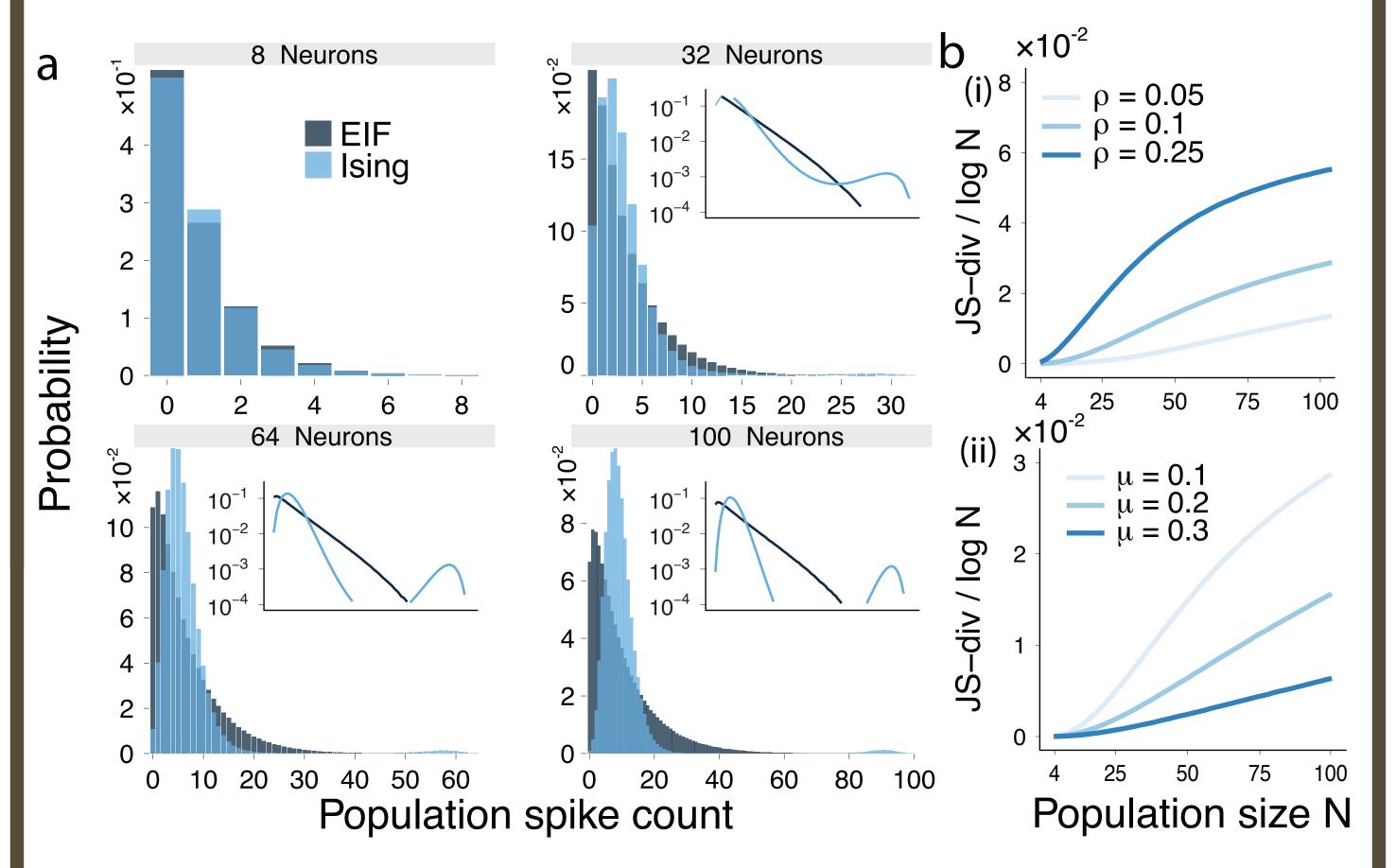
EIF neurons receiving common input



 The voltage of the EIF neurons evolves according to the eqn: $\tau_m V_i' = -V_i + \psi(V_i) + I(t)$ where $\psi(V_i) = \Delta_T \exp\left((V_i - V_S)/\Delta_T\right)$ defines the EIF neuron and the input current is:

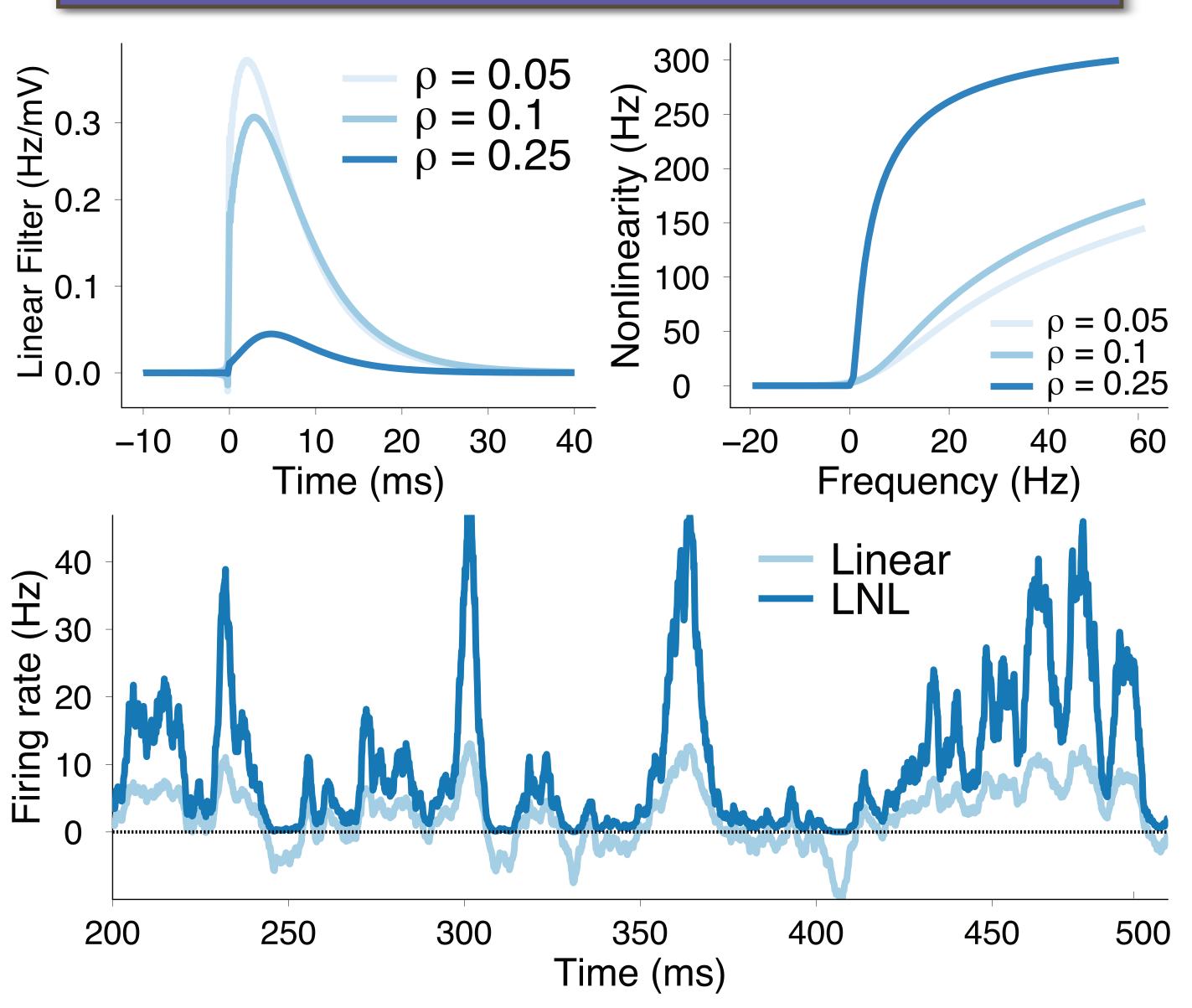
$$I(t) = \gamma + \sqrt{\sigma^2 \tau} \left[\sqrt{1 - \lambda \xi_i(t)} + \sqrt{\lambda \xi_c(t)} \right]$$

- Time is divided into bins of 10ms. A spike occurs when the voltage reaches a threshold of 20mV. The voltage is reset to the rest potential of -60mV and the neuron remains silent for the refractory period of 3ms.
- Mean firing rate is measured as the mean number of spikes per bin: $\mu=0.1$ Correlation coefficient is: $\rho = 0.1$



• Exponential integrate-and-fire neurons receiving common input give rise to higherorder correlations i.e. not well described by pairwise maximum entropy model

Linear-nonlinear cascade approximation



The firing rate is estimated as:

$$r(t) = F(r_0 + A * c(t))$$

where A(t) is the linear filter and F is the static non-linearity and c(t) is the common input.

 For an inhomogeneous poisson process with rate r(t) and common input c(t) the probability of a spike occuring in the interval $[t, t + \Delta t]$:

$$P(\text{spike} \in \Delta t | c) = 1 - \exp\left(-\int_0^{\Delta t} r(s+t) ds\right)$$

A simple mechanism for higher-order correlations in integrate-and-fire neurons

David Leen† and Eric Shea-Brown†‡

dleen@uw.edu

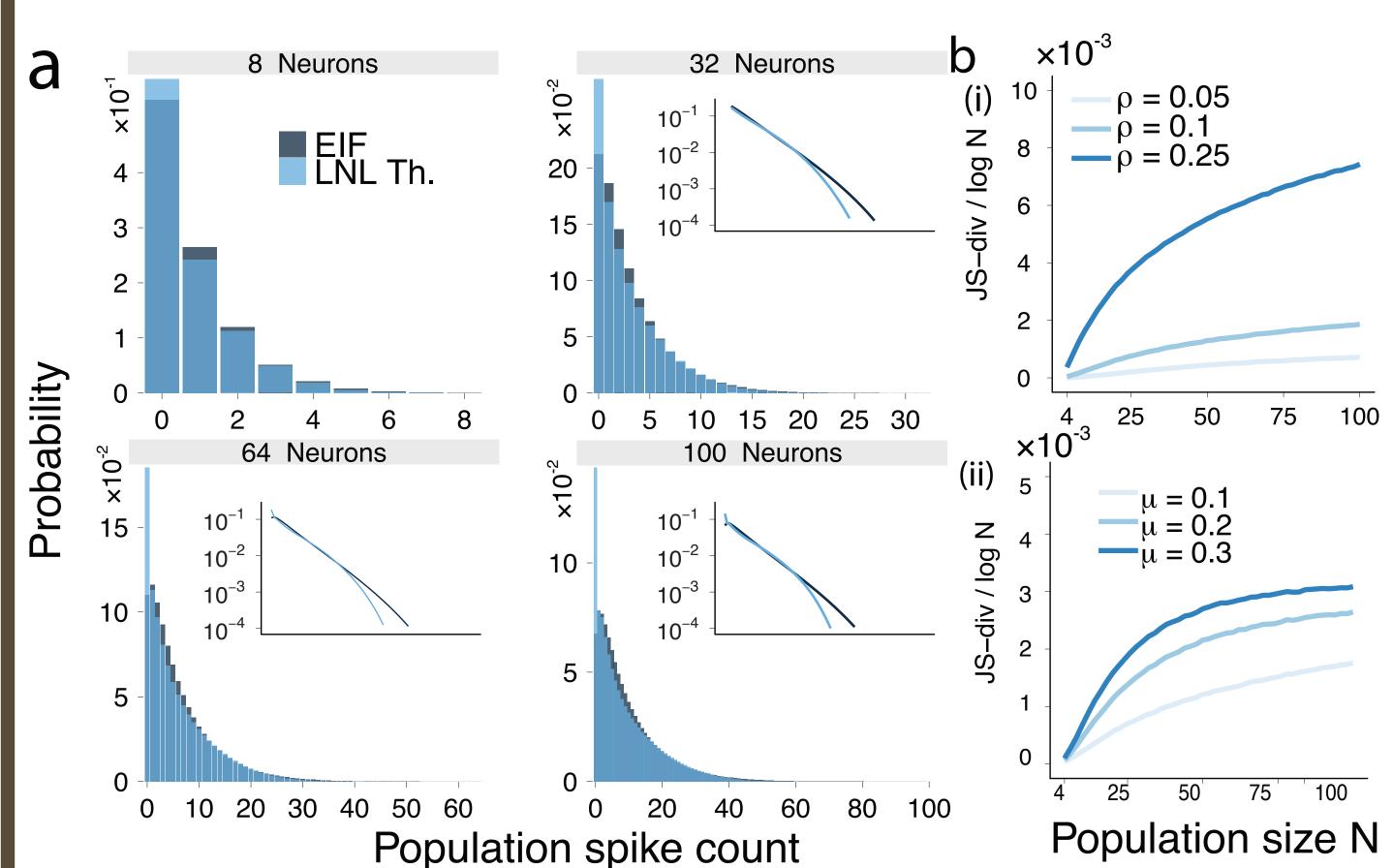
etsb@uw.edu



• By defining a new variable: $S = \int_{-\infty}^{\Delta t} r(s+t) \mathrm{d}s$ and the function: $\tilde{L}(\mathcal{S}) = 1 - \exp(-\tilde{\mathcal{S}})$ we can write the probability of observing k spikes occuring out of a population of n homogeneous neurons as:

$$P_{\rm LF}(k) = \binom{n}{k} \int_{-\infty}^{\infty} \phi_{LF}(\mathcal{S}) \left(1 - \tilde{L}(\mathcal{S})\right)^{n-k} \tilde{L}(\mathcal{S})^k d\mathcal{S}$$

where $\phi_{LF}(\mathcal{S})$ is the pdf of the new variable.



 LNL-cascade does an order of magnitude better job than the PME model.

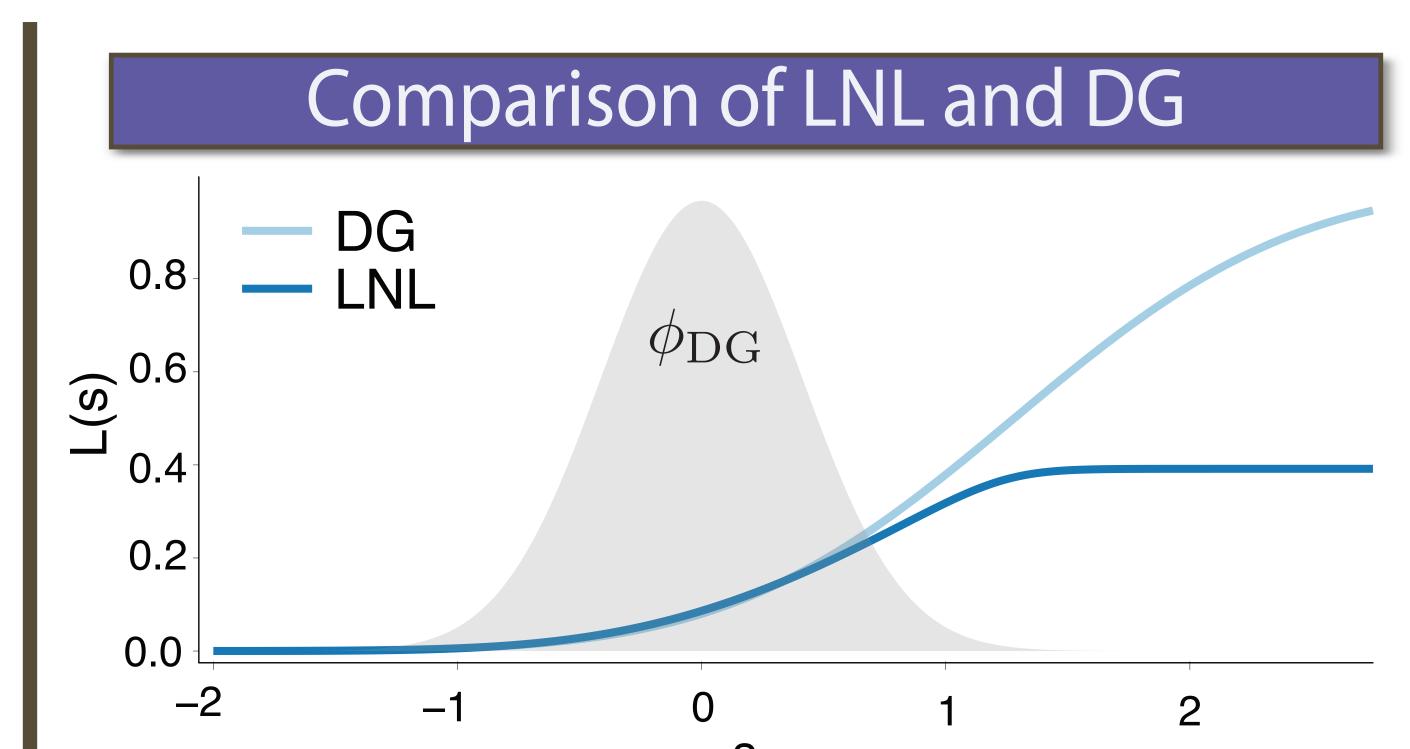
Dichotomized Gaussian model

- DG is a model of a binary neuron receiving a correlated Gaussian input. The neuron spikes if the input is positive and is silent otherwise.
- We can write the input as:

$$Z_i = \gamma + \sqrt{1 - \lambda} T_i + \sqrt{\lambda} S$$

 And so we can write the L(s) function like the previous section, using the CDF:

$$L(s) = \Phi\left(\frac{s+\gamma}{\sqrt{1-\lambda}}\right)$$



 By a change of variables, writing the LNL picture in terms of the DG, we can compare the L(s) functions over the support of the DG: ϕ_{DG}

Conclusions

[1] J. Macke, et. al. Common Input Explains Higher-Order Correlations and Entropy in a Simple Model of Neural Population Activity. PRL 106 May 2011 [2] S. Yu, et. al. Higher-Order Interactions Characterized in Cortical Activity

J. Neuroscience 31(48): 17514 Nov 2011 [3] S. Ostojic, N. Brunel. From Spiking Neuron Models to Linear-Nonlinear Models PLoS Comput Biol 7(1) 2011

[4] M. Richardson. Firing-rate response of linear and nonlinear integrateand-fire neurons... PRE 76 (2007)

This work was funded in part by the

Burroughs Wellcome Fund Scientific Interfaces Program.