# Algorithms and Problem Solving

#### Syllabus

#### **Classes**

- (1반) Tue. 10:30 & Thu. 13:00 (IT/BT 813, 202)
  - (2반) Tue. 16:00 & Thu. 9:00 (IT/BT 508)

Professor: 백은옥

eunokpaek@hanyang.ac.kr

#### Office Hour

- Tue. 15:00-16:00
- Thu 14:30-15:30

#### **Prerequisite**

Data structure

## Teaching Assistants

추유진

chooyu98@hanyang.ac.kr

박지선

sgs04023@hanyang.ac.kr

(02) 2220-4704

#### Evaluation

Exam 90% (Midterm I, II & Final)

Attendance 10%

4

# Introduction to Algorithms, 3<sup>rd</sup> Ed.

#### **MIT Press**

T. Cormen, C. Leiserson, R. Rivest, and C. Stein

Hanyang Univ.

#### **Topics**

#### Data structure

- List, stack, queue, skip list
- Trees: binary heap, BST, AVL, red-black tree, B-tree
- Hashing / Bloom filter
- Graph: Dijkstra algorithm

#### Algorithm

- Sorting: insertion, merge, quick, counting, radix
- Complexity analysis: Big-oh, recursion tree, amortized analysis, NP completeness
- Dynamic programming
- Graph: DFS, topological sort, minimum spanning tree, disjoint set, Bellman-Ford

6

#### What is an algorithm?

- What is a problem?
  - A well-specified input and output.
- What is an algorithm?
  - A well-defined procedure to solve a problem.

#### A problem example

- Cooking instant noodles
  - Input
    - chinese noodles,
    - Powder soup,
    - an egg,
    - green onions,...
  - Output
    - Cooked instant noodles

#### An algorithm example

#### Algorithm

- Boil 500cc of water.
- Put Chinese noodles and powder soup.
- Boil for 5 minutes.
- Put an egg and green onion.
- Boil for 1 minute.

#### A computer algorithm

# A computer algorithm

A well-defined computational procedure to solve a computational problem

# • A computational problem example

- Computing the sum of integers from 1 to n
  - $S = 1 + 2 \dots + n$

## Computer algorithm examples

# Elementary school algorithm

Compute each addition one by one from the left.

$$- S = (...(((1+2)+3)+4)...)+n$$

## High school algorithm

$$- S = n(n+1)/2$$

Are the algorithms above correct?

#### Correctness of algorithms

- Elementary school algorithm
  - Obvious
- High school algorithm

$$- S = n(n+1)/2$$

• 
$$2S = 2(1 + 2 + ... + n)$$

• 
$$2S = (1 + 2 + \dots n-1 + n) + (n + n-1 + \dots 2 + 1)$$

• 
$$2S = n(n+1)$$

• 
$$S = n(n+1)/2$$

## Comparison of algorithms

#### Which one is better?

- Elementary school algorithm
- High school algorithm

## Performance of algorithms

# Performance of algorithms

- Running time
- Space consumption

#### Performance of algorithms

## Performance of algorithms

- Running time
  - Elementary school algorithm?
  - High school algorithm?
- Space consumption
  - Elementary school algorithm?
  - High school algorithm?

#### Problem instance

#### Problem

- Computing the sum of integers from 1 to n
  - $S = 1 + 2 \dots + n$

#### A problem instance

- Computing the sum of integers from 1 to 100
  - 1 + 2 ... + 100

#### Class outline

#### Problem

- Why the problem?
- Problem definition.

# Algorithm

- Description
- Correctness
- Performance

7 Hanyang Univ.