$$i = \ell^2 + \ell + m + 1$$

$$0 \le \ell \le \ell_{\text{max}}$$

$$0 \le m \le m_{\text{max}}$$

$$(\ell, m) \le 100$$

$$x(0), \ldots, x(n-1), y(0), \ldots, y(n-1), z(0), \ldots, z(n-1)$$

```
x = \sin \theta \cos \phi
```

$$y = \sin \theta \sin \phi$$

$$z = \cos \theta$$

$$\cos^{-1}(\mathbf{V}.\mathbf{W})$$

$$2\sin^{-1}\left(||\mathbf{V} - \mathbf{W}||/2\right)$$

$$d_i = \operatorname{dist}(\mathbf{V}, \mathbf{W}_i)$$

$$d_i = \operatorname{dist}(\mathbf{V}_i, \mathbf{W})$$

$$d_i = \operatorname{dist}(\mathbf{V}_i, \mathbf{W}_i)$$

$$(x, y, z) = (1, 1, 1)/\sqrt{3}$$

$$\int d\mathbf{r} \ b(\mathbf{r}) \ Y_{\ell m}^*(\mathbf{r})$$

$$b_{\ell 0} \sqrt{\frac{4\pi}{2\ell + 1}}$$

$$\int b(\theta) P_{\ell}(\theta) \sin(\theta) \ d\theta \ 2\pi$$

 $\{0, \ldots, 4000\}$ 

$$C(b)\sqrt{2/((2l_b+1)\Delta l_b)}$$

$$l(l+1)/2\pi$$

$$b(\mathbf{r}) = \sum_{\ell m} b_{\ell m} Y_{\ell m}(\mathbf{r}),$$

$$b(\theta) = \sum_{\ell} b(\ell) P_{\ell}(\theta) \frac{2\ell + 1}{4\pi},$$

$$b(\ell) = b_{\ell 0} \sqrt{\frac{4\pi}{2\ell + 1}}$$

euler\_matrix\_new allows the generation of a rotation Euler matrix. The user can choose the three Euler angles, and the three axes of rotation. If vec is an  $N\times 3$  array containing N 3D vectors, vecr = vec # euler matrix new(a1,a2,a3,/Y)will be the rotated vectors. Alternatively, rotate coord can also be used to rotate vec into vecr. This routine supersedes euler matrix, which had inconsistent angle definitions. The relation between the two routines is as follows:  $euler\_matrix\_new(a,b,c,/X) = euler\_matrix(-a,-b,-c,/X)$  $= Transpose(euler\_matrix(c, b, a,/X))$ euler matrix new(a,b,c,/Y) = euler matrix(-a,b,-c,/Y) $= \text{Transpose}(\text{euler\_matrix}(c, -b, a, /Y))$  $euler_matrix_new(a,b,c,/Z) = euler_matrix(-a, b,-c,/Z)$ 

$$i = \ell^2 + \ell + m + 1.$$

$$\ell^2 + \ell + m + 1$$

$$C(\ell) = \sum_{m} a_{\ell m} a_{\ell m}^* / (2\ell + 1)$$

$$\ell(\ell+1)/2\pi$$

$$\ell(\ell+1)C(\ell)/2\pi$$

$$C(\ell)_{\text{meas}} = C(\ell)B(\ell)^2$$

should produce something like 196608 128 256 2 meaning that the map contained in that file has 196608 pixels, the resolution parameter is nside=128, the maximum multipole was 256. and this a full sky map (type 2).

$$C(\ell)_{\text{pix}} = C(\ell)W(\ell)^2$$

```
will print out
<Expression>
A+1
```

$$a_{\ell m}^{\rm OUT} = a_{\ell m}^{\rm IN} \frac{B^{\rm OUT}(\ell) P^{\rm OUT}(\ell)}{B^{\rm IN}(\ell) P^{\rm IN}(\ell)},$$

$$P(\ell) = 1$$



$$= \ell^2 + \ell + m + 1$$

$$y = \sinh^{-1}(x)$$

/ .,

$$y \approx \ln(2x)$$

$$y = \sinh^{-1}(x/2) / \ln(10)$$

$$y \approx \log(x)$$

..., 20 $\{2,$ 

$$P = \sqrt{U^2 + Q^2}$$

$$\phi = \tan^{-1}(U/Q)/2$$

$$\{1,\ldots,2^{29}\}$$

$$N_w \simeq N_{\rm pix}/16$$

$$N_w = \frac{(N_{\text{side}} + 1)(3N_{\text{side}} + 1)}{4}.$$

$$N_{\text{template}} = \frac{1 + N_{\text{side}}(N_{\text{side}} + 6)}{4}.$$

$$x(0),\ldots,x(n-1),$$

$$y(0),\ldots,y(n-1),$$

$$z(0),\ldots,z(n-1).$$

$$x_N(0),\ldots,x_N(n-1),$$

$$y_N(0),\ldots,y_N(n-1),$$

$$z_N(0),\ldots,z_N(n-1),$$

$$x_W(0),\ldots,x_W(n-1),$$

$$y_W(0),\ldots,y_W(n-1),$$

$$z_W(0),\ldots,z_W(n-1),$$

$$Q' = Q\cos(s\Delta\psi) - U\sin(s\Delta\psi),$$

$$U' = U\cos(s\Delta\psi) + Q\sin(s\Delta\psi),$$

$$z = \cos(\theta) \ge 2/3, \qquad 0 < \phi \le \pi/2,$$

 $2/3 > z \ge 0,$  $\phi = 0$ , or  $\phi = \frac{\pi}{4N_{\text{side}}}$ .  $2/3 > z \ge 0,$  $\phi = 0$ , or  $\phi = \frac{\pi}{4N_{\text{side}}}$ . if set, during **degradation** each big pixel containing one bad or missing small pixel is also considered as bad. if not set, each big pixel containing at least one good pixel is considered as good (optimistic) default = 0 (:not set)

$$N_w \simeq 0.75 N_{\rm side}^2 \simeq N_{\rm pix}/16$$

write fits sb writes out the information contained in Prim stc and Exten stc in the primary unit and extension of the FITS file File respectively. Coordinate systems can also be specified by Coordsys. Specifying the ordering scheme is compulsary for **HEALPix** data sets and can be done either in Header or by setting Ordering or Nested or Ring to the correct value. If Ordering or Nested or Ring is set, its value overrides what is given in Header. The data is assumed to represent a full sky data set with the number of data points npix = 12\*Nside\*Nside unlessPartial is set or the input FITS header contains OBJECT = 'PARTIAL' ANDthe Nside qualifier is given a valid value or the FITS header contains a NSIDE. In the **HEALPix** scheme, invalid or missing pixels should be given the value !healpix.bad value= $-1.6375010^{30}$ . If Nothealpix is set, the restrictions on Nside are void.