Homework 1

Context

This assignment reinforces ideas in Module 1: Reproducible computing in R. We focus specifically on implementing a large scale simulation study, but the assignment will also include components involving bootstrap and parallelization, Git/GitHub, and project organization.

Due date and submission

Please submit (via Canvas) a PDF knitted from .Rmd. Your PDF should include the web address of the GitHub repo containing your work for this assignment; git commits after the due date will cause the assignment to be considered late.

R Markdown documents included as part of your solutions must not install packages, and should only load the packages necessary for your submission to knit.

Points

Problem	Points
Problem 0	20
Problem 1.1	10
Problem 1.2	5
Problem 1.3	20
Problem 1.4	30
Problem 1.5	15

Problem 0

This "problem" focuses on structure of your submission, especially the use git and GitHub for reproducibility, R Projects to organize your work, R Markdown to write reproducible reports, relative paths to load data from local files, and reasonable naming structures for your files.

To that end:

- create a public GitHub repo + local R Project; I suggest naming this repo / directory bios731_hw1_YourLastName (e.g. bios731_hw1_wrobel for Julia)
- Submit your whole project folder to GitHub
- Submit a PDF knitted from Rmd to Canvas. Your solutions to the problem here should be implemented in your .Rmd file, and your git commit history should reflect the process you used to solve these Problems.

Problem 1

Simulation study: our goal in this homework will be to plan a well-organized simulation study for multiple linear regression and bootstrapped confidence intervals.

Below is a multiple linear regression model, where we are interested in primarily treatment effect.

$$Y_i = \beta_0 + \beta_{treatment} X_{i1} + \mathbf{Z_i}^T \boldsymbol{\gamma} + \epsilon_i$$

Notation is defined below:

- Y_i : continuous outcome
- X_{i1} : treatment group indicator; $X_{i1} = 1$ for treated
- $\mathbf{Z_{i}}$: vector of potential confounders
- $\beta_{treatment}$: average treatment effect, adjusting for $\mathbf{Z_i}$
- γ : vector of regression coefficient values for confounders
- ϵ_i : errors, we will vary how these are defined

In our simulation, we want to

- Estimate $\beta_{treatment}$ and $se(\hat{\beta}_{treatment})$
 - Evaluate $\beta_{treatment}$ through bias and coverage
 - We will use 3 methods to compute $se(\hat{\beta}_{treatment})$ and coverage:
 - 1. Wald confidence intervals (the standard approach)
 - 2. Nonparametric bootstrap percentile intervals
 - 3. Nonparametric bootstrap t intervals
 - Evaluate computation times for each method to compute a confidence interval
- Evaluate these properties at:
 - Sample size $n \in \{10, 50, 500\}$
 - True values $\beta_{treatment} \in \{0, 0.5, 2\}$
 - True ϵ_i normally distributed with $\epsilon_i \sim N(0,2)$
 - True ϵ_i coming from a right skewed distribution
 - * **Hint**: try $\epsilon_i \sim logNormal(0, log(2))$
- Assume that there are no confounders ($\gamma = 0$)
- Use a full factorial design

Problem 1.1 ADEMP Structure

Answer the following questions:

- How many simulation scenarios will you be running? We will be running 3*3*2=18 simulation scenarios
- What are the estimand(s) The estimands are the average treatment effect $\beta_{treatment}$ and the standard error of treatment effect $se(\beta_{treatment})$
- What method(s) are being evaluated/compared? 3 methods are being compared Wald confidence intervals, nonparametric bootstrap percentile intervals, and nonparametric bootstrap t-intervals.
- What are the performance measure(s)? The performance measures we are using are bias, coverage, and computation time.

Problem 1.2 nSim

Based on desired coverage of 95% with Monte Carlo error of no more than 1%, how many simulations (n_{sim}) should we perform for each simulation scenario? Implement this number of simulations throughout your simulation study.

[1] 475

We should perform 475 simulations for each simulation scenario.

Problem 1.3 Implementation

We will execute this full simulation study. For full credit, make sure to implement the following:

- Well structured scripts and subfolders following guidance from project_organization lecture
- Use relative file paths to access intermediate scripts and data objects
- Use readable code practices
- Parallelize your simulation scenarios
- Save results from each simulation scenario in an intermediate .Rda or .rds dataset in a data subfolder
 - Ignore these data files in your .gitignore file so when pushing and committing to GitHub they don't get pushed to remote
- Make sure your folder contains a Readme explaining the workflow of your simulation study
 - should include how files are executed and in what order
- Ensure reproducibility! I should be able to clone your GitHub repo, open your .Rproj file, and run your simulation study

Problem 1.4 Results summary

Create a plot or table to summarize simulation results across scenarios and methods for each of the following.

- Bias of $\hat{\beta}$
- Coverage of $\hat{\beta}$
- Distribution of $se(\hat{\beta})$
- Computation time across methods

If creating a plot, I encourage faceting. Include informative captions for each plot and/or table.

Bias

Table 2: Bias Summary Table

N	True Beta	Lognormal	Normal
10	0.0	-0.051	-0.093
10	0.5	-0.051	-0.093
10	2.0	-0.051	-0.093
50	0.0	-0.024	-0.006
50	0.5	-0.024	-0.006
50	2.0	-0.024	-0.006

N	True Beta	Lognormal	Normal
500	0.0	-0.009	-0.009
500	0.5	-0.009	-0.009
500	2.0	-0.009	-0.009
	0.0	0.000	0.0.

${\bf Coverage}$

Table 3: Coverage Summary Table

		Lognormal			Normal		
N	True Beta	Lognormal Wald CI	Lognormal Bootstrap Percentile CI	Lognormal Bootstrap t CI	Normal Wald CI	Normal Bootstrap Percentile CI	Normal Bootstrap t CI
10	0.0	95.368	82.737	53.263	94.105	83.368	54.947
10	0.5	95.368	82.737	53.263	94.105	83.368	54.947
10	2.0	95.368	82.737	53.263	94.105	83.368	54.947
50	0.0	95.368	89.263	88.842	94.316	90.316	91.579
50	0.5	95.368	89.263	88.842	94.316	90.316	91.579
50	2.0	95.368	89.263	88.842	94.316	90.316	91.579
500	0.0	93.474	90.737	92.000	92.842	89.895	92.211
500	0.5	93.474	90.737	92.000	92.842	89.895	92.211
500	2.0	93.474	90.737	92.000	92.842	89.895	92.211

Computation Time

Table 4: Computation Time Summary Table

		Lognormal		Lognormal Normal			
N	True	Lognormal	Lognormal	Lognormal	Normal	Normal	Normal
	Beta	Wald Time	Bootstrap	Bootstrap t	Wald Time	Bootstrap	Bootstrap t
			Percentile	Time		Percentile	Time
			Time			Time	
10	0.0	0.030	1.669	18.328	0.025	1.440	15.947
10	0.5	0.024	1.419	15.662	0.025	1.444	15.941
10	2.0	0.025	1.453	16.050	0.025	1.437	15.828
50	0.0	0.024	1.415	15.462	0.025	1.437	15.723
50	0.5	0.024	1.420	15.550	0.025	1.432	15.639
50	2.0	0.025	1.441	15.814	0.025	1.436	15.709
500	0.0	0.024	1.423	15.645	0.025	1.458	15.944
500	0.5	0.025	1.446	15.876	0.026	1.447	15.886
500	2.0	0.025	1.467	16.014	0.024	1.460	16.005

Standard Error of Beta (Distribution)

Problem 1.5 Discussion

Interpret the results summarized in Problem 1.4. First, write a **paragraph** summarizing the main findings of your simulation study. Then, answer the specific questions below.

- How do the different methods for constructing confidence intervals compare in terms of computation time?
- Which method(s) for constructing confidence intervals provide the best coverage when $\epsilon_i \sim N(0,2)$?
- Which method(s) for constructing confidence intervals provide the best coverage when $\epsilon_i \sim logNormal(0, log(2))$?