## Intermediate Test 5

## Stellenbosch Camp 2018

Time: 4 hours

- 1. The student lockers at Olympic High are numbered consecutively beginning with locker number 1. The plastic digits used to number the lockers cost 3 cents per piece. Thus, it costs 3 cents to number locker 9 and 6 cents to number locker 42. If it costs R206.91 to label all the lockers, how many lockers are there at the school?
- 2. Given the equation  $x^{2018} = y^x$ ,
  - (a) find all pairs (x, y) of solutions with x prime and y a positive integer;
  - (b) find all pairs (x, y) of positive integers satisfying the equation.

3.

4.

5. Determine the number of ways to choose five numbers from the first eighteen positive integers such that any two chosen numbers differ by at least 2.

6.

