

# Finite element models for the study of hydrogen embrittlement of steel structures

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**Thesis defense**

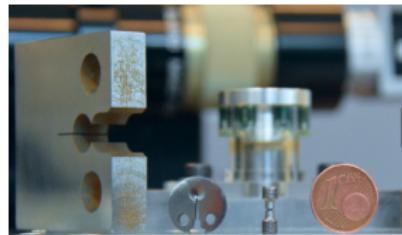
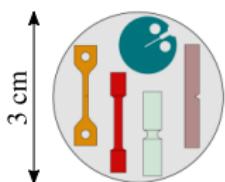
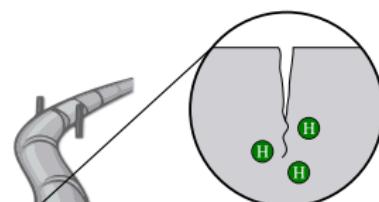
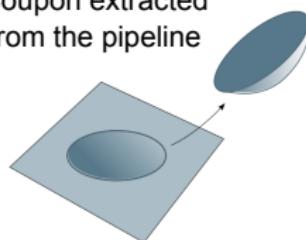
March 7<sup>th</sup> 2025

- ▶ In the context of **energy transition**, **hydrogen** plays an important role as an **energy vector**
- ▶ Hydrogen can be produced from other **renewable sources**, such as wind and solar
- ▶ Hydrogen transport using **existing natural gas pipelines** (40,000 km in France, 50 billion in assets, up to 80 years old) is a proposal for hydrogen transport

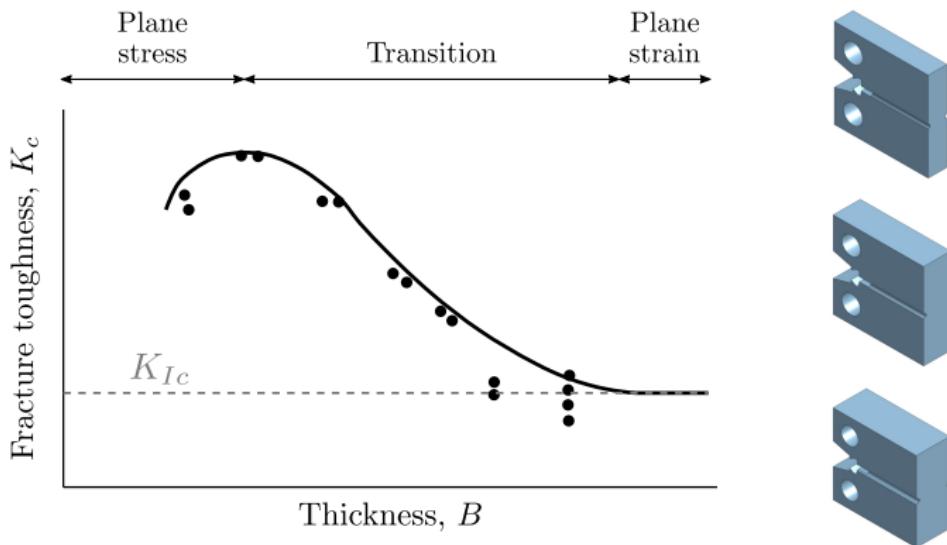


- ▶ The steels used in gas pipelines are typically susceptible to **hydrogen embrittlement**
- ▶ Hydrogen embrittlement: ductility and toughness reduction, premature failure
- ▶ **Measure material properties from small samples without service interruption**

Coupon extracted  
from the pipeline



- ▶ Experimental observations show that **toughness decreases with increasing specimen thickness** until reaching a plateau
- ▶ Beyond a critical thickness, toughness becomes relatively insensitive to further increases



Adapted from Barsom and Rolfe, 1987.

- ▶ Develop a model coupling **plasticity, damage, and hydrogen diffusion**
- ▶ Validate the model against experimental data
- ▶ Simulate size and thickness effects on toughness using sub-size specimens

## Introduction

## Hydrogen inside metals

## Finite element formulation

## Numerical simulations

Pressurized disks tests

Hydrogen embrittlement modeling

Simulation of fracture toughness tests

## Conclusions and perspectives

Introduction

## Hydrogen inside metals

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Numerical simulations

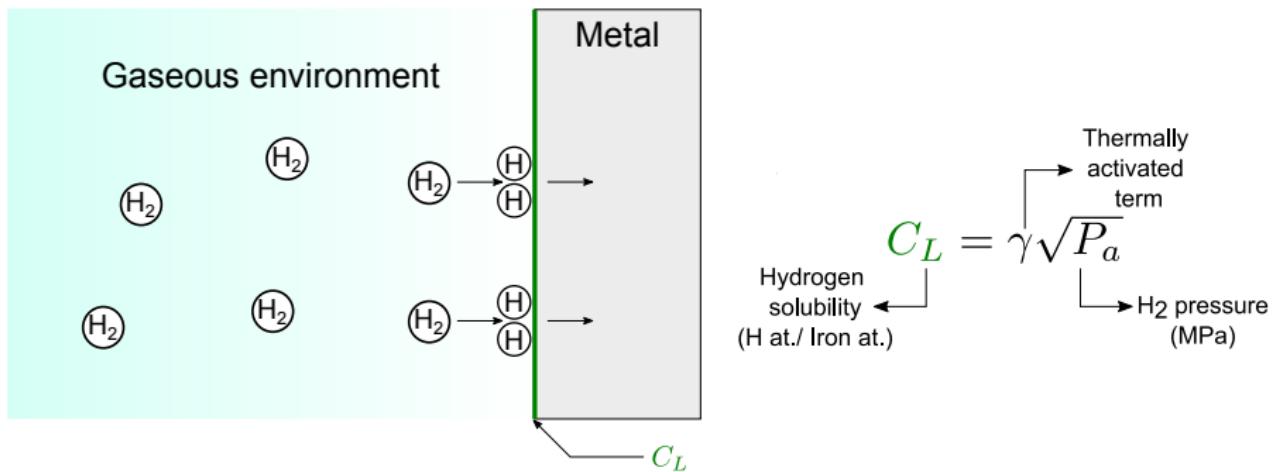
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- ▶ **Sieverts' law:** The solubility of a diatomic gas in a metal is proportional to the square root of the gas pressure

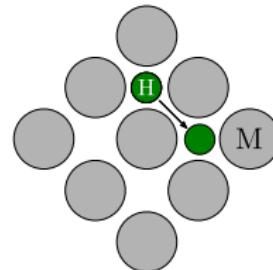


- Model from Sofronis and McMeeking (1989) and corrected by Krom *et al.* (1999)

- **Hydrogen concentration:**  $C = C_L + C_T$

- Lattice concentration:  $C_L = \beta N_L \theta_L$

- Trapped concentration:  $C_T = \sum_i^N C_T^i = N_T^i(\kappa) \theta_T^i$



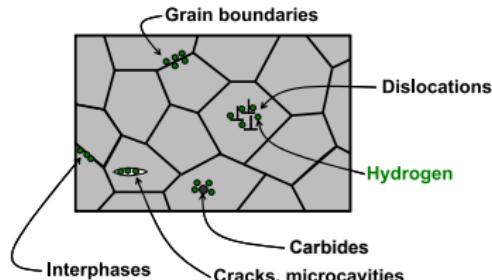
- **Hydrogen flux:**

$$J = -D_L \nabla C_L + \frac{D_L C_L V_H}{RT} \nabla p$$

- **Oriani's equilibrium:**

$$\frac{1 - \theta_L}{\theta_L} \frac{\theta_T^i}{1 - \theta_T^i} = K$$

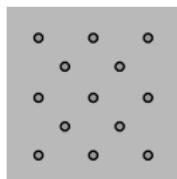
(Coupling terms)



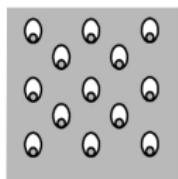
- The **ductile behavior** of the metal is described by the **GTN model** (Tvergaard *et al.* 1984):

$$\frac{\sigma_{eq}^2}{\sigma_F^2} + 2q_1 f_* \cosh \left( \frac{q_2}{2} \frac{\sigma_{ii}}{\sigma_F} \right) - 1 - q_1^2 f_*^2 = 0$$

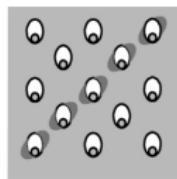
$$\dot{f} = \dot{f}_{nucleation} + \dot{f}_{growth}$$



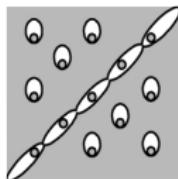
Impurities or second phase particles



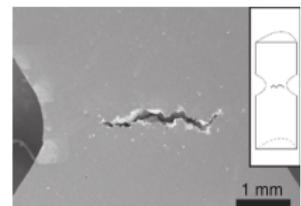
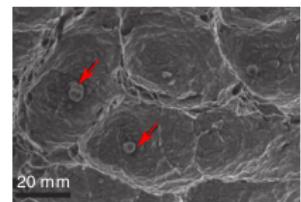
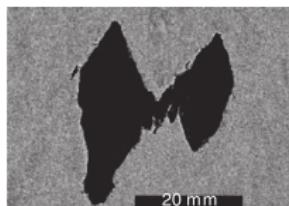
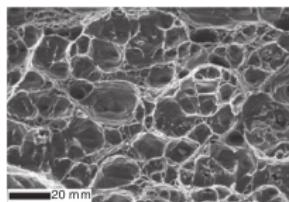
Void nucleation and growth



Strain localization



Void coalescence and fracture

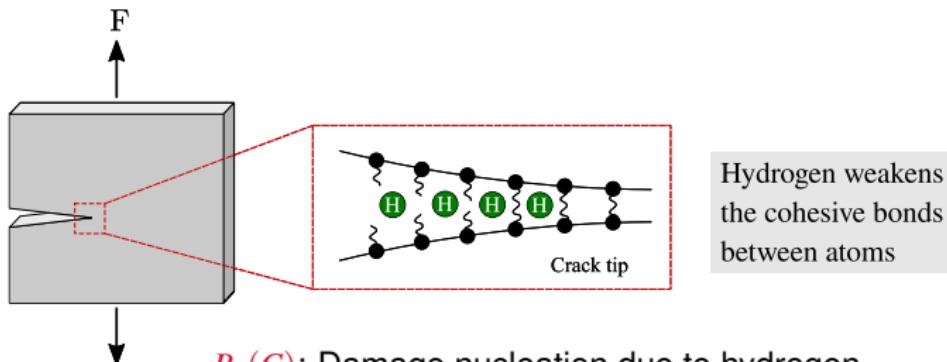


- **Void growth:** Unchanged due to mass conservation

$$\dot{f}_g = (1 - f_g) \text{trace}(\dot{\varepsilon}_p)$$

- **Void nucleation:** Proposed dependence on hydrogen concentration

$$\dot{f}_n = A_n(\kappa)\dot{\kappa} + B_n(C)\dot{\kappa} \quad (\text{Coupling terms})$$



Hydrogen weakens  
the cohesive bonds  
between atoms

$B_n(C)$ : Damage nucleation due to hydrogen  
**HEDE** (Hydrogen Enhanced Decohesion)

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Conclusions and perspectives

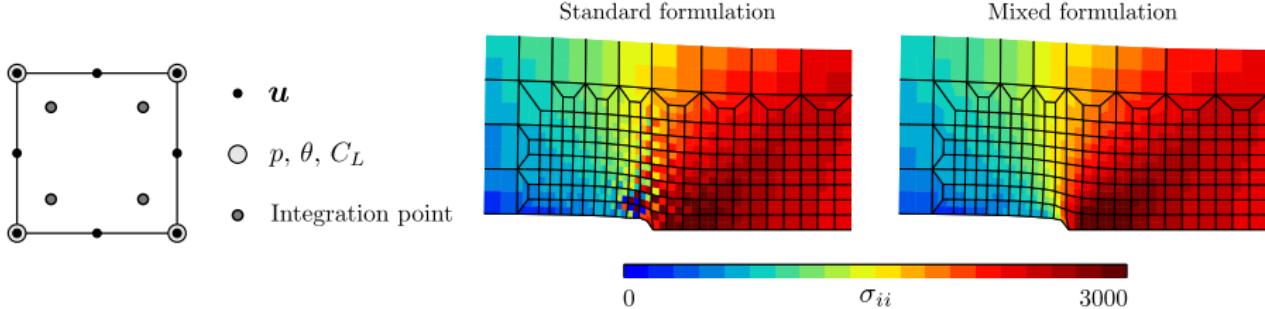
- ▶ Fully implicit finite strain framework
- ▶ Based on a mixed formulation:  $\underline{u}, P, \theta$  (Zhang et al. 2017) and  $C_L$
- ▶ Quadratic elements with reduced integration
- ▶ **Aim:** better pressure fields by avoiding volumetric locking



## Advantage

$\nabla p$  can be directly computed from nodal values

$$J = -D_L \nabla C_L + \frac{D_L C_L V_H}{RT} \nabla p$$



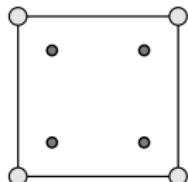
- ▶ The use of **quadratic elements** with additional dofs lead to **high simulation times**

- $B$ -bar (or  $\bar{B}$ ) formulation (Hughes, 1980):

- ▶ Linear elements with full integration
  - ▶ Solves volumetric locking by modifying the strain-displacement matrix:

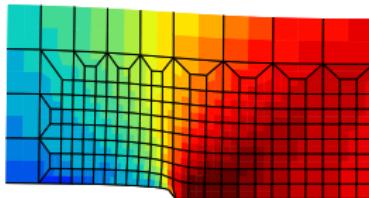
$$\bar{B} = B_d + \bar{B}_h$$

- To avoid extrapolating  $p$  to the nodes for  $\nabla p$  computation, it is considered as a dof

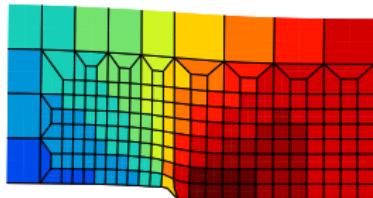


- $\mathbf{u}, p, C_L$
- Integration point

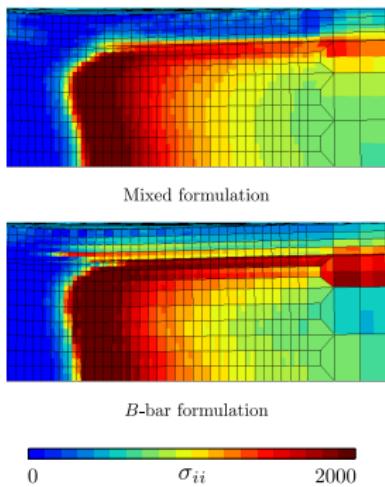
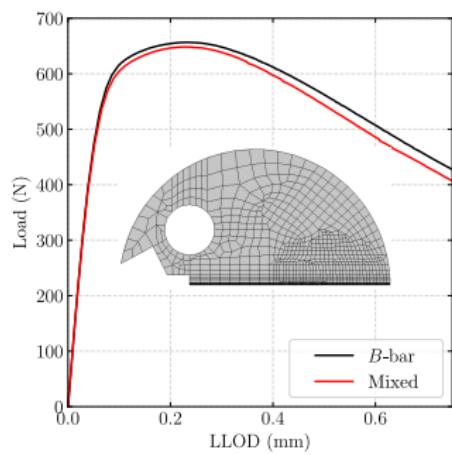
Mixed formulation



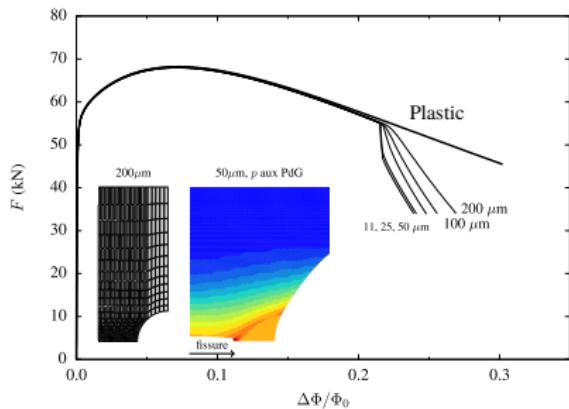
### B-bar formulation



- ▶ Test on a Disk Compact Tension (DCT) specimen with 5200 elements:
  - ▶ **Mixed formulation:** 103,762 dofs, 1h 40 minutes to complete
  - ▶ **B-bar formulation:** 33,974 dofs, 18 minutes to complete
- ▶ Slightly higher force for the **B-bar** formulation → Linear elements are inherently stiffer since they have less nodes

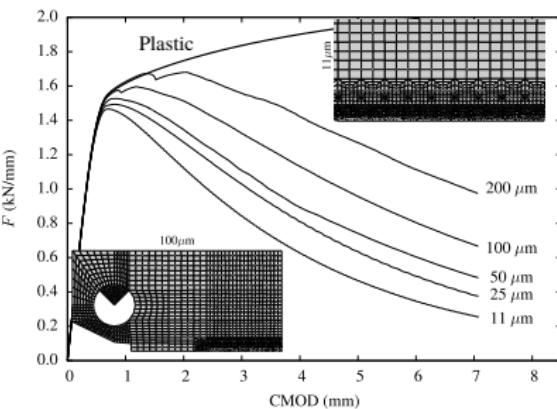


- ▶ Damage models such as the GTN model are known to induce **spurious mesh dependency** (element size, type and orientation)
- ▶ To solve this problem, it is proposed to use a **nonlocal damage model** based on the **implicit gradient** by Peerlings *et al.*, 1996



Notched tensile (NT) specimen

(Besson, 2021)

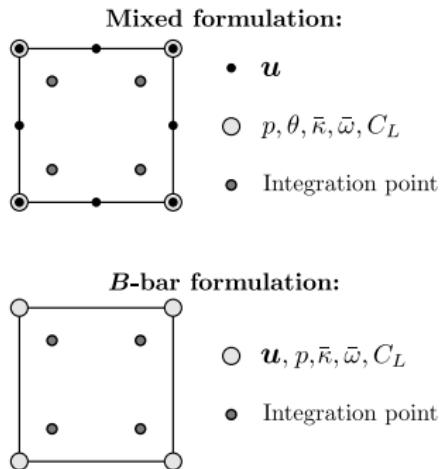
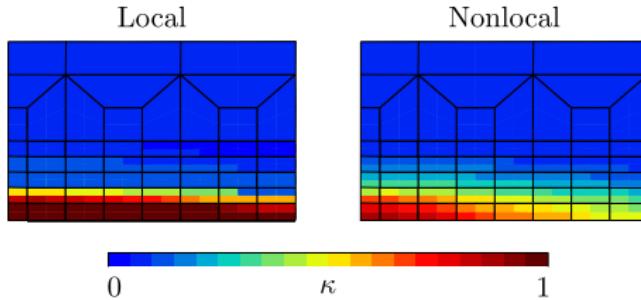


Compact tension (CT) specimen

- ▶ Two variables are used (two associated internal lengths:  $\bar{\omega}$  and  $\bar{\kappa}$ ):
    - ▶ **Plastic volume variation:**  $\bar{\omega} - \ell_{\omega}^2 \Delta \bar{\omega} = \omega$  where  $\omega = \text{trace}(\dot{\varepsilon}_p)$
    - ▶ **Accumulated plastic strain:**  $\bar{\kappa} - \ell_{\kappa}^2 \Delta \bar{\kappa} = \kappa$  - ▶ The modified evolution laws for the damage variables are now:

► **Void growth:**  $\dot{f}_g = (1 - f_g) \dot{\omega}$

► **Void nucleation:**  $\dot{f}_n \equiv A_n \dot{\kappa} + B_n(C) \dot{\kappa}$



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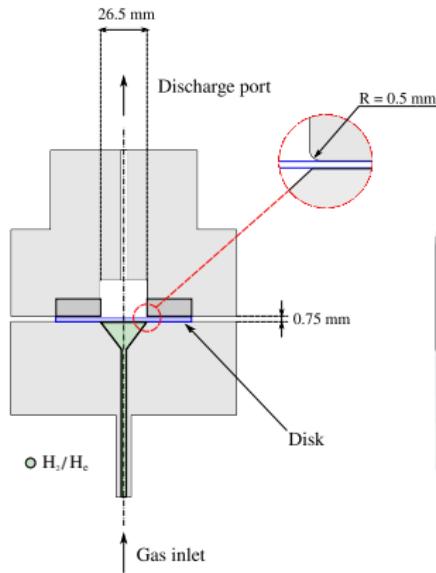
Pressurized disks tests

Hydrogen embrittlement modeling

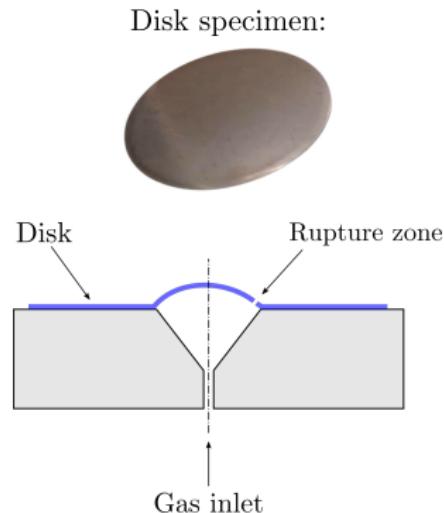
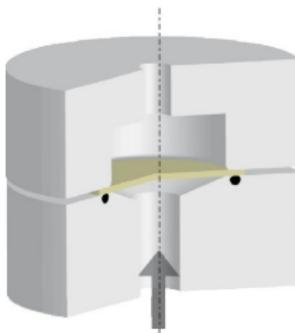
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Conclusions and perspectives

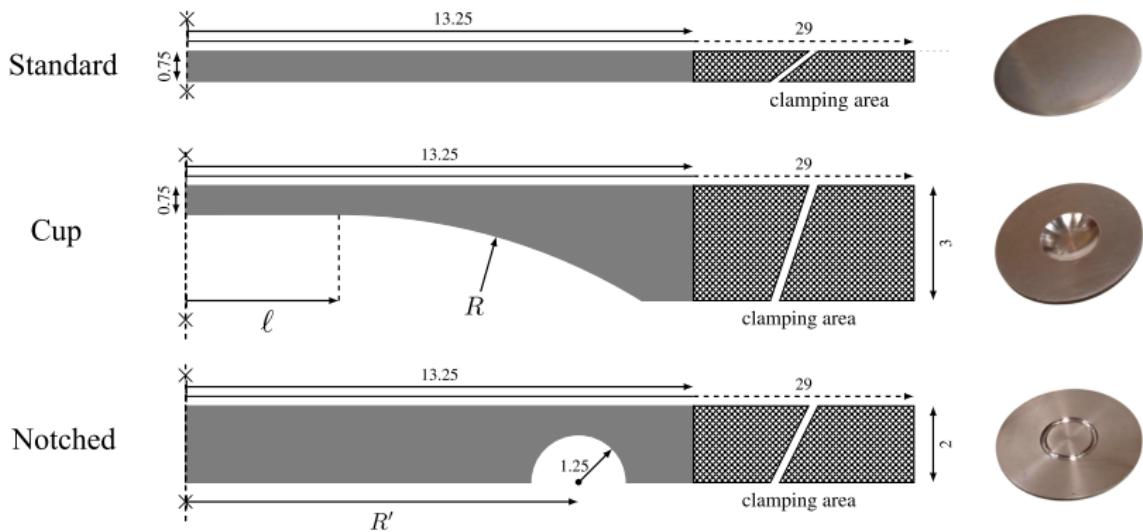
- ▶ **ISO 11114-4 standard:** uses pressurized disk tests for selecting metallic materials resistant to hydrogen embrittlement
- ▶ Disk often fails in the clamping zone
- ▶ **First step:** redesigning the disk geometry to control failure location



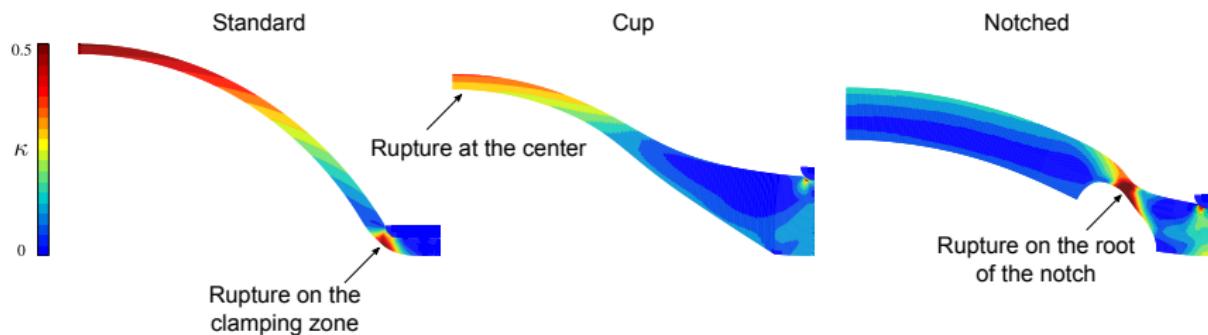
$$\text{HEI} = \frac{P_r(\text{He})}{P_r(\text{H}_2)}$$



- ▶ New proposed geometries:
  - ▶ No need to modify the test setup
  - ▶ Keep the same minimum thickness of the standard (0.75 mm)
- ▶ Optimization with respect to  $\ell$ ,  $R$  and  $R'$  with FE simulations considering an elasto-plastic behavior



- ▶ The location of the maximum accumulated plastic strain ( $\kappa$ ) corresponds to the failure location



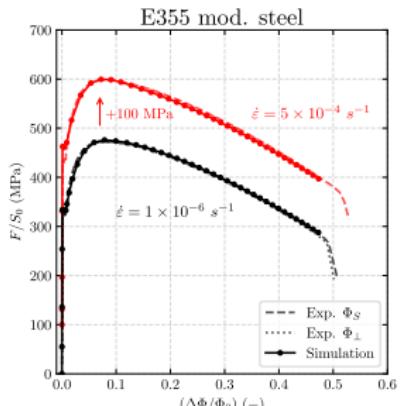
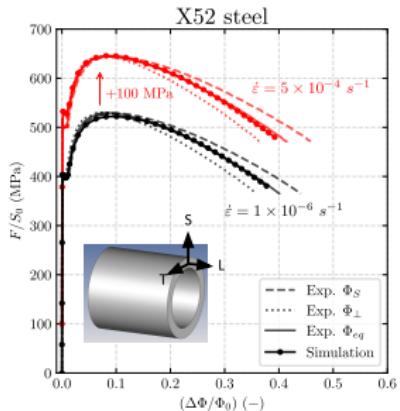
► **X52 vintage steel:**

- ▶ Yield strength: 400 MPa
- ▶ Different elongation at rupture in T and L directions

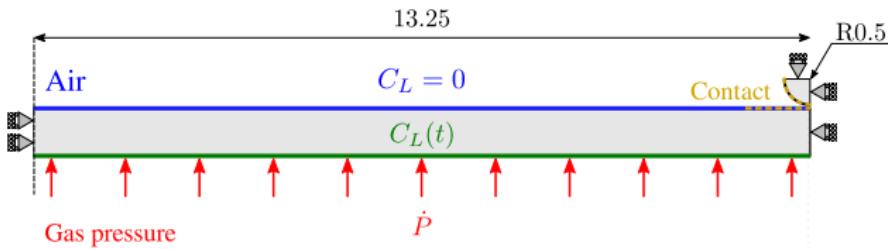
► **E355 mod. steel:**

- ▶ Yield strength: 330 MPa
  - ▶ Higher elongation at rupture and lower Ultimate Tensile Strength in relation with the vintage material
  - ▶ Similar elongation at rupture in both directions
- Elasto(visco)-plastic model coefficients' identified through optimization:

$$\sigma_F(p) = \max(\sigma_L, \sigma_0 + Q_1(1 - \exp(-b_1 p)) + Q_2(1 - \exp(-b_2 p)) + H p)$$

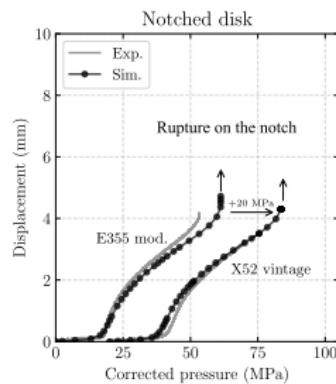
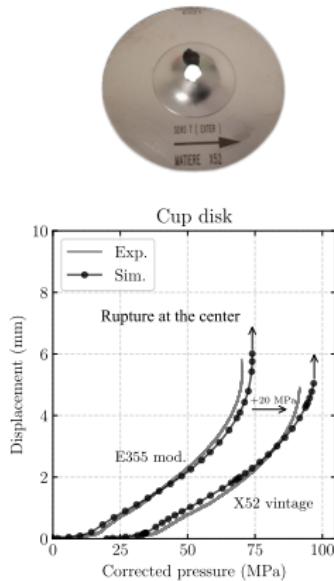
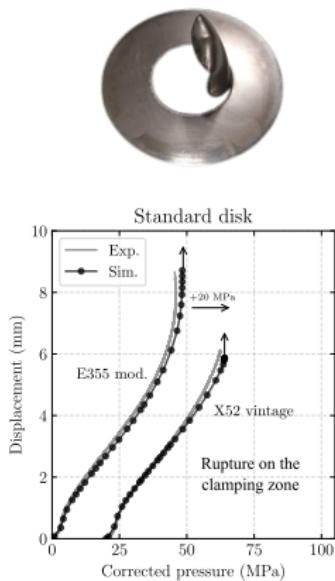
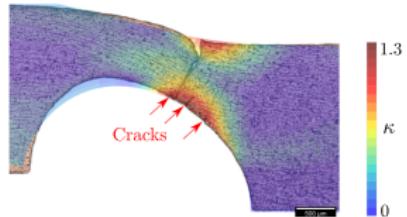


- ▶ Axisymmetric model, quadratic elements with reduced integration (mixed formulation)
- ▶ Hydrogen diffusion parameters taken from the literature
- ▶ Since damage is not considered into the numerical model, the simulations were stopped once they reached experimentally observed rupture pressure ( $P_r$ )
- ▶ Model's boundary conditions:



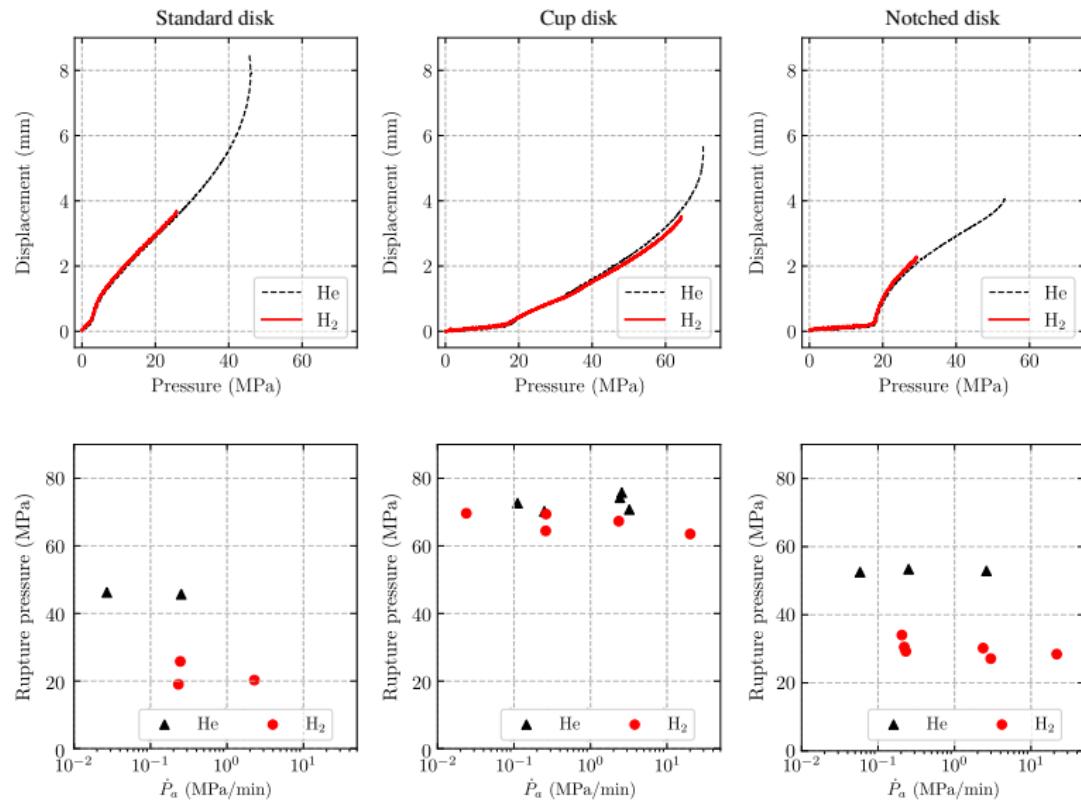
# Results under helium

- ▶ Successfully modification of fracture location
- ▶ Failure is primarily driven by plasticity and occurs under a limit load scenario



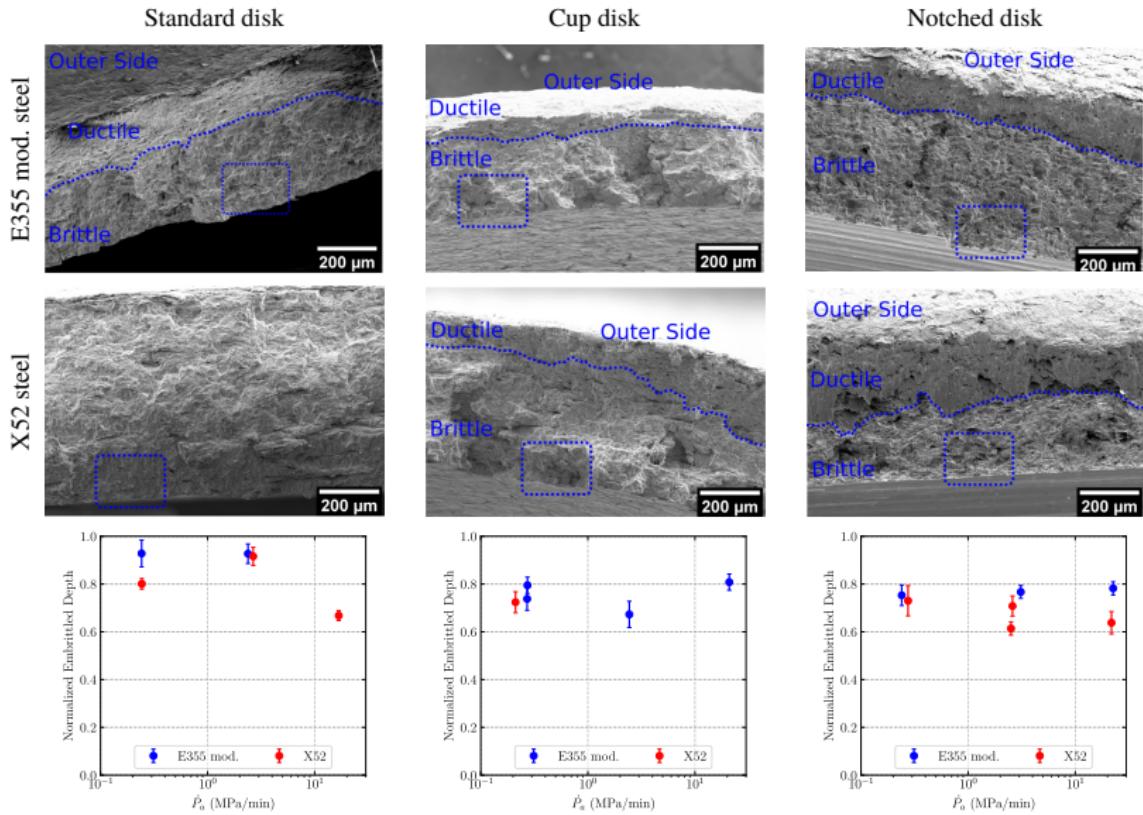
(Experimental data: Santana *et al.*, 2024)

# Results under hydrogen (E355 mod. steel)



(Experimental data: Santana *et al.*, 2024)

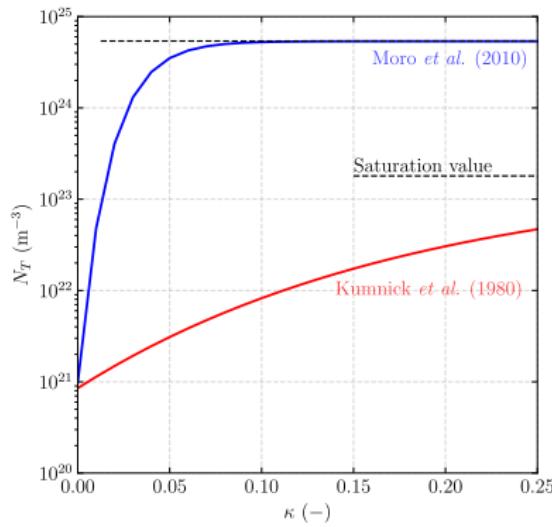
# Hydrogen embrittled depth



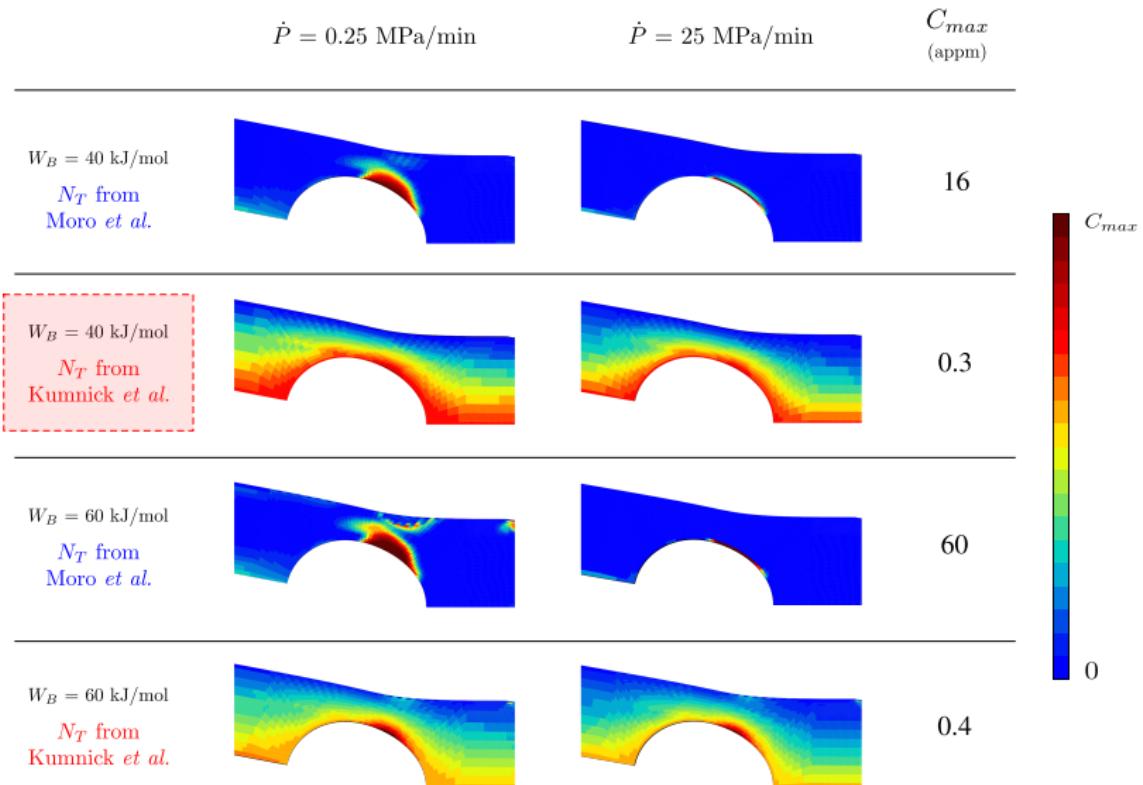
- ▶ Considers only one kind of trap: dislocations
- ▶ Trap binding energies ( $W_B$ ) and trap densities ( $N_T$ ) were taken from the literature and analyzed based on the experimental observations
- ▶ Based on the models proposed by Moro *et al.* (2010) and Kumnick *et al.* (1980), four cases emerge

$$W_B = \begin{cases} 40 \text{ kJ/mol} \\ 60 \text{ kJ/mol} \end{cases}$$

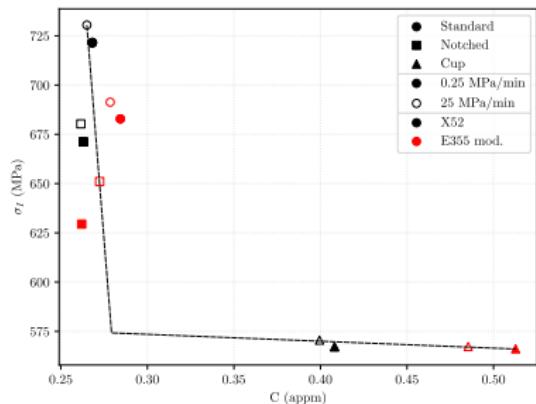
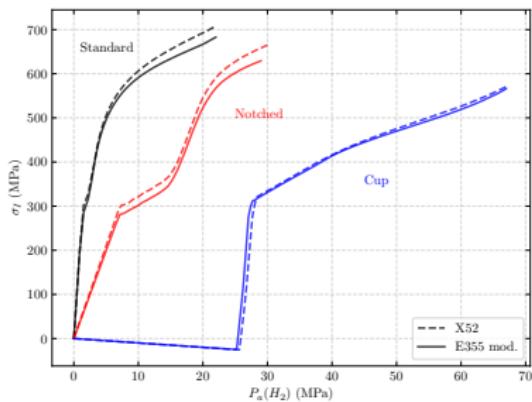
$$N_T = \begin{cases} \log_{10} N_T = 24.73 - 3.74 \exp(-60.17\kappa) \\ \log_{10} N_T = 23.26 - 2.33 \exp(-5.5\kappa) \end{cases}$$



# Hydrogen embrittled depth



- ▶ Specimens that develop higher principal stress ( $\sigma_I$ ) in the fracture zone fail at a lower hydrogen pressure ( $P_a(H_2)$ )
- ▶ The total hydrogen concentration reduces the maximum principal stress that triggers fracture



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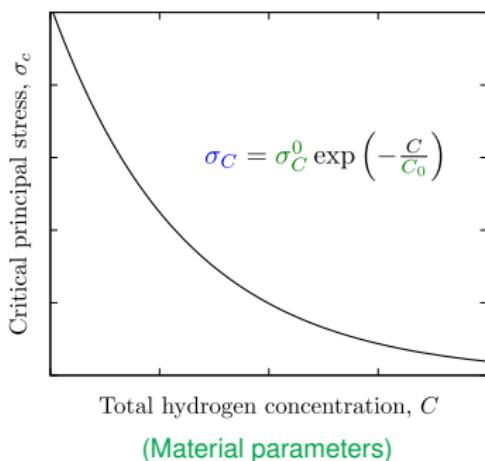
Simulation of fracture toughness tests

Conclusions and perspectives

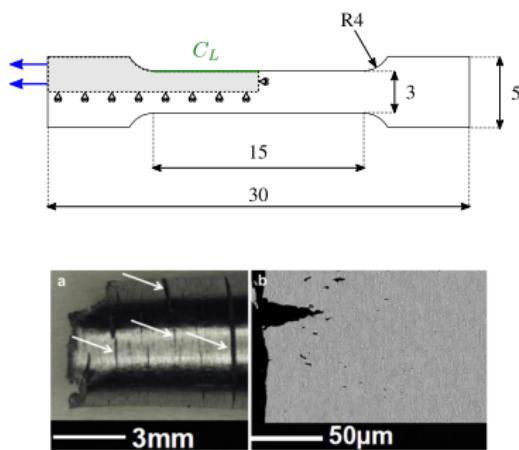
- ▶ **Database:** Briottet *et al.*, 2012 and Moro *et al.*, 2010: *Effect of gaseous hydrogen on the mechanical properties of steel*
- ▶ **Material:** high-strength steel (API X80 grade) in an environment of hydrogen and neutral gas
- ▶ As HE corresponds to **quasi-cleavage**, a **stress dependance** is introduced to the nucleation law
- ▶ The function expressing the nucleation rate due to quasi-cleavage is:

$$B_n(C) = \frac{B_0}{\sigma_C^0} (\sigma_I - (1 - q_1 f_*) \sigma_C)$$

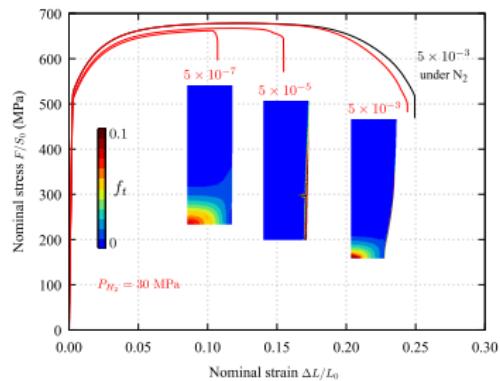
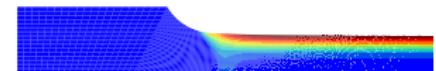
- ▶ Hydrogen decreases the critical stress to trigger void nucleation



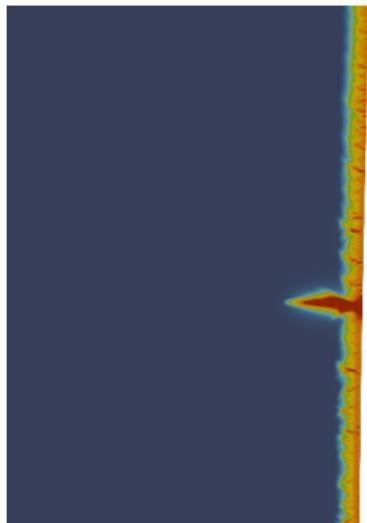
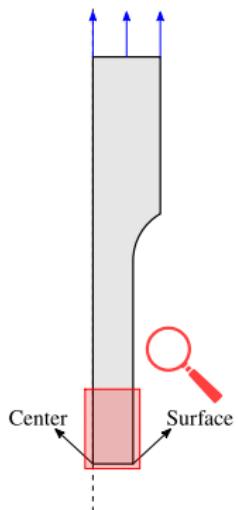
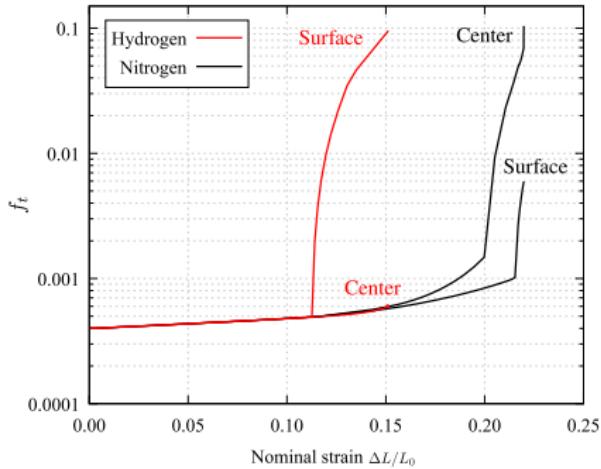
- ▶ Tensile tests under different strain rates under hydrogen gas
- ▶ Slower rates lead to important ductility losses



(Experimental data: Briottet *et al.*, 2012)

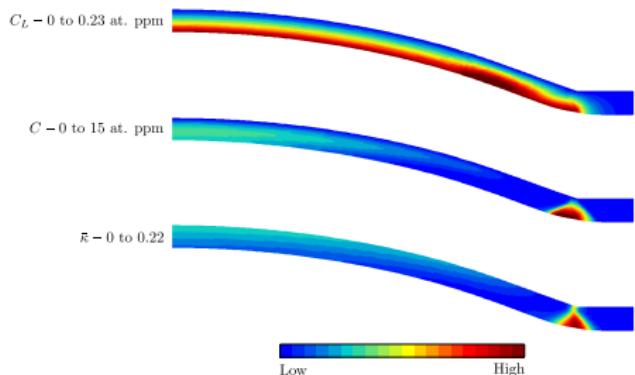
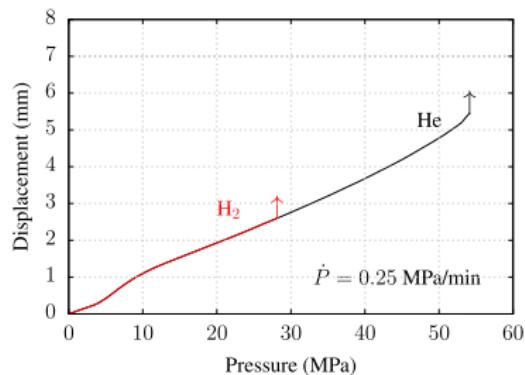


- ▶ Different damage evolution under hydrogen environment
- ▶ Multicrack initiation on the surface



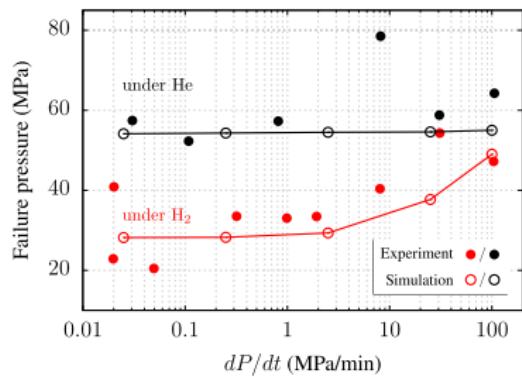
## Hydrogen effect:

- ▶ Lower pressure at rupture with decreased ductility
- ▶ Higher hydrogen concentration in the rupture zone

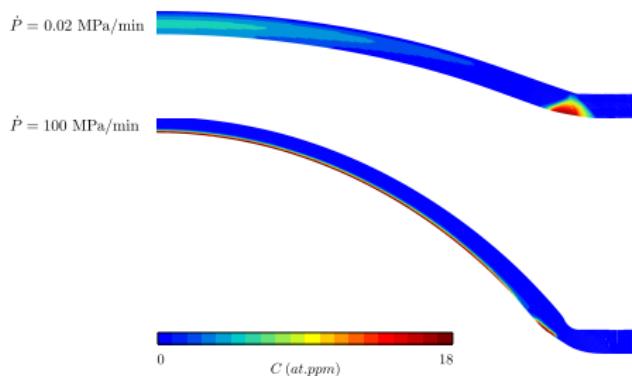


## Effect of the pressurization rate:

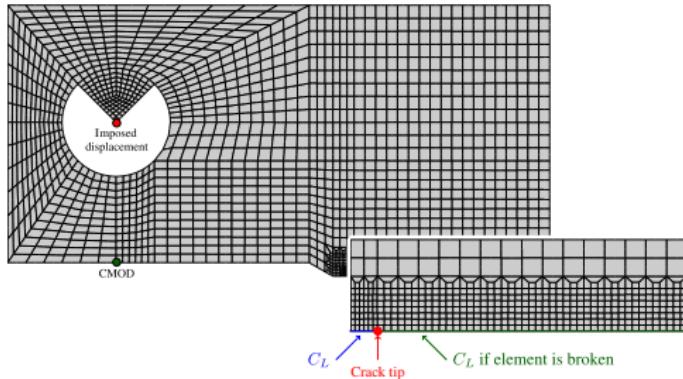
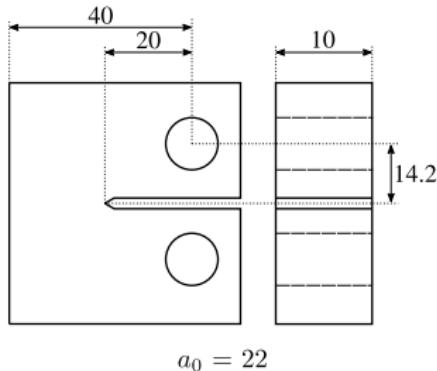
- ▶ Tests under different pressurization rates on H<sub>e</sub> and H<sub>2</sub> gases
- ▶ **Lower pressurization rate → Higher embrittlement** since has a longer time to diffuse



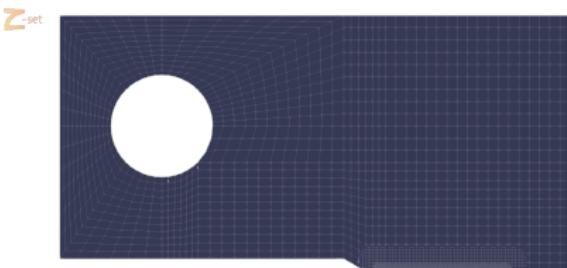
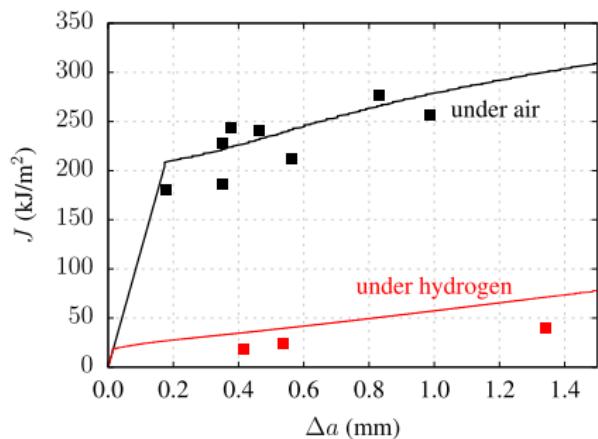
(Experimental data: Briottet *et al.*, 2012)



- ▶ 2D Compact Tension (CT) specimen - *plane strain*
- ▶ Uniaxial imposed displacement
- ▶ Environment: air and hydrogen (30 MPa)
- ▶ Lattice concentration ( $C_L$ ) derived from Sieverts' law imposed on the newly formed crack



- ▶ Crack length: post-processing considering broken elements  $f_* = 0.99 \times 1/q_1$
- ▶  $J$  computation: ASTM E1820 standard considering the simulated Load-CMOD curve



Introduction

Hydrogen inside metals

Finite element formulation

## Numerical simulations

Pressurized disks tests

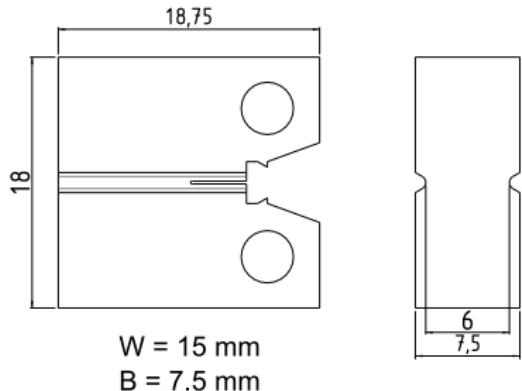
Hydrogen embrittlement modeling

Simulation of fracture toughness tests

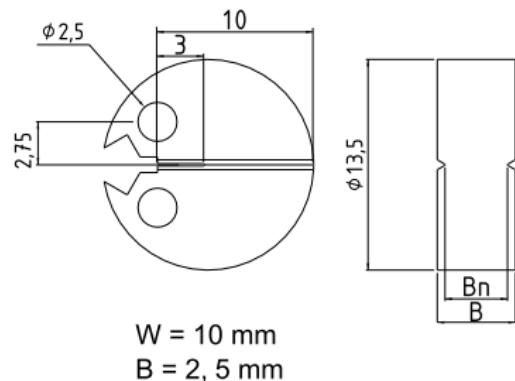
Conclusions and perspectives

- ▶ X52 vintage steel
- ▶ Tube thickness: 7.92 mm
- ▶ Tests using standard and sub-size specimens
- ▶ Pre-cracking and side grooves on both sides with  $B_n = 10\%B$

**Standard Compact Tension (CT):**

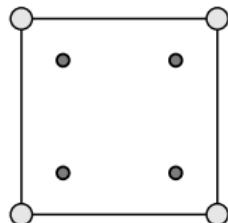


**Mini Disk Compact Tension (mDCT):**

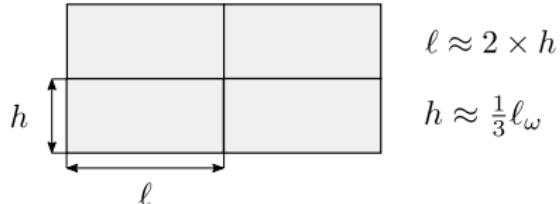


## ► Nonlocal GTN model with two internal lengths:

- ▶  $\ell_\kappa$ : accumulated plastic strain (void nucleation)
- ▶  $\ell_\omega$ : plastic volume change (void growth)
- ▶ Typical element size used in local models for pipeline steel simulations (Madi et al., 2020):  $\ell_\omega = 100 \mu\text{m}$
- ▶ The length scale associated with quasi-cleavage is likely smaller:  $\ell_\kappa = 33 \mu\text{m}$



- $\{\mathbf{u}\}, \{\bar{\omega}\}, \{\bar{\kappa}\}$
- Integration point



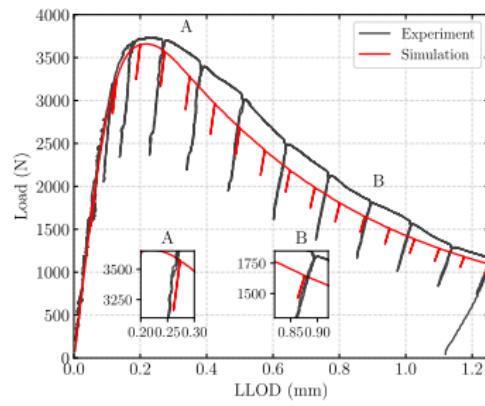
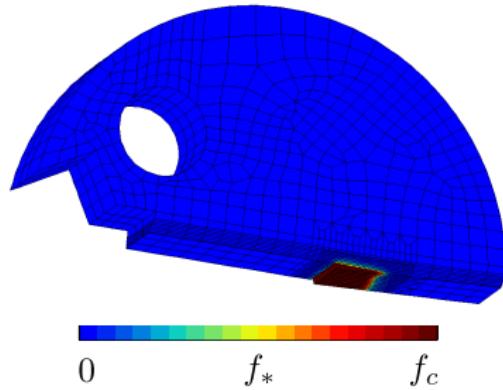
$$\ell \approx 2 \times h$$

$$h \approx \frac{1}{3} \ell_\omega$$

- ▶ **Element removal technique:** an element of the mesh is removed when a predefined number of its integration points reach this critical porosity value:

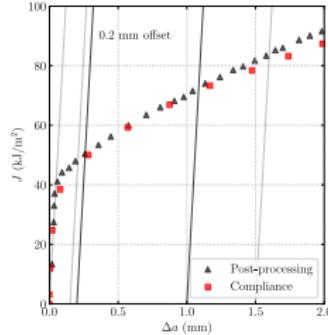
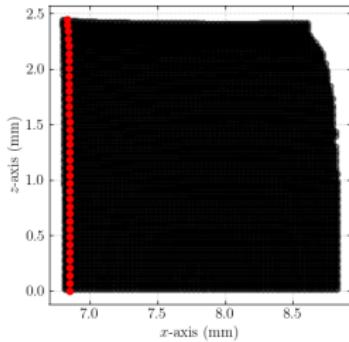
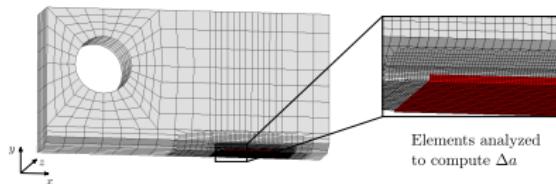
$$f_c = 1/q_1 - \epsilon$$

- ▶ **First method:** compliance technique  $\rightarrow \Delta a$  is computed at the same way as in the experiments
  - ▶ **Drawback:** the load, hold, and unload steps into simulations significantly increases computation time



## ► Second method: Post-processing

- The initial crack front is identified and the porosity values are analyzed on elements in the crack propagation zone
- Elements reaching the critical porosity value ( $f_c$ ) are considered broken. The crack front is updated after propagation.



- ▶ The coefficients of the constitutive law were directly identified using the fracture toughness specimens
- ▶ Hardening law:

$$\sigma_F(\kappa) = \max(340, 243 + 158(1 - \exp(-28.39\kappa)) + 399(1 - \exp(-269\kappa)))$$

- ▶ Damage coefficients:

$$q_1 = 1.25$$

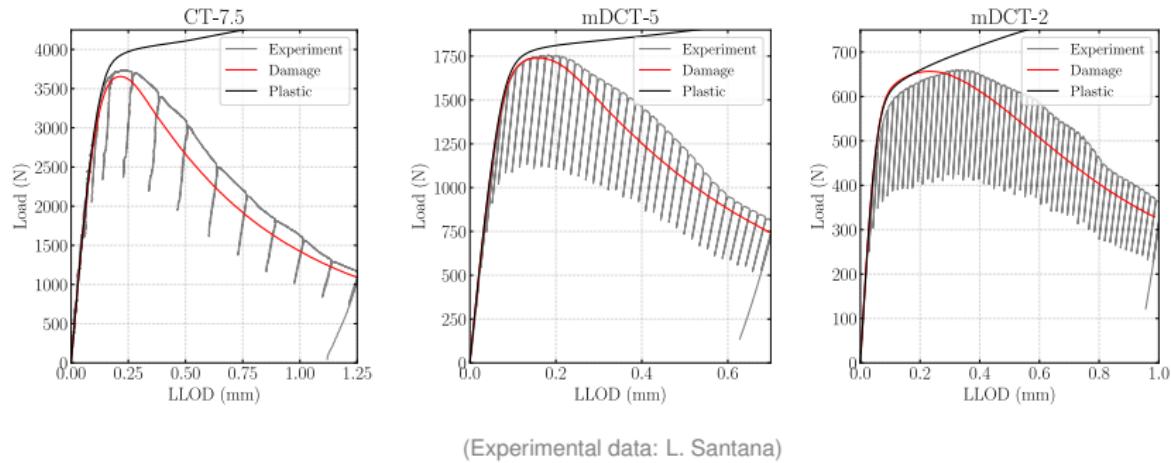
$$q_2 = 1.40$$

$$\dot{f}_n = A_n(\bar{\kappa} > \kappa_c)\dot{\bar{\kappa}} \quad \text{with}$$

$$A_n = 1.0 \quad \text{and} \quad \kappa_c = 0.15 \rightarrow \textbf{High and early void nucleation}$$

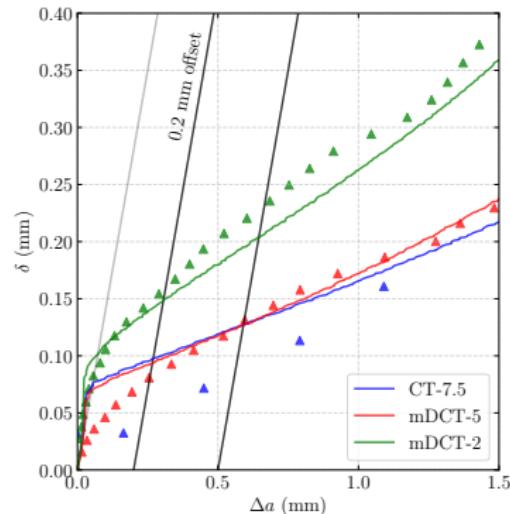
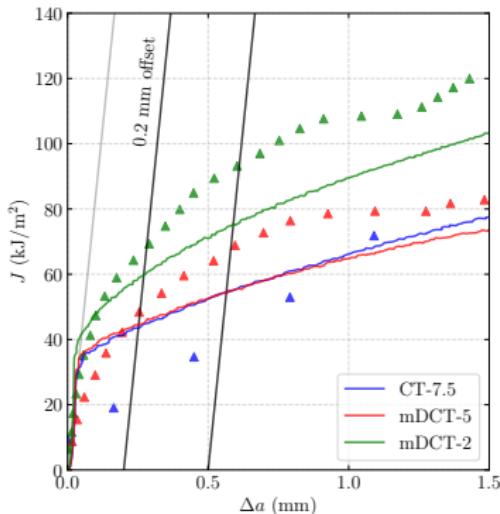
# Results: simulations vs. experiments

- ▶ Mesh dimensions precisely match the specimen dimensions for each test
- ▶ An elasto-plastic model fails to accurately represent the fracture toughness test once crack propagation begins



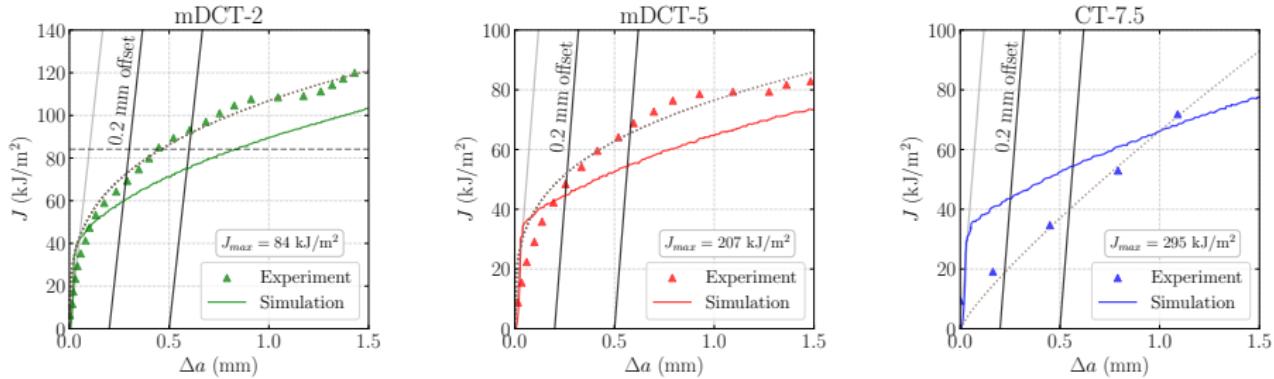
# Results: simulations vs. experiments

- ▶ Crack propagation initiates later for the simulations → This delay was partially addressed by reducing the void nucleation threshold
- ▶  $J$  and  $\delta$  (CTOD) values increase as specimen size decreases



(Experimental data: L. Santana)

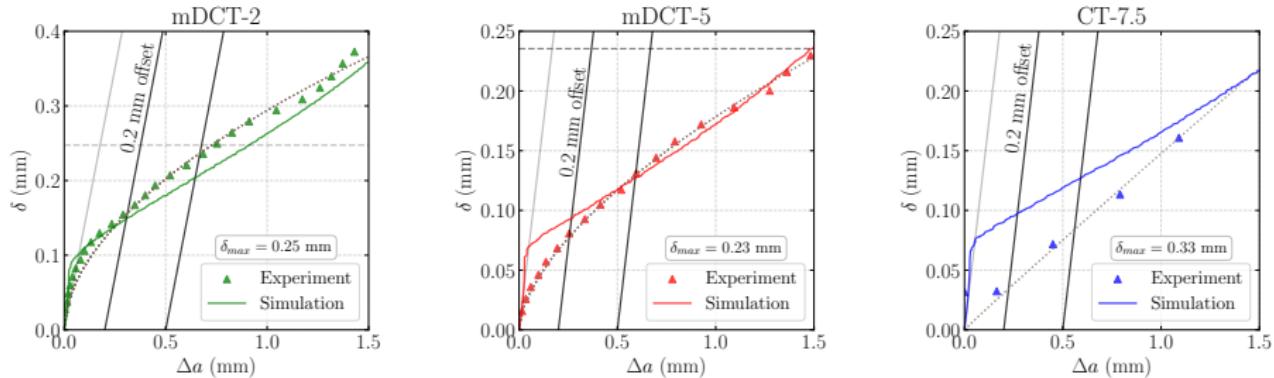
# Results: simulations vs. experiments



Specimen	$J_{max}$ (kJ/m <sup>2</sup> )	$J_{0.2}$ (kJ/m <sup>2</sup> )		$J_{0.5}$ (kJ/m <sup>2</sup> )	
		Experiment	Simulation	Experiment	Simulation
mDCT-2	84	73	59	92	76
mDCT-5	207	52	43	65	55
CT-7.5	295	19	40	42	55

Construction line:  $J = 2\sigma_0 \Delta a$  (ASTM E1820)

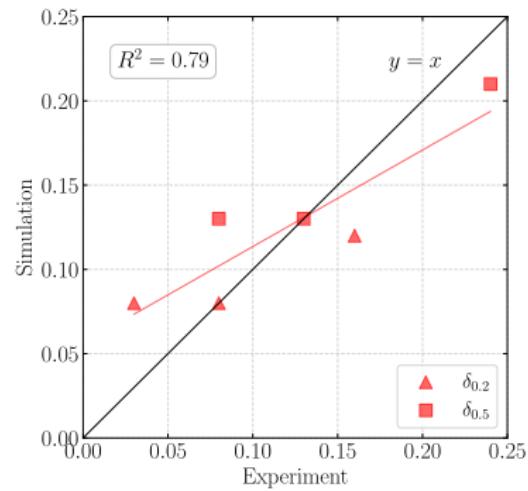
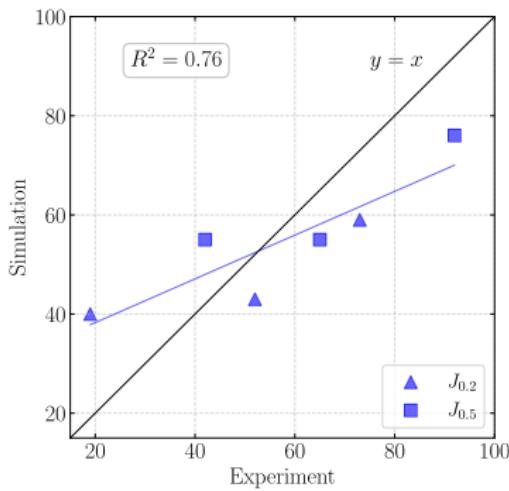
# Results: simulations vs. experiments



Specimen	$\delta_{max}$ (mm)	$\delta_{0.2}$ (mm)		$\delta_{0.5}$ (mm)	
		Experiment	Simulation	Experiment	Simulation
mDCT-2	0.25	0.16	0.12	0.24	0.21
mDCT-5	0.24	0.08	0.08	0.13	0.13
CT-7.5	0.33	0.03	0.08	0.08	0.13

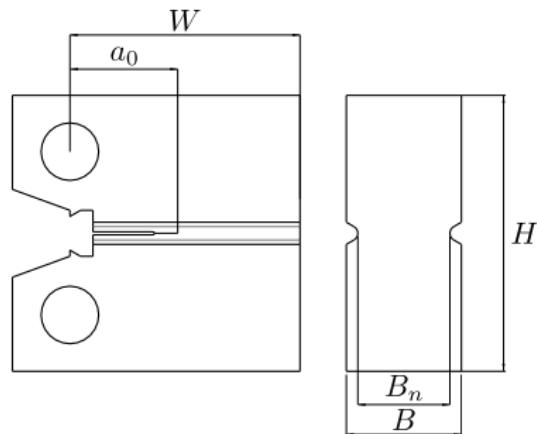
Construction line:  $\delta = 1.4\Delta a$  (ASTM E1820)

- ▶  $J$  and  $\delta$  provide overall good predictions of the experimental results
- ▶ In experiments,  $\delta$  is often **easier to correlate** with observed crack propagation  
→ **Directly measure**
- ▶ The  $J$ -integral relies on energy-based calculations that may not always align precisely with observed behavior



## Homothetic specimens:

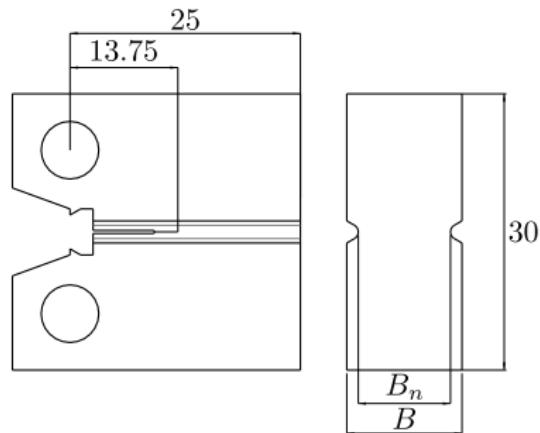
- ▶ **Homothetic CT specimens** → Dimensions scaled systematically from the smallest to the largest
- ▶  $B/W = 0.5$  for all cases
- ▶ Each mesh was generated individually, ensuring correct element size with respect to the internal length



	$W$ (mm)	$a_0$ (mm)	$B$ (mm)	$H$ (mm)
CT-3.125	6.25	3.4375	3.125	7.5
CT-6.25	12.5	6.875	6.25	15
CT-12.5	25	13.75	12.5	30
CT-20	40	22	20	60
CT-25	50	27.5	25	60
CT-50	100	55	50	120

## Varying thickness:

- **Varying thickness** → Specimen with the dimensions corresponding to a CT-12.5 with different thickness values



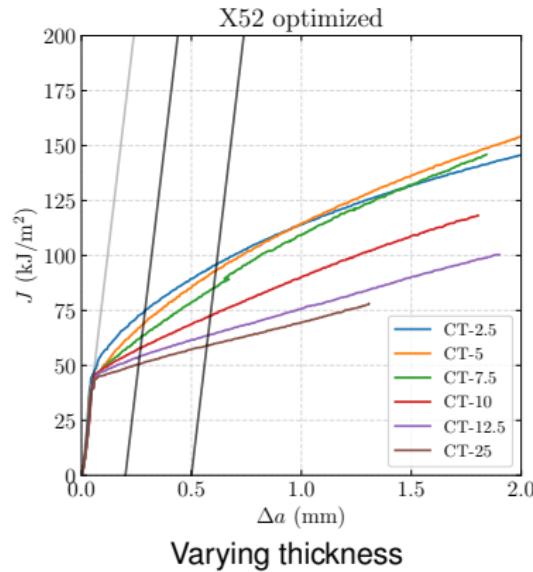
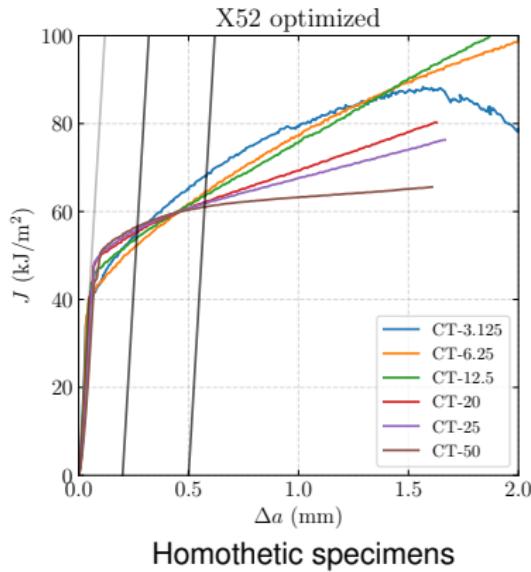
	$W$ (mm)	$a_0$ (mm)	$B$ (mm)	$H$ (mm)
CT-2.5	25	13.75	2.5	30
CT-5	25	13.75	5	30
CT-7.5	25	13.75	7.5	30
CT-10	25	13.75	10	30
CT-12.5	25	13.75	12.5	30
CT-25	25	13.75	25	30

- ▶ Coefficients identified for the X52 steel
- ▶ **Homothetic specimens:** Minor effect on toughness
- ▶ **Varying thickness:** Toughness decreased with thickness

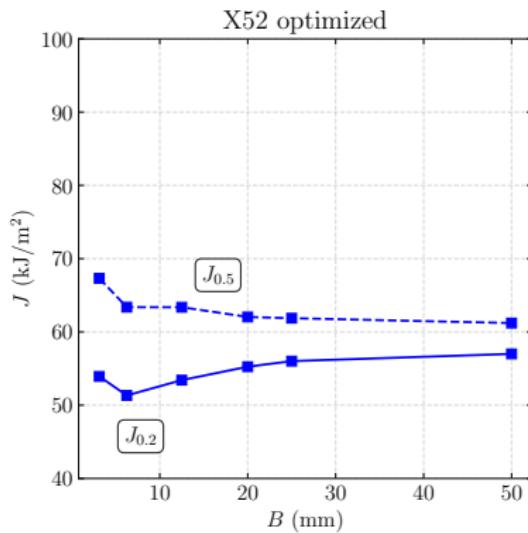
Hardening: X52

$q_1 = 1.25, q_2 = 1.40$

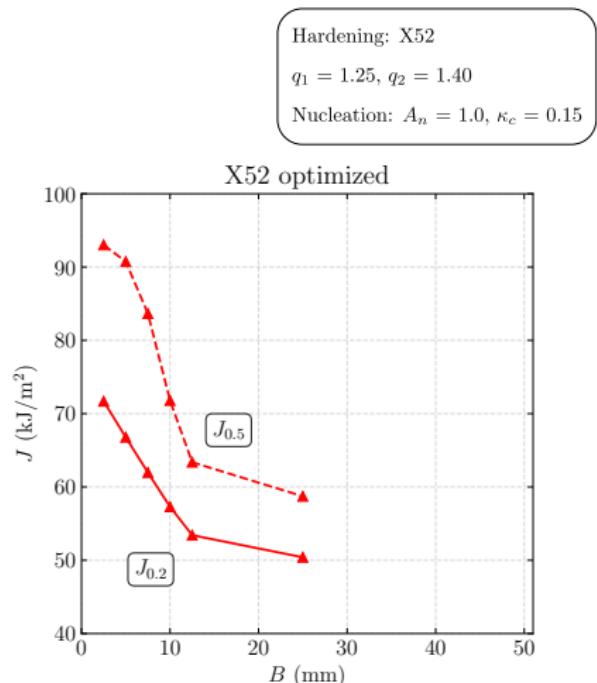
Nucleation:  $A_n = 1.0, \kappa_c = 0.15$



► Size and thickness effect on  $J_{0.2}$  and  $J_{0.5}$ :



Homothetic specimens



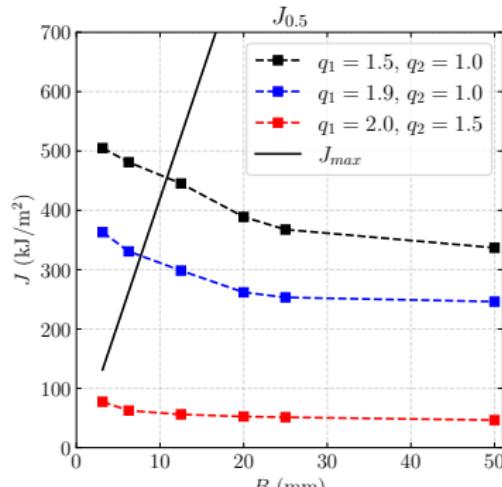
Varying thickness

## Varying damage coefficients:

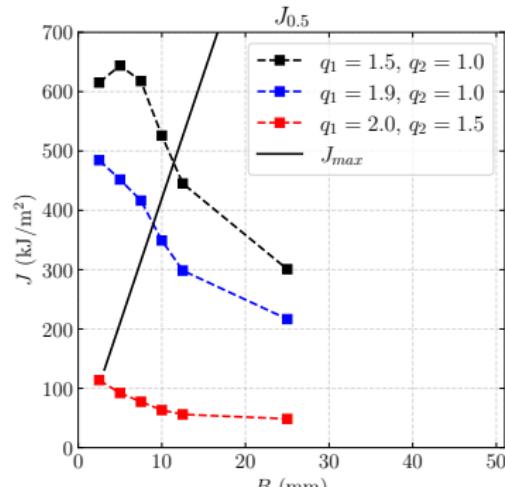
- ▶ **Hardening law:** same as the X52
- ▶ **GTN's coefficients:**
  - ▶  $q_1 = 1.5, q_2 = 1.0 \rightarrow$  **Most ductile case**
  - ▶  $q_1 = 1.9, q_2 = 1.0$
  - ▶  $q_1 = 2.0, q_2 = 1.5 \rightarrow$  **Less ductile case**
- ▶  $\uparrow q_1$ : increases void growth sensitivity, causing earlier growth and **reduced ductility**
- ▶  $\uparrow q_2$ : accelerates coalescence, leading to early crack initiation, **reduced ductility**, and abrupt fracture
- ▶ **Low void nucleation:**  $A_n = 0.2$  and  $\kappa_c = 0.8$

## Varying damage coefficients:

- ▶ Homothetic specimens exhibit more stable toughness values
- ▶ More ductile material present more size effects
- ▶ Even tests considered valid according to the standard can still display size effects



Homothetic specimens



Varying thickness

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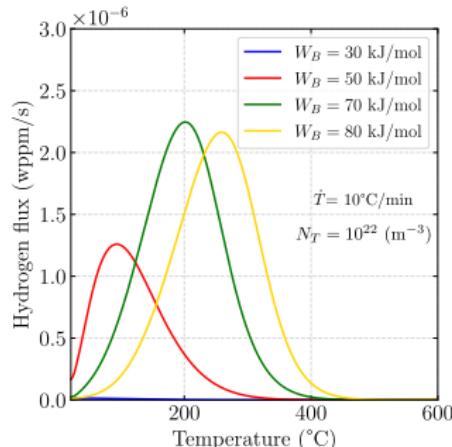
Simulation of fracture toughness tests

**Conclusions and perspectives**

- ▶ **Comprehensive HE modeling:** Developed a numerical framework integrating hydrogen diffusion, plasticity, and damage mechanisms.
- ▶ **Modified nonlocal GTN model:** Incorporated hydrogen-enhanced decohesion (HEDE) and diffusion effects, accelerating damage evolution and leading to premature failure.
- ▶ **Experimental validation & trends:** Applied the model to pressurized disk, tensile, and fracture toughness tests, accurately capturing key experimental trends such as toughness and ductility loss, strain rate effects, and the transition from ductile to quasi-brittle failure.
- ▶ **Fracture toughness & size effects:** Investigated the influence of specimen size and thickness on fracture toughness across different material configurations.
- ▶ **Key contributions:** Provided a robust framework for HE simulation, improving understanding of hydrogen-induced damage in pipeline steels.

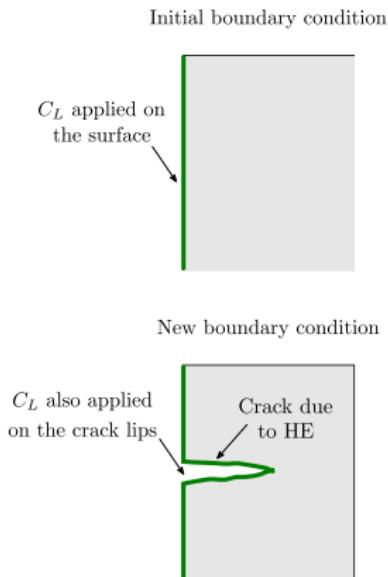
► Thermal Desorption Spectroscopy (TDS) simulations and tests:

- Conduct TDS tests to identify the various trapping sites.
- Simulate desorption curves under varying conditions.
- Consider implementing the McNabb-Foster model for improved peak predictions.



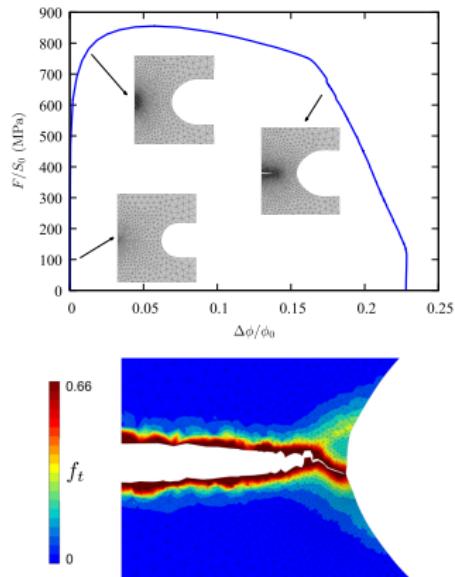
► Hydrogen boundary condition:

- Implementation of a new boundary condition that accounts for the newly created surfaces during crack propagation.



► Remeshing for crack propagation:

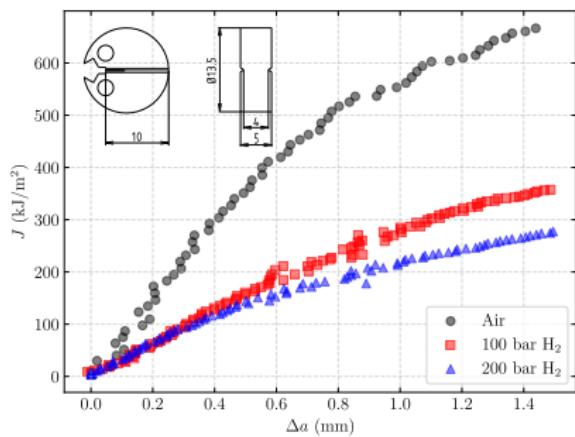
- Improve the remeshing framework to better handle 3D non-axisymmetric specimens.



(El Ouzani Tuhami *et al.*, 2022)

► Size effect & HE:

- Extend the study of hydrogen embrittlement in sub-size fracture toughness specimens.
- Analyze the interplay between size effects and hydrogen-induced damage.



(Experimental data: L. Santana)

# Thank you

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