

Finite element models for the study of hydrogen embrittlement of steel structures

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Thesis defense

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Hydrogen inside metals

Finite element formulation

Pressurized disks tests

Hydrogen uptake during a tensile test

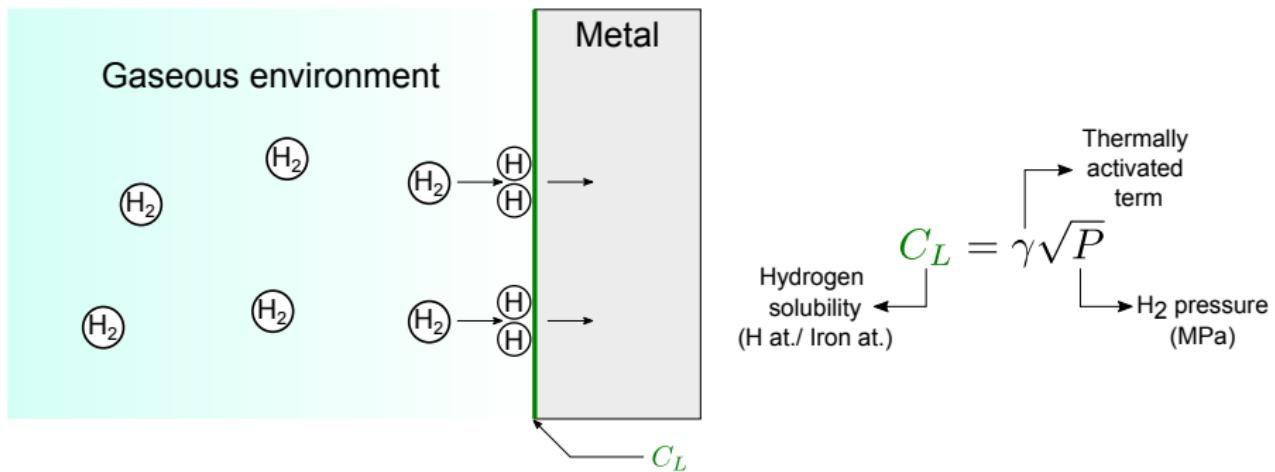
Hydrogen embrittlement modeling

Simulation of fracture toughness tests

Conclusions

Perspectives

- ▶ **Sieverts' law:** The solubility of a diatomic gas in a metal is proportional to the square root of the gas pressure

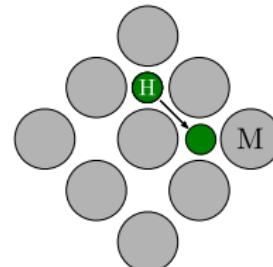


- Model from Sofronis and McMeeking (1989) and corrected by Krom *et al.* (1999)

- **Hydrogen concentration:** $C = C_L + C_T$

- Lattice concentration: $C_L = \beta N_L \theta_L$

- Trapped concentration: $C_T = \sum_i^N C_T^i = N_T^i(\kappa) \theta_T^i$



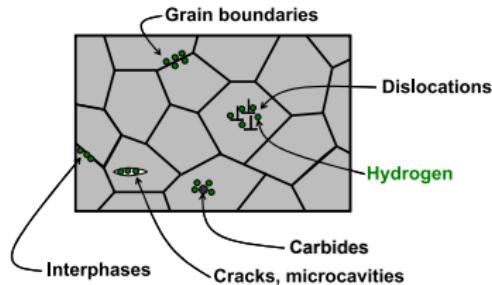
- **Hydrogen flux:**

$$J = -D_L \nabla C_L + \frac{D_L C_L V_H}{RT} \nabla p$$

- **Oriani's equilibrium:**

$$\frac{1 - \theta_L}{\theta_L} \frac{\theta_T^i}{1 - \theta_T^i} = K$$

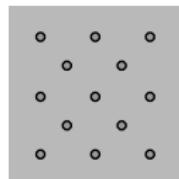
(Coupling terms)



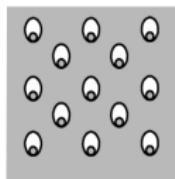
- The **ductile behavior** of the metal is described by the **GTN model** (Tvergaard *et al.* 1984):

$$\frac{\sigma_{eq}^2}{\sigma_F^2} + 2q_1 f_* \cosh \left(\frac{q_2}{2} \frac{\sigma_{ii}}{\sigma_F} \right) - 1 - q_1^2 f_*^2 = 0$$

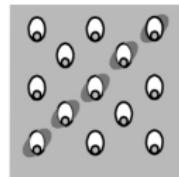
$$\dot{f} = \dot{f}_{nucleation} + \dot{f}_{growth}$$



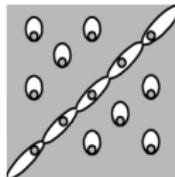
Impurities or second phase particles



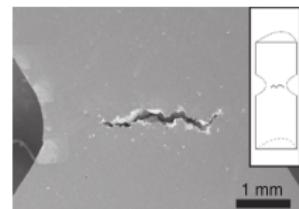
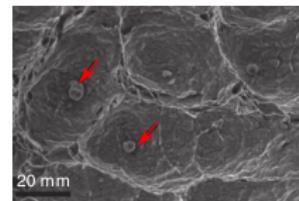
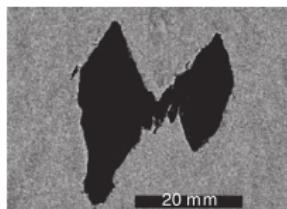
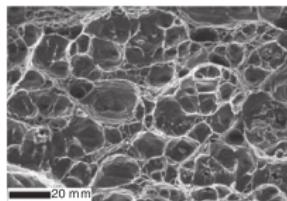
Void nucleation and growth



Strain localization



Void coalescence and fracture

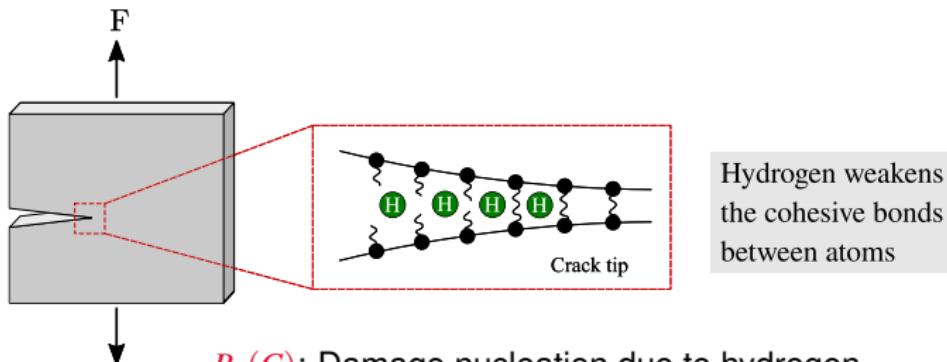


- **Void growth:** Unchanged due to mass conservation

$$\dot{f}_g = (1 - f_g) \text{trace}(\dot{\varepsilon}_p)$$

- **Void nucleation:** Proposed dependence on hydrogen concentration

$$\dot{f}_n = A_n(\kappa)\dot{\kappa} + B_n(C)\dot{\kappa} \quad (\text{Coupling terms})$$



Hydrogen weakens
the cohesive bonds
between atoms

$B_n(C)$: Damage nucleation due to hydrogen
HEDE (Hydrogen Enhanced Decohesion)

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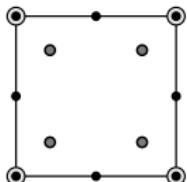
- ▶ Fully implicit finite strain framework
 - ▶ Based on a mixed formulation: \underline{u}, P, θ (Zhang *et al.* 2017) and C_L
 - ▶ Quadratic elements with reduced integration
 - ▶ **Aim:** better pressure fields by avoiding volumetric locking



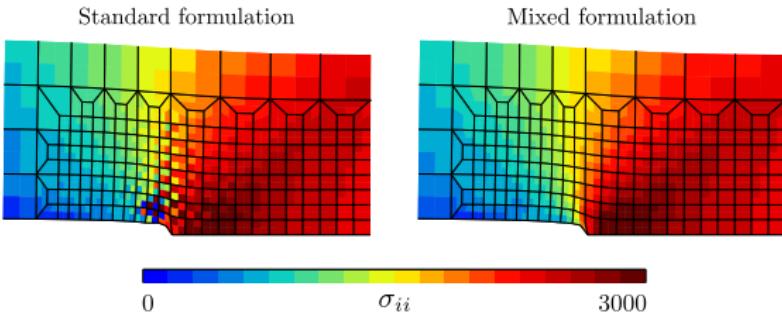
Advantage

∇p can be directly computed from nodal values

$$J = -D_L \nabla C_L + \frac{D_L C_L V_H}{RT} \nabla p$$



- u
 - p, θ, C_L
 - Integration point



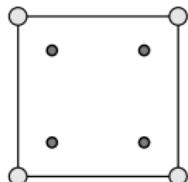
- ▶ The use of **quadratic elements** with additional dofs lead to **high simulation times**

- B -bar (or \bar{B}) formulation (Hughes, 1980):

- ▶ Linear elements with full integration
 - ▶ Solves volumetric locking by modifying the strain-displacement matrix:

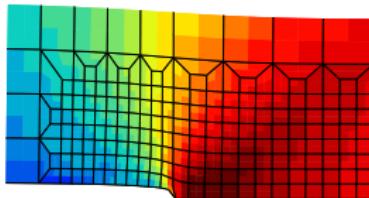
$$\bar{\mathbf{B}} = \mathbf{B}_d + \bar{\mathbf{B}}_h$$

- To avoid extrapolating p to the nodes for ∇p computation, it is considered as a dof

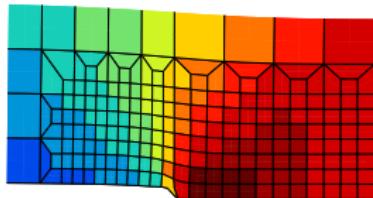


- \mathbf{u}, p, C_L
- Integration point

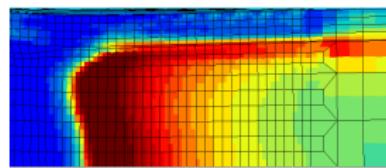
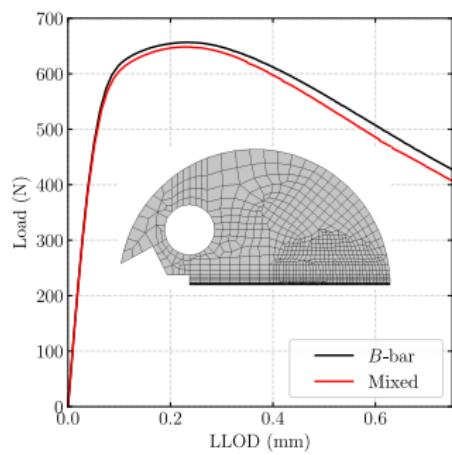
Mixed formulation



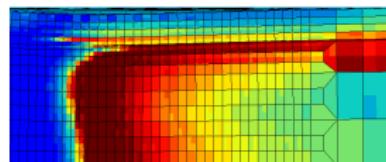
B-bar formulation



- ▶ Test on a Disk Compact Tension (DCT) specimen with 5200 elements:
 - ▶ **Mixed formulation:** 103,762 dofs, 1h 40 minutes to complete
 - ▶ **B-bar formulation:** 33,974 dofs, 18 minutes to complete
- ▶ Slightly higher force for the **B-bar** formulation → Linear elements are inherently stiffer since they have less nodes



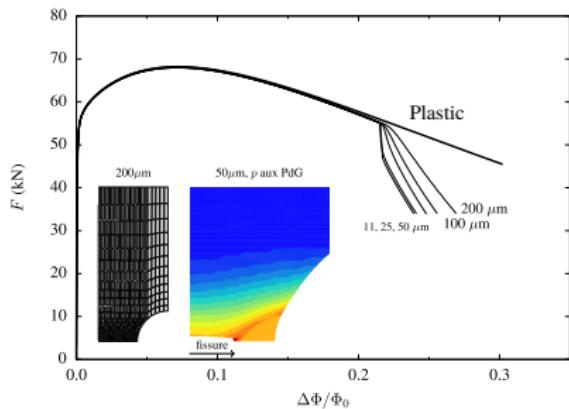
Mixed formulation



B-bar formulation

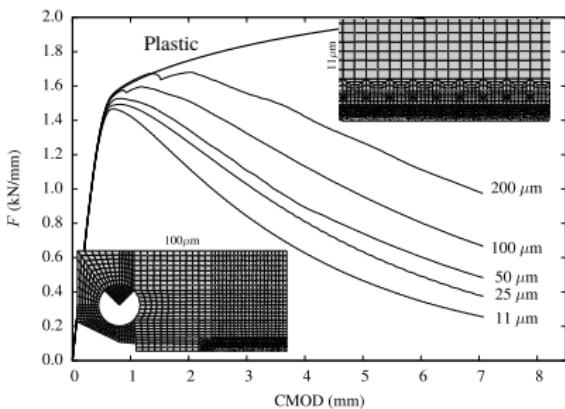


- ▶ Damage models such as the GTN model are known to induce **spurious mesh dependency** (element size, type and orientation)
- ▶ To solve this problem, it is proposed to use a **nonlocal damage model** based on the **implicit gradient** by Peerlings *et al.*, 1996



Notched tensile (NT) specimen

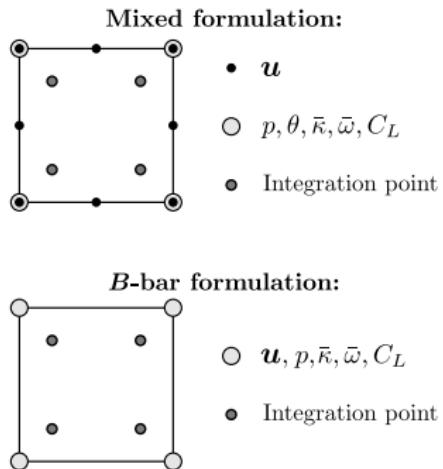
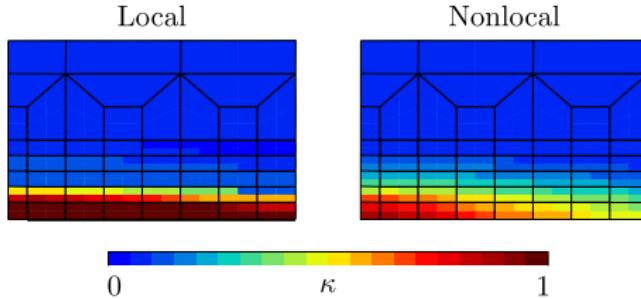
(Besson, 2021)



Compact tension (CT) specimen

- ▶ Two variables are used (two associated internal lengths: $\bar{\omega}$ and $\bar{\kappa}$):
 - ▶ **Plastic volume variation:** $\bar{\omega} - \ell_{\omega}^2 \Delta \bar{\omega} = \omega$ where $\omega = \text{trace}(\dot{\varepsilon}_p)$
 - ▶ **Accumulated plastic strain:** $\bar{\kappa} - \ell_{\kappa}^2 \Delta \bar{\kappa} = \kappa$ - ▶ The modified evolution laws for the damage variables are now:

- ▶ **Void growth:** $\dot{f}_g = (1 - f_g) \dot{\bar{\omega}}$
 - ▶ **Void nucleation:** $\dot{f}_n = A_n \dot{\bar{\kappa}} + B_n(C) \dot{\bar{\kappa}}$



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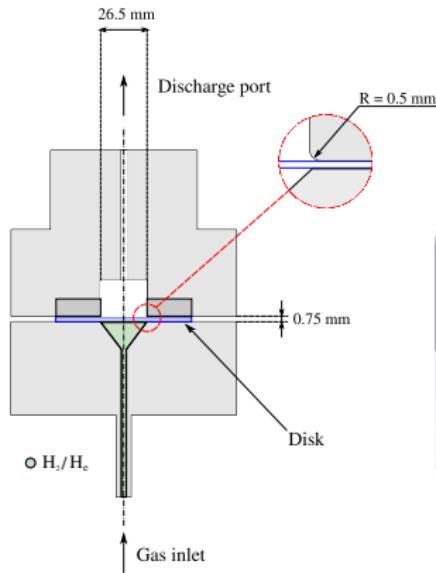
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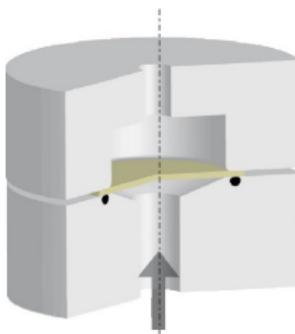
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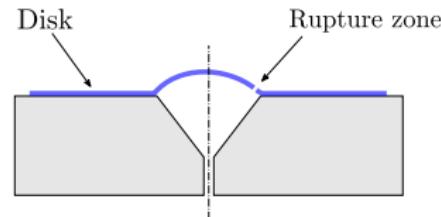
- ▶ **ISO 11114-4 standard:** uses pressurized disk tests for selecting metallic materials resistant to hydrogen embrittlement
- ▶ Disk often fails in the clamping zone → **Hard analysis**
- ▶ **First step:** redesigning the disk geometry to control failure location



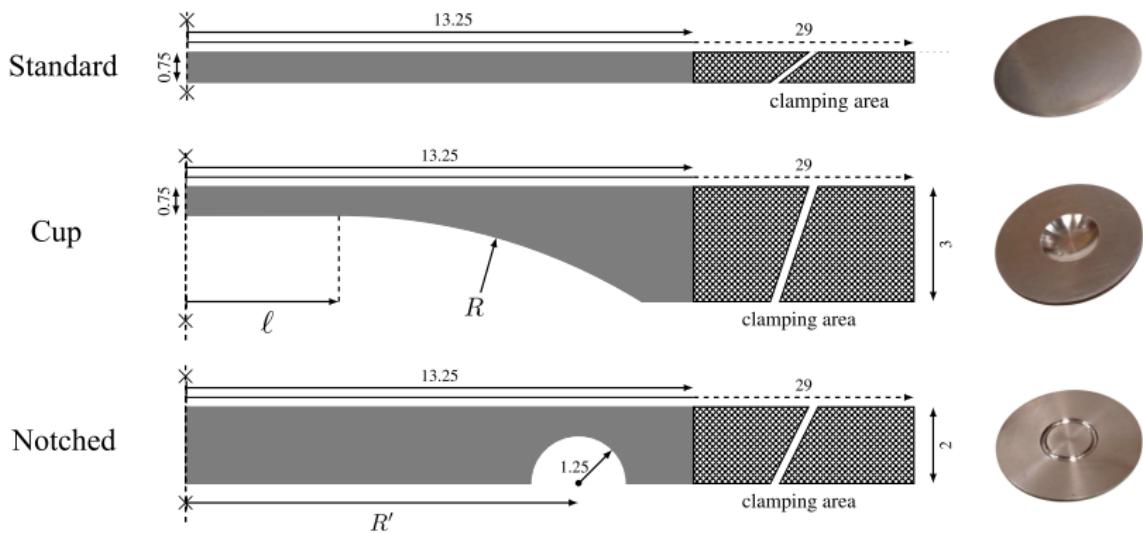
$$\text{HEI} = \frac{P_r(\text{He})}{P_r(\text{H}_2)}$$



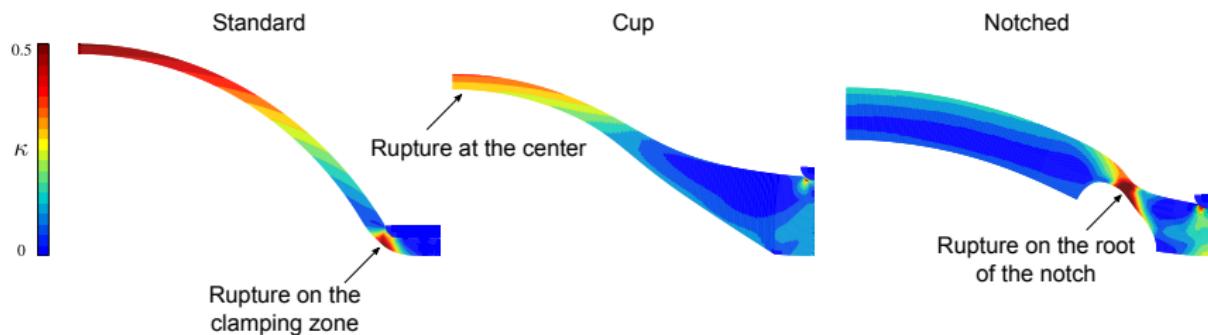
Disk specimen:



- ▶ New proposed geometries:
 - ▶ No need to modify the test setup
 - ▶ Keep the same minimum thickness of the standard (0.75 mm)
- ▶ Optimization with respect to ℓ , R and R' with FE simulations considering an elasto-plastic behavior



- ▶ The location of the maximum accumulated plastic strain (κ) corresponds to the failure location



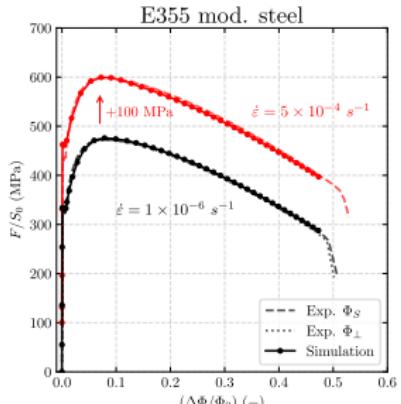
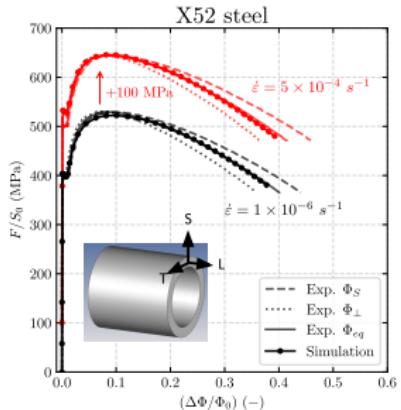
► X52 vintage steel:

- ▶ Yield strength: 400 MPa
- ▶ Different elongation at rupture in T and L directions

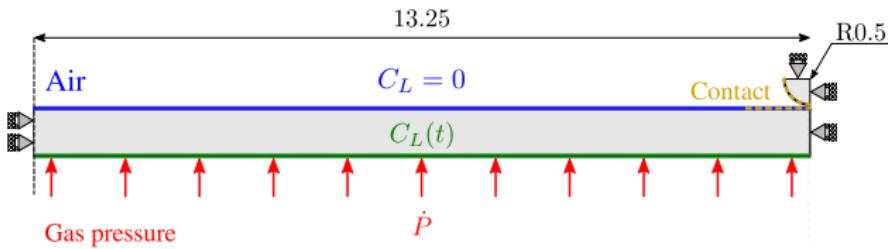
► E355 mod. steel:

- ▶ Yield strength: 330 MPa
 - ▶ Higher elongation at rupture and lower Ultimate Tensile Strength in relation with the vintage material
 - ▶ Similar elongation at rupture in both directions
- Elasto(visco)-plastic model coefficients' identified through optimization:

$$\sigma_F(p) = \max(\sigma_L, \sigma_0 + Q_1(1 - \exp(-b_1 p)) + Q_2(1 - \exp(-b_2 p)) + H p)$$

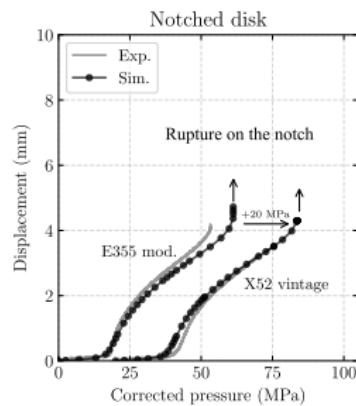
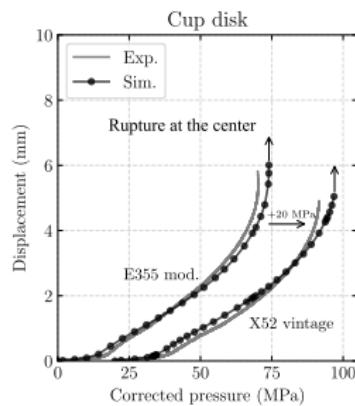
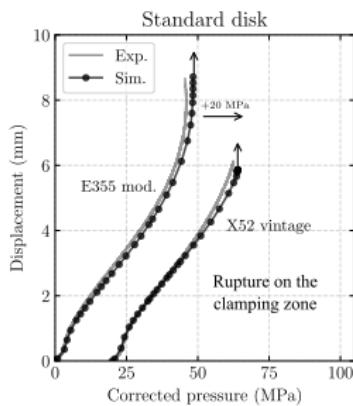


- ▶ Axisymmetric model, quadratic elements with reduced integration (mixed formulation)
- ▶ Hydrogen diffusion parameters taken from the literature
- ▶ Since damage is not considered into the numerical model, the simulations were stopped once they reached experimentally observed rupture pressure (P_r)
- ▶ Model's boundary conditions:



Geometry effect (under helium)

- ▶ Good agreement between experimental and numerical results
- ▶ Successfully modification of fracture location
- ▶ Failure is primarily driven by plasticity and occurs under a limit load scenario



- ▶ Considers only dislocations as traps

Thank you for your attention

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