

# Simulating Patterns of Patient Engagement, Treatment Adherence, and Viral Suppression: A System Dynamics Approach to Evaluating HIV Care Management

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## Abstract

System dynamics (SD) modeling belongs to the rapidly evolving, interdisciplinary field of system science research. This field adds value to more traditional health research by contributing to the design and testing of complex integrated models of change, to examine health system performance and patient outcomes. Using selected milestones in HIV care management to frame our simulation research, we created a SD model to examine three patient subgroups of women of color (WOC) represented in our multi-site cohort, classified by their health care seeking status at baseline. Asked to reflect on their circumstance 6 months prior to enrollment in the MSE cohort, 53% noted they were receiving some care (In Care,  $n = 341$ ), 31% that they had been seeking care (Seeking Care,  $n = 201$ ), and 16% that they were undecided about seeking care (i.e., answered that they may or may not look for care) for treatment of their HIV (May or May Not Seek Care,  $n = 103$ ). Our SD model compared simulated patterns of patient retention over 24 months in relation to: (1) access to antiretroviral therapy (ART), (2) adherence to ART, and (3) viral suppression. Assessed patterns yielded insights about system capacities and constraints in the context of the SPNS initiative under evaluation.

## Introduction

ONE COMPONENT OF THE MULTI-SITE EVALUATION (MSE) of the *Enhancing Access and Quality HIV Care for Women of Color* (WOC) Special Projects of National Significance (SPNS) initiative involved the application of systems thinking and system dynamics (SD) modeling—a computer-aided mathematical simulation methodology—to enhance understanding of the temporal relationship between the care delivery process and key patient outcomes. In this article, we describe how systems thinking and SD modeling can be used to elucidate ‘interdependencies’ in processes of patient engagement, treatment adherence, and viral suppression, and how a systems approach to studying HIV care management can help inform robust health care policy and practice at local, regional, and national levels.<sup>1,2</sup>

Systems thinking and SD belong to the rapidly evolving, interdisciplinary field of system science research.<sup>3–5</sup> This field adds value to more traditional health research methods by contributing to the design and testing of integrated models

of change, to examine health system performance and patient outcomes.<sup>6</sup> Methods include a variety of tools for better understanding complex problems,<sup>1,7</sup> with the objective being the move away from framing problems in terms of events and causes or outcomes, towards looking at them as a system comprised of interacting parts with a particular goal.<sup>8–10</sup> In addition to SD modeling, social network analysis, agent-based modeling, micro-simulation, discrete event analysis, Markov modeling, and many operations research and engineering methods constitute systems science approaches that show promise for health research and health policy studies.<sup>3,11</sup>

The hallmark of the SD approach to systems thinking and simulation is the study of feedback mechanisms, or cybernetics, which can be used to explain how things change over time.<sup>12–15</sup> Systems thinking typically employs qualitative tools that often support development of robust SD models, which are computer-aided, mathematical tools that use simulation techniques to explore complexity and change of a stated problem situation.<sup>8,16,17</sup> Once systems thinking and SD models are validated, and there is confidence in their structure

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and behavior, they can be put to the task of generating plausible, sustainable solutions by using the model for policy testing, scenario analyses, or intervention optimization.<sup>18–22</sup>

SD modeling has been used to examine health care quality improvement;<sup>11,23–28</sup> community-based systems of care;<sup>29–32</sup> epidemiology and disease surveillance;<sup>33–37</sup> global health care management;<sup>38–40</sup> behavioral health interventions in tobacco;<sup>37,41–45</sup> substance abuse;<sup>46–49</sup> and mental health;<sup>9,50</sup> as well as in managing chronic illness.<sup>32,51,52</sup> SD modeling to examine HIV epidemiology, prevention, and treatment has also been conducted.<sup>53–55</sup> In addition, a system dynamics model called *HealthBound*, originally developed for the Centers for Disease Control and Prevention (CDC), is currently being used in a project called *ReThink Health*, to help people understand the critical relationship between “upstream” efforts to prevent illness and the demand for the relationships between a community’s access to care, health status, and socioeconomic level.<sup>56</sup>

## Methods

SD model-building deploys an iterative research process that is complete when the model achieves sufficient ‘structural’ and ‘behavioral’ validity to its intended purpose.<sup>57–59</sup> Procedures for establishing structural and behavioral validity are organized around the purpose of the model, the type and quality of the sources of evidence, and calibration.<sup>13,21,60</sup> The model is a working set of algebraic and ordinary differential equations, generally shown as a diagram, which can then be used as a tool to explore hypotheses about the factors that contribute to the stated problem, as well as to compare problem-solving strategies.<sup>16,17,61</sup>

### Overview of system dynamics model-building steps

Major steps in SD model-building include *system conceptualization*, *model formulation*, and *model simulation*. System conceptualization is largely qualitative, whereby the model-building team names constructs of interest and drafts hypothesized causal influences and interdependent relationships. Model formulation involves translating the system conceptualization into a set of equations using SD modeling software and checks for structural validity of these equations. Model simulation refers to running the SD model and examining its output to ensure expected and/or plausible behavior. It also refers to conducting sensitivity analyses in which ranges of variable values are simulated to generate effects on selected outcomes in order to evaluate behavioral validity. Finally, model simulation includes the comparison of simulated outputs.

### System conceptualization

Broadly, we used SD to develop a tool to examine processes of HIV care management.<sup>2</sup> The Health Resources and Services Administration (HRSA)<sup>62</sup> and the Center for Disease Control and Prevention<sup>63</sup> have defined five key ‘stages of care,’ or milestones, for the purpose of evaluating overall progress in HIV testing and treatment success. These key stages are presented as a percentage of the estimated total patient population who are *diagnosed*, *linked to care*, *retained in care*, *prescribed antiretroviral therapy* (ART), and *who are virally suppressed*.

Part of the goal of the SPNS WOC initiative was to collect data on the patient population related to these metrics. Using the ‘stages of care’ as a framework for our simulation research, we created a SD model to examine three patient subgroups of WOC who were represented in our MSE cohort, classified by their health care seeking status at baseline. Asked to reflect on their circumstance 6 months prior to enrollment in the MSE cohort, 53% noted they were receiving some care (In Care,  $n=341$ ), 31% that they had been seeking care (Seeking Care,  $n=201$ ), and 16% that they were undecided about seeking care (i.e., answered that they may or may not look for care) for their HIV (May or May Not Seek Care,  $n=103$ ).<sup>64</sup> Our SD model compared simulated patterns of patient retention over 24 months in relation to: (1) access to antiretroviral therapy (ART), (2) adherence to ART, and (3) viral suppression.

Comparison of patterns for these groups was hypothesized to yield insights about system capacities and constraints, in the context of the SPNS initiative under evaluation.

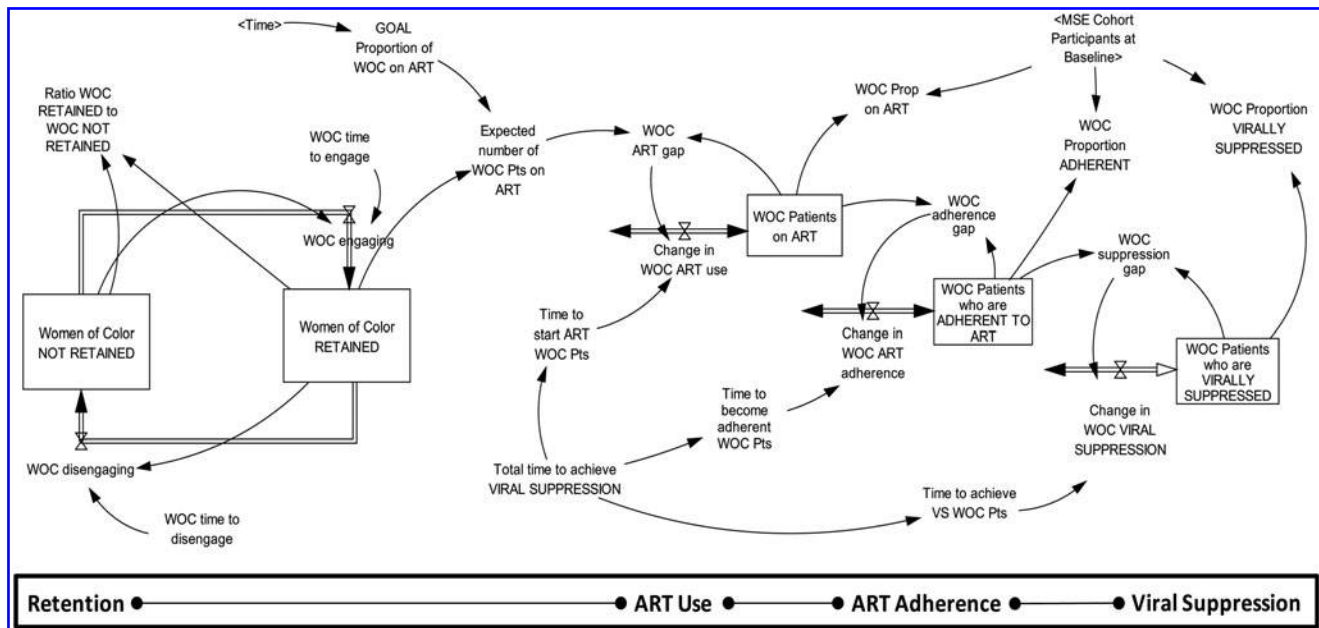
### Model formulation

Formulation of an SD model is facilitated by computer simulation software packages. Powersim<sup>®</sup>, iThink/Stella<sup>®</sup>, and Vensim<sup>®</sup> are among the most widely used packages for SD modeling. These software packages allow users to work with a graphical interface to build the model, equation by equation, examining preliminary simulation runs in an iterative fashion, to check and re-check the extent to which the model’s behavior (simulated output) conforms to key assumptions and sources of evidence guiding the project.

Figure 1 depicts our SD model, which is presented as a Vensim<sup>®</sup> stock-and-flow diagram. Three basic types of structure detail are shown: levels or *stocks*, rates of flow or *flows*, *auxiliary variables*, and constants (*parameters*). Stocks are accumulations of material or information at a given moment. Flows are what increase or decrease a stock, incrementally, over time. Parameters are variables that have a fixed value (at least over a specified simulation time period or time horizon). Auxiliaries are terms used to build algebraic equations. Stocks are represented by a rectangle. Flows are represented by a double-lined arrow and a faucet-like icon. Often one end of a flow structure will be attached to a cloud icon. The cloud represents a sink, or a source of material or information that accumulates outside of the model boundary.

Major structures (i.e., constructs) represented in our SD model include *Retention*, *ART Use*, and *Viral Suppression*, as well as a hypothesized mediating structure not explicitly referenced in the ‘stages of care’ framework: *ART Adherence*. The decision to add Adherence to our SD model was informed by results of the MSE cohort study, which found that WOC who reported good medication adherence at baseline were more likely to be virally suppressed at 12 months (OR = 2.077; 95% CI = 1.38, 3.12),<sup>64</sup> as well as by recent and robust HIV care literature on retention in HIV care, ART use and adherence, and viral suppression.<sup>65–71</sup>

The Retention structure is comprised of two stocks or persons (WOC), those who are ‘retained’ and those who are ‘not retained.’ We applied the HIV/AIDS Bureau’s (HAB) Core Clinical Performance Measures definition of ‘retained in care,’ such that one would have at least two visits, 3–6 months apart, within a given 12-month period to be classified



**FIG. 1.** Stock-and-flow structure of a system dynamics model depicting patient engagement, treatment adherence, and viral suppression.

as 'retained'.<sup>72</sup> The two stocks are linked by a flow of persons into and out of these stocks. The flow of persons is determined by the rate at which WOC 'engage' and 'disengage' from care. The initial value, the number of WOC in the stock at baseline ( $T_0$ ), is exactly half (50%) of the respective subgroup's sample size. Note that the number of WOC in the 'retained' stock is used to drive the dynamics of ART Use, ART Adherence, and Viral Suppression, which collectively form a *cascaded smooth structure*.

The *smooth* is a generic system dynamics structure that computes a moving average of the given variable. The smooth structure is defined by three parameters: its initial value and a future goal value, and the average time delay (i.e., time constant) to attain the goal. Note that the rate of change is intended to close the gap, or the difference between the expected value (or goal), and the smooth stock (or actual value). The stock adjusts toward the goal over time, unless it is impacted by another variable. The gap between the actual value and the expected value (or goal) is closed according to the specified smoothing time. The magnitude of the gap would decline to zero over the smoothing time if the net inflow were held constant, resulting in the actual value approaching the expected value (i.e., 'goal'). Hence, the smooth structure will ultimately generate a steady state condition.

The goal value for ART Use, the first smooth in the cascade structure, increases linearly from a baseline level at  $T_0$  (which was computed from the MSE cohort study data;<sup>64</sup>

Table 1) to a maximum of 90% after 12 months ( $T_{12}$ ), a clinical recommendation and performance measures cited by HAB.<sup>72</sup> Figure 2 graphs the reference modes (i.e., behavior-over-time graphs) for *Proportion of WOC who are prescribed ART* formulated in the model for each WOC subgroup. Note that the slope of the line from  $T_0$  to  $T_{12}$  is steepest for the May or May Not Seek Care subgroup ( $m=0.015917$ ), suggesting that the level of effort required to meet the goal for this subgroup of patients would be resource-intensive, relative to the ( $m=0.01667$ ) and ( $m=0.04833$ ) subgroups.

As the number of WOC retained in care changes over time, the cascaded smooth structure captures the average time it takes to access ART, to 'learn' how to become adherent, and ultimately how to achieve viral suppression. Due to limited journal space, the SD model and full equations comprising the model could not be presented here, but instead are packaged as supplementary material to the article, provided upon request to the corresponding author.

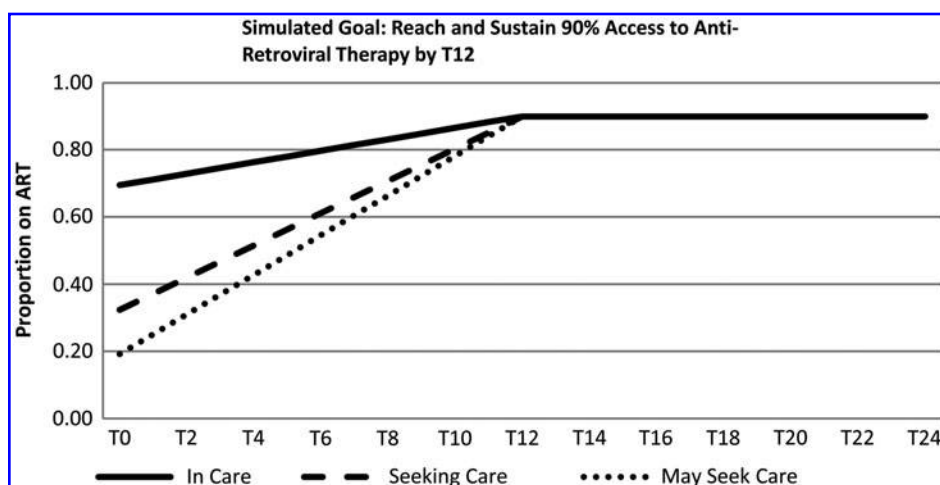
#### Model simulation

The incremental time unit for our SD model was 'months,' and the time horizon selected for simulation was 24 months. The first half of this period,  $T_0$  to  $T_{12}$ , allowed for an historical validation of the SD model's behavior, based on known retention and viral suppression point estimates (rates) for the three patient subgroups, per analyses of the MSE cohort data.

TABLE 1. PARAMETER ESTIMATES FOR CALIBRATED SYSTEM DYNAMICS MODEL

Model construct	Parameter	In Care %	Seeking Care %	May Seek Care %
ART use	Proportion of WOC on ART at baseline	0.70	0.32	0.19
ART adherence	Proportion of WOC w/'good' ART adherence at baseline	0.46	0.18	0.11
Viral suppression	Effect of ART adherence w/viral suppression	0.33	0.15	0.18

Source: Multi-Site Evaluation Cohort Study ( $N=645$ , In Care  $n=341$ , Seeking Care  $n=201$ , May Seek Care  $n=103$ ).



**FIG. 2.** References modes for ART use for baseline care status by WOC patient subgroup.

The second 12-month period ( $T_{13}$ – $T_{24}$ ), then, allowed us to simulate plausible ‘future’ trajectories for *Retention* in relation to *ART Use*, *ART Adherence*, and for *Viral Suppression*.

In order to generate reliable, valid simulation runs, the model must be appropriately calibrated. Model calibration involves choosing and testing estimates for initial values and other parameters in the SD model. An important goal of model calibration is the process of estimating the model parameters to obtain a match between observed and simulated behavior. Confidence that a particular structure, with reasonable parameter values, is a valid representation of reality increases if the structure is capable of generating the observed behavior.<sup>60,73</sup> For the current model, calibration was organized around the goal of simulating valid reference modes for (1) *Retention* and *Viral Suppression*, in relation to determined estimates of (2) other, key known parameters:

Reference modes for Retention and Viral Suppression rates. Statistical analyses of our MSE cohort data informed choice of parameter estimates in our SD model.<sup>64</sup> Specifically, we used estimated values for baseline ( $T_0$ ) and 12-

month ( $T_{12}$ ) retention and viral suppression rates for *In Care*, *Seeking Care*, and *May or May Not Seek Care* patient subgroups (Table 2).

**Key parameter estimates.** In addition, we used MSE cohort study data to derive estimates of other key model parameters for each patient subgroup, namely the proportion of WOC on ART at baseline, the proportion of WOC with ‘good’ ART adherence at baseline, and the effect size (Pearson Product Moment Correlation,  $r$ ) between ART adherence and viral suppression<sup>64</sup> (Table 1).

The calibration of the model was conducted iteratively, examining differences between simulated output and MSE cohort study data, identifying possible reasons for those differences, and adjusting time constants that control the flow of WOC between ‘not retained’ and ‘retained,’ and the flow of information depicting levels of *ART Use*, *ART Adherence*, and *Viral Suppression* for those who are ‘retained.’ Calibration is completed when the parameterized structure and the behavior of the model support a valid representation of the focal problem.

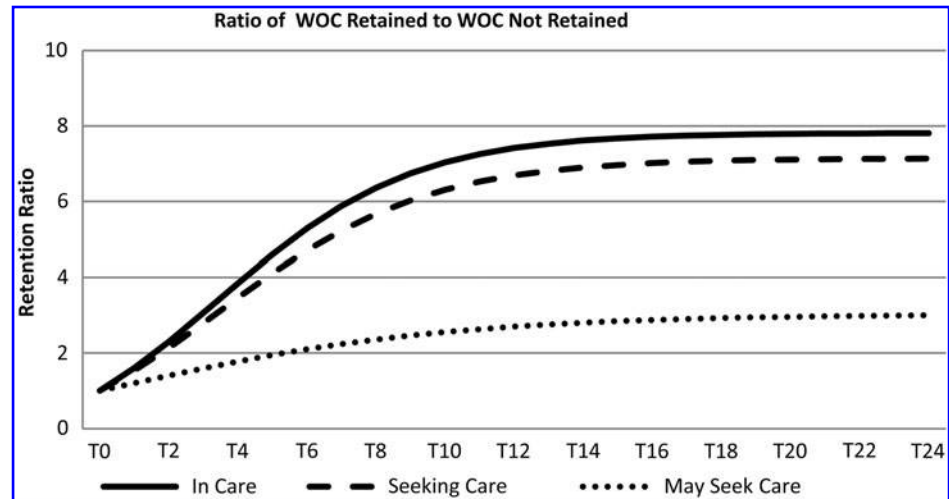
TABLE 2. EXPECTED PROPORTION OF RETAINED WOC WITH SUPPRESSED VIRAL LOAD AT 12 MONTHS

Baseline care seeking subgroup	Status at 12 months	Viral load test result					
		Total		Not suppressed		Suppressed <200	
		N	%	N	%	N	%
In Care	Not retained	41	12%	17	5%	24	7%
	Retained	300	88%	82	24%	218	64%
	Total	341	100%	99	29%	242	71%
Seeking Care	Not retained	26	13%	16	8%	10	5%
	Retained	175	87%	67	33%	108	54%
	Total	201	100%	83	41%	118	59%
May/May Not Seek Care	Not retained	27	26%	15	15%	12	12%
	Retained	76	74%	29	28%	47	46%
	Total	103	100%	44	43%	59	57%
Total	Not retained	94	15%	48	7%	46	7%
	Retained	551	85%	178	28%	373	58%
	Total	645	100%	226	35%	419	65%

Source: Multi-Site Evaluation Cohort Study.



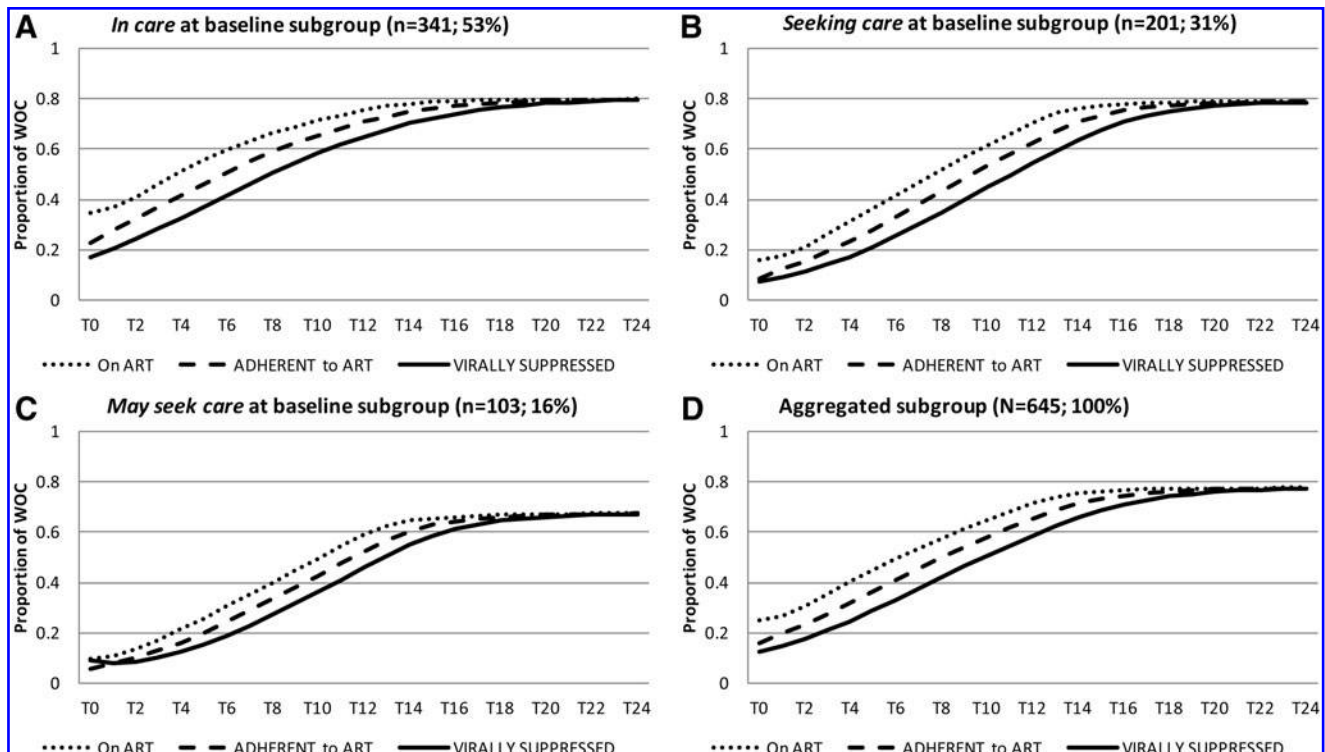
**FIG. 3.** Simulated dynamics of retention for baseline care status by WOC patient subgroup.



## Results

Using our calibrated SD model, the simulated output of the *Retention* structure and the cascaded smooth structure for *ART Use*, *ART Adherence*, and *Viral Suppression* displays trajectories over our 24-month time horizon (Figs. 3 and 4). Figure 3 presents the dynamics of retention for each subgroup of WOC. Figure 3 shows the ratio of ‘retained’ to ‘not retained’ WOC, showing that the *In Care* subgroup had the highest ratio of ‘retained’ to ‘not retained’ WOC (7.8 to 1 by T<sub>16</sub>), followed by the *Seeking Care* subgroup (7.1 to 1 by T<sub>18</sub>), and then by the *May or May Not Seek Care* subgroup (2.8 to 1 by T<sub>18</sub>).

Figure 4 presents simulated patterns of output for the third order cascaded smooth structure, representing the dynamics of *ART Use*, *ART Adherence*, and *Viral Suppression*. Panels A, B, and C show results for *In Care*, *Seeking Care*, and *May or May Not Seek Care* subgroups, respectively. Panel D shows the pattern for the full, aggregated cohort. By observation, simulation of the *In Care* subgroup (A) shows the highest (best) starting levels for *ART Use*, *Adherence*, and *Viral Suppression*, as well as a nearly linear upward slope, attaining the highest levels of viral suppression by T<sub>22</sub> (79% by T<sub>22</sub>). The *Seeking Care* subgroup (B) shows lower starting values than the *In Care* subgroup, but finishing at the same levels (79% virally suppressed by T<sub>22</sub>). In contrast, the *May*



**FIG. 4.** Simulated dynamics of HIV care management by baseline care status subgroup.

TABLE 3. FINAL TIME CONSTANTS FOR CALIBRATED SYSTEM DYNAMICS MODEL

Model construct	Time constant	In Care months	Seeking Care months	May Seek Care months
Retention	Time to engage	3.2	3.5	6.6
Retention	Time to disengage	25.0	25.0	20.0
	Total time to achieve viral suppression	6.0	5.1	4.2
ART use	Time to start ART	2.0	1.7	1.4
ART adherence	Time to become adherent	2.0	1.7	1.4
Viral suppression	Time to achieve viral suppression	2.0	1.7	1.4

or *May Not Seek Care* subgroup (C), which has the lowest proportion of WOC on ART at baseline (10%), has a higher proportion of persons who are virally suppressed at baseline (8% of *May Nots* compared to 7% of *Seeking*), though the lowest level of adherence (5%). The *May or May Nots* also attain the lowest level of viral suppression over the 24-month time horizon, stabilizing at 67% by T<sub>24</sub>. Notably, the *May or May Nots* exhibit a robust ‘S’ shaped curve, indicating relatively substantial improvement over time, relative to the patterns of the other two subgroups. Examination of Panel D shows an overall pattern most similar to the *In Care* subgroup, which reflects their size (53% of *N*=645) relative to the other two subgroups. Notably, the cohort level of viral suppression does not exceed 77%, which is not reached until T<sub>24</sub>.

Finally, based on our final model calibration, Table 3 presents a comparison of time constants, or the average time required to transition from one state to another (e.g., from ‘retained’ to ‘not retained,’ or from ‘not yet virally suppressed’ to ‘virally suppressed’). What is shown is that time *In Care* and *Seeking Care* subgroups are similar in terms of time to ‘engage’ in and ‘disengage’ from being retained in care (3.3–3.5 months to ‘engage,’ respectively; and 25 months both to ‘disengage’). In contrast, the *May or May Nots* take approximately twice as long (about 88% longer) to ‘engage’ and about 20% less time to ‘disengage’ from being retained. However, total average time to achieve viral suppression, for an individual in the *In Care* subgroup is 18% higher than for an individual in the *Seeking Care* subgroup, and 42% longer than for an individual in the *May or May Not* subgroup.

## Discussion

Our SD model demonstrates a useful application of simulation methods for evaluating HIV care management systems, by explicitly showing the dynamics of patient engagement relative to ART adherence and viral suppression. We build upon findings in the MSE of the *Enhancing Access and Quality HIV Care for WOC* initiative and upon a growing literature on the relationship between retention in high quality HIV care and achieving viral suppression.<sup>65,67–71,74–78</sup>

We embroidered on the ‘stages of care’ model for understanding HIV care management outcomes by adding ART adherence as a mediating structure. There is strong evidence that adherence improves outcomes for HIV patients.<sup>79,80</sup> Our simulation analyses show that patterns of adherence may differ for persons with different rates of engagement and levels of retention with health care. Notably, a smaller number of persons who are ambivalent about seeking care will be retained, although our analysis indicates that they respond to treatment comparatively quickly.

For clinicians, the need to actively set high goals for fostering patient access to ART is requisite for attaining and sustaining high levels of viral suppression among patients. In the current SD model, the goal for each patient subgroup was set to 90%, which is consistent with current national guidelines in HIV care management.<sup>2</sup> However, as simulated results for the *May or May Not Seek Care* subgroup showed, there may be a need for interventions that address the often multiple and complex needs of patients, as evidenced in by Eastwood et al. (this issue),<sup>64</sup> if we are to make greater strides in overall HIV care management. For example, factors such as substance abuse, exposure to violence, physical health, mental health, housing fragility, and having young children may all negatively impact efforts to help a patient stay in care and attain viral suppression.

Although the current SD model is a useful tool for examining patterns of HIV care management, it does not simulate any specific intervention to improve retention or viral suppression. However, the model could be expanded by adding new structures to represent interventions that would address one or more of these factors. For example, peer support interventions, which were common and well developed across many of the WOC SPNS demonstration sites, are worthy of greater study and development, particularly if they are designed to foster greater access to ART and skill-building to help patients better learn why and well as how to adhere HIV medication protocols.

Our calibrated model and its simulated output provided a different perspective on retention and suppression than more traditional statistical modeling approaches. For example, it permits the study of time delays involved in any change (e.g., for one additional WOC to access or become adherent to HIV care). Notably, we saw that the *May or May Not Seek Care* subgroup, who are ostensibly the most challenged to achieve viral suppression, could realize this goal in substantially less time than WOC who presented as better integrated with an HIV care management system. One implication is that patients have different demand characteristics, which may invoke greater support.

Last, this model has been developed using a data and information taken exclusively from the MSE of the WOC SPNS initiative. While providing a novel way to enhance the initiative’s evaluation, SD modeling tools such as ours could be applied to larger policy questions and calibrated to examine larger systems of care, using national data sets.

Good simulation models mimic important elements of the system under study in practicable, actionable ways. The MSE cohort study data provided a platform for exploring the dynamics of retention and HIV treatment for WOC. Real world problems are complex, and so is modeling them with

validity. Simulation methods such as SD have great potential to compliment more traditional evaluation methodologies. Overall, our modeling provides an enhanced understanding about the challenge of delivering high quality HIV care management to diverse patients. The ultimate objective behind applying SD and other systems science methods is to help practitioners, policy makers, researchers—as well as patients and clients—see and address problems that inhibit more effective care management.

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### Author Disclosure Statement

No competing financial interests exist.

### References

1. Luke DA, Stamatakis KA. Systems science methods in public health: Dynamics, networks, and agents. *Ann Rev Public Health* 2012;33:357–376.
2. Mugavero MJ, Norton WE, Saag MS. Health care system and policy factors influencing engagement in HIV medical care: Piecing together the fragments of a fractured health care delivery system. *Clin Infect Dis* 2011;52:S238–S246.
3. Mabry P, Olster D, Morgan G, Abrams D. Interdisciplinary and systems science to improve population health: A view from the NIH Office of Behavioral and Social Sciences Research. *Am J Prev Med* 2008;35:S211–S224.
4. Milstein B. *Hygeia's Constellation: Navigating Health Futures in a Dynamic and Democratic World*: Center for Disease Control, Syndemic Prevention Network, 2008.
5. Milstein B, Homer J. Background on system dynamics simulation modeling with a summary of major public health studies. 2006; [http://www.systemswiki.org/images/f/f5/SD\\_background\\_for\\_public\\_health\(4.11.05\).pdf](http://www.systemswiki.org/images/f/f5/SD_background_for_public_health(4.11.05).pdf) (Last accessed April 11, 2005).
6. Lounsbury DW, Hirsch GB, Vega C, Schwartz CE. Understanding social forces involved in diabetes outcomes: a systems science approach to quality-of-life research. *Qual Life Res* 2014;3:959–969.
7. Trochim WM, Cabera DA, Milstein B, Gallagher RS, Leischow SJ. Practical challenges of systems thinking and modeling in public health. *Am J Public Health* 2006;96:538–546.
8. Forrester JW. System dynamics, systems thinking, and soft OR. *System Dynamics Rev* 1994;10:245–256.
9. Huz S, Andersen DF, Richardson GP, Boothroyd R. A framework for evaluating systems thinking interventions: An experimental approach to mental health system change. *System Dynamics Rev* 1997;13:149–169.
10. Maani KE, Cavana RY. *Systems Thinking and Modeling: Understanding Change and Complexity*. Auckland, New Zealand: Pearson Education New Zealand Limited, 2000.
11. Hirsch G, Immediato CS. Microworlds and generic structures as resources for integrating care and improving health. *System Dynamics Rev* 1999;15:315–330.
12. Forrester JW. The model versus a modeling process. *System Dynamics Rev* 1987;1:133–134.
13. Repenning NA. A simulation-based approach to understanding the dynamics of innovation implementation. *Org Sci* 2002;13:109–127.
14. Richardson GP. *Feedback Thought in Social Science and Systems Theory*. Waltham, MA: Pegasus Communications, Inc., 1991.
15. Richardson GP, Pugh III AL. *Introduction to System Dynamics Modeling*. Portland, Oregon: Productivity Press, 1981.
16. Sterman J. Learning in and about complex systems. *System Dynamics Rev* 1994;10:291–230.
17. Wolstenholme EF. System dynamics: A system methodology or a system modelling technique. *Dynamica* 1983;9: 84–90.
18. Forrester JW. *Industrial Dynamics*. Cambridge: MIT Press, 1961.
19. Forrester JW. *Principles of Systems*. 2nd ed. Cambridge: Wright-Allen Press, 1971.
20. Morecroft J, Sterman J. *Modeling for Learning Organizations*. Portland, OR: Productivity Press, 1994.
21. Roberts N, Anderson D, Deal R, Garet M, Shaffer W. *Introduction to Computer Simulation: A System Dynamics Modeling Approach*. Reading, Massachusetts: Addison-Wiley Publishing Company, 1983.
22. Forrester JW, Senge PM. Tests for building confidence in system dynamics models. *TIMS Studies Manag Sci* 1980; 14:201–228.
23. Arboleda CA, Abraham DM, Lubitz R. Simulation as a tool to assess the vulnerability of the operation of a health care facility. *J Perform Constructed Facilities* 2007;21:302–312.
24. Cavana RY, Davies PK, Robson RM, Wilson KJ. Drivers of quality in health services: Different worldviews of clinicians and policy managers revealed. *System Dynamics Rev* 1999;15:331–340.
25. Hirsch G, Miller S. Evaluating HMO policies with a computer simulation model. *Med Care* 1974;12:668–681.
26. Hovmand PS, Gillespie DF. Implementation of evidence-based practice and organizational performance. *J Behav Health Serv Res* 2010;37:79–94.
27. Royston G, Dost A, Townshend J, Turner H. Using system dynamics to help develop and implement policies and programmes in health care in England. *System Dynamics Rev* 1999;15:293–313.
28. Wolstenholme E, Monk D, McKelvie D, Arnold S. Coping but not coping in health and social care: Masking the reality of running organisations beyond safe design capacity. *System Dynamics Rev* 2007;23:371–389.
29. Braithwaite J, Westbrook JI, Ranmuthugala G, et al. The development, design, testing, refinement, simulation and application of an evaluation framework for communities of practice and social-professional networks. *BMC Health Serv Res* 2009;9:162.
30. Elf M, Poutilova M, Ohrn K. A dynamic conceptual model of care planning. *Scand J Caring Sci* 2007;21:530–538.
31. Taylor K, Dangerfield B. Modelling the feedback effects of reconfiguring health services. *J Operat Res Soc* 2005;56: 659–675.
32. Homer J, Hirsch G, Minniti M, Pierson M. Models for collaboration: How system dynamics helped a community



- organize cost-effective care for chronic illness. *System Dynamics Rev* 2004;20:199–222.
33. Dangerfield BC, Fang YX, Roberts CA. Model-based scenarios for the epidemiology of HIV/AIDS: The consequences of highly active antiretroviral therapy. *System Dynamics Rev* 2001;17:119–150.
  34. Flessa S. Decision support for AIDS control programmes in eastern Africa. *OR Spectrum* 2003;25:265–291.
  35. Lebcir RM, Atun RA, Coker RJ. System Dynamic simulation of treatment policies to address colliding epidemics of tuberculosis, drug resistant tuberculosis and injecting drug users driven HIV in Russia. *J Operat Res Soc* 2010;61:1238–1248.
  36. Roberts C, Dangerfield B. Modeling the epidemiologic consequences of HIV infection and AIDS: A contribution from operational research. *J Operat Res Soc* 1990;41:273–289.
  37. Roberts EB, Homer J, Kasabian A, Varrell M. A systems view of the smoking problem: Perspective and limitations of the role of science in decision-making. *Intl J Bio-Med Comput* 1982;13:69–86.
  38. Chick SE, Mamani H, Simchi-Levi D. Supply chain coordination and influenza vaccination. *Operat Res* 2008;56:1493–1506.
  39. Homer J, Ritchie-Dunham J, Rabbino H, Puente LM, Jorgensen J, Hendricks K. Toward a dynamic theory of antibiotic resistance. *System Dynamics Rev* 2000;16:287–319.
  40. Thompson KM, Tebbens RJD. Using system dynamics to develop policies that matter: Global management of poliomyelitis and beyond. *System Dynamics Rev* 2008;24:433–449.
  41. Ahmad S. The cost-effectiveness of raising the legal smoking age in California. *Med Decision Making* 2005;25:330–340.
  42. Ahmad S. Closing the youth access gap: The projected health benefits and cost savings of a national policy to raise the legal smoking age to 21 in the United States. *Health Policy* 2005;75:74–84.
  43. Cavana RY, Clifford LV. Demonstrating the utility of system dynamics for public policy analysis in New Zealand: The case of excise tax policy on tobacco. *System Dynamics Rev* 2006;22:321–348.
  44. Tengs TO, Osgood ND, Chen LL. The cost-effectiveness of intensive national school-based anti-tobacco education: Results from the Tobacco Policy Model. *Prevent Med* 2001;33:558–570.
  45. Lounsbury D, Levine R, Ostroff J. Using Dynamics Modeling to Promote Effective Tobacco Treatment Practices in Community-based Primary Care Settings. Paper presented at: 28th International Conference of the System Dynamics Society, 28 July 2010, 2010, Seoul, Korea.
  46. Homer JB. A system dynamics model of national cocaine prevalence. *System Dynamics Rev* 1993;9:49–78.
  47. Homer JB, StClair CL. A model of HIV transmission through needle sharing. *Interfaces* 1991;21:26–49.
  48. Smith PC, van Ackere A. A note on the integration of system dynamics and economic models. *J Econ Dynam Control* 2002;26:1–10.
  49. Wakeland W, Schmidt T, Gilson AM, Haddox JD, Webster LR. System dynamics modeling as a potentially useful tool in analyzing mitigation strategies to reduce overdose deaths associated with pharmaceutical opioid treatment of chronic pain. *Pain Med* 2011;12:S49–S58.
  50. Smits M. Impact of policy and process design on the performance of intake and treatment processes in mental health care: A system dynamics case study. *J Operat Res Soc* 2010;61:1437–1445.
  51. Homer J, Hirsch G, Milstein B. Chronic illness in a complex health economy: The perils and promises of downstream and upstream reforms. *System Dynamics Rev* 2007;23:313–343.
  52. Siegel CA, Siegel LS, Hyams JS, et al. Real-time tool to display the predicted disease course and treatment response for children with Crohn's disease. *Inflamm Bowel Dis* 2011;17:30–38.
  53. Dangerfield B, Roberts C. Optimisation as a statistical estimation tool: An example in estimating the AIDS treatment-free incubation period distribution. *System Dynamics Rev* 1999;15:273–291.
  54. Dangerfield BC, Fang Y, Roberts CA. Model-based scenarios for the epidemiology of HIV/AIDS: The consequences of highly active antiretroviral therapy. *System Dynamics Rev* 2001;17:119–150.
  55. Lounsbury DW. *Understanding the Dynamics of Prevention, Care, and Empowerment: A Systems Approach to HIV/AIDS Policy Innovation*. East Lansing, MI: Michigan State University, 2002.
  56. Milstein B, Homer J, Hirsch GB. Analyzing national health reform strategies with a dynamic simulation model. *Am J Public Health* 2010;100:811–819.
  57. Barlas Y. Multiple tests for validation of system dynamics type of simulation models. *Eur J Operat Res* 1989;42:59–87.
  58. Barlas Y. Formal aspects of model validity and validation in system dynamics. *System Dynamics Rev* 1996;12:183–210.
  59. Martinez-Moyano JJ. Documentation for model transparency. *System Dynamics Rev* 2012;28:199–208.
  60. Oliva R. Model calibration as a testing strategy for system dynamics models. *Eur J Operat Res* 2003;151:522–568.
  61. Forrester JW. Counterintuitive behavior of social systems. *Technol Rev* 1971;73:52–68.
  62. Doshi R, Matthews T, Insensberg D, et al. Continuum of HIV Care Among Ryan White HIV/AIDS Program Clients: US, 2010. Paper presented at: 20th Conference on Retroviruses and Opportunistic Infections 2013, Atlanta, GA.
  63. CDC. HIV In the United States: The Stages of Care. 2012; [http://www.cdc.gov/hiv/pdf/research\\_mmp\\_stagesofcare.pdf](http://www.cdc.gov/hiv/pdf/research_mmp_stagesofcare.pdf) (Last accessed August 1, 2014).
  64. Eastwood EA, Fletcher J, Quinlivan EB, Verdecias N, Birnbaum JM, Blank AE. Baseline social characteristics and barriers to care from SPNS women of color with HIV study: A comparison of urban and rural women and barriers to HIV Care. *AIDS Patient Care STDs* 2015;29(Suppl 1):S00–S00.
  65. Adeyemi OM, Livak B, McLoyd P, Smith KY, French AL. Racial/ethnic disparities in engagement in care and viral suppression in a large urban HIV clinic. *Clin Infect Dis* 2013;56:1512–1514.
  66. Axelrad JE, Mimiaga MJ, Grasso C, Mayer KH. Trends in the spectrum of engagement in HIV care and subsequent clinical outcomes among men who have sex with men (MSM) at a Boston Community Health Center. *AIDS Patient Care STDs* 2013;27:287–296.
  67. Geng EH, Nash D, Kambugu A, et al. Retention in care among HIV-infected patients in resource-limited settings: Emerging insights and new directions. *Curr HIV/AIDS Rep* 2010;7:234–244.



68. Helleberg M, Engsig FN, Kronborg G, Larsen CS, Pedersen G. Retention in a public healthcare system with free access to treatment: A Danish nationwide HIV cohort study. *AIDS (London)* 2012;26:741–748.
69. Mayer KH. Introduction: Linkage, engagement, and retention in HIV care: Essential for optimal individual- and community-level outcomes in the era of highly active antiretroviral therapy. *Clin Infect Dis* 2011;52:S205–S207.
70. Mugavero MJ, Westfall AO, Zinski A, Davila J, Drainoni M-L. Measuring retention in HIV care: The elusive gold standard. *J Acq Immune Defic Syndromes* (1999). 2012;61: 574–580.
71. Yehia BR, Fleishman JA, Metlay JP, Korthuis PT, Agwu AL. Comparing different measures of retention in outpatient HIV care. *AIDS (London)*. 2012;26:1131–1139.
72. HAB. HIV/AIDS Bureau Core Clinical Performance Measures for Adult/Adolescent Clients: Group 1. In: Services USDoHaH, ed. Washington, DC: U.S. Department of Health and Human Services, 2008.
73. Walker R, Wakeland W. *Calibration of Complex System Dynamics Models: A Practitioner's Report*. Portland, OR: Portland State University, January 24, 2011 2011.
74. Giordano TP, Gifford AL, White AC, Jr., et al. Retention in care: A challenge to survival with HIV infection. *Clin Infect Dis* 2007;44:1493–1499.
75. Mugavero MJ. Improving engagement in HIV care: What can we do? *Topics HIV Med* 2008;16:156–161.
76. Arnsten JH, Demas PA, Grant RW, et al. Impact of active drug use on antiretroviral therapy adherence and viral suppression in HIV-infected drug users. *J Gen Int Med* 2002;17:377–381.
77. Bangsberg DR, Hecht FM, Charlebois ED, et al. Adherence to protease inhibitors, HIV-1 viral load, and development of drug resistance in an indigent population. *AIDS* 2000; 14:357–366.
78. Waldrop-Valverde D, Valverde E. Homelessness and psychological distress as contributors to antiretroviral nonadherence in HIV-positive injecting drug users. *AIDS Patient Care STDs* 2005;19:326–334.
79. Gonzalez JS, Batchelder AW, Psaros C, Safren SA. Depression and HIV/AIDS treatment nonadherence: A review and meta-analysis. *J Acq Immune Defic Syndromes* (1999). 2011;58:181–187.
80. Brennan AT, Maskew M, Sanne I, Fox MP. The importance of clinic attendance in the first six months on antiretroviral treatment: A retrospective analysis at a large public sector HIV clinic in South Africa. *J Intl AIDS Soc* 2010;13:49.

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