

# Urban Physics

7S0X0, 2021-2022 Quartile 3

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EINDHOVEN  
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TECHNOLOGY

# Urban Acoustics

Week 1

Acoustics quantities  
Acoustic pressure and velocity  
Sound pressure level  
A-weighting  
Octave bands

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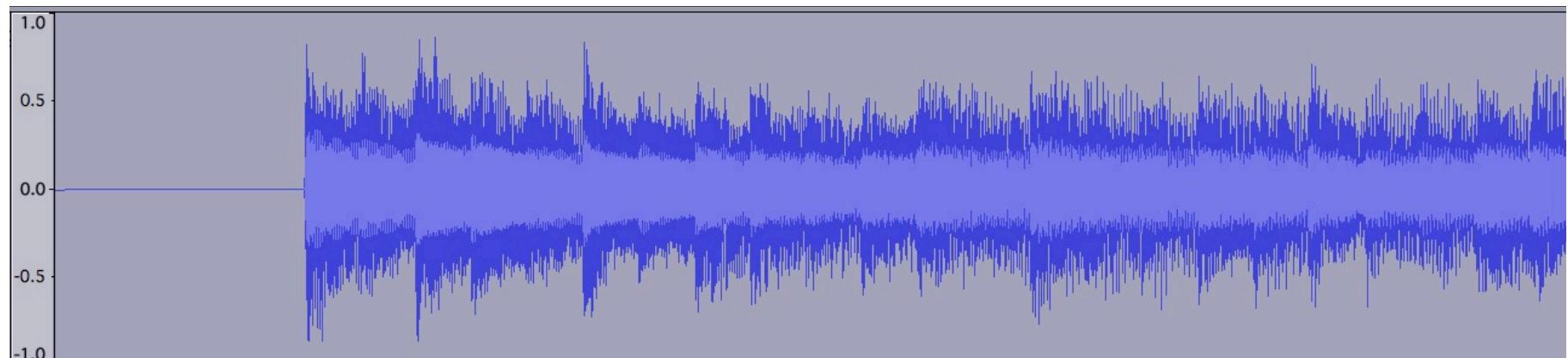
# Contents

- Acoustic pressure and velocity
- $L_p$  : sound pressure level dB
- $L_w$  : sound power level dB
- $L_I$  : sound intensity level dB
- Frequency, speed of sound
- Octave band analysis
- $L_A$  : A-weighted sound level dB(A)

# Sound propagation in air

$$p_{tot}(t) = p_0(t) + p(t)$$

$$\rho_{tot}(t) = \rho_0(t) + \rho(t)$$



# Sound propagation in air

$$\vec{u}_{tot}(t) = \vec{u}_0(t) + \vec{u}(t)$$

$$p(t) \sim \vec{u}(t)$$

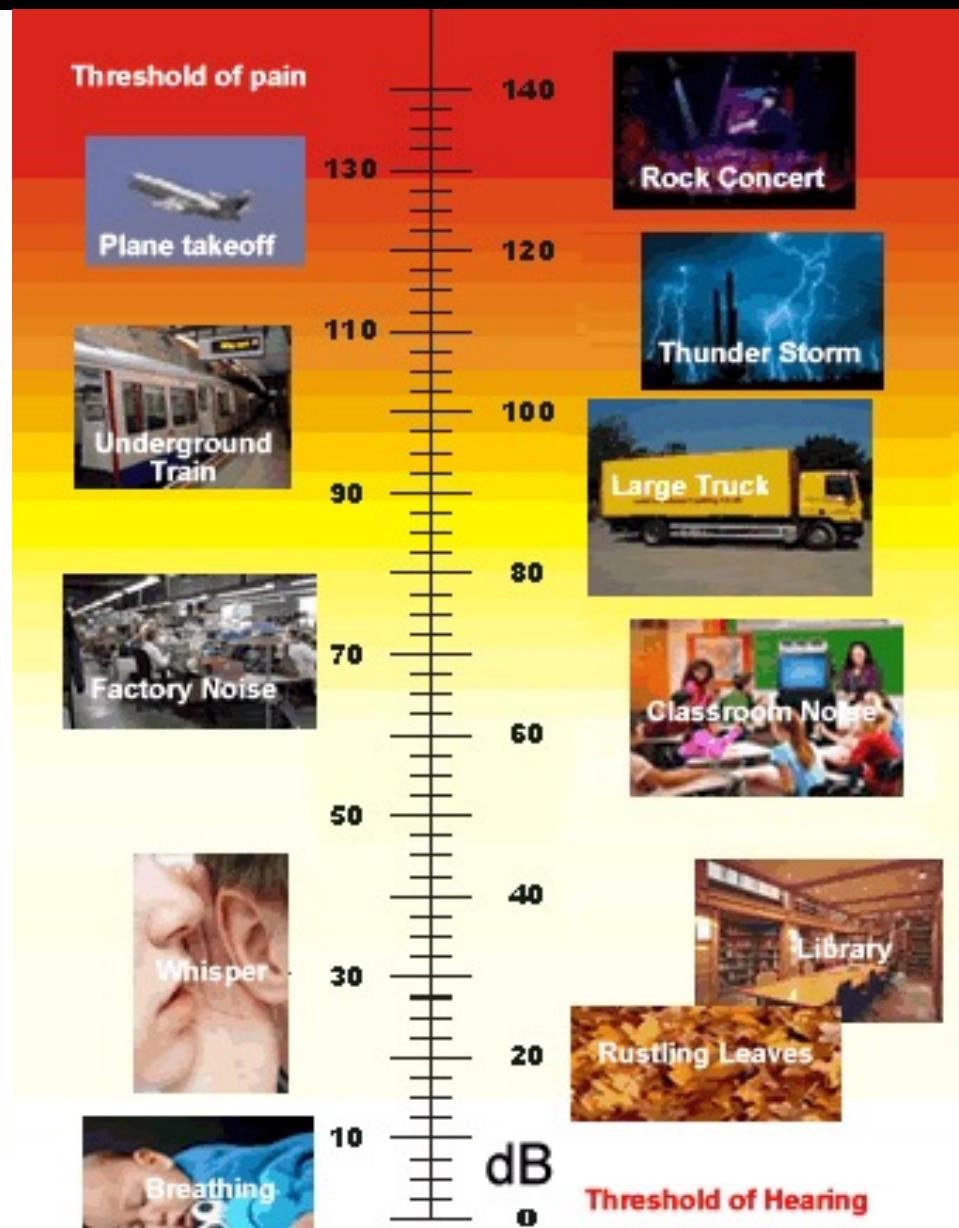
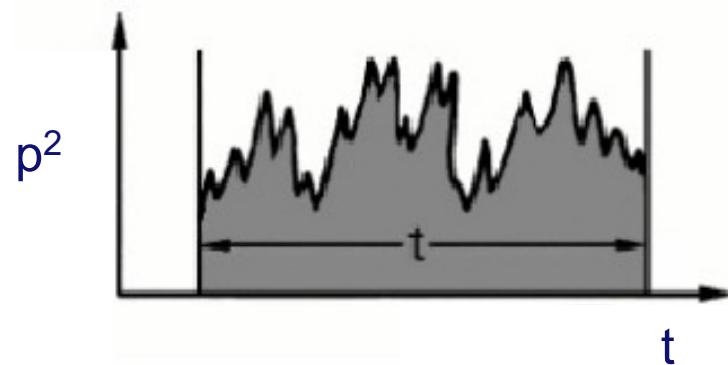


<http://img.ehowcdn.com/article-new-intro-modal/ehow/images/a06/ep/vp/fix-vibrating-audio-speakers-800x800.jpg>

# Sound pressure level $L_p(t)$

$$L_p(t) = 10 \log_{10} \left( \frac{p^2(t)}{p_{ref}^2} \right) \text{ [dB]}$$

$$p_{ref} = 2 \cdot 10^{-5} \text{ [Pa]}$$

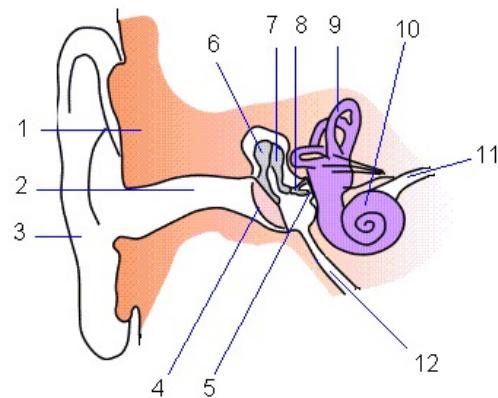


<http://www.cyberphysics.co.uk/topics/waves/sound/decibel.html>

# Sound pressure level $L_p(t)$

$$L_p(t) = 10 \log_{10} \left( \frac{\frac{1}{T_{\text{int}}} \int_0^{T_{\text{int}}} p^2(t) dt}{p_{\text{ref}}^2} \right) \text{ [dB]}$$

$T_{\text{int}}$  = time of integration [s]



<http://upload.wikimedia.org/wikipedia/commons/6/65/Ear-anatomy.png>



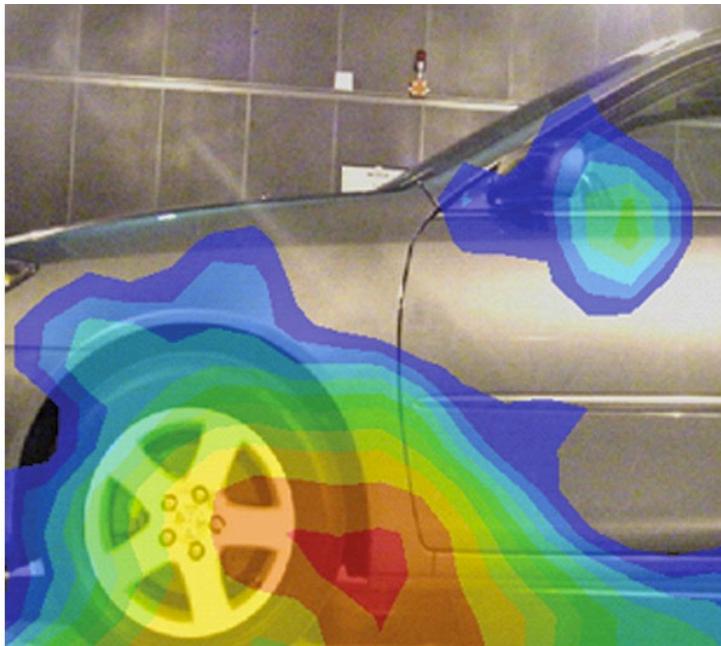
[www.bksv.com](http://www.bksv.com)

# Sound intensity

- *Sound intensity*: describes the rate of flow of acoustic energy per unit area in a certain direction [W/m<sup>2</sup>]
- Sound intensity level:

$$L_I(t) = 10 \log_{10} \left( \frac{I}{I_0} \right) \text{ [dB]}$$

$$I_0 = 1 \cdot 10^{-12} \text{ [W]}$$



<http://www.bksv.jp>

# Sound power

- *Sound power:* the acoustic energy emitted by a sound source over time and is a property of the sound source alone. It is measured in terms of Watts [W]
- Sound power level:

$$L_W(t) = 10 \log_{10} \left( \frac{W}{W_0} \right) \text{ [dB]}$$

$$W_0 = 1 \cdot 10^{-12} \text{ [W]}$$



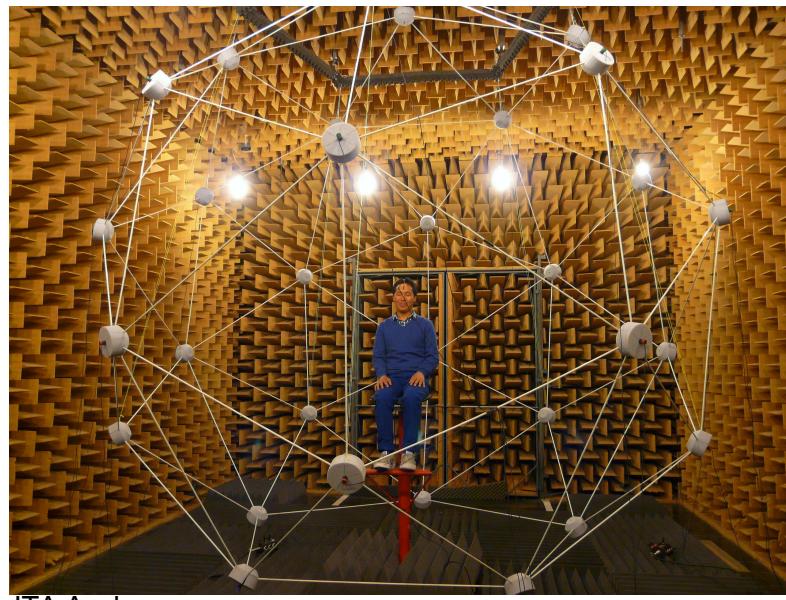
<http://www.southampton.ac.uk>

# Sound power

- *Sound power:* the acoustic energy emitted by a sound source over time and is a property of the sound source alone. It is measured in terms of Watts [W]
- Sound power level:

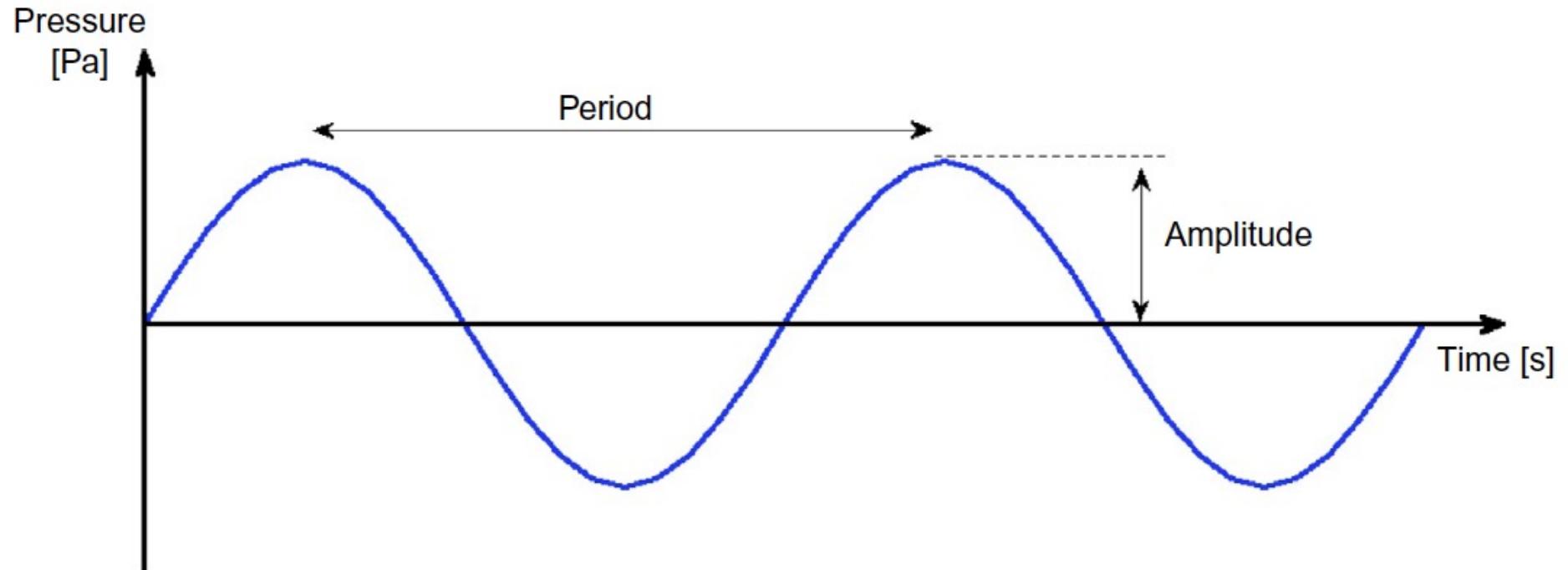
$$L_W(t) = 10 \log_{10} \left( \frac{W}{W_0} \right) \text{ [dB]}$$

$$W_0 = 1 \cdot 10^{-12} \text{ [W]}$$



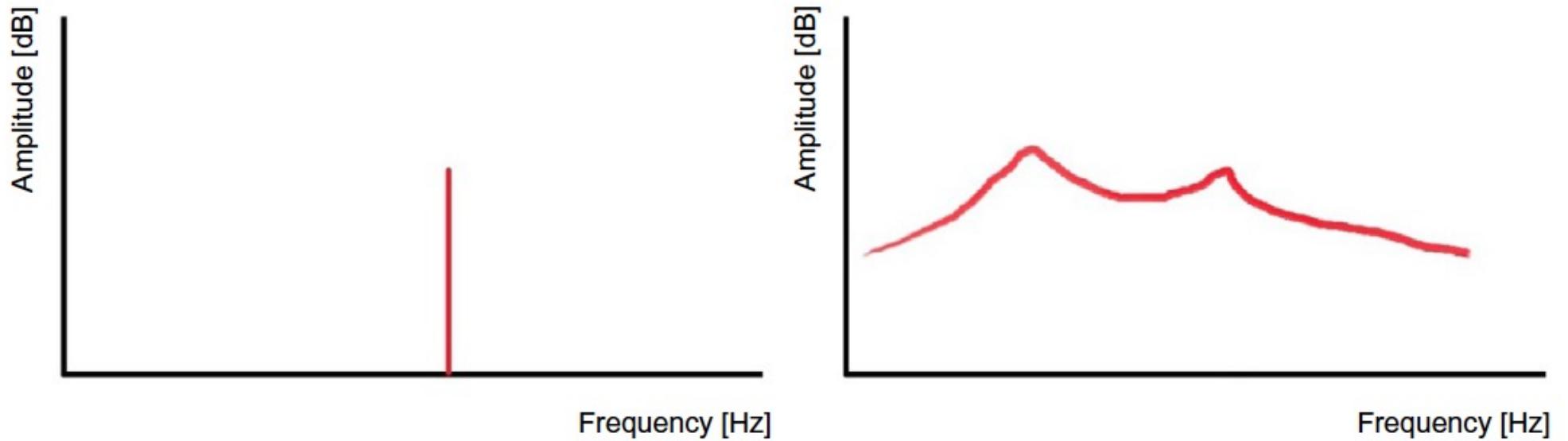
# Frequency

- Frequency = 1/period [Hz] ( $f = 1/T$ )
- $c = f\lambda$



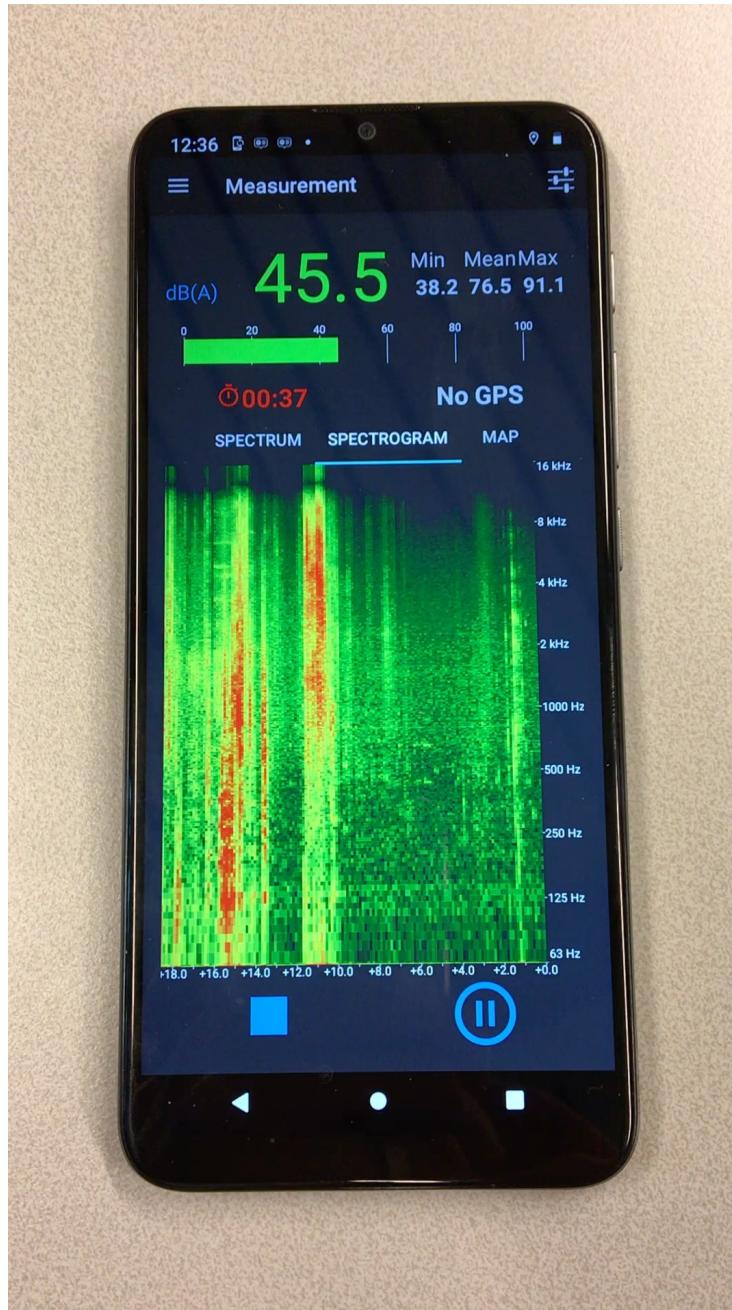
Murphy, E., & King, E. (2014). *Environmental noise pollution: Noise mapping, public health, and policy*. Newnes.

# Broadband versus tonal sounds



Murphy, E., & King, E. (2014). *Environmental noise pollution: Noise mapping, public health, and policy*. Newnes.

# Broadband versus tonal sounds

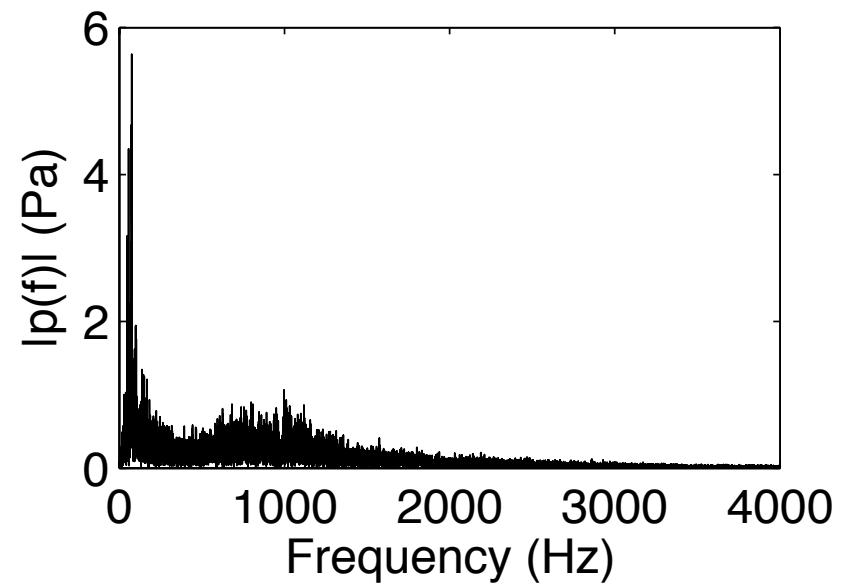
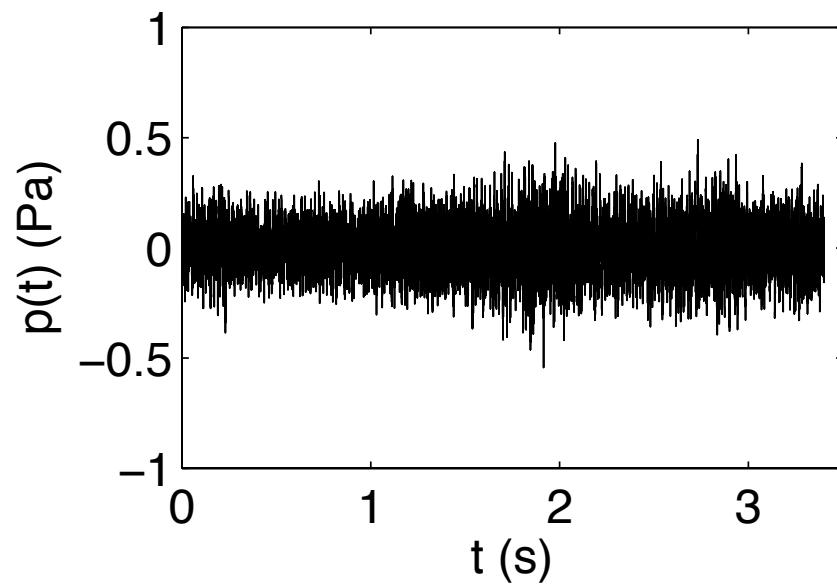


# From $p(t)$ to $p(f)$ : the Fourier transform

$$p(f) = \int_{-\infty}^{\infty} p(t) e^{j\omega t} dt$$

$$\omega = 2\pi f \quad (1/s)$$

$f$  = frequency [Hz]



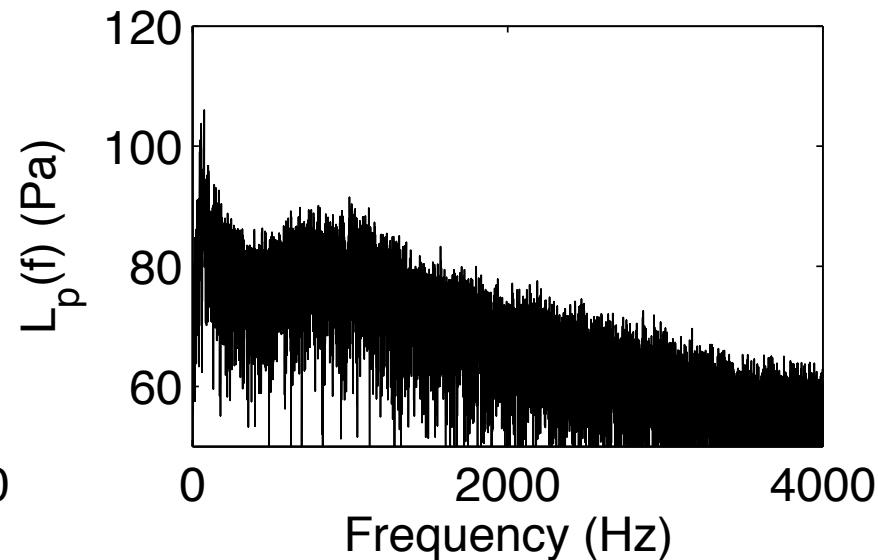
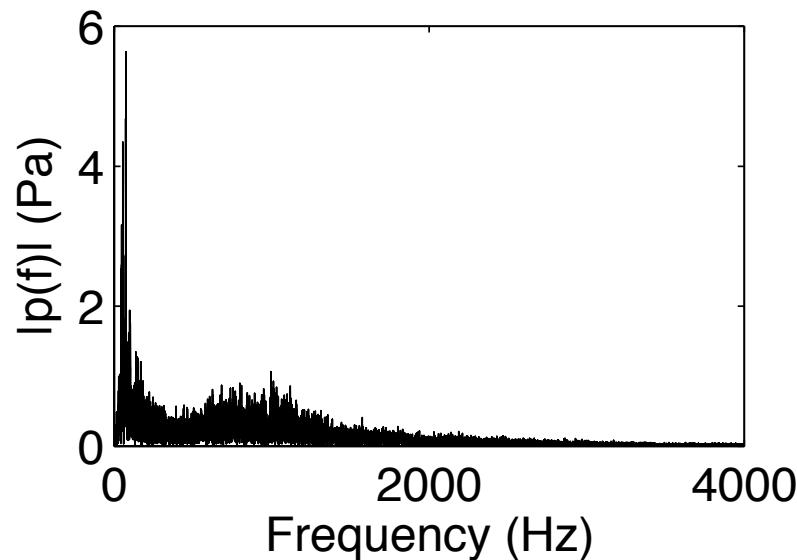
# Sound pressure level $L_p(f)$

$$p(f) = A(f) \sin(\omega t + \varphi)$$

$$\frac{1}{T} \int_0^T p(f)^2 dt = \frac{A(f)^2}{2} = \frac{|p(f)|^2}{2} = p_{eff}^2(f)$$

$$L_p(f) = 10 \log_{10} \left( \frac{\frac{1}{T} \int_0^T p^2(f) dt}{p_{ref}^2} \right) \text{ [dB]}$$

$$L_p(f) = 10 \log_{10} \left( \frac{p_{eff}^2(f)}{p_{ref}^2} \right)$$



# 1/3 octave band sound pressure level $L_p(f)$

Lower Band Limit [Hz]	Centre Frequency [Hz]	Upper Band Limit [Hz]
44	63	88
88	125	177
177	250	355
355	500	710
710	1000	1420
1420	2000	2840
2840	4000	5680
5680	8000	11,360

Murphy, E., & King, E. (2014). *Environmental noise pollution: Noise mapping, public health, and policy*. Newnes.

# 1/3 octave band sound pressure level $L_p(f)$

$$L_{p,1/3\text{octave},j} = 10 \log_{10} \left( \frac{\sum_{i=1}^{N_j} p_{eff}^2(f_{j,i})}{p_{ref}^2} \right) \text{ [dB]}$$
$$= 10 \log_{10} \left( \sum_{i=1}^{N_j} 10^{\frac{L_p(f_{j,i})}{10}} \right) \text{ [dB]}$$

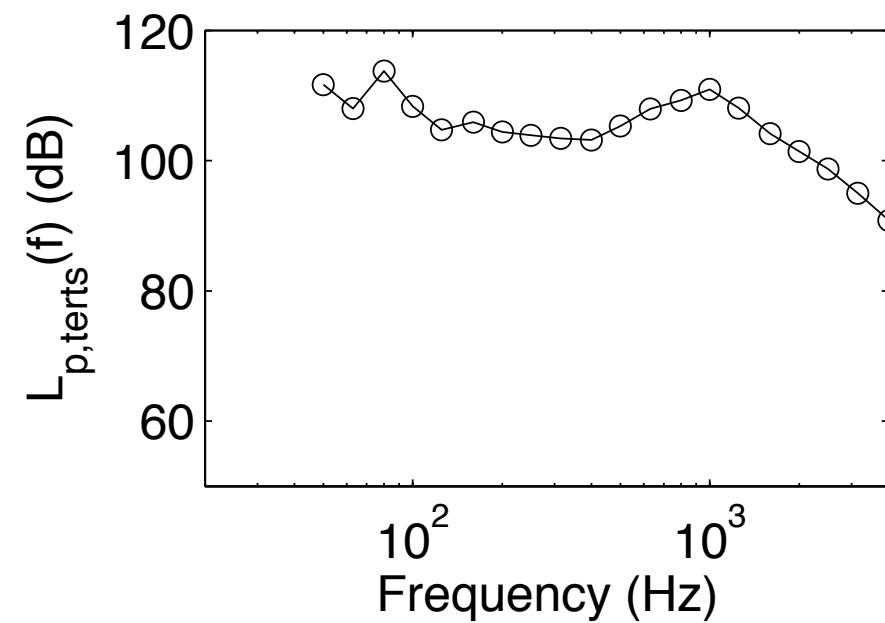
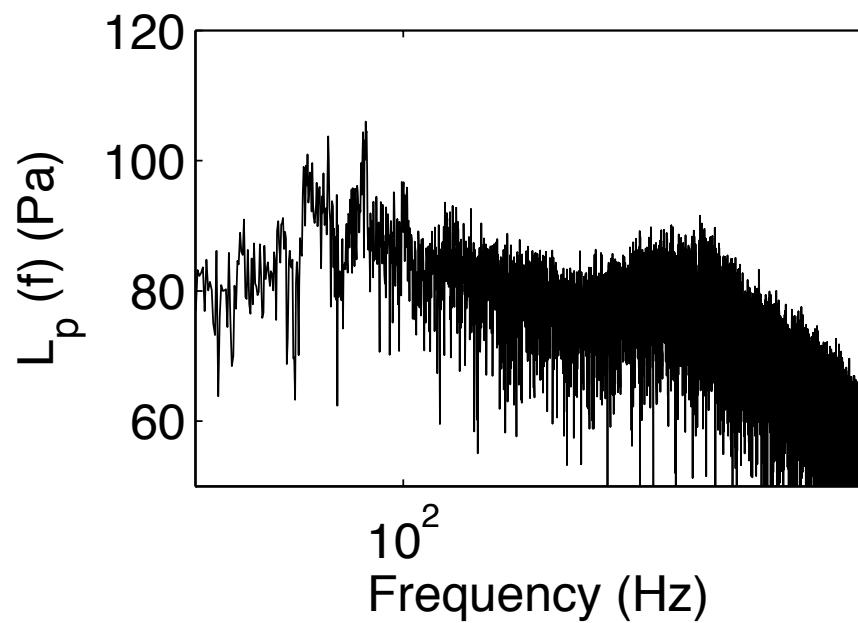
$j$  = 1/3 octave band index [-]

$i$  = frequency number within 1/3 octave band [-]

$N_j$  = number of frequencies in 1/3 octave band j [-]

# 1/3 octave band sound pressure level $L_p(f)$

$$L_{p,1/3octave,j} = 10 \log_{10} \left( \frac{\sum_{i=1}^{i=N_j} p_{eff}^2(f_{j,i})}{p_{ref}^2} \right) [\text{dB}]$$

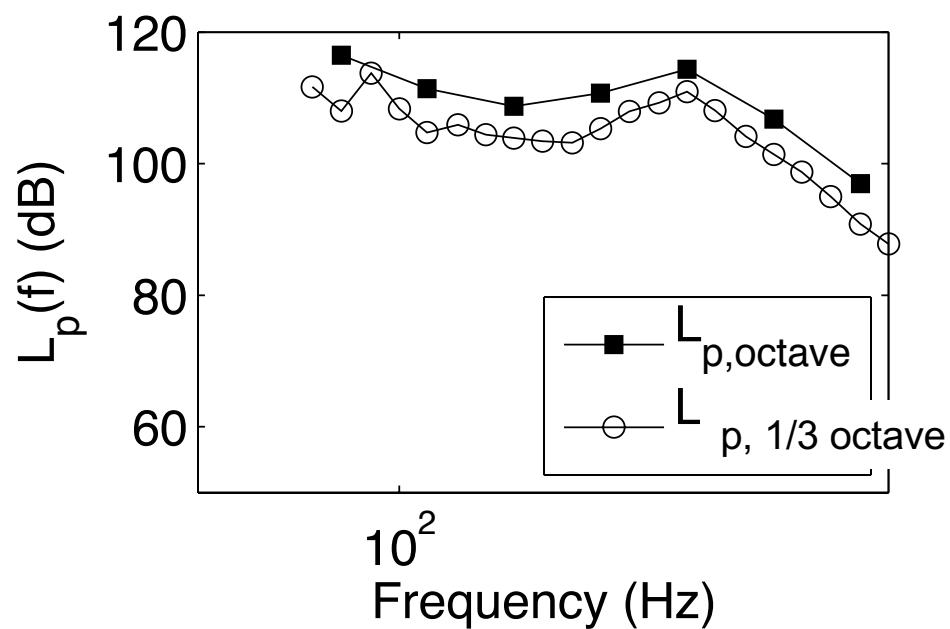


# 1/1 octave band sound pressure level $L_p(f)$

$$L_{p,m} = 10 \log_{10} \left( \sum_{i=1}^{i=3} 10^{\frac{L_{p,1/3\text{octave},3m-1+i}}{10}} \right) \text{ [dB]}$$

$m$  = 1/1 octave band index [-]

$3m - 1 + i$  = 1/3 octave band number [-]

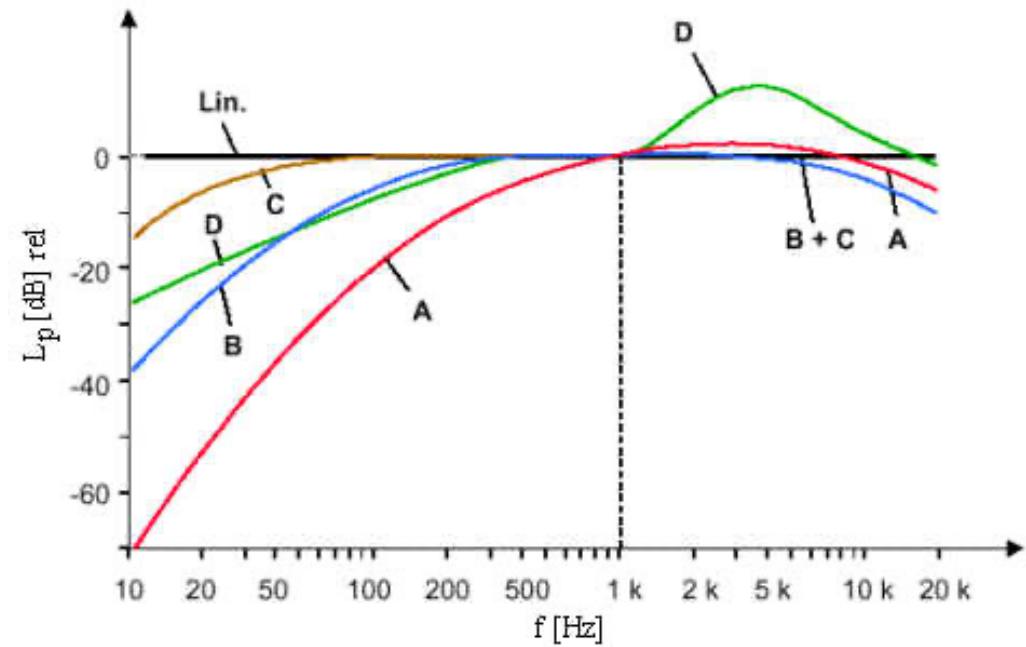
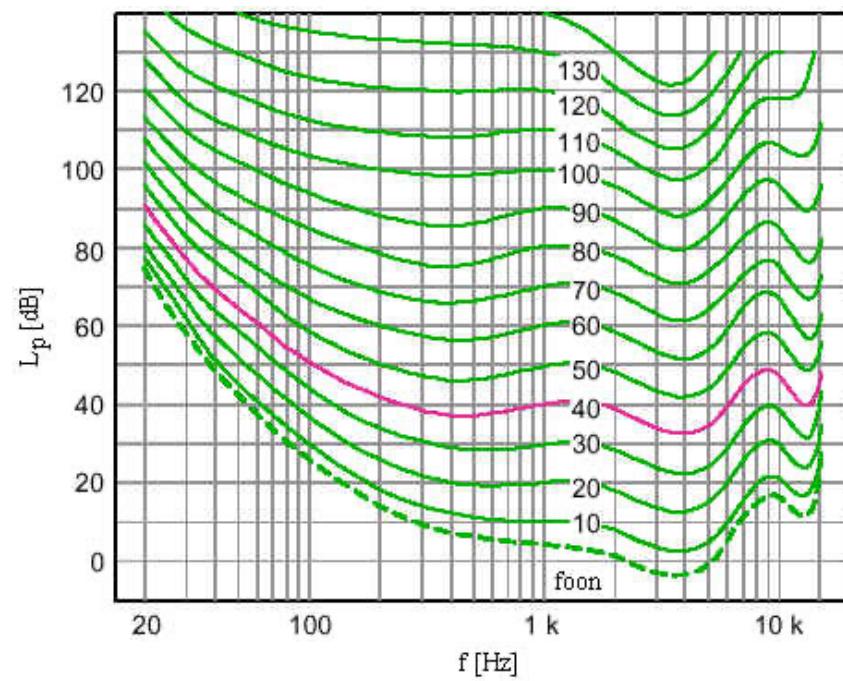


# 1/1 octave and 1/3 octave band frequencies

<b>Octave band center frequency <math>f_m</math> (Hz)</b>	<b>1/3-octave band center freq. <math>f_m</math> (Hz)</b>
125	100 125 160
250	200 250 315
500	400 500 630
1000	800 1000 1250

# A-weighting

- Weighted to human sensitivity: A-corrections



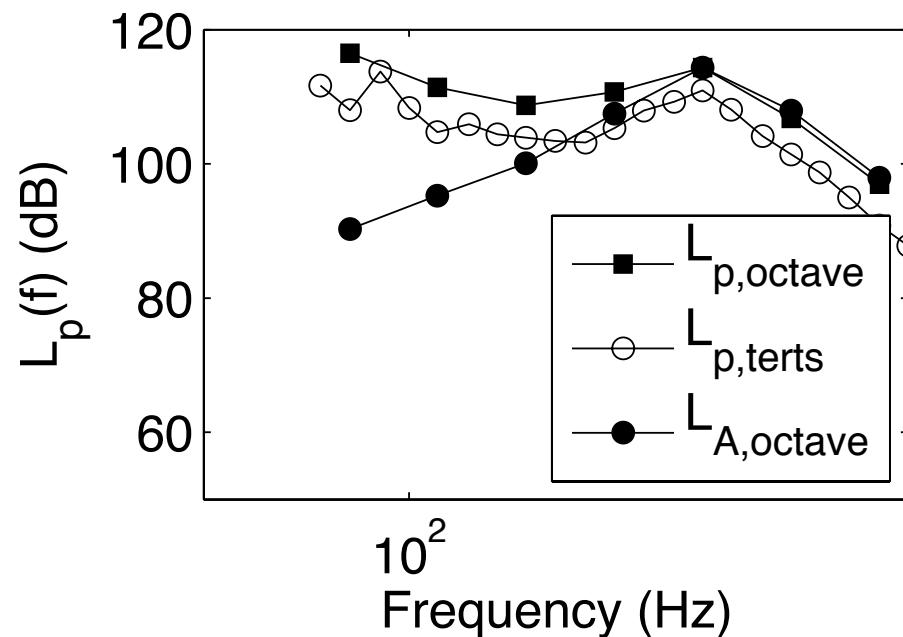
# $L_A$ : A-weighted sound level dB(A)

$$L_A = 10 \log_{10} \left( \sum_{m=1}^{M} 10^{\frac{L_{p,m} + W_m}{10}} \right) \text{ [dB]}$$

$m$  = 1/1 octave band index [-]

$M$  = number of 1/1 octave bands [-]

$W_m$  = A - weighting [-]



# References

- Murphy, E. and King, E., 2014. *Environmental noise pollution: Noise mapping, public health, and policy*. Newnes.