Physics

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CHAPTER 1

Classical mechanics

In Hamiltonian mechanics, the phase space M is defined to be cotangent bundle of a configuration manifold. According to Newton's principle of determinacy, a particle at a specific time corresponds to a point in M, and the point contains all informations of a particle. A function on M is a physical quantity, such as position, momentum, angular momentum, etc. Especially, positions and momenta with respect to each dimension provide with canonical coordinate functions on M. Therefore, every function on M can be realized by a function of positions and momenta.

A Hamiltonian function H is also just a function on M. In physics, if a Hamiltonian function is given, the equation of motion is generated. In other words, Hamiltonian function defines a physical problem.

DEFINITION 0.1 (Hamilton's equations of motion). For a Hamiltonian function H, Hamilton's equations of motion are given by

$$\dot{x} = \frac{\partial H}{\partial p}, \qquad \dot{p} = -\frac{\partial H}{\partial x}.$$

Using the Poisson bracket, the equations can be represented by

$$\frac{df}{dt} = \{f, H\} + \frac{\partial f}{\partial t}.$$

PROBLEM 0.1 (Harmonic oscillator). Let $M = T^*\mathbb{R}$ and

$$H(x,p) = \frac{p^2}{2m} + \frac{1}{2}kx^2.$$

This Hamiltonian function defines a problem of 1-dimensional harmonic oscillator. The equations of motion are

$$\dot{x} = \frac{\partial H}{\partial p} = \frac{p}{m}, \qquad \dot{p} = -\frac{\partial H}{\partial x} = -kx.$$

Therefore, we get the familiar equation for a harmonic oscillator

SOLUTION.

- (1) Here is the proof.
- (2) Here is a proof.

If H has a symmetry under transformations in time, namely, H does not depend on t explicitly, then

A problem that H is explicitly independent on p is difficult to occur physically.

$CHAPTER \ 2$

Classical field theory

CHAPTER 3

Relativity theory

CHAPTER 4

Quantum mechanics

Problem 0.1 (Hydrogen atom). Hydrogen hydrogen

1. Particle physics

PROBLEM 1.1 (Yukawa potential). The wave equation for a massive field is given by the Klein-Gordon equation

$$(\Box + m^2)u(t, x) = 0,$$

where m is mass.

(1) Derive the Yukawa potential

$$u(x) = k \frac{e^{-\frac{r}{m}}}{r}$$

where r = |x|, as a Green function by assuming static case.

- (2) Letting m = 0, discuss the relation with Coulomb potential.
- (3) By taking Fourier transform.
- (4) Find an approximate range of strong nuclear force and mass of pion.

PROBLEM 1.2 (Negative energy solution and antiparticles). Dirac's interpretation. negative energy solution of the Klein-Gordon equation time reversal?

PROBLEM 1.3 (Polarization of photon field).

PROBLEM 1.4 (Aharonov-Bohm effect).