Problem Set : Differential Equations

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PROBLEM 1.1. Let Ω be a bounded Lipschitz domain. Consider an eigenvalue problem

$$\begin{cases} -\Delta u = \lambda u, & x \in \Omega, \\ u = 0, & x \in \partial\Omega. \end{cases}$$