

# CHOOSING AN INFERENCE PROCEDURE

## I. Inference On Means

### A. One Sample

#### 1. $\sigma^2$ known

Use one-sample  $z$  procedures (Chapter 6)

$$\text{confidence interval: } \bar{x} \pm z^* \frac{\sigma_x}{\sqrt{n}}$$

$$\text{test statistic: } z = \frac{\bar{x} - \mu_0}{\sigma_x / \sqrt{n}}$$

#### 2. $\sigma^2$ unknown

Use one-sample  $t$  procedures (Section 7.1)

$$\text{confidence interval: } \bar{x} \pm t^* \frac{s}{\sqrt{n}}$$

$$\text{test statistic: } t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$$

### B. Two Samples

#### 1. Dependent

Use matched pairs  $t$  procedures (Section 7.1)

$$\text{confidence interval: } \bar{x}_d \pm t^* \frac{s_d}{\sqrt{n}}$$

$$\text{test statistic: } t = \frac{\bar{x}_d - \mu_{d0}}{s_d / \sqrt{n}}$$

#### 2. Independent

Use two-sample  $t$  procedures (Section 7.2)

$$\text{confidence interval: } (\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$\text{test statistic: } t = \frac{(\bar{x}_1 - \bar{x}_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_1}}}$$

## II. Inference on Proportions

### A. One Sample

Use the one-sample z procedures (Section 8.1)

$$\text{confidence interval: } \tilde{p} \pm z^* \sqrt{\frac{\tilde{p}(1 - \tilde{p})}{n + 4}}$$

$$\text{test statistic: } z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1 - p_0)}{n}}}$$

### B. Two Independent Samples

Use the two-sample z procedures (Section 8.2)

$$\text{confidence interval: } (\tilde{p}_1 - \tilde{p}_2) \pm z^* \sqrt{\frac{\tilde{p}_1(1 - \tilde{p}_1)}{n_1 + 2} + \frac{\tilde{p}_2(1 - \tilde{p}_2)}{n_2 + 2}}$$

$$\text{test statistic: } z = \frac{(\hat{p}_1 - \hat{p}_2)}{\sqrt{\hat{p}(1 - \hat{p}) \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

### C. k Samples

Use the  $\chi^2$  procedures (Chapter 9)

$$\text{test statistic: } X^2 = \sum \frac{(\text{obs} - \text{exp})^2}{\text{exp}}$$