

# Undergraduate Research at Georgia Tech

Matt Baker

Associate Professor  
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# About me

- Ph.D. in Mathematics in 1999 from U.C. Berkeley
- Benjamin Peirce Assistant Professor, Harvard University 1999-2002
- Currently Associate Professor at GT
- Research interests: number theory, algebraic geometry, combinatorics, algebraic dynamics
- Coach of the Putnam team
- Undergraduate research coordinator for the SoM since 2005
- Member of the International Brotherhood of Magicians

# Overview of REU program

- 10-15 REU students per summer for the last six summers
- NSF currently funds 10 REU students per summer at \$5K each (MCTP grant)
- Intensive one-on-one mentoring
- Competitive application process
- Most participants are GT students

# Awards and publications

- Three SoM REU students have won the prestigious Georgia Tech Sigma Xi Undergraduate Research Award in the last six years
- Many of our undergraduate students have published research papers in professional math journals

# Selected REU publications

- Brian Benson: “G-parking functions and acyclic orientations of graphs”, with P. Tetali, to appear in [Discrete Mathematics](#))
- Reginald McGee (Florida Atlantic University): “Optimizing a fin ray for stiffness”, with S. Alben, [Journal of the Mechanics and Physics of Solids](#) 58, 656-664 (2010).
- Ander Steele: “Carmichael Numbers in Abelian Extensions of  $\mathbf{Q}$ ”, [Journal of Number Theory](#) 128, no. 4 (2008), 910-917. **Sigma Xi Award.**
- Ioana Soran, “Weights whose Biorthogonal Polynomials admit a Rodrigues Formula”, with D. Lubinsky, [Journal of Mathematical Analysis and Applications](#), 324 (2006), 805-819.) **Sigma Xi Award.**

# Profile: Ander Steele



- REU in 2005-2006, currently a Math Ph.D. student at Boston University
- Research on Carmichael numbers and primality testing, with applications to cryptography

# Carmichael numbers

- If  $p$  is a prime number then for any integer  $a$ ,  $p$  divides  $a^p - a$  (Fermat).
- So if  $N$  does *not* divide  $a^N - a$  for some integer  $a$ , then  $N$  is *not* prime.
- Question: if  $N$  divides  $a^N - a$  for all integers  $a$ , must  $N$  be prime?
- Answer: **No.** (Carmichael numbers “masquerade” as primes.)

# Carmichael numbers (cont.)

- Ander's idea: use "*Gaussian integers*"  
 $a = x + iy$  instead of regular integers.
- Many Carmichael numbers reveal themselves to be composite using this "extended Fermat primality test". **But there are still impostors...**
- Follow-up idea: Use other "cyclotomic integers".
- **Conjecture:** Every composite number will reveal itself as composite for some suitably chosen cyclotomic integer  $a$ .



# Profile: Daniel Connelly



- 2008 REU, currently working for MIT's Lincoln Labs.
- Generated computer images of some new fractals...



