

Numeric.LinearAlgebra.Data

This module provides functions for creation and manipulation of vectors and matrices, IO, and other utilities.

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License	BSD3
Maintainer	Alberto Ruiz
Stability	provisional
Safe Haskell	None
Language	Haskell98

Elements

```
type R = Double | # Source
```

```
type C = Complex Double | # Source
```

```
type I = CInt | # Source
```

```
type Z = Int64 | # Source
```

```
type (./.) x n = Mod n x | infixr 5 | # Source
```

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Vector

1D arrays are storable vectors directly reexported from the vector package.

```
fromList :: Storable a => [a] -> Vector a | #
```

$O(n)$ Convert a list to a vector

```
toList :: Storable a => Vector a -> [a] | # Source
```

```
(|>) :: Storable a => Int -> [a] -> Vector a | infixl 9 | # Source
```

Create a vector from a list of elements and explicit dimension. The input list is truncated if it is too long, so it may safely be used, for instance, with infinite lists.

```
>>> 5 |> [1..]
[1.0,2.0,3.0,4.0,5.0]
it :: (Enum a, Num a, Foreign.Storable.Storable a) => Vector a
```

```
vector :: [R] -> Vector R | # Source
```

Create a real vector.

```
>>> vector [1..5]
[1.0,2.0,3.0,4.0,5.0]
it :: Vector R
```

```
range :: Int -> Vector I | # Source
```

```
>>> range 5
[0,1,2,3,4]
it :: Vector I
```

```
idxs :: [Int] -> Vector I
```

[# Source](#)

Create a vector of indexes, useful for matrix extraction using '(??)'

Matrix

The main data type of hmatrix is a 2D dense array defined on top of a storable vector. The internal representation is suitable for direct interface with standard numeric libraries.

Synopsis

```
(><) :: Storable a => Int -> Int -> [a] -> Matrix a
```

[# Source](#)

Create a matrix from a list of elements

```
>>> (2><3) [2, 4, 7+2*ic, -3, 11, 0]
(2><3)
[      2.0 :+ 0.0i,  4.0 :+ 0.0i,  7.0 :+ 2.0i
, (-3.0) :+ (-0.0i), 11.0 :+ 0.0i,  0.0 :+ 0.0i ]
```

The input list is explicitly truncated, so that it can safely be used with lists that are too long (like infinite lists).

```
>>> (2><3) [1..]
(2><3)
[ 1.0, 2.0, 3.0
, 4.0, 5.0, 6.0 ]
```

This is the format produced by the instances of Show (Matrix a), which can also be used for input.

```
matrix
```

[# Source](#)

```
  :: Int      number of columns
  -> [R]      elements in row order
  -> Matrix R
```

Create a real matrix.

```
>>> matrix 5 [1..15]
(3><5)
[ 1.0, 2.0, 3.0, 4.0, 5.0
, 6.0, 7.0, 8.0, 9.0, 10.0
, 11.0, 12.0, 13.0, 14.0, 15.0 ]
```

```
tr :: Transposable m mt => m -> mt
```

[# Source](#)

conjugate transpose

```
tr' :: Transposable m mt => m -> mt
```

[# Source](#)

transpose

Dimensions

```
size :: Container c t => c t -> IndexOf c
```

[# Source](#)

```
>>> size $ vector [1..10]
10
>>> size $ (2><5) [1..10::Double]
(2,5)
```

```
rows :: Matrix t -> Int
```

[# Source](#)

```
cols :: Matrix t -> Int
```

[# Source](#)

Conversion from/to lists

Synopsis <<

```
fromLists :: Element t => [[t]] -> Matrix t
```

[# Source](#)

Creates a `Matrix` from a list of lists (considered as rows).

```
>>> fromLists [[1,2],[3,4],[5,6]]
(3<2)
[ 1.0, 2.0
, 3.0, 4.0
, 5.0, 6.0 ]
```

```
toLists :: Element t => Matrix t -> [[t]]
```

[# Source](#)

the inverse of `fromLists`

```
row :: [Double] -> Matrix Double
```

[# Source](#)

create a single row real matrix from a list

```
>>> row [2,3,1,8]
(1<4)
[ 2.0, 3.0, 1.0, 8.0 ]
```

```
col :: [Double] -> Matrix Double
```

[# Source](#)

create a single column real matrix from a list

```
>>> col [7,-2,4]
(3<1)
[ 7.0
, -2.0
, 4.0 ]
```

Conversions vector/matrix

```
flatten :: Element t => Matrix t -> Vector t
```

[# Source](#)

Creates a vector by concatenation of rows. If the matrix is ColumnMajor, this operation requires a transpose.

```
>>> flatten (ident 3)
[1.0,0.0,0.0,0.0,1.0,0.0,0.0,0.0,1.0]
it :: (Num t, Element t) => Vector t
```

```
reshape :: Storable t => Int -> Vector t -> Matrix t
```

[# Source](#)

Creates a matrix from a vector by grouping the elements in rows with the desired number of columns. (GNU-Octave groups by columns. To do it you can define `reshapeF r = tr' . reshape r` where `r` is the desired number of rows.)

```
>>> reshape 4 (fromList [1..12])
(3<>4)
[ 1.0,  2.0,  3.0,  4.0
, 5.0,  6.0,  7.0,  8.0
, 9.0, 10.0, 11.0, 12.0 ]
```

```
asRow :: Storable a => Vector a -> Matrix a
```

[# Source](#)

creates a 1-row matrix from a vector

```
>>> asRow (fromList [1..5])
(1<>5)
[ 1.0, 2.0, 3.0, 4.0, 5.0 ]
```

```
asColumn :: Storable a => Vector a -> Matrix a
```

[# Source](#)

creates a 1-column matrix from a vector

```
>>> asColumn (fromList [1..5])
(5<>1)
[ 1.0
, 2.0
, 3.0
, 4.0
, 5.0 ]
```

```
fromRows :: Element t => [Vector t] -> Matrix t
```

[# Source](#)

Create a matrix from a list of vectors. All vectors must have the same dimension, or dimension 1, which is automatically expanded.

```
toRows :: Element t => Matrix t -> [Vector t]
```

[# Source](#)

extracts the rows of a matrix as a list of vectors

```
fromColumns :: Element t => [Vector t] -> Matrix t
```

[# Source](#)

Creates a matrix from a list of vectors, as columns

```
toColumns :: Element t => Matrix t -> [Vector t]
```

[# Source](#)

Creates a list of vectors from the columns of a matrix

Indexing

```
atIndex :: Container c e => c e -> IndexOf c -> e
```

[# Source](#)

generic indexing function

```
>>> vector [1,2,3] `atIndex` 1
2.0
```

```
>>> matrix 3 [0..8] `atIndex` (2,0)
6.0
```

```
class Indexable c t | c -> t, t -> c where
```

[# Source](#)

Alternative indexing function.

```
>>> vector [1..10] ! 3
4.0
```

On a matrix it gets the k-th row as a vector:

```
>>> matrix 5 [1..15] ! 1
[6.0,7.0,8.0,9.0,10.0]
it :: Vector Double
```

```
>>> matrix 5 [1..15] ! 1 ! 3
9.0
```

Methods

(!) :: c -> Int -> t	infixl 9	# Source
----------------------	----------	----------

Instances

⊕ Indexable (Vector Double) Double	# Source
⊕ Indexable (Vector Float) Float	# Source
⊕ Indexable (Vector Z) Z	# Source
⊕ Indexable (Vector I) I	# Source
⊕ Indexable (Vector (Complex Double)) (Complex Double)	# Source
⊕ Indexable (Vector (Complex Float)) (Complex Float)	# Source
⊕ Element t => Indexable (Matrix t) (Vector t)	# Source
⊕ (Storable t, Indexable (Vector t) t) => Indexable (Vector (Mod m t)) (Mod m t)	# Source

Construction

scalar :: Container c e => e -> c e	# Source
-------------------------------------	----------

create a structure with a single element

```
>>> let v = fromList [1..3::Double]
>>> v / scalar (norm2 v)
fromList [0.2672612419124244,0.5345224838248488,0.8017837257372732]
```

class Konst e d c d -> c, c -> d where	# Source
--	----------

Methods

konst :: e -> d -> c e	# Source
------------------------	----------

```
>>> konst 7 3 :: Vector Float
fromList [7.0,7.0,7.0]
```

```
>>> konst i (3::Int,4::Int)
(3<4)
[ 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0
, 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0
, 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0, 0.0 :+: 1.0 ]
```

▼ Instances

<code>⊢ Container Vector e => Konst e Int Vector</code>	# Source
--	----------

<code>⊢ (Num e, Container Vector e) => Konst e (Int, Int) Matrix</code>	# Source
--	----------

<code>class Build d f c e d -> c, c -> d, f -> e, f -> d, f -> c, c e -> f, d e -> f</code>	# Source
<code>where</code>	

Methods

<code>build :: d -> f -> c e</code>	# Source
---	----------

```
>>> build 5 (**2) :: Vector Double
[0.0,1.0,4.0,9.0,16.0]
it :: Vector Double
```

Hilbert matrix of order N:

```
>>> let hilb n = build (n,n) (\i j -> 1/(i+j+1)) :: Matrix Double
>>> putStr . dispf 2 $ hilb 3
3x3
1.00  0.50  0.33
0.50  0.33  0.25
0.33  0.25  0.20
```

▼ Instances

<code>⊢ Container Vector e => Build Int (e -> e) Vector e</code>	# Source
--	----------

<code>⊢ Container Matrix e => Build (Int, Int) (e -> e -> e) Matrix e</code>	# Source
---	----------

<code>assoc</code>	# Source
--------------------	----------

<code>:: Container c e</code>	
<code>=> IndexOf c</code>	size
<code>-> e</code>	default value
<code>-> [(IndexOf c, e)]</code>	association list
<code>-> c e</code>	result

Create a structure from an association list

```
>>> assoc 5 0 [(3,7),(1,4)] :: Vector Double
fromList [0.0,4.0,0.0,7.0,0.0]
```

```
>>> assoc (2,3) 0 [((0,2),7),((1,0),2*i-3)] :: Matrix (Complex Double)
(2<3)
[ 0.0 :+ 0.0, 0.0 :+ 0.0, 7.0 :+ 0.0
, (-3.0) :+ 2.0, 0.0 :+ 0.0, 0.0 :+ 0.0 ]
```

<code>accum</code>	# Source
--------------------	----------

<code>:: Container c e</code>	
<code>=> c e</code>	initial structure
<code>-> (e -> e -> e)</code>	update function
<code>-> [(IndexOf c, e)]</code>	association list
<code>-> c e</code>	result

Modify a structure using an update function

```
>>> accum (ident 5) (+) [((1,1),5),((0,3),3)] :: Matrix Double
(5<>5)
[ 1.0, 0.0, 0.0, 3.0, 0.0
 , 0.0, 6.0, 0.0, 0.0, 0.0
 , 0.0, 0.0, 1.0, 0.0, 0.0
 , 0.0, 0.0, 0.0, 1.0, 0.0
 , 0.0, 0.0, 0.0, 0.0, 1.0 ]
```

computation of histogram:

```
>>> accum (konst 0 7) (+) (map (flip (,) 1) [4,5,4,1,5,2,5]) :: Vector Double
fromList [0.0,1.0,1.0,0.0,2.0,3.0,0.0]
```

```
linspace :: (Fractional e, Container Vector e) => Int -> (e, e) -> Vector e | # Source
```

Creates a real vector containing a range of values:

```
>>> linspace 5 (-3,7::Double)
[-3.0,-0.5,2.0,4.5,7.0]
it :: Vector Double
```

```
>>> linspace 5 (8,3:+2) :: Vector (Complex Double)
[8.0 :+ 0.0i,6.75 :+ 0.5i,5.5 :+ 1.0i,4.25 :+ 1.5i,3.0 :+ 2.0i]
it :: Vector (Complex Double)
```

Logarithmic spacing can be defined as follows:

```
logspace n (a,b) = 10 ** linspace n (a,b)
```

Diagonal

```
ident :: (Num a, Element a) => Int -> Matrix a | # Source
```

creates the identity matrix of given dimension

```
diag :: (Num a, Element a) => Vector a -> Matrix a | # Source
```

Creates a square matrix with a given diagonal.

```
diag1 :: [Double] -> Matrix Double | # Source
```

create a real diagonal matrix from a list

```
>>> diag1 [1,2,3]
(3<>3)
[ 1.0, 0.0, 0.0
 , 0.0, 2.0, 0.0
 , 0.0, 0.0, 3.0 ]
```

```
diagRect :: Storable t => t -> Vector t -> Int -> Int -> Matrix t | # Source
```

creates a rectangular diagonal matrix:

```
>>> diagRect 7 (fromList [10,20,30]) 4 5 :: Matrix Double
(4<>5)
[ 10.0, 7.0, 7.0, 7.0, 7.0
 , 7.0, 20.0, 7.0, 7.0, 7.0
 , 7.0, 7.0, 30.0, 7.0, 7.0
 , 7.0, 7.0, 7.0, 7.0, 7.0 ]
```

```
takeDiag :: Element t => Matrix t -> Vector t
```

[# Source](#)

extracts the diagonal from a rectangular matrix

Vector extraction

```
subVector
```

[# Source](#)

```

:: Storable t
=> Int      index of the starting element
-> Int      number of elements to extract
-> Vector t source
-> Vector t result

```

takes a number of consecutive elements from a Vector

```

>>> subVector 2 3 (fromList [1..10])
[3.0,4.0,5.0]
it :: (Enum t, Num t, Foreign.Storable.Storable t) => Vector t

```

```
takesV :: Storable t => [Int] -> Vector t -> [Vector t]
```

[# Source](#)

Extract consecutive subvectors of the given sizes.

```

>>> takesV [3,4] (linspace 10 (1,10::Double))
[[1.0,2.0,3.0],[4.0,5.0,6.0,7.0]]
it :: [Vector Double]

```

```
vjoin :: Storable t => [Vector t] -> Vector t
```

[# Source](#)

concatenate a list of vectors

```

>>> vjoin [fromList [1..5::Double], konst 1 3]
[1.0,2.0,3.0,4.0,5.0,1.0,1.0,1.0]
it :: Vector Double

```

Matrix extraction

```
data Extractor
```

[# Source](#)

Specification of indexes for the operator `??`.

Constructors

```

All
Range Int Int Int
Pos (Vector I)
PosCyc (Vector I)
Take Int
TakeLast Int
Drop Int
DropLast Int

```


▼ Instances

[+ Show Extractor](#) | [# Source](#)

```
(??) :: Element t => Matrix t -> (Extractor, Extractor) -> Matrix t
```

infixl 9

| [# Source](#)

General matrix slicing.

```
>>> m
(4><5)
[  0,  1,  2,  3,  4
,  5,  6,  7,  8,  9
, 10, 11, 12, 13, 14
, 15, 16, 17, 18, 19 ]
```

```
>>> m ?? (Take 3, DropLast 2)
(3><3)
[  0,  1,  2
,  5,  6,  7
, 10, 11, 12 ]
```

```
>>> m ?? (Pos (idxs[2,1]), All)
(2><5)
[ 10, 11, 12, 13, 14
,  5,  6,  7,  8,  9 ]
```

```
>>> m ?? (PosCyc (idxs[-7,80]), Range 4 (-2) 0)
(2><3)
[ 9, 7, 5
, 4, 2, 0 ]
```

```
(?) :: Element t => Matrix t -> [Int] -> Matrix t
```

infixl 9

| [# Source](#)

extract rows

```
>>> (20><4) [1..] ? [2,1,1]
(3><4)
[ 9.0, 10.0, 11.0, 12.0
, 5.0,  6.0,  7.0,  8.0
, 5.0,  6.0,  7.0,  8.0 ]
```

```
(&) :: Element t => Matrix t -> [Int] -> Matrix t
```

infixl 9

| [# Source](#)

extract columns

(unicode 0x00bf, inverted question mark, Alt-Gr ?)

```
>>> (3><4) [1..] & [3,0]
(3><2)
[ 4.0, 1.0
, 8.0, 5.0
, 12.0, 9.0 ]
```

```
flipr1 :: Element t => Matrix t -> Matrix t
```

| [# Source](#)

Reverse columns

```
flipud :: Element t => Matrix t -> Matrix t
```

| [# Source](#)

Reverse rows

subMatrix

Source

```

:: Element a
=> (Int, Int) (r0,c0) starting position
-> (Int, Int) (rt,ct) dimensions of submatrix
-> Matrix a   input matrix
-> Matrix a   result

```

reference to a rectangular slice of a matrix (no data copy)

```
takeRows :: Element t => Int -> Matrix t -> Matrix t
```

Source

```
dropRows :: Element t => Int -> Matrix t -> Matrix t
```

Source

```
takeColumns :: Element t => Int -> Matrix t -> Matrix t
```

Source

```
dropColumns :: Element t => Int -> Matrix t -> Matrix t
```

Source

```
remap :: Element t => Matrix I -> Matrix I -> Matrix t -> Matrix t
```

Source

Extract elements from positions given in matrices of rows and columns.

```

>>> r
(3><3)
[ 1, 1, 1
, 1, 2, 2
, 1, 2, 3 ]
>>> c
(3><3)
[ 0, 1, 5
, 2, 2, 1
, 4, 4, 1 ]
>>> m
(4><6)
[ 0, 1, 2, 3, 4, 5
, 6, 7, 8, 9, 10, 11
, 12, 13, 14, 15, 16, 17
, 18, 19, 20, 21, 22, 23 ]

```

```

>>> remap r c m
(3><3)
[ 6, 7, 11
, 8, 14, 13
, 10, 16, 19 ]

```

The indexes are autoconformable.

```

>>> c'
(3><1)
[ 1
, 2
, 4 ]
>>> remap r c' m
(3><3)
[ 7, 7, 7

```

```
, 8, 14, 14
, 10, 16, 22 ]
```

Block matrix

fromBlocks :: **Element** t => **[[Matrix** t]] -> **Matrix** t

Source

Create a matrix from blocks given as a list of lists of matrices.

Single row-column components are automatically expanded to match the corresponding common row and column:

```
disp = putStr . dispf 2
```

```
>>> disp $ fromBlocks [[ident 5, 7, row[10,20]], [3, diag1[1,2,3], 0]]
8x10
1  0  0  0  0  7  7  7  10  20
0  1  0  0  0  7  7  7  10  20
0  0  1  0  0  7  7  7  10  20
0  0  0  1  0  7  7  7  10  20
0  0  0  0  1  7  7  7  10  20
3  3  3  3  3  1  0  0  0  0
3  3  3  3  3  0  2  0  0  0
3  3  3  3  3  0  0  3  0  0
```

(|||) :: **Element** t => **Matrix** t -> **Matrix** t -> **Matrix** t

infixl 3

Source

horizontal concatenation

```
>>> ident 3 ||| konst 7 (3,4)
(3><7)
[ 1.0, 0.0, 0.0, 7.0, 7.0, 7.0, 7.0
, 0.0, 1.0, 0.0, 7.0, 7.0, 7.0, 7.0
, 0.0, 0.0, 1.0, 7.0, 7.0, 7.0, 7.0 ]
```

(===) :: **Element** t => **Matrix** t -> **Matrix** t -> **Matrix** t

infixl 2

Source

vertical concatenation

diagBlock :: (**Element** t, **Num** t) => **[Matrix** t] -> **Matrix** t

Source

create a block diagonal matrix

```
>>> disp 2 $ diagBlock [konst 1 (2,2), konst 2 (3,5), col [5,7]]
7x8
1  1  0  0  0  0  0  0
1  1  0  0  0  0  0  0
0  0  2  2  2  2  2  0
0  0  2  2  2  2  2  0
0  0  2  2  2  2  2  0
0  0  0  0  0  0  0  5
0  0  0  0  0  0  0  7
```

```
>>> diagBlock [(0><4)[], konst 2 (2,3)] :: Matrix Double
(2><7)
[ 0.0, 0.0, 0.0, 0.0, 2.0, 2.0, 2.0
, 0.0, 0.0, 0.0, 0.0, 2.0, 2.0, 2.0 ]
```

```
repmat :: Element t => Matrix t -> Int -> Int -> Matrix t
```

[# Source](#)

creates matrix by repetition of a matrix a given number of rows and columns

```
>>> repmat (ident 2) 2 3
(4><6)
[ 1.0, 0.0, 1.0, 0.0, 1.0, 0.0
, 0.0, 1.0, 0.0, 1.0, 0.0, 1.0
, 1.0, 0.0, 1.0, 0.0, 1.0, 0.0
, 0.0, 1.0, 0.0, 1.0, 0.0, 1.0 ]
```

Synopsis

```
toBlocks :: Element t => [Int] -> [Int] -> Matrix t -> [[Matrix t]]
```

[# Source](#)

Partition a matrix into blocks with the given numbers of rows and columns. The remaining rows and columns are discarded.

```
toBlocksEvery :: Element t => Int -> Int -> Matrix t -> [[Matrix t]]
```

[# Source](#)

Fully partition a matrix into blocks of the same size. If the dimensions are not a multiple of the given size the last blocks will be smaller.

Mapping functions

```
conj :: Container c e => c e -> c e
```

[# Source](#)

complex conjugate

```
cmap :: (Element b, Container c e) => (e -> b) -> c e -> c b
```

[# Source](#)

like `fmap` (cannot implement instance Functor because of Element class constraint)

```
cmod :: (Integral e, Container c e) => e -> c e -> c e
```

[# Source](#)

`mod` for integer arrays

```
>>> cmod 3 (range 5)
fromList [0,1,2,0,1]
```

```
step :: (Ord e, Container c e) => c e -> c e
```

[# Source](#)

A more efficient implementation of `cmap (\x -> if x>0 then 1 else 0)`

```
>>> step $ linspace 5 (-1,1::Double)
5 |> [0.0,0.0,0.0,1.0,1.0]
```

```
cond
```

[# Source](#)

<code>:: (Ord e, Container c e, Container c x)</code>	
<code>=> c e</code>	a
<code>-> c e</code>	b
<code>-> c x</code>	l
<code>-> c x</code>	e
<code>-> c x</code>	g
<code>-> c x</code>	result

Element by element version of case compare a b of {LT -> l; EQ -> e; GT -> g}.

Arguments with any dimension = 1 are automatically expanded:

```
>>> cond ((1<4)[1..]) ((3><1)[1..]) 0 100 ((3><4)[1..]) :: Matrix Double
(3><4)
[ 100.0,    2.0,    3.0,    4.0
,    0.0, 100.0,    7.0,    8.0
,    0.0,    0.0, 100.0, 12.0 ]
```

```
>>> let chop x = cond (abs x) 1E-6 0 0 x
```

Find elements

```
find :: Container c e => (e -> Bool) -> c e -> [IndexOf c] | # Source
```

Find index of elements which satisfy a predicate

```
>>> find (>0) (ident 3 :: Matrix Double)
[(0,0),(1,1),(2,2)]
```

```
maxIndex :: Container c e => c e -> IndexOf c | # Source
```

index of maximum element

```
minIndex :: Container c e => c e -> IndexOf c | # Source
```

index of minimum element

```
maxElement :: Container c e => c e -> e | # Source
```

value of maximum element

```
minElement :: Container c e => c e -> e | # Source
```

value of minimum element

```
sortVector :: (Ord t, Element t) => Vector t -> Vector t | # Source
```

```
sortIndex :: (Ord t, Element t) => Vector t -> Vector I | # Source
```

```
>>> m <- randn 4 10
>>> disp 2 m
4x10
-0.31    0.41    0.43   -0.19   -0.17   -0.23   -0.17   -1.04   -0.07   -1.24
 0.26    0.19    0.14    0.83   -1.54   -0.09    0.37   -0.63    0.71   -0.50
-0.11   -0.10   -1.29   -1.40   -1.04   -0.89   -0.68    0.35   -1.46    1.86
 1.04   -0.29    0.19   -0.75   -2.20   -0.01    1.06    0.11   -2.09   -1.58
```

```
>>> disp 2 $ m ?? (All, Pos $ sortIndex (m!1))
4x10
-0.17   -1.04   -1.24   -0.23    0.43    0.41   -0.31   -0.17   -0.07   -0.19
-1.54   -0.63   -0.50   -0.09    0.14    0.19    0.26    0.37    0.71    0.83
-1.04    0.35    1.86   -0.89   -1.29   -0.10   -0.11   -0.68   -1.46   -1.40
-2.20    0.11   -1.58   -0.01    0.19   -0.29    1.04    1.06   -2.09   -0.75
```

Sparse

```
type AssocMatrix = [((Int, Int), Double)]
```

[# Source](#)

```
toDense :: AssocMatrix -> Matrix Double
```

[# Source](#)

```
mkSparse :: AssocMatrix -> GMatrix
```

[# Source](#)

```
mkDiagR :: Int -> Int -> Vector Double -> GMatrix
```

[# Source](#)

```
mkDense :: Matrix Double -> GMatrix
```

[# Source](#)

Synopsis

IO

```
disp :: Int -> Matrix Double -> IO ()
```

[# Source](#)

print a real matrix with given number of digits after the decimal point

```
>>> disp 5 $ ident 2 / 3
2x2
0.33333  0.00000
0.00000  0.33333
```

```
loadMatrix :: FilePath -> IO (Matrix Double)
```

[# Source](#)

load a matrix from an ASCII file formatted as a 2D table.

```
loadMatrix' :: FilePath -> IO (Maybe (Matrix Double))
```

[# Source](#)

```
saveMatrix
```

[# Source](#)

```

:: FilePath
-> String      "printf" format (e.g. "%.2f", "%g", etc.)
-> Matrix Double
-> IO ()
```

save a matrix as a 2D ASCII table

```
latexFormat
```

[# Source](#)

```

:: String  type of braces: "matrix", "bmatrix", "pmatrix", etc.
-> String  Formatted matrix, with elements separated by spaces and newlines
-> String
```

Tool to display matrices with latex syntax.

```
>>> latexFormat "bmatrix" (dispf 2 $ ident 2)
"\\begin{bmatrix}\\n1 & 0\\n\\\\\\n0 & 1\\n\\end{bmatrix}"
```

```
dispf :: Int -> Matrix Double -> String
```

[# Source](#)

Show a matrix with a given number of decimal places.

```
>>> dispf 2 (1/3 + ident 3)
"3x3\n1.33  0.33  0.33\n0.33  1.33  0.33\n0.33  0.33  1.33\n"
```

```
>>> putStr . dispf 2 $ (3<4)[1,1.5..]
3x4
1.00  1.50  2.00  2.50
3.00  3.50  4.00  4.50
5.00  5.50  6.00  6.50
```

```
>>> putStr . unlines . tail . lines . dispf 2 . asRow $ linspace 10 (0,1)
0.00  0.11  0.22  0.33  0.44  0.56  0.67  0.78  0.89  1.00
```

```
disps :: Int -> Matrix Double -> String
```

[# Source](#)

Show a matrix with "autoscaling" and a given number of decimal places.

```
>>> putStr . disps 2 $ 120 * (3<4) [1..]
3x4  E3
0.12  0.24  0.36  0.48
0.60  0.72  0.84  0.96
1.08  1.20  1.32  1.44
```

```
dispcf :: Int -> Matrix (Complex Double) -> String
```

[# Source](#)

Pretty print a complex matrix with at most n decimal digits.

```
format :: Element t => String -> (t -> String) -> Matrix t -> String
```

[# Source](#)

Creates a string from a matrix given a separator and a function to show each entry. Using this function the user can easily define any desired display function:

```
import Text.Printf(printf)
```

```
disp = putStr . format " " (printf "%.2f")
```

```
dispDots :: Int -> Matrix Double -> IO ()
```

[# Source](#)

```
dispBlanks :: Int -> Matrix Double -> IO ()
```

[# Source](#)

```
dispShort :: Int -> Int -> Int -> Matrix Double -> IO ()
```

[# Source](#)

Element conversion

```
class Convert t where
```

[# Source](#)

Methods

```
real :: Complexable c => c (RealOf t) -> c t
```

[# Source](#)

```
complex :: Complexable c => c t -> c (ComplexOf t)
```

[# Source](#)

```
single :: Complexable c => c t -> c (SingleOf t)
```

[# Source](#)

```
double :: Complexable c => c t -> c (DoubleOf t)
```

[# Source](#)

```
toComplex :: (Complexable c, RealElement t) => (c t, c t) -> c (Complex t) Source
```

#

```
fromComplex :: (Complexable c, RealElement t) => c (Complex t) -> (c t, c t)
```

Source

▼ Instances

```
+ Convert Double | # Source
```

```
+ Convert Float | # Source
```

```
+ Convert (Complex Double) | # Source
```

```
+ Convert (Complex Float) | # Source
```

Synopsis <<

```
roundVector :: Vector Double -> Vector Double
```

Source

```
fromInt :: Container c e => c I -> c e
```

Source

```
>>> fromInt ((2><2) [0..3]) :: Matrix (Complex Double)
(2><2)
[ 0.0 :+ 0.0, 1.0 :+ 0.0
, 2.0 :+ 0.0, 3.0 :+ 0.0 ]
```

```
toInt :: Container c e => c e -> c I
```

Source

```
fromZ :: Container c e => c Z -> c e
```

Source

```
toZ :: Container c e => c e -> c Z
```

Source

Misc

```
arctan2 :: (Fractional e, Container c e) => c e -> c e -> c e
```

Source

```
separable :: Element t => (Vector t -> Vector t) -> Matrix t -> Matrix t
```

Source

matrix computation implemented as separated vector operations by rows and columns.

```
fromArray2D :: Storable e => Array (Int, Int) e -> Matrix e
```

Source

```
module Data.Complex
```

```
data Mod (n :: Nat) t
```

Source

Wrapper with a phantom integer for statically checked modular arithmetic.

▼ Instances

```
+ KnownNat m => Container Vector (Mod m Z) | # Source
```

```
+ KnownNat m => Container Vector (Mod m I) | # Source
```

```
+ KnownNat m => Num (Vector (Mod m Z)) | # Source
```

```
+ KnownNat m => Num (Vector (Mod m I)) | # Source
```


<code>⊕ KnownNat m => Testable (Matrix (Mod m I))</code>	<code># Source</code>
<code>⊕ KnownNat m => Normed (Vector (Mod m Z))</code>	<code># Source</code>
<code>⊕ KnownNat m => Normed (Vector (Mod m I))</code>	<code># Source</code>
<code>⊕ (Storable t, Indexable (Vector t) t) => Indexable (Vector (Mod m t)) (Mod m t)</code>	<code># Source</code>
<code>⊕ (Integral t, Enum t, KnownNat m) => Enum (Mod m t)</code>	<code>Source</code> <code>#</code>
<code>⊕ (Eq t, KnownNat m) => Eq (Mod m t)</code>	<code># Source</code>
<code>⊕ (Show (Mod m t), Num (Mod m t), Eq t, KnownNat m) => Fractional (Mod m t)</code>	<code># Source</code>
<code>⊕ (Integral t, KnownNat m, Num (Mod m t)) => Integral (Mod m t)</code>	<code># Source</code>
<code>⊕ (Integral t, KnownNat n) => Num (Mod n t)</code>	<code># Source</code>
<code>⊕ (Ord t, KnownNat m) => Ord (Mod m t)</code>	<code># Source</code>
<code>⊕ (Integral t, Real t, KnownNat m, Integral (Mod m t)) => Real (Mod m t)</code>	<code># Source</code>
<code>⊕ Show t => Show (Mod n t)</code>	<code># Source</code>
<code>⊕ Storable t => Storable (Mod n t)</code>	<code># Source</code>
<code>⊕ NFData t => NFData (Mod n t)</code>	<code># Source</code>
<code>⊕ KnownNat m => Element (Mod m Z)</code>	<code># Source</code>
<code>⊕ KnownNat m => Element (Mod m I)</code>	<code># Source</code>
<code>⊕ KnownNat m => Product (Mod m Z)</code>	<code># Source</code>
<code>⊕ KnownNat m => Product (Mod m I)</code>	<code># Source</code>
<code>⊕ KnownNat m => Numeric (Mod m Z)</code>	<code># Source</code>
<code>⊕ KnownNat m => Numeric (Mod m I)</code>	<code># Source</code>
<code>⊕ type RealOf (Mod n Z)</code>	<code># Source</code>
<code>⊕ type RealOf (Mod n I)</code>	<code># Source</code>

this instance is only valid
for prime m

Synopsis

data **Vector** a #

Storable-based vectors

▼ Instances

<code>⊕ Complexable Vector</code>	<code># Source</code>
<code>⊕ LSDiv Vector</code>	<code># Source</code>
<code>⊕ Storable a => Vector Vector a</code>	
<code>⊕ Container Vector t => Linear t Vector</code>	<code># Source</code>
<code>⊕ Container Vector Double</code>	<code># Source</code>
<code>⊕ Container Vector Float</code>	<code># Source</code>
<code>⊕ Container Vector Z</code>	<code># Source</code>

<code>+</code> <code>Container Vector I</code>	<code># Source</code>
<code>+</code> <code>Container Vector e => Konst e Int Vector</code>	<code># Source</code>
<code>+</code> <code>Container Vector (Complex Double)</code>	<code># Source</code>
<code>+</code> <code>Container Vector (Complex Float)</code>	<code># Source</code>
<code>+</code> <code>KnownNat n => Sized ℂ (C n) Vector</code>	<code># Source</code>
<code>+</code> <code>KnownNat n => Sized ℝ (R n) Vector</code>	<code># Source</code>
<code>+</code> <code>KnownNat m => Container Vector (Mod m Z)</code>	<code># Source</code>
<code>+</code> <code>KnownNat m => Container Vector (Mod m I)</code>	<code># Source</code>
<code>+</code> <code>Container Vector e => Build Int (e -> e) Vector e</code>	<code># Source</code>
<code>+</code> <code>Storable a => IsList (Vector a)</code>	
<code>+</code> <code>(Storable a, Eq a) => Eq (Vector a)</code>	
<code>+</code> <code>Floating (Vector Double)</code>	<code># Source</code>
<code>+</code> <code>Floating (Vector Float)</code>	<code># Source</code>
<code>+</code> <code>Floating (Vector (Complex Double))</code>	<code># Source</code>
<code>+</code> <code>Floating (Vector (Complex Float))</code>	<code># Source</code>
<code>+</code> <code>(Container Vector a, Num (Vector a), Fractional a) => Fractional (Vector a)</code>	<code># Source</code>
<code>+</code> <code>(Data a, Storable a) => Data (Vector a)</code>	
<code>+</code> <code>Num (Vector Double)</code>	<code># Source</code>
<code>+</code> <code>Num (Vector Float)</code>	<code># Source</code>
<code>+</code> <code>Num (Vector (Complex Double))</code>	<code># Source</code>
<code>+</code> <code>Num (Vector (Complex Float))</code>	<code># Source</code>
<code>+</code> <code>Num (Vector Z)</code>	<code># Source</code>
<code>+</code> <code>Num (Vector I)</code>	<code># Source</code>
<code>+</code> <code>KnownNat m => Num (Vector (Mod m Z))</code>	<code># Source</code>
<code>+</code> <code>KnownNat m => Num (Vector (Mod m I))</code>	<code># Source</code>
<code>+</code> <code>(Storable a, Ord a) => Ord (Vector a)</code>	
<code>+</code> <code>(Read a, Storable a) => Read (Vector a)</code>	
<code>+</code> <code>(Show a, Storable a) => Show (Vector a)</code>	
<code>+</code> <code>Storable a => Semigroup (Vector a)</code>	
<code>+</code> <code>Storable a => Monoid (Vector a)</code>	
<code>+</code> <code>(Binary a, Storable a) => Binary (Vector a)</code>	<code># Source</code>
<code>+</code> <code>NFData (Vector a)</code>	
<code>+</code> <code>Storable t => TransArray (Vector t)</code>	<code># Source</code>
<code>+</code> <code>Container Vector t => Additive (Vector t)</code>	<code># Source</code>
<code>+</code> <code>Normed (Vector Float)</code>	<code># Source</code>
<code>+</code> <code>Normed (Vector (Complex Float))</code>	<code># Source</code>
<code>+</code> <code>Normed (Vector C)</code>	<code># Source</code>
<code>+</code> <code>Normed (Vector R)</code>	<code># Source</code>
<code>+</code> <code>Normed (Vector Z)</code>	<code># Source</code>

<code>⊕ Normed (Vector I)</code>	<code># Source</code>
<code>⊕ KnownNat m => Normed (Vector (Mod m Z))</code>	<code># Source</code>
<code>⊕ KnownNat m => Normed (Vector (Mod m I))</code>	<code># Source</code>
<code>⊕ Indexable (Vector Double) Double</code>	<code># Source</code>
<code>⊕ Indexable (Vector Float) Float</code>	<code># Source</code>
<code>⊕ Indexable (Vector Z) Z</code>	<code># Source</code>
<code>⊕ Indexable (Vector I) I</code>	<code># Source</code>
<code>⊕ Indexable (Vector (Complex Double)) (Complex Double)</code>	<code># Source</code>
<code>⊕ Indexable (Vector (Complex Float)) (Complex Float)</code>	<code># Source</code>
<code>⊕ Element t => Indexable (Matrix t) (Vector t)</code>	<code># Source</code>
<code>⊕ (Storable t, Indexable (Vector t) t) => Indexable (Vector (Mod m t)) (Mod m t)</code>	<code># Source</code>
<code>⊕ type Mutable Vector</code>	
<code>⊕ type IndexOf Vector</code>	<code># Source</code>
<code>⊕ type Item (Vector a)</code>	
<code>⊕ type Trans (Vector t) b</code>	<code># Source</code>
<code>⊕ type TransRaw (Vector t) b</code>	<code># Source</code>

`data Matrix t` `# Source`

Matrix representation suitable for BLAS/LAPACK computations.

▼ Instances

<code>⊕ Complexable Matrix</code>	<code># Source</code>
<code>⊕ LSDiv Matrix</code>	<code># Source</code>
<code>⊕ Container Matrix t => Linear t Matrix</code>	<code># Source</code>
<code>⊕ (Num a, Element a, Container Vector a) => Container Matrix a</code>	<code># Source</code>
<code>⊕ (Num e, Container Vector e) => Konst e (Int, Int) Matrix</code>	<code># Source</code>
<code>⊕ (KnownNat m, KnownNat n) => Sized ℂ (M m n) Matrix</code>	<code># Source</code>
<code>⊕ (KnownNat m, KnownNat n) => Sized ℝ (L m n) Matrix</code>	<code># Source</code>
<code>⊕ Container Matrix a => Eq (Matrix a)</code>	<code># Source</code>
<code>⊕ (Floating a, Container Vector a, Floating (Vector a), Fractional (Matrix a)) => Floating (Matrix a)</code>	<code># Source</code>
<code>⊕ (Container Vector a, Fractional a, Fractional (Vector a), Num (Matrix a)) => Fractional (Matrix a)</code>	<code># Source</code>
<code>⊕ (Container Matrix a, Num a, Num (Vector a)) => Num (Matrix a)</code>	<code># Source</code>
<code>⊕ (Element a, Read a) => Read (Matrix a)</code>	<code># Source</code>
<code>⊕ (Show a, Element a) => Show (Matrix a)</code>	<code># Source</code>
<code>⊕ (Container Vector t, Eq t, Num (Vector t), Product t) => Semigroup (Matrix t)</code>	<code># Source</code>

<code>⊕ (Container Vector t, Eq t, Num (Vector t), Product t) => Monoid (Matrix t)</code>	# Source
<code>⊕ (Binary (Vector a), Element a) => Binary (Matrix a)</code>	# Source
<code>⊕ (Storable t, NFData t) => NFData (Matrix t)</code>	# Source
<code>⊕ Storable t => TransArray (Matrix t)</code>	# Source
<code>⊕ Testable (Matrix I)</code>	# Source
<code>⊕ KnownNat m => Testable (Matrix (Mod m I))</code>	# Source
<code>⊕ Container Matrix t => Additive (Matrix t)</code>	# Source
<code>⊕ Normed (Matrix C)</code>	# Source
<code>⊕ Normed (Matrix R)</code>	# Source
<code>⊕ (CTrans t, Container Vector t) => Transposable (Matrix t) (Matrix t)</code>	# Source
<code>⊕ Element t => Indexable (Matrix t) (Vector t)</code>	# Source
<code>⊕ Container Matrix e => Build (Int, Int) (e -> e -> e) Matrix e</code>	# Source
<code>⊕ type IndexOf Matrix</code>	# Source
<code>⊕ type Trans (Matrix t) b</code>	# Source
<code>⊕ type TransRaw (Matrix t) b</code>	# Source

`data GMatrix` # Source

General matrix with specialized internal representations for dense, sparse, diagonal, banded, and constant elements.

```
>>> let m = mkSparse [((0,999),1.0),((1,1999),2.0)]
>>> m
SparseR {gmCSR = CSR {csrVals = fromList [1.0,2.0],
                      csrCols = fromList [1000,2000],
                      csrRows = fromList [1,2,3],
                      csrNRows = 2,
                      csrNCols = 2000},
          nRows = 2,
          nCols = 2000}
```

```
>>> let m = mkDense (mat 2 [1..4])
>>> m
Dense {gmDense = (2><2)
      [ 1.0, 2.0
        , 3.0, 4.0 ], nRows = 2, nCols = 2}
```

▼ Instances

<code>⊕ Show GMatrix</code>	# Source
<code>⊕ Testable GMatrix</code>	# Source
<code>⊕ Transposable GMatrix GMatrix</code>	# Source

`nRows :: GMatrix -> Int` # Source

`nCols :: GMatrix -> Int` # Source

