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Drude model σ and ϵ 1

Our ultimate goal will be to find the conductivity σ and the dielectric constant ϵ in the Drude model, with Drude relaxation time τ , electron density n and electron mass m. We'll find

$$\sigma_{\rm DC} = \frac{ne^2\tau}{m} \tag{1}$$

$$\sigma_{\rm AC} = \frac{ne^2\tau}{m} \frac{1}{1 - i\omega\tau} \tag{2}$$

$$\epsilon = 1 + i\frac{4\pi\sigma}{\omega} \tag{3}$$

Our dielectric constant can be rewritten to plug in for σ , giving us

$$\epsilon = 1 + i \frac{4\pi\sigma}{\omega} \tag{4}$$

$$= 1 + i \frac{4\pi\sigma_{\rm DC}}{\omega} \frac{1}{1 - i\omega\tau}$$

$$= 1 + i \frac{4\pi\sigma_{\rm DC}}{\omega} \frac{1}{1 - i\omega\tau} \frac{1 + i\omega\tau}{1 + i\omega\tau}$$
(5)

$$= 1 + i \frac{4\pi\sigma_{\rm DC}}{\omega} \frac{1}{1 - i\omega\tau} \frac{1 + i\omega\tau}{1 + i\omega\tau} \tag{6}$$

$$=1+i\frac{4\pi\sigma_{\rm DC}}{\omega}\frac{1+i\omega\tau}{1+\omega^2\tau^2}\tag{7}$$

$$= 1 + i \frac{4\pi\sigma_{\rm DC}}{\omega} \frac{1 + i\omega\tau}{1 + \omega^2\tau^2}$$

$$= \left(1 - \frac{4\pi\sigma_{\rm DC}\omega\tau}{\omega(1 + \omega^2\tau^2)}\right) + i\left(\frac{4\pi\sigma_{\rm DC}}{\omega(1 + \omega^2\tau^2)}\right)$$
(8)

$$= \left(1 - \frac{4\pi\sigma_{\rm DC}\tau}{1 + \omega^2\tau^2}\right) + i\left(\frac{4\pi\sigma_{\rm DC}}{\omega\left(1 + \omega^2\tau^2\right)}\right) \tag{9}$$