Minimax and Alpha-Beta Search on the Game Chomp

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The minimax and alpha-beta search algorithms are commonly used for AI programming. They help find the best possible outcomes for a given scenario. I decided to use this algorithm to help me with a game I recently published on the app store called "Choco Chomp" ([Choco Chomp](https://itunes.apple.com/us/app/choco-chomp/id1213722025?ls=1&mt=8)). It is based on a similarly named game "chomp". The impartial game "chomp" is a two-player game with perfect information which means that both players can make the same moves and no information is hidden from any player. For example, chess is not an impartial game since player 2 cannot move player 1's pieces. A game with *imperfect* information would be poker since player 1 cannot see player 2's cards.

The game chomp is played on a rectangular board with n rows and m columns. Where m, n > 1. The bottom left piece is poison. For example, consider the following board.

**Initial Board**

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
|  |  |  |  |
| p |  |  |  |

Each player takes turns making moves until only the poison piece is remaining. A move consists of selecting any square and removing all squares above it and to the right of it. Selecting the poison square is a loss for the respective player.

**First Player's Turn**

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
|  |  | 1 |  |
| p |  |  |  |

**Second Player's Turn**

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
|  |  |  |  |
| p | 2 |  |  |

**First Player's Turn**

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
| 1 |  |  |  |
| p |  |  |  |

**Second Player's Turn**

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
|  |  |  |  |
| p |  |  |  |

Second player would lose in this case.

It can be shown that for any rectangular board of chomp with n rows and m columns where n, m > 1 first player has a winning strategy, however, finding the winning strategy can be very difficult for large games of chomp. Currently my game Choco Chomp on the app store can only be played between 2 human players. My plan is to use the minimax algorithm to find the winning strategy to potentially add single player mode to my game. I will be using the Swift language to program since that is the language for IOS development. I will also try to do use other similar algorithms like alpha-beta search to improve the search time. Below is a simple example of the winning strategy for a 2 by 2 chomp game. The winning strategy is highlighted in red.

**Minimax on Chomp**

|  |  |
| --- | --- |
|  |  |
| p |  |

|  |  |
| --- | --- |
|  |  |
| p |  |

|  |  |
| --- | --- |
|  |  |
| p |  |

|  |  |
| --- | --- |
|  |  |
| p |  |

|  |  |
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|  |  |
| p |  |

|  |  |
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|  |  |
| p |  |

|  |  |
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|  |  |
| p |  |

|  |  |
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|  |  |
| --- | --- |
|  |  |
| p |  |

|  |  |
| --- | --- |
|  |  |
| p |  |