CS440 : Introduction to Artificial Intelligence **Spring 2014**

Problem Set 2 - Part 1

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1. **Solution to problem 1**

   (a) **Training on data set 1**

   a) The final weights

   $StartingThreshhold = 0.0$
   $CalculatedThreshhold = -54.0$

   Weights:
   $w_1 \rightarrow -752.0$
   $w_2 \rightarrow 4771.0$
   $w_3 \rightarrow 17714.0$
   $w_4 \rightarrow 762.0$
   $w_5 \rightarrow 6.0$
   $w_6 \rightarrow 676.0$
   $w_7 \rightarrow 3060.0$
   $w_8 \rightarrow -2004.0$
   $w_9 \rightarrow 5459.0$
   $w_{10} \rightarrow 9591.2999999989$
   $w_{11} \rightarrow 3832.0$
   $w_{12} \rightarrow 14963.0$
   $w_{13} \rightarrow 20912.0$

   b) The number of training epochs required
   The training took 1980 epochs.

   c) The margin
   $\gamma \rightarrow 1.5226515850810045 \times 10^{-5}$

   (b) **Test on data set 1**

   a) A confusion matrix

54	0
0	63

   b) Two lists of example indices
   No errors were found with this dataset since the weight vectors were calculated from this dataset.

c) The total loss summed over the misclassified examples
The loss for this dataset is 0.0 since it is the training data set.

(c) **Test on data set 2**

a) A confusion matrix

12	1
0	20

b) Two lists of example indices
False Negatives:
Index: 22
Inputs: $(60.0, 1.0, 4.0, 140.0, 293.0, 0.0, 2.0, 170.0, 0.0, 1.2, 2.0, 2.0, 7.0)$

False Positives:
There were no false positives

c) The total loss summed over the misclassified examples
Total loss: 77.440000001312

(d) **Application to data set 3**
Classifications:
$1 \rightarrow 0.0$
$2 \rightarrow 1.0$
$3 \rightarrow 0.0$
$4 \rightarrow 1.0$
$5 \rightarrow 1.0$
$6 \rightarrow 0.0$
$7 \rightarrow 0.0$
$8 \rightarrow 0.0$
$9 \rightarrow 0.0$
$10 \rightarrow 1.0$
$11 \rightarrow 1.0$
$12 \rightarrow 0.0$
$13 \rightarrow 1.0$
$14 \rightarrow 0.0$
$15 \rightarrow 0.0$
$16 \rightarrow 0.0$
$17 \rightarrow 1.0$
$18 \rightarrow 0.0$
$19 \rightarrow 0.0$
$20 \rightarrow 0.0$
$21 \rightarrow 0.0$

Which feature is the most important?
In order to determine the most influential property I have used the correlation

coefficients to find the most correlation between each property and the classification. The source code to find this property is also within the project.

Label	Correlation Coefficient
age	0.576399638726158
sex	0.15811388300841894
chest	0.4934637712198269
resting blood pressure	0.08008953852726183
serum cholestoral	−0.32382553481251514
fasting blood sugar	0.31622776601683766
resting electrocardiographic results	0.1386750490563073
maximum heart rate achieved	−0.5353426981014223
exercise induced angina	0.685994340570035
oldpeak	0.8086701966434094
slope	0.6123724356957945
number of major vessels	0.8152133857595864
thal	0.43905703995876144

Property With Maximum Correlation
Label: number of major vessels
Correlation Coefficient: 0.8152133857595864

1 Source Code

The following is the source code for the assignment. It consists of 5 classes to get all the required output.

- CorrelationCoefficient
  This class is used to calculate the correlation coefficient on the resultant classifications when running the learner in application mode to tell which is the most important input.
- Pair
  This is mainly a utility class used to group the weight and input together for clarity in traversal of the arrays.
- VectorUtils
  This is a collection of vector utilities that are used throughout the application such as: dot product, addition, scaling, finding the norm, etc.
- WidrowHoffLearner
  This class has the Widrow Hoff Learning specific code as defined in the assignment and lectures.

- Main
  This class simply runs all the classes and displays the output.

  I have excluded the source for DataSet for brevity.

1.1 Main.java

```
1  package hw2.widrowhoff;
2
3  import java.util.List;
4
5  public class Main {
6
7    public static void main(String[] args) {
8      final String dataSet1Csv = "DataSet1.csv";
9      final String dataSet2Csv = "DataSet2.csv";
10     final String dataSet3Csv = "DataSet3.csv";
11
12     DataSet dataSet1 = new DataSet(dataSet1Csv);
13     DataSet dataSet2 = new DataSet(dataSet2Csv);
14     DataSet dataSet3 = new DataSet(dataSet3Csv);
15
16     WidrowHoffLearner learner = new WidrowHoffLearner( dataSet1, 0.0 );
17     learner.trainWeightVector();
18
19     for( int i = 0; i < learner.getWeights().length; i++ ) {
20       System.out.println("\\( w_{" + (i+1) + "} \\rightarrow " + learner.
             getWeights()[i] + " \\)");
21     }
22
23     System.out.println("-------------------------");
24     System.out.println("Data set 1 test");
25     System.out.println("-------------------------");
26     learner.testWeightVector(dataSet1);
27     System.out.println("-------------------------");
28     System.out.println("Data set 2 test");
29     System.out.println("-------------------------");
30     learner.testWeightVector(dataSet2);
31
32     System.out.println("-------------------------");
33     System.out.println("Data set 3 application");
34     System.out.println("-------------------------");
35
36     final List<Double> classifications = learner.applyWeightVector(dataSet3);
37     for( int i = 0; i < classifications.size(); i++ ) {
38       System.out.println( "\\( " + (i+1) + " \\rightarrow " + classifications.
             get(i) + " \\) \\\\" );
39     }
40
41     final List<Pair<String,Double>> coefficients = CorrelationCoefficient.
           calculate(dataSet3, classifications);
42     System.out.println("-------------------------");
```

```
43      System.out.println("Correlation Coefficients");
44      System.out.println("-------------------------");
45      String maxProp = "";
46      Double maxCorrelation = Double.MIN_VALUE;
47      System.out.println("\\( \\begin{array}{l|l}");
48      System.out.println("\\bf{Label} & \\bf{Correlation Coefficient} \\\\");
49      System.out.println("\\hline");
50      for(final Pair<String, Double> coefficient : coefficients ) {
51        System.out.println("\\text{ " + coefficient.getLeft().trim().replaceAll(
              "[^A-Za-z0-9]", " ") + " } & " + coefficient.getRight() + " \\\\");
52        if( coefficient.getRight().compareTo(maxCorrelation) > 0 ) {
53          maxProp = coefficient.getLeft();
54          maxCorrelation = coefficient.getRight();
55        }
56      }
57      System.out.println("\\end{array} \\)");
58      System.out.println();
59
60
61      System.out.println("-------------------------");
62      System.out.println("Maximum Correlation Prop");
63      System.out.println("-------------------------");
64      System.out.println("\\bf{ Property With Maximum Correlation} \\\\ ");
65      System.out.println("Label: " + maxProp.replaceAll("[^A-Za-z0-9]", " ") + "
            \\\\");
66      System.out.println("Correlation Coefficient: \\(" + maxCorrelation + "\\)"
            );
67    }
68
69  }
```

1.2 Pair.java

```
1  package hw2.widrowhoff;
2
3  public class Pair<T1, T2> {
4    private final T1 left;
5    private final T2 right;
6
7    public Pair(T1 left, T2 right) {
8      this.left = left;
9      this.right = right;
10   }
11
12   public T1 getLeft() {
13     return left;
14   }
15   public T2 getRight() {
16     return right;
17   }
18 }
```

1.3 VectorUtils.java

```
1  package hw2.widrowhoff;
2
3  import java.util.ArrayList;
4  import java.util.List;
5
6  public class VectorUtils {
7
8    public static double dotProduct( final double[] x, final double[] y ) {
9      double sum = 0;
10     for( int i = 0; i < x.length && i < y.length; i++ ) {
11       sum += x[i] * y[i];
12     }
13
14     return sum;
15   }
16
17   public static double[] scale( final double[] x, final double scalar ) {
18     double[] xCopy = x.clone();
19     for( int i = 0; i < x.length; i++ ) {
20       xCopy[i] *= scalar;
21     }
22     return xCopy;
23   }
24
25   public static double[] add( double[] x, final double[] y ) {
26     double[] xCopy = x.clone();
27     double[] yCopy = y.clone();
28     for( int i = 0; i < xCopy.length && i < yCopy.length; i++ ) {
29       xCopy[i] += yCopy[i];
30     }
31
32     return xCopy;
33   }
34
35   public static List<Pair<Double, Double> > zip( double[] x, double[] y ) {
36     List<Pair<Double, Double> > zippedVector = new ArrayList<Pair<Double,
         Double>>();
37     for( int i = 0; i < x.length && i < y.length; i++ ) {
38       zippedVector.add( new Pair<Double,Double>(x[i], y[i]) );
39     }
40     return zippedVector;
41   }
42
43   public static double[] concat( double[] left, double[] right) {
44     if( left == null || right == null ) {
45       throw new IllegalArgumentException("The left or right arguments must not
             be null");
46     }
47
48     final int totalLength = left.length + right.length;
49     double[] concatted = new double[totalLength];
50     for(int i = 0; i < left.length; i++ ) {
```

```
51        concatted[i] = left[i];
52      }
53      for(int i = 0; i < right.length; i++ ) {
54        concatted[i + left.length] = right[i];
55      }
56      return concatted;
57    }
58
59    public static double[] unitVector( double[] x ) {
60      double[] copy = x.clone();
61      double norm = norm(copy);
62      return scale(x, 1.0 / norm );
63    }
64
65    public static double norm( double[] x ) {
66      double sum = 0;
67      for( int i = 0; i < x.length; i++) {
68        sum += Math.pow(x[i], 2.0);
69      }
70      return Math.sqrt(sum);
71    }
72  }
```

1.4 CorrelationCoefficient.java

```
1  package hw2.widrowhoff;
2
3  import java.util.ArrayList;
4  import java.util.List;
5
6  public class CorrelationCoefficient {
7
8    public static List<Pair<String,Double>> calculate(final DataSet dataSet,
       final List<Double> classifications ) {
9      final String[] labels = dataSet.fields;
10     List<Pair<String,Double>> coefficients = new ArrayList<Pair<String,Double
         >>();
11
12     final List<List<Double>> transformedArray = transform(dataSet.exData);
13     final double classificationMean = mean(classifications);
14
15     int i = 0;
16     for( final List<Double> array : transformedArray ) {
17       final double mean = mean(array);
18       final String label = labels[i];
19
20       double numeratorSum = 0.0;
21       double xDenominatorSum = 0.0;
22       double yDenominatorSum = 0.0;
23
24       int j = 0;
25       for( final Double x : array ) {
```

```
26          final double xDiff = x - mean;
27          final double yDiff = classifications.get(j) - classificationMean;
28
29          numeratorSum += xDiff * yDiff;
30          xDenominatorSum += xDiff * xDiff;
31          yDenominatorSum += yDiff * yDiff;
32
33          j++;
34        }
35
36        final Double correlationCoefficient = numeratorSum / Math.sqrt(
              xDenominatorSum * yDenominatorSum);
37        final Pair<String,Double> coefficientWithLabel = new Pair<String,Double
              >(label, correlationCoefficient);
38        coefficients.add(coefficientWithLabel);
39        i++;
40      }
41
42      return coefficients;
43    }
44
45    private static List< List<Double> > transform(double[][] data ) {
46      List<List<Double>> transformed = new ArrayList<List<Double>>();
47
48      for( int i = 0; i < data[0].length; i++ ) {
49        List<Double> column = new ArrayList<Double>();
50        for( int j = 0; j < data.length; j++ ) {
51          column.add(data[j][i]);
52        }
53        transformed.add(column);
54      }
55
56      return transformed;
57    }
58
59    @SuppressWarnings("unused")
60    private static double mean(final double[] array) {
61      double sum = 0.0;
62      for( int i = 0; i < array.length; i++ ) {
63        sum+= array[i];
64      }
65      return sum / (double) array.length;
66    }
67
68    private static double mean(final List<Double> array) {
69      double sum = 0.0;
70      for( int i = 0; i < array.size(); i++ ) {
71        sum+= array.get(i);
72      }
73      return sum / (double) array.size();
74    }
75  }
```

1.5 WidrowHoffLearner.java

```
1  package hw2.widrowhoff;
2
3  import java.util.ArrayList;
4  import java.util.List;
5
6  public class WidrowHoffLearner {
7
8    private double[] weights;
9    private double[] homogeneousWeights;
10   private double[][] x;
11   private double alpha = 1;
12   private double threshold;
13   private double[] labels;
14   private double margin;
15
16   public WidrowHoffLearner( final DataSet dataSet, final double[] weights,
         final double threshold ) {
17     this.x = dataSet.exData;
18     this.labels = dataSet.exLabels;
19     this.threshold = threshold;
20   }
21
22   public WidrowHoffLearner( final DataSet dataSet, final double threshold ) {
23     this.x = dataSet.exData;
24     this.labels = dataSet.exLabels;
25     final int inputLength = x[0].length; // get input vector length less the
           value of the class
26
27     double[] weightsVector = new double[inputLength];
28     for( int i = 0; i < inputLength; i++ ) {
29       weightsVector[i] = 0;
30     }
31     this.weights = weightsVector;
32
33     homogeneousWeights = VectorUtils.concat(new double[] { threshold },
           weights );
34
35     this.threshold = threshold;
36   }
37
38   public void trainWeightVector() {
39     int iterations = 0;
40     int errors;
41     do {
42       errors = 0;
43       for( int i = 0; i < x.length; i++ ) {
44         double[] heterogeneousInputs = VectorUtils.concat(new double[] { -1.0
               }, x[i]);
45
46         double err = labels[i] - percepW( heterogeneousInputs ); // use last
               value in array as label
47
```

```
48          // 0 - correct
49          // -1 - false positive
50          // 1 - false negative
51          if( err != 0.0 ) {
52            errors++;
53 //           double loss = -1.0 * err * VectorUtils.dotProduct(inputs, weights)
       ;
54
55            final double[] scaledInputs = VectorUtils.scale(heterogeneousInputs,
                  alpha * err );
56            homogeneousWeights = VectorUtils.add(scaledInputs,
                  homogeneousWeights);
57          }
58        }
59
60        iterations++;
61
62      } while( errors != 0);
63
64      calculateMargin();
65
66      for( int i = 1; i < homogeneousWeights.length; i++ ) {
67        weights[i-1] = homogeneousWeights[i];
68      }
69
70      System.out.println("The training took " + iterations + " epochs.");
71      System.out.println("Threshhold: " + homogeneousWeights[0]);
72      System.out.println("\\( \\gamma \\rightarrow " + margin + " \\)");
73    }
74
75    public void testWeightVector(DataSet dataSet) {
76      int falseNegatives = 0;
77      int falsePositives = 0;
78      int truePositives = 0;
79      int trueNegatives = 0;
80      double totalLoss = 0.0;
81      for( int i = 0; i < dataSet.exData.length; i++ ) {
82        double[] heterogeneousInputs = VectorUtils.concat(new double[] { -1.0 },
              dataSet.exData[i]);
83
84        final double percepResult = percepW( heterogeneousInputs );
85        final double err = dataSet.exLabels[i] - percepResult; // use last value
              in array as label
86
87        // 0 - correct
88        // -1 - false positive
89        // 1 - false negative
90        if( err > 0.0 ) {
91          falseNegatives++;
92          System.out.println("False Negative Found: ");
93          System.out.println("Index: " + i);
94          System.out.println("Inputs: " + vectorToString(heterogeneousInputs));
95          totalLoss += Math.abs(-1.0 * err * VectorUtils.dotProduct(
                heterogeneousInputs, homogeneousWeights ));
```

```
96        } else if ( err < 0.0 ) {
97          falsePositives++;
98          System.out.println("False Positive Found: ");
99          System.out.println("Index: " + i);
100         System.out.println("Inputs: " + vectorToString(heterogeneousInputs));
101         totalLoss += Math.abs(-1.0 * err * VectorUtils.dotProduct(
                heterogeneousInputs, homogeneousWeights ));
102       } else {
103         if( percepResult == 1 ) {
104           truePositives++;
105         } else {
106           trueNegatives++;
107         }
108       }
109     }
110
111     System.out.println("True Positives: " + truePositives );
112     System.out.println("True Negatives: " + trueNegatives );
113     System.out.println("False positives: " + falsePositives);
114     System.out.println("False negatives: " + falseNegatives);
115     System.out.println("Total loss: " + totalLoss);
116     System.out.println("Total items: " + dataSet.exData.length );
117   }
118
119   private String vectorToString( final double[] x ) {
120     StringBuilder stringBuilder = new StringBuilder();
121     stringBuilder.append("(");
122     for( int i = 1; i < x.length; i++ ) {
123       stringBuilder.append(x[i]);
124       if( i != x.length - 1) {
125         stringBuilder.append(", ");
126       }
127     }
128     stringBuilder.append(")");
129     return stringBuilder.toString();
130   }
131
132   public List<Double> applyWeightVector(DataSet dataSet) {
133     List<Double> classifications = new ArrayList<Double>();
134     for( int i = 0; i < dataSet.exData.length; i++ ) {
135       double[] heterogeneousInputs = VectorUtils.concat(new double[] { -1.0 },
              dataSet.exData[i]);
136       double classification = percepW(heterogeneousInputs);
137       classifications.add(classification);
138     }
139     return classifications;
140   }
141
142   private void calculateMargin() {
143     margin = Double.MAX_VALUE;
144     final double[] unitWeightVector = VectorUtils.unitVector(
          homogeneousWeights);
145
146     for( int i = 0; i < x.length; i++ ) {
```

```
147         double[] heterogeneousInputs = VectorUtils.concat(new double[] { -1.0 },
                x[i]);
148
149         double dotProduct = Math.abs( VectorUtils.dotProduct(unitWeightVector,
                heterogeneousInputs) );
150         double norm = VectorUtils.norm(heterogeneousInputs);
151
152         double marginPart = dotProduct / norm;
153
154         margin = Math.min(margin, marginPart);
155       }
156     }
157
158     private double percepW( final double[] curInputVector ) {
159       double sum = 0.0;
160
161       sum += VectorUtils.dotProduct( curInputVector, homogeneousWeights );
162
163       if( sum > 0 ) return 1;
164       else if ( sum < 0 ) return 0;
165       else return 0;
166     }
167
168     public double[] getWeights() {
169       return weights;
170     }
171     public double[][] getX() {
172       return x;
173     }
174
175     public double getAlpha() {
176       return alpha;
177     }
178
179     public double getThreshold() {
180       return threshold;
181     }
182
183     public double[] getLabels() {
184       return labels;
185     }
186
187     public double getMargin() {
188       return margin;
189     }
190
191 }
```